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Sensorless Fault Tolerant Control Based On Backstepping Strategy For Induction Motors

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Abstract: In this paper, a fault tolerant control for induction motors based on backstepping strategy is designed. The proposed approach permits to compensate both the rotor resistance variations and the load torque disturbance. Moreover, to avoid the use of speed and flux sensors, a second order sliding mode observer is used to estimate the flux and the speed. The used observer converges in a finite time and permits to give a good estimate of flux and speed even in presence of rotor resistance variations and load torque disturbance. The simulation results show the efficiency of the proposed control scheme.

1. INTRODUCTION

Induction Motors (IM) are widely used in many industrial processes due to their reliability, low cost and high performance. However, because of several stresses (mechanical, environmental, thermal, electrical), IM are subjected to various faults, such as stator short-circuits and rotor failures such as broken bars or rings,...etc. The diagnostic of IM has shown that the presence of faults leads to parameters variations (Moreau et al. [1999]). In this work, we focus on the rotor resistance variations.

Fault Tolerant Control (FTC) systems are able to maintain specific systems performances not only under nominal conditions but also when faults occur (change in system parameters or characteristic properties). There are two types of FTC: active and passive approaches. In the passive approach, the controller is designed to maintain acceptable performances against a set of faults without any change in the control law. In the active approach, first the faults are detected and isolated (fault detection and isolation step), second the control law is changed (control reconfiguration step) to maintain specific performances (blanke et al. [2003], blanke et al. [2001]). This paper is concerned with the passive fault tolerant controller for IM in order to compensate the rotor resistance variations and the load torque disturbance. The proposed approach uses a direct field oriented controller based on backstepping strategy to steer the flux and the speed to their desired references in presence of rotor resistance variations and load torque disturbance. Moreover, sensorless control is considered. This control method avoids the use of the speed sensor (Holtz [2006], Ghanes et al. [2009], Ghanes et al. [2010]). For instance, in Ghanes et al. [2010] the feedback controller uses an adaptive observer in order to estimate the flux and the speed, in Ghanes et al. [2009] the control scheme is based on a first order sliding mode observer. The sliding mode observers are widely used due to their finite time convergence, robustness with respect to

uncertainties and the possibility of uncertainty estimation (Perruqueti et al. [2002], Edwards et al. [2000]). When we use the first order sliding mode approach the chattering effect appears. To avoid the chattering effect, the high order sliding mode techniques have been developed. In this work, the controller uses a second order sliding mode observer (Solvar et al. [2010], Levant [1998], Floquet et al. [2007]) to estimate the speed and the flux.

Compared to the existing fault tolerant control schemes reported in the literature (Diallo et al. [2004], Bonivento et al. [2004], Djeghali et al. [2010], Tahami et al. [2006], Fekih [2008]) the contribution of this paper is first the design of a backstepping controller in presence of rotor resistance variations and load torque disturbance and second is the estimation of the speed by a second order sliding mode observer which uses only the measured stator currents.

This paper is organized as follows: Section 2 describes the IM oriented model in presence of rotor resistance variations. Section 3 gives some definitions on the practical stability. Section 4 is devoted to the design of the backstepping controller which is able to steer the flux and speed variables to their desired references in presence of rotor resistance variations and load torque disturbance. Section 5 presents the speed and flux estimation by using a second order sliding mode observer. Section 6 shows the simulation results. Section 7 gives some concluding remarks on the proposed fault tolerant controller.

2. INDUCTION MOTOR ORIENTED MODEL

In field oriented control, the flux vector is forced on the d-axis ($\phi_{qr} = \frac{d\phi_{qr}}{dt} = 0$). The resulting induction motor model in the ($d-q$) reference frame is described by the following state equations (Canudas [2000]):

$$\begin{aligned}
\frac{di_{ds}}{dt} &= -ai_{ds} + \omega_s i_{qs} + \frac{L_m}{\sigma L_s L_r \tau_r} \phi_{dr} + \frac{V_{ds}}{\sigma L_s} \\
\frac{di_{qs}}{dt} &= -ai_{qs} - \omega_s i_{ds} - \frac{L_m}{\sigma L_s L_r} P\Omega \phi_{dr} + \frac{V_{qs}}{\sigma L_s} \\
\frac{d\phi_{dr}}{dt} &= \frac{L_m}{\tau_r} i_{ds} - \frac{1}{\tau_r} \phi_{dr} \\
\frac{d\Omega}{dt} &= \frac{P L_m}{L_r J} i_{qs} \phi_{dr} - \frac{f}{J} \Omega - \frac{T}{J}
\end{aligned} \tag{1}$$

with:

$$\begin{aligned}
\omega_s &= P\Omega + \frac{L_m}{\tau_r \phi_{dr}} i_{qs} \\
a &= \left(\frac{R_s}{\sigma L_s} + \frac{1 - \sigma}{\sigma \tau_r} \right)
\end{aligned} \tag{2}$$

