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Enhancing the computation of distributed shortest paths on real dynamic networks*

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Abstract. The problem of finding and updating shortest paths in distributed networks is considered crucial in today’s practical applications. In the recent past, there has been a renewed interest in devising new efficient distance-vector algorithms as an attractive alternative to link-state solutions for large-scale Ethernet networks, in which scalability and reliability are key issues or the nodes can have limited storage capabilities. In this paper we present *Distributed Computation Pruning* (DCP), a new technique, which can be combined with every distance-vector routing algorithm based on shortest paths, allowing to reduce the total number of messages sent by that algorithm and its space occupancy per node. To check its effectiveness, we combined DCP with DUAL (Diffuse Update ALgorithm), one of the most popular distance-vector algorithm in the literature, which is part of CISCO’s widely used EIGRP protocol, and with the recently introduced LFR (Loop Free Routing) which has been shown to have good performances on real networks. We give experimental evidence that these combinations lead to a significant gain both in terms of number of messages sent and memory requirements per node.

1 Introduction

The problem of computing and updating shortest paths in a distributed network whose topology dynamically changes over the time is a core functionality of today’s communication networks. This problem has been widely studied in the literature, and the solutions found are classified as *distance-vector* and *link-state*.

Distance-vector algorithms require that a node knows the distance from each of its neighbors to every destination and stores them in a

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data structure called *routing table*; a node uses its own routing table to compute the distance and the next node in the shortest path to each destination. Most of the known distance-vector solutions (see e.g. [?, ?, ?]) are based on the classical Distributed Bellman-Ford method (DBF), originally introduced in the Arpanet [?], which is still used in real networks and implemented in the RIP protocol [?]. DBF has been shown to converge to the correct distances if the link weights stabilize and all cycles have positive lengths [?]. However, the convergence can be very slow (possibly infinite) due to the well-known *looping* and *count-to-infinity* phenomena.

Link-state algorithms, as for example the *Open Shortest Path First (OSPF)* protocol widely used in the Internet [?], require that a node knows the entire network topology, to compute its distance to any destination, usually running the centralized Dijkstra's algorithm, thus requiring quadratic space per node. Link-state algorithms are free of looping, however each node needs to receive and store up-to-date information on the entire network topology after a change. This is achieved by broadcasting each change of the network topology to all nodes [?] and by using a centralized algorithm for dynamic shortest paths as for example that in [?].

Related works. In the last years, there has been a renewed interest in devising new efficient light-weight distributed shortest paths solutions for large-scale Ethernet networks (see, e.g., [?, ?, ?, ?, ?]), where distance-vector algorithms seem to be an attractive alternative to link-state solutions when scalability and reliability are key issues or when the memory power of the nodes of the network is limited. Notwithstanding this increasing interest, the most important distance vector algorithm is still DUAL (Diffuse Update ALgorithm) [?], which is free of looping and is part of CISCO's widely used EIGRP protocol, although it requires a quite big space occupancy per node. Another distance vector algorithm, named LFR (Loop Free Routing), has been recently proposed in [?]. Compared with DUAL, LFR has the same theoretical message complexity but it uses an amount of data structures per node which is much smaller than that of DUAL. Moreover, it has been experimentally shown to be very effective in terms of both messages sent and memory requirements per node in some real-world networks.

Recently, in [?] a general strategy named DLP (Distributed Leaf Pruning) has been introduced which can be combined with every distance vector algorithm with the aim of reducing the number of messages sent by that algorithm. In particular, DLP is able to avoid any distributed computation involving degree-one nodes. In [?] the effectiveness of DLP has

been confirmed by combining it with DUAL and by running experiments on real-world and artificial instances.

Results of the paper. In this paper, we provide a new technique, named *Distributed Computation Pruning* (DCP), which is a generalization of DLP and can be combined with every distance-vector algorithm with the aim of overcoming some of their main limitations in real-world networks (high number of messages sent, high space occupancy per node, low scalability, poor convergence). DCP has been designed to be efficient mainly in networks following a power-law node degree distribution, which from now on will be referred as *power-law networks*. The main idea underlying DCP rely on the fact that a power-law network with n nodes typically has average node degree much smaller than n and a high number of nodes with small degree (less than 3). Nodes with small degree often do not provide any useful information for the distributed computation of shortest paths, that is there are many topological situations in which these nodes should neither perform nor be involved in any kind of distributed computation, as their shortest paths depend on those of higher degree nodes.

