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Robust Gain Scheduling techniques for Adaptive control

Patrice Antoinette and Gilles Ferreres

Abstract—Robust and gain-scheduling analysis and design techniques are used to realize an adaptive controller. LFT representations of the plant and controller are used so that the stability and performance properties of the adaptive scheme can be studied off-line, and the on-line computational time for implementing the LFT controller is reduced. This controller is scheduled as a function of the parameters to be estimated.

I. INTRODUCTION

A controller is said to be *adaptive* when it adapts to the unknown plant. Generally, measurements of input and output signals are used to adjust the controller. To achieve this type of control, two schemes can be identified : direct and indirect schemes. In the latter, using input and output signals of the plant, parameters of the *plant model* are estimated, and this estimation is used to adjust on-line the controller. The situation is described by figure 1, where the vector of parameters (θ) is estimated ($\hat{\theta}$) thanks to the measurements of input ($u \in \mathbb{R}^{m_u}$) and output ($y \in \mathbb{R}^{r_y}$) signals of the plant ($H(s, \theta)$). These estimations are transmitted to the controller ($K(s, \hat{\theta})$) to adjust it. $d \in \mathbb{R}^{m_d}$ is an unmeasured perturbation, and $p \in \mathbb{R}^{r_p}$ is a controlled output. On the contrary, in direct adaptive schemes, the controller is directly adjusted from the input and output signals of the plant, without any estimator : this is the case of the well known Model Reference Adaptive Control (MRAC). See [1] and included references. Another example is the STAC technique (Set Theoretic Adaptor Control) that is based on the concept of falsification [2], [3], [4].

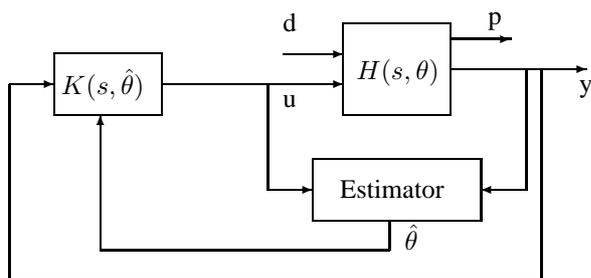


Fig. 1. General scheme of indirect adaptive control. θ is a vector of plant parameters, $\hat{\theta}$ is the estimation of θ , $H(s, \theta)$ is the plant, and $K(s, \hat{\theta})$ is the controller.

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Results now exist on the key stability and robustness issues of adaptive control, see e.g. [5], [1], [6], [7]. To some extent, our technique could be considered as reminiscent of the theoretical framework proposed in [5]. It is especially possible to use Lyapunov and passivity techniques extracted from nonlinear analysis tools, i.e. the adaptive controller is considered as a nonlinear one [8], [9]. Despite their popularity, the application to adaptive control of linear robust control techniques (H_∞ design and μ analysis) and of gain-scheduled control (LPV methods) has been (much) less investigated, see for instance [10], [11].

It is worth emphasizing that several issues can be studied, namely the mere asymptotic stability of the adaptive scheme or its performance, i.e. the quality of its transient (before the estimator converges in the context of indirect adaptive control) or asymptotic responses. It is also possible in some cases to prove the finite-time convergence of the direct or indirect adaptive scheme [2], [3], [10], [1]. Noting that controlling the transient response is a key issue in practice, otherwise the plant (e.g. an airplane) could be endangered.

In the present article, only indirect adaptive control of linear time invariant plants is dealt with. As a consequence, the vector θ is constant. The approach is distinguished by the fact that the estimator doesn't "physically" appear in the analysis and synthesis schemes. Only design features on the estimation errors are considered.

The article is organised in 7 sections. The problem is stated in section II. Then synthesis (III) and validation (IV) methods for an adaptive controller are described : a modal LFT gain design and a robustness analysis techniques extracted from [12], [13] are used. Section V deals with the estimation of a continuous state space representation with a standard recursive least squares algorithm [14]. All these methods set out are then applied to a transport aircraft in section VI, before the conclusion in section VII.