Where σ is the coefficient of dispersion, given by:

$$\sigma = 1 - \frac{L_m^2}{L_s L_r}$$

L_s , L_r , L_m are stator, rotor and mutual inductance, respectively. R_s , R_r are respectively stator and rotor resistance. ω_s is the stator pulsation. τ_r is the rotor time constant ($\tau_r = \frac{L_r}{R_r}$). P is the number of pole pairs. V_{ds} , V_{qs} are stator voltage components. ϕ_{dr} , ϕ_{qr} are the rotor flux components. Ω is the mechanical speed. T is the load torque. i_{ds} , i_{qs} are stator current components. J is the moment of inertia of the motor. f is the friction coefficient. In presence of rotor resistance variations, the model (1) becomes:

$$\begin{aligned}
\frac{di_{ds}}{dt} &= -ai_{ds} + \omega_s i_{qs} + \frac{L_m}{\sigma L_s L_r \tau_r} \phi_{dr} + \frac{V_{ds}}{\sigma L_s} + h_1(x) \\
\frac{di_{qs}}{dt} &= -ai_{qs} - \omega_s i_{ds} - \frac{L_m}{\sigma L_s L_r} P\Omega \phi_{dr} + \frac{V_{qs}}{\sigma L_s} + h_2(x) \\
\frac{d\phi_{dr}}{dt} &= \frac{L_m}{\tau_r} i_{ds} - \frac{1}{\tau_r} \phi_{dr} + h_3(x) \\
\frac{d\Omega}{dt} &= \frac{P L_m}{L_r J} i_{qs} \phi_{dr} - \frac{f}{J} \Omega - \frac{T}{J}
\end{aligned} \tag{3}$$

where $x = (i_{ds}, i_{qs}, \phi_{dr}, \Omega)$. $h_1(x)$, $h_2(x)$, $h_3(x)$ represent the fault terms due to rotor resistance variations, they are given by:

$$\begin{aligned}
h_1(x) &= \Delta R_r \left(-\left(\frac{1 - \sigma}{\sigma L_r}\right) i_{ds} + \frac{L_m}{\phi_{dr} L_r} i_{qs}^2 + \frac{L_m}{\sigma L_s L_r^2} \phi_{dr} \right) \\
h_2(x) &= \Delta R_r \left(-\left(\frac{1 - \sigma}{\sigma L_r}\right) i_{qs} - \frac{L_m}{\phi_{dr} L_r} i_{ds} i_{qs} \right) \\
h_3(x) &= \Delta R_r \left(\frac{L_m}{L_r} i_{ds} - \frac{\phi_{dr}}{L_r} \right)
\end{aligned}$$

Here we introduce some definitions on the practical stability which will be used in the next section.

3. PRELIMINARY

Consider the following system:

$$\begin{aligned}
\dot{x} &= f(t, x) \\
x(t_0) &= x_0, t_0 \geq 0
\end{aligned} \tag{4}$$

where $x \in R^n$, $t \in R_{\geq 0}$ and $f : R_{\geq 0} \times R^n \rightarrow R^n$ is piecewise continuous in t and locally Lipschitz in x . (t_0, x_0) are the initial conditions. We introduce the following definition in which B_r denotes the closed loop ball in R^n of radius r centered at the origin, i.e: $B_r = \{x \in R^n : \|x\| \leq r\}$, with $\|\cdot\|$ denotes the Euclidean norm of vectors.

Definition 1. The system (4) is said to be globally uniformly exponentially practically stable (or convergent to a ball B_r with radius $r > 0$), if there exists $\beta > 0$, such that for all $t_0 \in R_{\geq 0}$ and all $x_0 \in R^n$ there exists $k \geq 0$ such that $\|x\| \leq k\|x_0\| \exp(-\beta(t - t_0)) + r$, $\forall t \geq t_0$ (Lashmikantham et al. [1990]).

4. BACKSTEPPING CONTROL DESIGN

This part deals with the speed and flux control by means of backstepping control. This nonlinear control technique can be applied efficiently to linearize a nonlinear system with the existence of uncertainties, it is usually incorporated with the nonlinear damping to enhance robustness (Chen [1996], Polycarpou et al. [1993]).

In this work in order to compensate the rotor resistance variations and the load disturbance the backstepping technique is used. The idea of backstepping design is to select recursively some appropriate functions of state variables as virtual control inputs for lower dimension subsystems of the overall system. At each step of the backstepping a new virtual control input is designed. When the procedure terminates, the actual control input results which achieves the original design objective by virtue of a final Lyapunov function, which is formed by summing up the Lyapunov functions associated with each individual design step.

4.1 Step1: Flux control

The objective is to steer the flux ϕ_{dr} to a desired reference ϕ_{dr}^* , let $e_\phi = \phi_{dr} - \phi_{dr}^*$ be the flux tracking error. The dynamic of e_ϕ is:

$$\dot{e}_\phi = \frac{L_m}{\tau_r} i_{ds} - \frac{1}{\tau_r} \phi_{dr} + h_3(x) - \dot{\phi}_{dr}^* \tag{5}$$

A Lyapunov function is defined as:

$$V_\phi = \frac{1}{2} e_\phi^2 \tag{6}$$

By deriving (6) we obtain:

$$\dot{V}_\phi = e_\phi \dot{e}_\phi = e_\phi \left(\frac{L_m}{\tau_r} i_{ds} - \frac{1}{\tau_r} \phi_{dr} + h_3(x) - \dot{\phi}_{dr}^* \right) \tag{7}$$

To make \dot{V}_ϕ negative definite, i_{ds} is chosen as virtual element of control for stabilizing the flux, its desired value i_{ds}^* is defined as:

$$i_{ds}^* = \frac{\tau_r}{L_m} \left(-k_\phi e_\phi - k_1 \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right) + \frac{\phi_{dr}}{\tau_r} + \dot{\phi}_{dr}^* \right) \tag{8}$$

where $h = 0.2785$. k_1, k_ϕ and ε_1 are positive design parameters.