In order to check the effectiveness of DCP, we combined it with DUAL and LFR by obtaining two new algorithms named DUAL-DCP and LFR-DCP, respectively. Then, we implemented the two new algorithms in the OMNeT++ simulation environment [?], a network simulator which is widely used in the literature. We also implemented DUAL, LFR, DUAL-DLP and LFR-DLP, where the last two algorithms are the combination of DUAL and LFR with DLP [?]. As input to the algorithms, we considered instances of power-law networks similar to those used in [?] and [?], that is the Internet topologies of the *CAIDA IPv4 topology dataset* [?] (CAIDA, Cooperative Association for Internet Data Analysis, is an association which provides data and tools for the analysis of the Internet infrastructure) and the random topologies generated by the *Barabási-Albert* algorithm [?].

The results of our experiments can be summarized as follows: the combination of DUAL and LFR with DCP provides a huge improvement in the number of messages sent with respect to DUAL and LFR, respectively. In particular, on the CAIDA instances, the number of messages sent by DUAL-DCP is always between 3% and 16% that of DUAL, while the number of messages sent by LFR-DCP is always between 10% and 26% that of LFR. The gain is significant also with respect to DUAL-DLP and LFR-DLP. In particular, DUAL-DCP sends a number of messages which is between 11% and 40% that of DUAL-DLP, while

LFR-DCP sends a number of messages which is between 21% and 58% that of LFR-DLP. We observed also an improvement in the maximum space occupancy per node of DUAL-DCP and LFR-DCP, and in the average space occupancy per node of DUAL-DCP. This is due to the fact that nodes with small degree do not need to store some of the data structures implemented by DUAL and LFR, respectively. We obtained similar results also for the *Barabási-Albert* instances.

2 Preliminaries

We consider a network made of processors linked through communication channels that exchange data using a message passing model, in which: each processor can send messages only to its neighbors; messages are delivered to their destination within a finite delay but they might be delivered out of order; there is no shared memory among the nodes; the system is asynchronous, that is, a sender of a message does not wait for the receiver to be ready to receive the message. We are interested in the practical case of networks whose topologies dynamically change over the time due to update operations on the edges (weight increase, weight decrease, insert, delete).

Graph notation. We represent a network by an undirected weighted graph $G = (V, E, w)$, where V is a finite set of n nodes, one for each processor, E is a finite set of m edges, one for each communication channel, and w is a weight function $w : E \rightarrow \mathbb{R}^+$ that assigns to each edge a real value representing the optimization parameter associated to the corresponding channel. An edge in E that links nodes $u, v \in V$ is denoted as $\{u, v\}$. Given $v \in V$, $N(v)$ denotes the set of neighbors of v , and $deg(v) = |N(v)|$ denotes the degree of v . The maximum degree of the nodes in G is denoted by $maxdeg$. A path P in G between nodes u and v is denoted as $P = \{u, \dots, v\}$. The *weight* of P , denoted as $w(P)$ is the sum of the weights of the edges in P . A *shortest path* between nodes u and v is a path from u to v with the minimum weight. The *distance* $d(u, v)$ from u to v is the weight of a shortest path from u to v . Given two nodes $u, v \in V$, the *via* from u to v is the set of neighbors of u that belong to a shortest path from u to v . Formally: $via(u, v) \equiv \{z \in N(u) \mid d(u, v) = w(u, z) + d(z, v)\}$. Given a time t , we denote as $w^t()$, $d^t()$, and $via^t()$ the edge weight, the distance, and the via at time t , respectively. We denote a sequence of update operations on the edges of G by $\mathcal{C} = (c_1, c_2, \dots, c_k)$. Assuming $G_0 \equiv G$, we denote as G_i , $0 \leq i \leq k$, the graph obtained by applying c_i to G_{i-1} . We con-

sider the case that operation c_i either increases or decreases the weight of an existing edge in G_i . The extension to *delete* and *insert* operations is straightforward.