II. PROBLEM STATEMENT

During the realization of an indirect adaptive controller it is essential to face up to two crucial problems. The first is the on-line computational time of the controller implementation which must be reasonable. The second is to ensure closed loop stability and performance. In fact, the parameters are not directly measured but estimated. This estimation introduces a difference $\delta\theta = \hat{\theta} - \theta \neq 0$. This difference is produced by errors during the transient and steady states of the estimator. The goal is to ensure stability and "satisfactory" performance despite this error. So the controller must be robust in the face of estimation errors of θ , and other modeling errors.

In order to solve these problems, the scheme presented on

figure 2 is proposed, where the controller and the plant are both under an LFT form.

NOTATIONS : In the following, notations are defined by $\theta = [\theta_1, \dots, \theta_n]^T$, $\hat{\theta} = [\hat{\theta}_1, \dots, \hat{\theta}_n]^T$ and $\delta\theta = [\delta\theta_1, \dots, \delta\theta_n]^T$. Without loss of generality, it is supposed that $\theta_i \in [-1, 1]$. Then it is assumed that $\Delta_h(\theta) = \text{diag}(\theta_1 I_{h_1}, \dots, \theta_n I_{h_n})$ and $\Delta_k(\hat{\theta}) = \text{diag}(\hat{\theta}_1 I_{k_1}, \dots, \hat{\theta}_n I_{k_n})$, with integers $h_1, \dots, h_n, k_1, \dots, k_n$. Let

$$\tilde{\Delta} = \text{diag}(\theta_1 I_{q_1}, \dots, \theta_n I_{q_n}) \quad (1)$$

be the matrix obtained by merging and ordering the elements of matrices $\Delta_h(\theta)$ and $\Delta_k(\theta)$, with $q_i = h_i + k_i$, and $B_o = \{\tilde{\Delta}(\theta) \mid \theta_1, \dots, \theta_n \in [-1, 1]\}$, $B_{\delta o} = \{\Delta_k(\delta\theta) \mid \delta\theta_1, \dots, \delta\theta_n \in [-1, 1]\}$.

It is worth emphasizing that the set of possible values of θ , the true values of the plant parameters, is assumed to be a priori given. After normalization, all θ_i belong to the interval $[-1, 1]$.

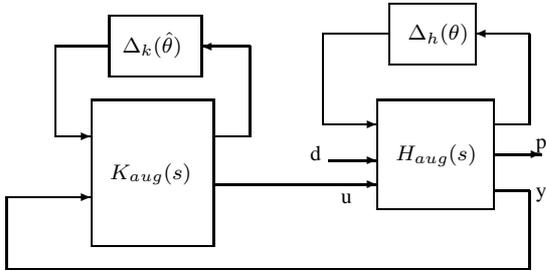


Fig. 2. Adaptive control scheme with LFT modeling. $K_{aug}(s)$ is the part of the controller designed off-line. $\Delta_h(\theta)$ and $\Delta_k(\hat{\theta})$ represent the dependence of the plant and the controller on respectively the parameter θ and its estimated value $\hat{\theta}$.

The LFT modeling presents two interests :

- First of all, thanks to this controller pattern, the computation time of the controller adjustment is expected to be reduced. In fact, in this case, the computation of $K(s, \hat{\theta}) = \mathcal{F}_u(K_{aug}(s), \Delta_k(\hat{\theta}))$ is made of two parts : K_{aug} is designed off-line, and only $\Delta_k(\hat{\theta})$ is adjusted on-line [15].
- Furthermore, this pattern allows the off-line analysis of stability and performance properties of the adaptive closed loop with the help of robustness analysis tools [12].

In this scheme, the adaptive controller is a set composed of an estimator and a gain-scheduled controller. The robustness of the controller in the face of estimation errors on θ and other modeling errors is ensured thanks to methods of robust synthesis and analysis.

To design a controller $\mathcal{F}_u(K_{aug}, \Delta_k(\hat{\theta}))$, a method in two stages is presented : the first is the synthesis of an LFT controller, and the second is its validation.

III. GAIN SCHEDULING CONTROL DESIGN

A. Synthesis of the LFT gain

Contrary to the assumptions made later for the analysis, during the synthesis, the *Certainty Equivalence* principle is applied, and it is considered that $\hat{\theta}(t) = \theta$ for all t . Then a gain scheduled controller synthesis algorithm presented in [13] is used.