By setting $i_{ds} = i_{ds}^*$ in (7) we get :

$$\dot{V}_\phi = -k_\phi e_\phi^2 - k_1 \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right) e_\phi + h_3 e_\phi \tag{9}$$

for $k_1 > |h_3|_{max}$ we get:

$$\dot{V}_\phi \leq -k_\phi e_\phi^2 - k_1 \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right) e_\phi + k_1 |e_\phi| \tag{10}$$

with:

$$|e_\phi| = e_\phi \text{sign} e_\phi \tag{11}$$

The derivative of the Lyapunov function (10) becomes:

$$\dot{V}_\phi \leq -k_\phi e_\phi^2 - k_1 \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right) e_\phi + k_1 e_\phi \text{sign} e_\phi \tag{12}$$

we have (see Polycarpou et al. [1993]):

$$0 \leq k_1 e_\phi \operatorname{sign} e_\phi - k_1 \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right) e_\phi \leq \varepsilon_1 \quad (13)$$

The derivative of the Lyapunov function (12) becomes:

$$\dot{V}_\phi \leq -k_\phi e_\phi^2 + \varepsilon_1 \quad (14)$$

This implies that the variable e_ϕ converges to a ball whose radius can be reduced by making small the tuning parameter ε_1 .

4.2 Step2: Speed control

The objective is to steer the speed Ω to the desired reference Ω^* , let $e_\Omega = \Omega - \Omega^*$ be the speed tracking error. The error dynamic of the speed is:

$$\dot{e}_\Omega = \frac{PL_m}{L_r J} i_{qs} \phi_{dr} - \frac{f}{J} \Omega - \frac{T}{J} - \dot{\Omega}^* \quad (15)$$

A Lyapunov function is defined as:

$$V_\Omega = \frac{1}{2} e_\Omega^2 \quad (16)$$

By deriving (16) we obtain:

$$\dot{V}_\Omega = e_\Omega \dot{e}_\Omega = e_\Omega \left(\frac{PL_m}{L_r J} i_{qs} \phi_{dr} - \frac{f}{J} \Omega - \frac{T}{J} - \dot{\Omega}^* \right) \quad (17)$$

i_{qs} is chosen as virtual element of control for stabilizing the speed, its desired value i_{qs}^* is defined as:

$$i_{qs}^* = \frac{JL_r}{L_m P \phi_{dr}} \left(-k_\Omega e_\Omega - k_2 \tanh\left(\frac{k_2 h}{\varepsilon_2} e_\Omega\right) e_\Omega + \frac{f}{J} \Omega + \dot{\Omega}^* \right), \phi_{dr} \neq 0 \quad (18)$$

where $h = 0.2785$. k_2 and k_Ω and ε_2 are positive design parameters.

By setting $i_{qs} = i_{qs}^*$ in (17) we get:

$$\dot{V}_\Omega = e_\Omega \left(-k_\Omega e_\Omega - k_2 \tanh\left(\frac{k_2 h}{\varepsilon_2} e_\Omega\right) e_\Omega - \frac{T}{J} \right) \quad (19)$$

For $k_2 > \left| \frac{T}{J} \right|_{max}$ we obtain:

$$\dot{V}_\Omega \leq -k_\Omega e_\Omega^2 - k_2 \tanh\left(\frac{k_2 h}{\varepsilon_2} e_\Omega\right) e_\Omega + k_2 |e_\Omega| \leq -k_\Omega e_\Omega^2 + \varepsilon_2 \quad (20)$$

This implies that the variable e_Ω converges to a ball whose radius can be reduced by making small the tuning parameter ε_2 .

4.3 Step3: Currents control

The objective is to steer the currents i_{ds} and i_{qs} to their desired references i_{ds}^* and i_{qs}^* , respectively. Let $e_d = i_{ds} - i_{ds}^*$ and $e_q = i_{qs} - i_{qs}^*$ be the tracking errors of the currents, then the dynamic of the tracking errors are:

$$\begin{aligned} \dot{e}_d &= -a i_{ds} + \omega_s i_{qs} + \frac{L_m}{\sigma L_s L_r \tau_r} \phi_{dr} + \frac{V_{ds}}{\sigma L_s} + h_1(x) - \frac{di_{ds}^*}{dt} \\ \dot{e}_q &= -a i_{qs} - \omega_s i_{ds} - \frac{L_m}{\sigma L_s L_r} P \Omega \phi_{dr} + \frac{V_{qs}}{\sigma L_s} + h_2(x) - \frac{di_{qs}^*}{dt} \\ \dot{e}_\phi &= \frac{L_m}{\tau_r} e_d + \frac{L_m}{\tau_r} i_{ds}^* - \frac{1}{\tau_r} \phi_{dr} + h_3(x) - \dot{\phi}_{dr}^* \\ \dot{e}_\Omega &= \frac{PL_m}{L_r J} e_q \phi_{dr} + \frac{PL_m}{L_r J} i_{qs}^* \phi_{dr} - \frac{f}{J} \Omega - \frac{T}{J} - \dot{\Omega}^* \end{aligned} \quad (21)$$

with:

$$\begin{aligned} i_{ds}^* &= \frac{\tau_r}{L_m} \left(-k_\phi e_\phi - k_1 \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right) e_\phi + \frac{\phi_{dr}}{\tau_r} + \dot{\phi}_{dr}^* \right) \\ i_{qs}^* &= \frac{JL_r}{L_m P \phi_{dr}} \left(-k_\Omega e_\Omega - k_2 \tanh\left(\frac{k_2 h}{\varepsilon_2} e_\Omega\right) e_\Omega + \frac{f}{J} \Omega + \dot{\Omega}^* \right) \\ \frac{di_{ds}^*}{dt} &= \frac{\tau_r}{L_m} F_1(e_\phi) \left(\frac{L_m}{\tau_r} i_{ds} - \frac{\phi_{dr}}{\tau_r} + h_3(x) \right) \\ &\quad - \frac{\tau_r}{L_m} \left(F_1(e_\phi) - \frac{1}{\tau_r} \right) \dot{\phi}_{dr}^* + \frac{\tau_r}{L_m} \ddot{\phi}_{dr}^* \\ \frac{di_{qs}^*}{dt} &= \frac{JL_r}{L_m P \phi_{dr}} F_2(e_\Omega) \left(\frac{PL_m}{L_r J} i_{qs} \phi_{dr} - \frac{f}{J} \Omega \right) \\ &\quad + F_3(e_\Omega, \Omega, \phi_{dr}) + \frac{JL_r}{L_m P \phi_{dr}} \left(\frac{f}{J} - F_2(e_\Omega) \right) \dot{\Omega}^* \\ &\quad + \frac{JL_r}{L_m P \phi_{dr}} \ddot{\Omega}^* - \frac{L_r F_2(e_\Omega)}{PL_m \phi_{dr}} T + F_4 h_3(x) \end{aligned} \quad (22)$$

where:

$$F_1(e_\phi) = -k_\phi - \frac{k_1^2 h}{\varepsilon_1} \left(1 - \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right)^2 \right) + \frac{1}{\tau_r}$$

$$F_2(e_\Omega) = -k_\Omega - \frac{k_2^2 h}{\varepsilon_2} \left(1 - \tanh\left(\frac{k_2 h}{\varepsilon_2} e_\Omega\right)^2 \right) + \frac{f}{J}$$

$$F_3(e_\Omega, \Omega, \phi_{dr}) = \left(\frac{L_m}{\tau_r} i_{ds} - \frac{\phi_{dr}}{\tau_r} \right) F_4(e_\Omega, \Omega, \phi_{dr})$$

$$\begin{aligned} F_4(e_\Omega, \Omega, \phi_{dr}) &= \frac{JL_r}{PL_m \phi_{dr}^2} \left(k_\Omega e_\Omega + k_2 \tanh\left(\frac{k_2 h}{\varepsilon_2} e_\Omega\right) e_\Omega \right) \\ &\quad + \frac{JL_r}{PL_m \phi_{dr}^2} \left(-\frac{f}{J} \Omega - \dot{\Omega}^* \right) \end{aligned}$$

By substituting i_{ds}^* , i_{qs}^* , $\frac{di_{ds}^*}{dt}$ and $\frac{di_{qs}^*}{dt}$ by their expressions, the system of the tracking errors (21) becomes:

$$\begin{aligned} \dot{e}_d &= -a i_{ds} + \omega_s i_{qs} + \frac{L_m}{\sigma L_s L_r \tau_r} \phi_{dr} + \frac{V_{ds}}{\sigma L_s} + h_1(x) \\ &\quad - \frac{\tau_r}{L_m} F_1(e_\phi) \left(\frac{L_m}{\tau_r} i_{ds} - \frac{\phi_{dr}}{\tau_r} + h_3(x) \right) \\ &\quad + \frac{\tau_r}{L_m} \left(F_1(e_\phi) - \frac{1}{\tau_r} \right) \dot{\phi}_{dr}^* - \frac{\tau_r}{L_m} \ddot{\phi}_{dr}^* \\ \dot{e}_q &= -a i_{qs} - \omega_s i_{ds} - \frac{L_m}{\sigma L_s L_r} P \Omega \phi_{dr} + \frac{V_{qs}}{\sigma L_s} + h_2(x) \\ &\quad - \frac{JL_r}{L_m P \phi_{dr}} F_2(e_\Omega) \left(\frac{PL_m}{L_r J} i_{qs} \phi_{dr} - \frac{f}{J} \Omega \right) \\ &\quad - F_3(e_\Omega, \Omega, \phi_{dr}) - \frac{JL_r}{L_m P \phi_{dr}} \left(\frac{f}{J} - F_2(e_\Omega) \right) \dot{\Omega}^* \\ &\quad - \frac{JL_r}{L_m P \phi_{dr}} \ddot{\Omega}^* - \frac{L_r F_2(e_\Omega)}{PL_m \phi_{dr}} T - F_4 h_3(x) \\ \dot{e}_\phi &= -k_\phi e_\phi - k_1 \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right) e_\phi + \frac{L_m}{\tau_r} e_d + h_3(x) \\ \dot{e}_\Omega &= \frac{PL_m}{L_r J} e_q \phi_{dr} - k_\Omega e_\Omega - k_2 \tanh\left(\frac{k_2 h}{\varepsilon_2} e_\Omega\right) e_\Omega - \frac{T}{J} \end{aligned} \quad (23)$$