Distance-vector algorithms. Given a graph $G = (V, E, w)$, distance-vector routing algorithms based on shortest-paths usually share a set of common features. In detail, a generic node v of G : (i) knows the identity of every other node of G , the identity of all its neighbors and the weights of the edges incident to it; (ii) maintains and updates its own routing table that has one entry for each $s \in V$, which consists of at least two fields: $D[v, s]$, the estimated distance between v and s , and $VIA[v, s]$, the neighbor used to forward data from v to s ; (iii) handles edge weight increases and decreases either by a single procedure (see, e.g., [?]), which we denote as `WEIGHTCHANGE`, or separately (see, e.g., [?, ?]) by two procedures, which we denote as `WEIGHTINCREASE` and `WEIGHTDECREASE`; (iv) asks information to its neighbors through a message denoted as *query*, receives replies by them through a message denoted as *reply*. If the routing information on a node changes, a distance vector algorithm propagates such a variation as follows:

- if v is performing `WEIGHTCHANGE`, then it sends to its neighbors a message, from now on denoted as *update*; a node that receives this kind of message executes a procedure named `UPDATE`;
- if v is performing `WEIGHTINCREASE` or `WEIGHTDECREASE`, then it sends to its neighbors message *increase* or *decrease*, resp.; a node that receives *increase/decrease* executes a procedure named `INCREASE/DECREASE`, respectively.

Power-Law networks. Power-law networks are very important in practice and includes many of the currently implemented communication infrastructures, like the Internet, the World Wide Web, some social networks, and so on [?]. Practical examples of power-law networks are the Internet topologies of the *CAIDA IPv4 topology dataset* [?]. The CAIDA dataset is collected by a globally distributed set of monitors. The monitors collect data by sending probe messages continuously to destination IP addresses. Destinations are selected randomly from each routed IPv4/24 prefix on the Internet such that a random address in each prefix is probed approximately every 48 hours. The current prefix list includes approximately 7.4 million prefixes. For each destination selected, the path from the source monitor to the destination is collected, in particular, data collected for each path probed includes the set of IP addresses of the hops which form the path and the Round Trip Times (RTT) of both inter-

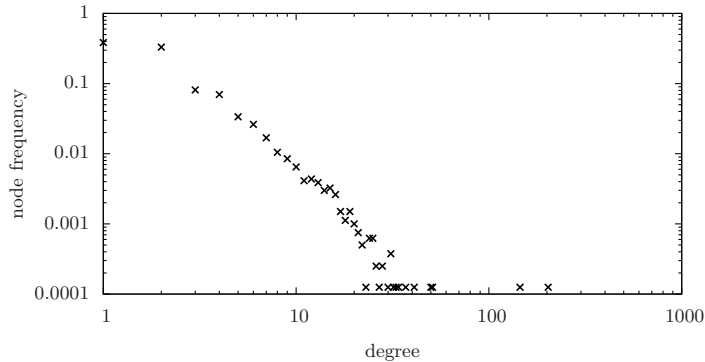


Fig. 1: Power-law node degree distribution of a *CAIDA* graph with 8000 nodes and 11141 edges

mediate hops and the destination. In Fig. 1 we report the node degree distributions of a CAIDA network.

3 Dynamic scenarios

In this section, we introduce some preliminary definitions that are useful to capture the possible dynamic scenarios typical of power-law networks and we show some properties of shortest paths in these scenarios. Given an undirected weighted graph $G = (V, E, w)$, we classify the nodes of G with respect to their degree as follows. A node $v \in V$ is:

- *central* if $\deg(v) \geq 3$;
- *peripheral* if $\deg(v) = 1$;
- *semiperipheral* if $\deg(v) = 2$.

An edge $\{u, v\}$ of G is:

- *central* if both u and v are central;
- *peripheral* if either u or v is peripheral;
- *semiperipheral* if either u or v is semiperipheral and neither of them is peripheral.