Proposition 1 (Algorithm of modal design): Let $(A(\theta), B(\theta), C(\theta), D(\theta))$ be a state space representation, with n_s states and r_y outputs. If the number of measurements is greater or equal than the number r_d of dominant modes the following algorithm can be proposed :

- 1) Choose r_d closed loop eigenvalues $\lambda_i(\theta)$.
- 2) Compute r_d pairs $(v_i(\theta), w_i(\theta))$ so that :

$$\begin{bmatrix} A(\theta) - \lambda_i(\theta)I_{n_s} & B(\theta) \end{bmatrix} \begin{bmatrix} v_i(\theta) \\ w_i(\theta) \end{bmatrix} = 0 \quad (2)$$

- 3) Compute $K(\theta)$ as a solution of the equation :

$$K(\theta) \begin{bmatrix} C(\theta) & D(\theta) \end{bmatrix} \begin{bmatrix} V(\theta) \\ W(\theta) \end{bmatrix} = W(\theta) \quad (3)$$

with $W(\theta) = [w_1(\theta), \dots, w_{r_d}(\theta)]$ and $V(\theta) = [v_1(\theta), \dots, v_{r_d}(\theta)]$.

In this algorithm, $A(\theta), B(\theta), C(\theta), D(\theta), K(\theta)$ and $\lambda_i(\theta)$ are under an LFT form.

It's worth noting that no more than r_y eigenvalues can be assigned. In practice, only dominant modes are assigned, and for instance the actuator modes placement is uncontrolled. So, contrary to LPV methods which offer a guarantee of robust stability, in the algorithm used, the stability of the closed loop must be checked a posteriori. But in another respect, as θ is time invariant parameter, in the modal design there is no loss of performance due to conservative stability requirements, contrary to LPV methods which deal with time varying parameters.

B. Well-posedness problem

The result of the previous synthesis is a static LFT gain $K(\theta) = \mathcal{F}_u(K_{aug}, \Delta_k(\theta))$, with $K_{aug} = \begin{pmatrix} K_{11} & K_{12} \\ K_{21} & K_{22} \end{pmatrix}$. Then

$$K(\theta) = K_{22} + K_{21}\Delta_k(\theta)(I - K_{11}\Delta_k(\theta))^{-1}K_{12} \quad (4)$$

The LFT gain is well-posed if and only if $\forall \Delta_k(\theta) \in B_{\delta o}$, $\det(I - K_{11}\Delta_k(\theta)) \neq 0$. In order to verify the well-posedness, the structured singular value is used ([16]).

Definition 1: Let M be a complex matrix with the same dimensions as $\tilde{\Delta}$ in equation (1). The structured singular value $\mu(M)$, associated to M and to a real perturbation $\tilde{\Delta}$ is defined as

$$\frac{1}{\mu(M)} = \min \left\{ k \mid \exists \tilde{\Delta} \in k B_o, \text{ s.t. } \det(I - M\tilde{\Delta}) = 0 \right\} \quad (5)$$

and $\mu(M) = 0$ if no $\tilde{\Delta}$ satisfies $\det(I - M\tilde{\Delta}) = 0$.

The well-posedness of $K(\theta)$ can be checked with the following proposition.

Proposition 2: $\mathcal{F}_u(K_{aug}, \Delta_k(\theta))$ is well-posed for all $\Delta_k(\theta) \in B_{\delta o}$ if and only if $\mu(K_{11}) < 1$. A sufficient condition is that there exist scaling matrices $D_0 = D_0^* > 0$ and $G_0 = G_0^*$, with $D_0 \Delta_k(\theta) = \Delta_k(\theta) D_0$ and $G_0 \Delta_k(\theta) = \Delta_k(\theta) G_0$ which satisfy

$$K_{11} D_0 K_{11}^* + j(G_0 K_{11}^* - K_{11} G_0) \leq D_0 \quad (6)$$

Condition (6) can be checked with standard Matlab routines of the μ Analysis and Synthesis Toolbox or of the LMI Control Toolbox.

Once the well-posedness of the controller is checked, as explained previously, the next stages are to verify that the designed controller ensures the stability of the closed loop for all considered values of θ , and then to compute the maximal allowable estimation error.