The actual control inputs are chosen as follows:

$$\begin{aligned}
V_{ds} = & \sigma L_s \left(-k_d e_d - k_3 \tanh\left(\frac{k_3 h}{\varepsilon_3} e_d\right) + a i_{ds} - \frac{L_m}{\tau_r} e_\phi \right. \\
& - \omega_s i_{qs} - \frac{L_m}{\sigma L_s L_r \tau_r} \phi_{dr} + \frac{\tau_r}{L_m} F_1 \left(\frac{L_m}{\tau_r} i_{ds} - \frac{\phi_{dr}}{\tau_r} \right) \\
& \left. - \frac{\tau_r}{L_m} \left(F_1 - \frac{1}{\tau_r} \right) \dot{\phi}_{dr}^* + \frac{\tau_r}{L_m} \ddot{\phi}_{dr}^* \right) \\
V_{qs} = & \sigma L_s \left(-k_q e_q - k_4 \tanh\left(\frac{k_4 h}{\varepsilon_4} e_q\right) + a i_{qs} + \omega_s i_{ds} \right. \\
& + \frac{L_m}{\sigma L_s L_r} P \Omega \phi_{dr} - \frac{P L_m}{J L_r} e_\Omega \phi_{dr} + \frac{J L_r}{L_m P \phi_{dr}} F_2(e_\Omega) \\
& \left. \left(\frac{P L_m}{L_r J} i_{qs} \phi_{dr} - \frac{f}{J} \Omega \right) + F_3(e_\Omega, \Omega, \phi_{dr}) \right. \\
& \left. + \frac{J L_r}{L_m P \phi_{dr}} \left(\frac{f}{J} - F_2(e_\Omega) \right) \dot{\Omega}^* + \frac{J L_r}{L_m P \phi_{dr}} \ddot{\Omega}^* \right)
\end{aligned} \tag{24}$$

$$\begin{aligned}
V_{qs} = & \sigma L_s \left(-k_q e_q - k_4 \tanh\left(\frac{k_4 h}{\varepsilon_4} e_q\right) + a i_{qs} + \omega_s i_{ds} \right. \\
& + \frac{L_m}{\sigma L_s L_r} P \Omega \phi_{dr} - \frac{P L_m}{J L_r} e_\Omega \phi_{dr} + \frac{J L_r}{L_m P \phi_{dr}} F_2(e_\Omega) \\
& \left. \left(\frac{P L_m}{L_r J} i_{qs} \phi_{dr} - \frac{f}{J} \Omega \right) + F_3(e_\Omega, \Omega, \phi_{dr}) \right. \\
& \left. + \frac{J L_r}{L_m P \phi_{dr}} \left(\frac{f}{J} - F_2(e_\Omega) \right) \dot{\Omega}^* + \frac{J L_r}{L_m P \phi_{dr}} \ddot{\Omega}^* \right)
\end{aligned} \tag{25}$$

Proposition 1. Consider the system (3) and the control inputs (24) and (25) where : k_d, k_q, k_3, k_4 are positive design parameters. $\varepsilon_1, \varepsilon_2, \varepsilon_3$ and ε_4 are positive and arbitrary small parameters. Then, if $k_3 > \left| h_1(x) - \frac{\tau_r}{L_m} F_1 h_3(x) \right|_{max}$ and $k_4 > \left| h_2(x) - F_4 h_3(x) + \frac{L_r F_2(e_\Omega)}{P L_m \phi_{dr}} T \right|_{max}$, the error variables e_ϕ, e_Ω, e_d and e_q are globally uniformly exponentially practically stable.

Proof. By substituting the control laws (24) and (25) in the error system (23) we get:

$$\begin{aligned}
\dot{e}_d = & -k_d e_d - k_3 \tanh\left(\frac{k_3 h}{\varepsilon_3} e_d\right) - \frac{L_m}{\tau_r} e_\phi + h_1(x) \\
& - \frac{\tau_r}{L_m} F_1 h_3(x) \\
\dot{e}_q = & -k_q e_q - k_4 \tanh\left(\frac{k_4 h}{\varepsilon_4} e_q\right) - \frac{P L_m}{J L_r} e_\Omega \phi_{dr} + h_2(x) \\
& - F_4 h_3(x) + \frac{L_r F_2(e_\Omega)}{P L_m \phi_{dr}} T \\
\dot{e}_\phi = & -k_\phi e_\phi - k_1 \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right) + \frac{L_m}{\tau_r} e_d + h_3(x) \\
\dot{e}_\Omega = & \frac{P L_m}{L_r J} e_q \phi_{dr} - k_\Omega e_\Omega - k_2 \tanh\left(\frac{k_2 h}{\varepsilon_2} e_\Omega\right) - \frac{T}{J}
\end{aligned} \tag{26}$$