A path $P = \{v_0, v_1, \dots, v_{j-1}\}$ in G is:

- *central* if it is made only of central edges;
- *peripheral* if it contains exactly one peripheral edge and exactly one central node; the unique central node of P is called *owner* of P ;

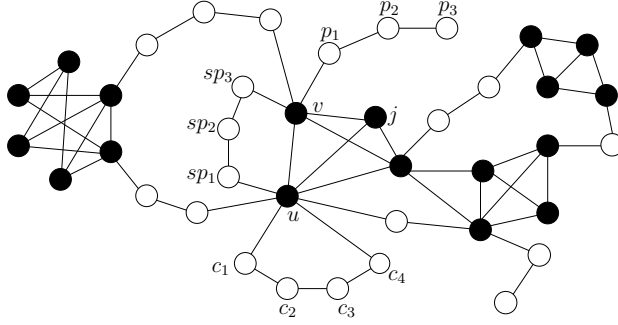


Fig. 2: A graph G and its corresponding nodes classification.

- *semiperipheral* if it is formed only by semiperipheral edges. If v_0 and v_{j-1} are two distinct central nodes, then they are called *semiowners* of P . If $v_0 \equiv v_{j-1}$, then P is a *semiperipheral cycle*, and $v_0 \equiv v_{j-1}$ is called the *cycleowner* of P .

In Fig. 2 we report an example of a graph G and its nodes classification. Central nodes are drawn in black while the non-central ones are drawn in white. The path $\{u, j, v\}$ is a central path, the path $\{v, p_1, p_2, p_3\}$ is a peripheral path whose owner is v , the path $\{u, sp_1, sp_2, sp_3, v\}$ is a semiperipheral path whose semiowners are u and v , while the path $\{u, c_1, c_2, c_3, c_4, u\}$ is a semiperipheral cycle whose cycleowner is u .

The following lemmata introduce some basic relationships between central and non-central shortest paths of the network.

Lemma 1 (Peripheral shortest paths). *Given a graph $G = (V, E, w)$, let $P = \{v, p_1, \dots, p_{j-1}\}$ be a peripheral path of G whose owner is node v , and let $P' = \{v, p_1, \dots, p_i\}$, $1 \leq i \leq j - 1$, be a sub-path of P containing v . Then, for each $x \in V \setminus \{p_1, \dots, p_{j-1}\}$, $d(x, p_i) = d(x, v) + w(P')$.*

Proof. Let us assume, by contradiction, that $d(x, p_i) \neq d(x, v) + w(P')$. Then, two cases may arise: $d(x, p_i) > d(x, v) + w(P')$ or $d(x, p_i) < d(x, v) + w(P')$. In the first case, it follows that $d(x, p_i)$ is not a distance, which is a contradiction. In the second case, it follows that there must exist at least two different paths with different weights from x to p_i , which is again a contradiction as p_i belongs to a peripheral path and P' is the shortest path between v and p_i in G . \square

Lemma 2 (Semi-peripheral shortest paths). *Given a graph $G = (V, E, w)$, let $S = \{u, sp_1, \dots, sp_{j-2}, v\}$ be a semiperipheral path of G whose*

semiowners are nodes u and v , and let $S' = \{u, sp_1, \dots, sp_i\}$, $1 \leq i \leq j - 2$, and $S'' = \{sp_i, \dots, sp_{j-2}, v\}$ be two sub-paths of S , containing u and v , respectively. Then, for each $x \in V \setminus \{sp_1, \dots, sp_{j-2}\}$, $d(x, sp_i) = \min\{d(x, u) + w(S'), d(x, v) + w(S'')\}$.

Proof. By contradiction, assume that $d(x, sp_i) \neq \min\{d(x, u) + w(S'), d(x, v) + w(S'')\}$. Two cases may occur: $d(x, sp_i) > \min\{d(x, u) + w(S'), d(x, v) + w(S'')\}$ or $d(x, sp_i) < \min\{d(x, u) + w(S'), d(x, v) + w(S'')\}$. In the first case, it follows that $d(x, sp_i)$ is not a distance, which is a contradiction. In the second case, it follows that there must exist a third different path from x to sp_i , with different weight, which is a contradiction, as sp_i is a semiperipheral node. \square