IV. VALIDATION WITH μ -ANALYSIS

A. Building of the validation scheme

Applying the ‘‘Certainty Equivalence’’ principle, so far it was supposed that $\hat{\theta}(t) = \theta$. In the following, this principle is not valid anymore and it is considered that $\hat{\theta}_i(t) = \theta_i(1 + \delta\theta_i(t))$, where $\delta\theta_i(t)$ is the relative error on parameter θ_i . Noting that $\Delta_k(\hat{\theta}) = \Delta_k(\theta) [I + \Delta_k(\delta\theta)]$, the scheme of figure 2 is transformed into the one of figure 3. Then, keeping the connexions between the blocks, $H_{aug}(s)$ and $K_{aug}(s)$ are merged into the block $N(s)$ of figure 4. Its first inputs are the vectors f_1 and f_2 merged and ordered following the order of $\tilde{\Delta}$, see equation (1). Next come f_3 and the unmeasured perturbation d . The outputs of $N(s)$ follow the same logic. Noting $\Delta_\delta = \Delta_k(\delta\theta)$, the described scheme is presented on figure 4.

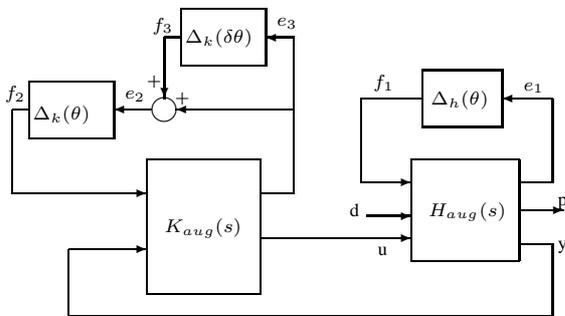


Fig. 3. Adaptive control scheme emphasizing the estimation error.

First of all, as indicated previously, in order to end the synthesis, the stability of the scheme of figure 4 without estimation errors (i.e $\Delta_\delta = 0$) must be checked with the following proposition.

Proposition 3: Let $N_{11}(s)$ be the asymptotically stable transfer matrix between w and z on figure 4. Robust stability of the closed loop of figure 4 is ensured for all $\tilde{\Delta} \in B_o$, with $\Delta_\delta = 0$, if and only if $\mu(N_{11}(j\omega)) \leq 1$, $\forall \omega \in [0, +\infty)$. A sufficient condition is that there exist frequency dependent scaling matrices $D_1(\omega) = D_1^*(\omega) > 0$ and $G_1(\omega) = G_1^*(\omega)$ which satisfy $D_1(\omega) \tilde{\Delta} = \tilde{\Delta} D_1(\omega)$ and $G_1(\omega) \tilde{\Delta} =$

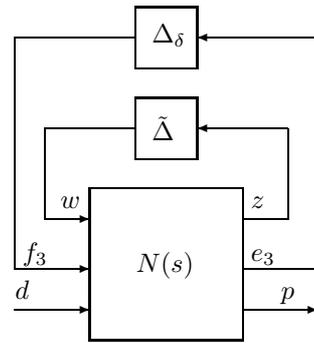


Fig. 4. Scheme used to validate the adaptive control scheme.

$\tilde{\Delta}^* G_1(\omega)$. The interconnection structure of figure 4 is stable for $\Delta_\delta = 0$ and $\tilde{\Delta} \in B_o$ if there exist $D_1(\omega)$ and $G_1(\omega)$ satisfying $\forall \omega \in [0, +\infty)$

$$N_{11}(j\omega) D_1(\omega) N_{11}^*(j\omega) + j(G_1(\omega) N_{11}^*(j\omega) - N_{11}(j\omega) G_1(\omega)) \leq D_1(\omega) \quad (7)$$

B. Validation procedure

Then, the robust stability margin considering errors of estimation is dealt with. Let α_m be this margin defined by :

$$\alpha_m = \max\{r \in \mathbb{R}^+ \mid \forall \tilde{\Delta} \in B_o, \forall \Delta_\delta \in r B_{\delta o}, \text{ the transfer matrix } p = \mathcal{F}_u(N(s), \text{diag}(\tilde{\Delta}, \Delta_\delta)) \text{ is stable.}\} \quad (8)$$