Consider the following Lyapunov function:

$$V = \frac{1}{2} (e_d^2 + e_q^2 + e_\phi^2 + e_\Omega^2) \tag{27}$$

The derivative of V with respect to time is:

$$\begin{aligned}
\dot{V} = & e_d \left(-k_d e_d - k_3 \tanh\left(\frac{k_3 h}{\varepsilon_3} e_d\right) - \frac{L_m}{\tau_r} e_\phi + h_1(x) \right. \\
& \left. - \frac{\tau_r}{L_m} F_1 h_3(x) \right) \\
& + e_q \left(-k_q e_q - k_4 \tanh\left(\frac{k_4 h}{\varepsilon_4} e_q\right) - \frac{P L_m}{J L_r} e_\Omega \phi_{dr} + h_2(x) \right. \\
& \left. - F_4 h_3(x) + \frac{L_r F_2(e_\Omega)}{P L_m \phi_{dr}} T \right) \\
& + e_\phi \left(-k_\phi e_\phi - k_1 \tanh\left(\frac{k_1 h}{\varepsilon_1} e_\phi\right) + \frac{L_m}{\tau_r} e_d + h_3(x) \right) \\
& + e_\Omega \left(\frac{P L_m}{L_r J} e_q \phi_{dr} - k_\Omega e_\Omega - k_2 \tanh\left(\frac{k_2 h}{\varepsilon_2} e_\Omega\right) - \frac{T}{J} \right)
\end{aligned} \tag{28}$$

From the step 1 and 2 we have $k_1 > |h_3|_{max}$ and $k_2 > \left| \frac{T}{J} \right|_{max}$, then the derivative of the Lyapunov function (28) becomes:

$$\begin{aligned}
\dot{V} \leq & -k_\phi e_\phi^2 - k_\Omega e_\Omega^2 + \varepsilon_1 + \varepsilon_2 - k_d e_d^2 - k_q e_q^2 \\
& - k_3 \tanh\left(\frac{k_3 h}{\varepsilon_3} e_d\right) e_d - k_4 \tanh\left(\frac{k_4 h}{\varepsilon_4} e_q\right) e_q \\
& + \left(h_2(x) - F_4 h_3(x) + \frac{L_r F_2(e_\Omega)}{P L_m \phi_{dr}} T \right) e_q \\
& + \left(h_1(x) - \frac{\tau_r}{L_m} F_1 h_3(x) \right) e_d
\end{aligned} \tag{29}$$

For

$$k_3 > \left| h_1(x) - \frac{\tau_r}{L_m} F_1 h_3(x) \right|_{max}$$

and

$$k_4 > \left| h_2(x) - F_4 h_3(x) + \frac{L_r F_2(e_\Omega)}{P L_m \phi_{dr}} T \right|_{max}$$

we get:

$$\dot{V} \leq -k_\phi e_\phi^2 - k_\Omega e_\Omega^2 - k_d e_d^2 - k_q e_q^2 + \varepsilon_1 + \varepsilon_2 + \varepsilon_3 + \varepsilon_4 \tag{30}$$

This implies that the error variables e_ϕ, e_Ω, e_d and e_q converge to a ball whose radius can be reduced by making small the tuning parameters $\varepsilon_1, \varepsilon_2, \varepsilon_3$ and ε_4 . This means that the error variables are globally uniformly exponentially practically stable (see the definition 1).

In order to implement the control laws without flux and speed sensors, a second order sliding mode observer is used to estimate the speed Ω and the flux ϕ_{dr} .

5. SECOND ORDER SLIDING MODE OBSERVER DESIGN

The IM model in $(\alpha - \beta)$ reference frame is given by:

$$\begin{aligned}
\dot{i}_{\alpha s} = & -a i_{\alpha s} + \frac{L_m}{\sigma L_s L_r \tau_r} \phi_{\alpha r} + \frac{L_m}{\sigma L_s L_r} P \Omega \phi_{\beta r} + \frac{V_{\alpha s}}{\sigma L_s} \\
\dot{i}_{\beta s} = & -a i_{\beta s} - \frac{L_m}{\sigma L_s L_r} P \Omega \phi_{\alpha r} + \frac{L_m}{\sigma L_s L_r \tau_r} \phi_{\beta r} + \frac{V_{\beta s}}{\sigma L_s} \\
\dot{\phi}_{\alpha r} = & -P \Omega \phi_{\beta r} + \frac{L_m}{\tau_r} i_{\alpha s} - \frac{1}{\tau_r} \phi_{\alpha r} \\
\dot{\phi}_{\beta r} = & P \Omega \phi_{\alpha r} + \frac{L_m}{\tau_r} i_{\beta s} - \frac{1}{\tau_r} \phi_{\beta r} \\
\dot{\Omega} = & \frac{P L_m}{L_r J} (i_{\beta s} \phi_{\alpha r} - i_{\alpha s} \phi_{\beta r}) - \frac{f}{J} \Omega - \frac{T}{J}
\end{aligned} \tag{31}$$

with $V_{\alpha s}, V_{\beta s}$ are stator voltage components. $\phi_{\alpha r}, \phi_{\beta r}$ are the rotor flux components. Ω is the mechanical speed. T is the load torque. $i_{\alpha s}, i_{\beta s}$ are stator current components. The currents $i_{\alpha s}, i_{\beta s}$ are assumed to be measured.