Lemma 3 (Semi-peripheral cycle shortest paths). *Given a graph $G = (V, E, w)$, let $C = \{u, c_1, \dots, c_{j-1}, u\}$ be a semiperipheral cycle of G whose cycleowner is node u , and let $C' = \{u, c_1, \dots, c_i\}$ and $C'' = \{c_i, \dots, c_{j-1}, u\}$, $1 \leq i \leq j - 1$, be two sub-paths of C . Then, for each $x \in V \setminus \{c_1, \dots, c_{j-1}\}$, $d(x, c_i) = \min\{d(x, u) + w(C'), d(x, u) + w(C'')\}$.*

Proof. The proof is similar to that of Lemma 2 \square

Some useful additional relationships can be derived introducing time instants in the above Lemmata. In particular, by Lemma 1 we know that, if between the time instants t_i and t_{i+1} the weight of the edge $\{p_1, p_2\}$ between two nodes belonging to a peripheral path $P = \{v, \dots, p_1, p_2, \dots, p_{j-1}\}$ changes, that is $w^{t_i}(p_1, p_2) \neq w^{t_{i+1}}(p_1, p_2)$, then for each $x \in V$ that does not belong to P , the distance from p_1 to x does not change, while the distance from p_2 to x changes as follows:

$$d^{t_{i+1}}(p_2, x) = d^{t_i}(p_2, x) + w^{t_{i+1}}(p_1, p_2) - w^{t_i}(p_1, p_2) \quad (1)$$

By Lemma 2 we know that, if between the time instants t_i and t_{i+1} the weight of the edge $\{sp_1, sp_2\}$ between two nodes belonging to a semiperipheral path $S = \{u, \dots, sp_1, sp_2, \dots, v\}$ changes, that is $w^{t_i}(sp_1, sp_2) \neq w^{t_{i+1}}(sp_1, sp_2)$, then for each $x \in V$, both the distances from sp_1 to x and from sp_2 to x change as follows:

$$d^{t_{i+1}}(sp_1, x) = \min_{z \in N(sp_1)} \{d^{t_{i+1}}(z, x) + w^{t_{i+1}}(sp_1, z)\} \quad (2)$$

$$d^{t_{i+1}}(sp_2, x) = \min_{z \in N(sp_2)} \{d^{t_{i+1}}(z, x) + w^{t_{i+1}}(sp_2, z)\} \quad (3)$$

Let us assume that, between t_i and t_{i+1} , the weight of the edge $\{c_1, c_2\}$ between two nodes belonging to a semiperipheral cycle $C =$

$\{u, \dots, c_0, c_1, c_2, c_3, \dots, u\}$ changes, that is $w^{t_i}(c_1, c_2) \neq w^{t_{i+1}}(c_1, c_2)$. If we denote as $C_0 = (u, \dots, c_0, c_1)$, $C_1 = (c_1, c_2, \dots, u)$, $C_2(u, \dots, c_1, c_2)$ and $C_3 = (c_2, c_3, \dots, u)$ then by Lemma 3, for each $x \in V$, the distances from c_1 to x and from c_2 to x change as follows:

$$d^{t_{i+1}}(c_1, x) = d^{t_i}(x, u) + \min\left\{ \sum_{\{l,q\} \in C_0} w^{t_{i+1}}(l, q), \sum_{\{l,q\} \in C_1} w^{t_{i+1}}(l, q) \right\} \quad (4)$$

$$d^{t_{i+1}}(c_2, x) = d^{t_i}(x, u) + \min\left\{ \sum_{\{l,q\} \in C_2} w^{t_{i+1}}(l, q), \sum_{\{l,q\} \in C_3} w^{t_{i+1}}(l, q) \right\} \quad (5)$$

If the distance between a generic node $x \in V$ and a central node c changes between the time instants t_i and t_{i+1} (that is, $d^{t_{i+1}}(x, c) \neq d^{t_i}(x, c)$), then the following relationships hold:

- by Lemma 1, for each peripheral path $P = \{c, \dots, \bar{p}, \dots, p_{j-1}\}$ with owner c , and for each $\bar{p} \in P$:

$$d^{t_{i+1}}(x, \bar{p}) = d^{t_i}(x, \bar{p}) + d^{t_{i+1}}(x, c) - d^{t_i}(x, c), \quad (6)$$