This margin allows to determine the maximal magnitude that the error of estimation can reach without causing the instability of the closed loop. However, the computation of α_m is difficult because the uncertainties considered are both time invariant ($\tilde{\Delta}$) and time varying (Δ_δ). To deal with them, the Robust Feedforward Design Toolbox (RFDT)[12] is used. Thanks to it, a lower bound of α_m is determined. Furthermore, for a margin of stability $\alpha = (1 - \epsilon)\alpha_m$ ($\epsilon > 0$ given), one computes a guaranteed value of the worst case induced L_2 norm of the time varying uncertain transfer matrix, i.e a value γ such that $\forall \tilde{\Delta} \in B_o$, and $\forall \Delta_\delta \in \alpha B_{\delta o}$,

$$\|\mathcal{F}_u(N(s), \text{diag}(\tilde{\Delta}, \Delta_\delta))\|_{iL_2} \leq \gamma \quad (9)$$

The algorithms of this toolbox are based on the next proposition.

Proposition 4: Let $\Phi = \text{diag}(\tilde{\Delta}, \Delta_\delta, \Delta_c)$, where $\Delta_c \in \mathbb{C}^{m_d \times r_p}$ is an unstructured complex matrix. Let $D = D^* > 0$ and $G = G^*$ be scaling matrices such that for all Φ having the indicated pattern they satisfy $D\Phi = \Phi D$ and $G\Phi = \Phi^* G$. The matrices D and G are divided as $D = \text{diag}(D_1, D_2, I)$ and $G = \text{diag}(G_1, G_2, 0)$ in order to correspond to the decomposition of Φ in $\tilde{\Delta}$, Δ_δ and Δ_c . D_2 and G_2 are constant, while D_1 and G_1 vary with the frequency. Let $P = \Lambda(\alpha, \gamma) N$, with $\Lambda(\alpha, \gamma) = \text{diag}(I_{r_1}, \frac{1}{\alpha} I_{r_2}, \frac{1}{\gamma} I_{r_p})$, $r_1 = q_1 + \dots + q_n$ and $r_2 = k_1 + \dots + k_n$. If $D(\omega)$ and $G(\omega)$ exist such that $\forall \omega \in [0, +\infty)$

$$P(j\omega) D(\omega) P^*(j\omega) + j(G(\omega) P^*(j\omega) - P(j\omega) G(\omega)) \leq D(\omega) \quad (10)$$

nominal value, the stability of the closed loop is ensured, even during the transient states. Furthermore, the guaranteed value γ (9) of the induced L_2 norm of the transfer matrix between d and $p = [\alpha, q]^T$ is visualized on figure 6 as a function of the size α of the estimation error.

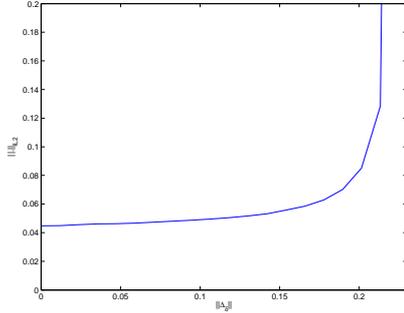


Fig. 6. Variation of the upper bound of the induced norm with the minimal relative estimation error Δ_s ensuring the stability.

C. Time simulation

As indicated in the paragraph V, the estimation of parameters is obtained from measurements of the state $x = [\alpha, q]^T$ and the input u of the system. These signals are filtered using the second order filter $\left[\frac{1}{D(s)}\right]$ with

$$D(s) = (1 + \tau_1 s)(1 + \tau_2 s) \quad (22)$$

and $\tau_1 = 5 \times 10^{-2}$, $\tau_2 = \frac{\tau_1}{100}$.

The estimator is discrete, and its sampling interval is 0.01 s. From equation (16), assuming $\phi(t) = [\alpha_f, u_f]^T$ and $\beta(t) = \dot{q}_f - M_q q_f$, one obtains $\beta(t) = \theta^T \phi(t)$. Then, using the recursive least squares algorithm described by equations (13, 14, 15), an estimation $\hat{\theta}$ is obtained.