By applying the following change of variable:

$$\begin{aligned}
z_1 = & i_{\alpha s} \\
z_2 = & i_{\beta s} \\
z_3 = & \frac{L_m}{\sigma L_s L_r \tau_r} \phi_{\alpha r} + \frac{L_m}{\sigma L_s L_r} P \Omega \phi_{\beta r} \\
z_4 = & -\frac{L_m}{\sigma L_s L_r} P \Omega \phi_{\alpha r} + \frac{L_m}{\sigma L_s L_r \tau_r} \phi_{\beta r} \\
z_5 = & \dot{z}_3 \\
z_6 = & \dot{z}_4
\end{aligned} \tag{32}$$

the system (31) becomes as follows:

$$\begin{aligned}
\dot{z}_1 &= -az_1 + z_3 + \frac{V_{\alpha s}}{\sigma L_s} \\
\dot{z}_2 &= -az_2 + z_4 + \frac{V_{\beta s}}{\sigma L_s} \\
\dot{z}_3 &= z_5 \\
\dot{z}_4 &= z_6 \\
\dot{z}_5 &= z_7 \\
\dot{z}_6 &= z_8
\end{aligned} \tag{33}$$

A second order sliding mode observer is defined as (Levant [1998], Floquet et al. [2007]):

$$\begin{aligned}
\dot{\hat{z}}_1 &= -az_1 + \tilde{z}_3 + \lambda_1 |z_1 - \hat{z}_1|^{0.5} \text{sign}(z_1 - \hat{z}_1) + \frac{V_{\alpha s}}{\sigma L_s} \\
\dot{\hat{z}}_3 &= \alpha_1 \text{sign}(z_1 - \hat{z}_1) \\
\dot{\hat{z}}_2 &= -az_2 + \tilde{z}_4 + \lambda_2 |z_2 - \hat{z}_2|^{0.5} \text{sign}(z_2 - \hat{z}_2) + \frac{V_{\beta s}}{\sigma L_s} \\
\dot{\hat{z}}_4 &= \alpha_2 \text{sign}(z_2 - \hat{z}_2) \\
\dot{\hat{z}}_3 &= E_1 E_2 (\tilde{z}_5 + \lambda_3 |\tilde{z}_3 - \hat{z}_3|^{0.5} \text{sign}(\tilde{z}_3 - \hat{z}_3)) \\
\dot{\hat{z}}_5 &= E_1 E_2 \alpha_3 \text{sign}(\tilde{z}_3 - \hat{z}_3) \\
\dot{\hat{z}}_4 &= E_1 E_2 (\tilde{z}_6 + \lambda_4 |\tilde{z}_4 - \hat{z}_4|^{0.5} \text{sign}(\tilde{z}_4 - \hat{z}_4)) \\
\dot{\hat{z}}_6 &= E_1 E_2 \alpha_4 \text{sign}(\tilde{z}_4 - \hat{z}_4) \\
\dot{\hat{z}}_5 &= E_1 E_2 E_3 E_4 (\tilde{z}_7 + \lambda_5 |\tilde{z}_5 - \hat{z}_5|^{0.5} \text{sign}(\tilde{z}_5 - \hat{z}_5)) \\
\dot{\hat{z}}_7 &= E_1 E_2 E_3 E_4 \alpha_5 \text{sign}(\tilde{z}_5 - \hat{z}_5) \\
\dot{\hat{z}}_6 &= E_1 E_2 E_3 E_4 (\tilde{z}_8 + \lambda_6 |\tilde{z}_6 - \hat{z}_6|^{0.5} \text{sign}(\tilde{z}_6 - \hat{z}_6)) \\
\dot{\hat{z}}_8 &= E_1 E_2 E_3 E_4 \alpha_6 \text{sign}(\tilde{z}_6 - \hat{z}_6)
\end{aligned} \tag{34}$$

where $E_i = 1$ if $\tilde{z}_i - \hat{z}_i = 0$ else $E_i = 0$ for $i=1, \dots, n$, with $\tilde{z}_1 = z_1$, $\tilde{z}_2 = z_2$. For a suitable choice of the parameters λ_i and α_i : $\alpha_1 > z_{5max}$, $\lambda_1 > (\alpha_1 + z_{5max})\sqrt{\frac{2}{\alpha_1 - z_{5max}}}$, $\alpha_2 > z_{6max}$, $\lambda_2 > (\alpha_2 + z_{6max})\sqrt{\frac{2}{\alpha_2 - z_{6max}}}$...etc (for proof see Levant [1998], Floquet et al. [2007]), the observation errors ($\tilde{z}_i - \hat{z}_i$) tend to zero in finite time, then the speed and the flux are estimated as follows:

From equations (32) we have:

$$\begin{aligned}
z_3 &= b\phi_{\alpha r} + c\Omega\phi_{\beta r} \\
z_4 &= -c\Omega\phi_{\alpha r} + b\phi_{\beta r}
\end{aligned} \tag{35}$$

where: $b = \frac{L_m}{\sigma L_s L_r \tau_r}$, $c = \frac{L_m}{\sigma L_s L_r} P$

By solving the above equations we get:

$$\phi_{\alpha r} = \frac{bz_3 - c\Omega z_4}{b^2 + c^2\Omega^2}$$

$$\phi_{\beta r} = \frac{c\Omega z_3 + bz_4}{b^2 + c^2\Omega^2}$$

By substituting z_3 , z_4 and Ω by their estimates \hat{z}_3 , \hat{z}_4 and $\hat{\Omega}$ we obtain the flux estimates as follows:

$$\hat{\phi}_{\alpha r} = \frac{b\hat{z}_3 - c\hat{\Omega}\hat{z}_4}{b^2 + c^2\hat{\Omega}^2}$$

$$\hat{\phi}_{\beta r} = \frac{c\hat{\Omega}\hat{z}_3 + b\hat{z}_4}{b^2 + c^2\hat{\Omega}^2}$$