- by Lemma 2, for each semiperipheral path $S = \{c, \dots, \bar{sp}, \dots, d\}$ with semiowners c and d and for each $\bar{sp} \in S$ such that c belongs to the shortest path from \bar{sp} to x at time t_i , if we denote as $D = (d, \dots, \bar{sp})$ the sub-path of S from d to \bar{sp} , then:

$$d^{t_{i+1}}(x, \bar{sp}) = \min\{d^{t_{i+1}}(x, \bar{sp}) + d^{t_{i+1}}(x, c) - d^{t_i}(x, c), d^{t_i}(x, d) + \sum_{\{l,q\} \in D} w^{t_i}(l, q)\}$$

- by Lemma 3, for each cyclic path $C = \{c, c_1, \dots, \bar{c}, \dots, c_{j-1}, c\}$ with cycleowner c , and for each $\bar{c} \in C$:

$$d^{t_{i+1}}(x, \bar{c}) = d^{t_i}(x, \bar{c}) + d^{t_{i+1}}(x, c) - d^{t_i}(x, c), \quad (8)$$

4 The new technique

Distributed Computation Pruning (DCP) has been designed to be efficient mainly in power-law networks, by forcing the distributed computation to be carried out only by the central nodes, which are few in practice. The non-central nodes, which are the great majority in power-law networks, receive updates about routing information passively from the respective owners, without starting any kind of distributed computation. Then, the larger is the set of non-central nodes of the network, the bigger

is the improvement in the pruning of the distributed computation and, consequently, in the global number of messages sent.

Data structures. Given a generic distance-vector algorithm **A**, DCP requires that a generic node of G stores some additional information with respect to those required by **A**. In particular, a node v needs to store and update information about non-central paths of G . To this aim, v maintains a data structure called *ChainPath*, denoted as CHP_v , which is an array containing one entry $\text{CHP}_v[s]$, for each central node s . $\text{CHP}_v[s]$ stores the list of all edges, with the corresponding weight, belonging to the non-central paths containing s .

A central node is obviously not present in any list of CHP_v . A peripheral node is present in exactly one list $\text{CHP}_v[s]$, where $s \in V$ is its owner. A semi-peripheral node is present in exactly two lists $\text{CHP}_v[v_0]$ and $\text{CHP}_v[v_{j-1}]$, if it belongs to a semi-peripheral path (v_0 and v_{j-1} are its semi-owners), while it is present in a single list $\text{CHP}_v[v_0]$, if it belongs to a semi-peripheral cycle (v_0 is its cycle-owner). The space occupancy overhead per node due to *ChainPath* can be quantified using the following observations:

- the *ChainPath* contains at most as many entries as the number of the central nodes;
- the sum of the sizes of all the lists in the *ChainPath* is twice the number of non-central edges of G in the worst case;
- the number of non-central edges of G is $O(n)$, as they belong to paths in which every node has degree at most two.

Hence, the space overhead per node due to CHP_v is $O(n)$. Note that, despite the overhead due to the *ChainPath* data structure, the use of DCP can induce a decrease in the space occupancy per node required by **A** for the following observations: (i) in most of the cases nodes do not ask and do not need to store information received from non-central nodes; (ii) computations which involves the whole network are performed only with respect to central destinations. In Section 5 we will experimentally confirm this behavior.

Distributed Computation Pruning. The combination of DCP with a distance vector algorithm **A** induces a new algorithm denoted as **A-DCP**. The behavior of **A-DCP** can be summarized as follows. While in a classic routing algorithm every node performs the same code thus having the same behavior, in **A-DCP** central and non-central nodes have different behaviors. In particular, central nodes detect changes concerning all kind

of edges, while semiperipheral, peripheral and cyclic nodes detect changes concerning only semiperipheral, peripheral and cyclic edges, respectively.