The time simulation scheme is described by figure 7. Noting $\theta_0 = [M_{\alpha 0}, M_{u 0}]^T$ the nominal values of the

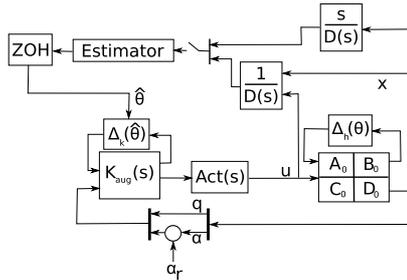


Fig. 7. Scheme of time simulation. (ZOH=Zero-Order Hold)

parameters, θ was chosen such that $M_\alpha = 1.01 \times M_{\alpha 0}$, $M_u = 1.7 \times M_{u 0}$. The initial relative estimation error was set such that $\delta\theta = [0.06 \times M_{\alpha 0}, -0.16 \times M_{u 0}]^T$.

The graph 8 shows the time responses to the input α_r . The dashdot curves were obtained without the estimator, and the controller parameters are not adjusted while the solid ones correspond to the time responses with the estimator. The time responses when there is no estimation error are the

dashed curves. But on this figure, the difference between the dashdot and dashed curves are not visible, because the estimator converges very quickly. The graph 9 shows the evolution of the estimation error.

It is noticed that the time response is improved when the estimator is added and is very close to the response without any estimation error. The pattern proposed guarantees good performances despite the initial unsuitable controller.

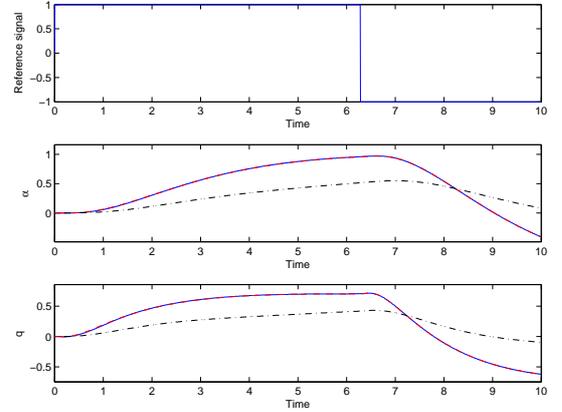


Fig. 8. Time responses of the simulation. The dashed curves are obtained when $\delta\theta = 0$, the solid ones with an initial error estimation, and the dashdot ones were realized without estimator, so without any correction on the estimation error. The difference between the solid and the dashed curves is not visible.

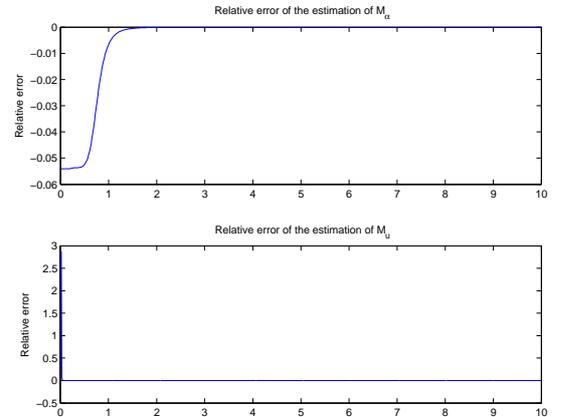


Fig. 9. Evolution of relative errors during the simulation with respect to the number of iterations.

VII. CONCLUSION

In this article, robust and gain-scheduling analysis and design techniques were used to realize an adaptive controller. To analyse the stability and the performances of the closed loop, and to minimize the computational time of the controller adjustment, the plant and the controller are modeled in LFT form. This pattern allows the use of algorithms of modal design and validation through μ -analysis. The approach is distinguished by the fact that the estimator doesn't appear explicitly in the analysis and synthesis schemes. Only bounds

on the estimation errors are determined.

This technique is applied to control a transport aircraft. The model used is extracted from the IMMUNE project. A time domain simulation illustrates the nice transient properties of the adaptive scheme.

In the application, the scheme of the adaptive control gathers a continuous controller with a discrete estimator. An improvement of this scheme would be an adaptation of synthesis methods to a discrete plant in order to obtain a discrete controller, or an adaptation of analysis methods in order to take into account the hybrid nature of the scheme.

To apply this technique to the non-linear model of the transport aircraft of the IMMUNE project, another goal is to realize a “satisfactory” estimator of slowly time-varying parameters. Some tracks are given in the paragraph V.

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