By deriving the equations (35) we get:

$$z_5 = \dot{z}_3 = -\frac{1}{\tau_r} z_3 - P\Omega z_4 + b\frac{L_m}{\tau_r} i_{\alpha s} + c\frac{L_m}{\tau_r} \Omega i_{\beta s} + c\phi_{\beta r} \dot{\Omega} \tag{36}$$

$$z_6 = \dot{z}_4 = -\frac{1}{\tau_r} z_4 + P\Omega z_3 + b\frac{L_m}{\tau_r} i_{\beta s} - c\frac{L_m}{\tau_r} \Omega i_{\alpha s} - c\phi_{\alpha r} \dot{\Omega} \tag{37}$$

Finally, by neglecting the speed variation $\dot{\Omega}$, the estimate of the speed is obtained from the above equations as follows:

$$\hat{\Omega} = \frac{\hat{z}_5 + \frac{1}{\tau_r} \hat{z}_3 - b\frac{L_m}{\tau_r} i_{\alpha s}}{c\frac{L_m}{\tau_r} i_{\beta s} - P\hat{z}_4}$$

6. SIMULATION RESULTS

Numerical simulations have been performed to validate the proposed control scheme. The IM parameters are given in the appendix. The controller parameters are chosen as follows: $k_\Omega = 0.5$, $k_\phi = 10$, $k_1 = 10$, $k_2 = 300$, $k_3 = 100$, $k_4 = 100$, $k_d = 700$ and $k_q = 500$. The speed and flux references are fixed at $\Omega_* = 100\text{rad/s}$ and $\phi_{dr}^* = 0.9\text{Wb}$, respectively, also a load disturbance $T = 3\text{N.m}$ is applied. Figure 1 shows the responses of the IM without parameters variations (un-faulty mode), we see that the speed and the flux trajectories converge to their desired references, also the estimated flux and speed converge to their actual values. Figure 2 and 3 show the responses of the IM with rotor resistance variations of $+50\%R_r$ and $+100\%R_r$, respectively. In each case, the controller rejects the rotor resistance variations.

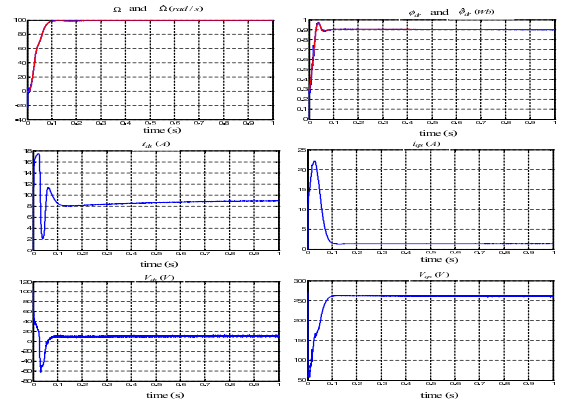


Fig. 1. Responses of the IM in un-faulty mode

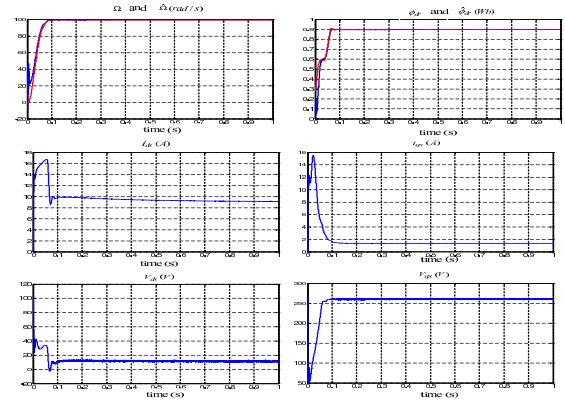


Fig. 2. Responses of the IM with rotor resistance variation of $+50\%R_r$

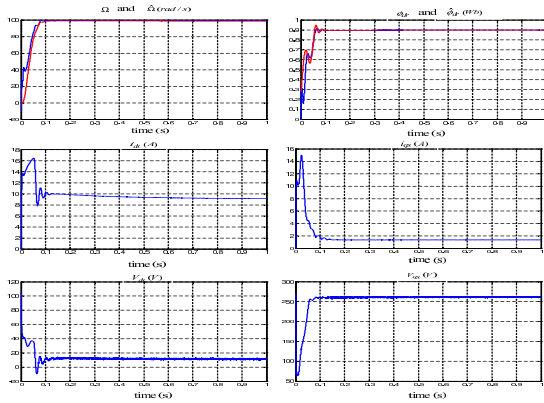


Fig. 3. Responses of the IM with rotor resistance variation of $+100\%R_r$

7. CONCLUSION

In this paper a sensorless fault tolerant controller for IM has been presented. First, a field oriented controller based on backstepping strategy is designed to steer the flux and the speed to their desired references in presence of rotor resistance variations and load torque disturbance. Second, to achieve the sensorless fault tolerant control, a second order sliding mode observer is used to estimate the speed and the flux from the stator currents measurements. The simulation results show the robustness of the proposed control scheme. Certain points remain to be studied. The stability analysis of the closed loop system (observer+controller) and the experimental validation of the proposed control scheme will be included in the future work.

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Appendix

The induction motor used in this work is a $1.5KW$, $U = 220V$, $50Hz$, $I_n = 7.5A$. The parameters are: $R_s = 1.633\Omega$, $R_r = 0.93\Omega$, $L_r = 0.076H$, $L_s = 0.142H$, $L_m = 0.099H$, $J = 0.0111Kg.m^2$, $f = 0.0018N.m/rad/s$ and $P = 2$.