If the weight of a central edge $\{u, v\}$ changes, then node u (v , resp.) performs the procedure provided by **A** for the distributed computation of the shortest paths, only with respect to central nodes. During this computation, if u (v) needs information by its neighbors, it asks only to central neighbors or, if u (v) is the semiowner of one or more semiperipheral paths, it asks information also to the other semiowner of each semiperipheral path, by means of a strategy we called *Mod-DBF*. In detail, node u (v) sends to each semiperipheral neighbor a *queryDBF* message, whose aim is to traverse the semiperipheral path, in order to get information by the other semiowner. The *queryDBF* message contains just one field, the source object of the computation. A semiperipheral node, which receives a *queryDBF* message from one of its two neighbors, simply performs a store-and-forward step and sends a *queryDBF* message to the other neighbor. A central node, which receives a *queryDBF* message, simply replies the information that *queryDBF* is asking for. Once u (v) has updated its own routing information, it propagates the variation to all its neighbors through the *update*, *increase* or *decrease* messages of **A**. When a generic node x receives an *update*, *increase* or *decrease* message, it stores the current value of $D[x, s]$ in a temporary variable.

Now, if x is a central node, then it handles the change and updates its routing information toward s , by using the proper procedure of **A** (UPDATE, INCREASE, or DECREASE) and propagates the new information to its neighbors. Otherwise, if x is a peripheral, semiperipheral or cyclic node, it handles the change and updates its routing information toward s by using Lemmata 1–3, and the data provided by its owner, semiowner and cycleowner, respectively. At the end, x verifies whether the routing table entry of s is changed or not and, in the affirmative case, it updates the routing information about the non-central neighbors of s , if they exist, by implementing Equations 6–8. Note that, node x uses the data contained in **CHP** in order to properly update its routing information towards the non-central nodes of s , if they exist.

If a weight change occurs on a peripheral edge $\{u, v\}$, then nodes u and v both send a $p_change(u, v, w(u, v))$ message to each of their neighbors. When a generic node x receives message *p_change*, it first verifies whether the update has been already processed or not, by comparing the new value of $w(u, v)$ with the one stored in its **CHP**. In the first case the message is discarded. Otherwise, node x updates its **CHP** with the updated value of $w(u, v)$ and its routing information by using Equation 1. Then,

it propagates the change by a flooding algorithm to forward the message over the network.

If the weight of a semiperipheral edge $\{u, v\}$ changes, then node u (v resp.) sends two kind of messages: a $sp_change(u, v, w(u, v))$, to each of its owners, and a $sp_update(s, D[u, s])$ ($sp_update(s, D[v, s])$) to v (u), for each s such that $VIA[u, s] \neq v$ ($VIA[v, s] \neq u$). When a generic node x receives message sp_change , it first verifies whether the update has been already processed or not, by comparing the new value of $w(u, v)$ with the one stored in its CHP. In the first case the message is discarded. Otherwise, node x simply updates its CHP with the updated value of $w(u, v)$. When a generic node x receives a $sp_update(s, D[u, s])$ message from a neighbor u , two cases can occur. If x is a central node, it simply performs procedure *update* of **A**. Otherwise, it updates routing information towards s by using Equations 2–3. Note that, in this case, node x uses the information contained in CHP in order to verify whether it belongs or not to the same semiperipheral path of s and to properly update its routing information.

If the weight of a cyclic edge $\{u, v\}$ changes, nodes u and v both send a $cy_update(u, v, w(u, v))$ message to each of their neighbors. When a generic node x receives message cy_update , it first verifies whether the update has been already processed or not, by comparing the new value of $w(u, v)$ with the one stored in its CHP. In the first case the message is discarded. Otherwise, node x updates its CHP with the updated value of $w(u, v)$ and its routing information by using Equations 4–5. Then, it propagates the change by a flooding algorithm to forward the message over the network.

5 Experimental analysis

In this section we report the results of our experimental study on DUAL, LFR, DUAL-DLP, LFR-DLP, DUAL-DCP and LFR-DCP. Our experiments have been performed on a workstation equipped with a Quad-core 3.60 GHz Intel Xeon X5687 processor, with 12MB of internal cache and 24 GB of main memory, and consist of simulations within the OM-NeT++ 4.0p1 environment [?]. The programs have been compiled with GNU g++ compiler 4.4.3 under Linux (Kernel 2.6.32).

Executed tests. For the experiments we used the power-law networks of the *CAIDA IPv4 topology dataset* [?]. We parsed the files provided by CAIDA to obtain a weighted undirected graph, denoted as G_{IP} , where a node represents an IP address in the dataset (both source/destination hosts and intermediate hops), edges represent links among hops and

weights are given by Round Trip Times. As the graph G_{IP} consists of almost 35000 nodes, we could not use it for the experiments, as the amount of memory required to store the routing tables of all the nodes is $O(n^2 \cdot maxdeg)$ for DUAL. Hence, we performed our tests on connected subgraphs of G_{IP} , with a variable number of nodes and edges, induced by the settled nodes of a breadth first search starting from a node taken at random. We denoted a h nodes subgraph of G_{IP} with G_{IP-h} . We generated a set of different tests, each test consists of a subgraph of G_{IP} and a set of k edge updates, where k assumes values in $\{5, 10, \dots, 200\}$. An edge update consists of multiplying the weight of a random selected edge by a percentage value randomly chosen in $[50\%, 150\%]$. For each test configuration (a graph with a fixed value of k) we performed 5 different experiments (for a total amount of 200 runs) and we report average values.

Analysis. We ran simulations on CAIDA instances with different number of nodes $n \in \{1200, 5000, 8000\}$. The results of our experiments on the different instances are similar, hence we report those on the bigger instances, which has 8000 nodes and 11141 edges.

In particular, in Figures 3(left) and 3(right) we report the number of messages sent by DUAL, DUAL-DLP and DUAL-DCP and by LFR, LFR-DLP and LFR-DCP, respectively, on $G_{IP-8000}$. Notice that, $G_{IP-8000}$ has average node degree equal to 2.8, a percentage of degree 1 nodes approximately equal to 38.5%, and a percentage of degree 2 nodes approximately equal to 33%. The figures show that the combinations of DUAL and LFR with DCP provide a huge improvement in the global number of messages sent. The gain is significant also with respect to DUAL-DLP and LFR-DLP. In the tests of Fig. 3(left) the ratio between the number of messages sent by DUAL-DCP and DUAL is within 0.03 and 0.16 which means that DUAL-DCP sends a number of messages which is between 3% and 16% that of DUAL. Similarly, the ratio between the number of messages sent by DUAL-DCP and DUAL-DLP is within 0.11 and 0.40. In the tests of Fig. 3(right) the ratio between the number of messages sent by LFR-DCP and LFR is within 0.10 and 0.26 which means that the number of messages sent by LFR-DCP is always between 10% and 26% that of LFR. Similarly, the ratio between the number of messages sent by LFR-DCP and LFR-DLP is within 0.21 and 0.58.

To conclude our analysis, we consider the space occupancy per node of each algorithm. The results are summarized in Table 1 where we report the maximum and the average space occupancy per node, in Bytes, of each algorithm on $G_{IP-8000}$. We also report the ratio between the space

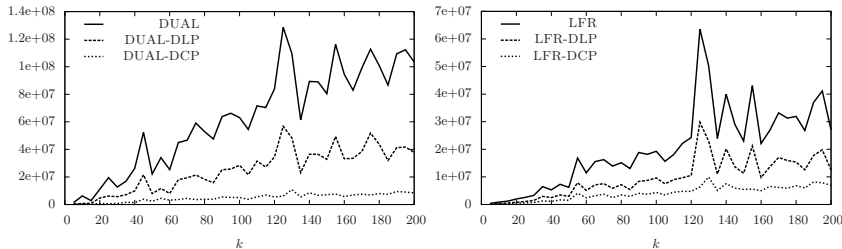


Fig. 3: Number of messages sent by DUAL, DUAL-DLP and DUAL-DCP (left) and by LFR, LFR-DLP and LFR-DCP (right) on $G_{IP-8000}$.

occupancy per node of the algorithms integrating DLP and DCP and that of the original algorithms, for each test instance. Note that, since the space occupancy per node of LFR, LFR-DLP and LFR-DCP depends on the number of weight change operations, we show median values for each of these algorithms.

Our experiments show that the use of DCP induces, in most of the cases, a clear improvement also in the space requirements per node. In particular, DUAL-DCP (LFR-DCP) requires a maximum space occupancy per node which is 0.30 (0.72) and 0.29 (0.83) times that of DUAL (LFR) in $G_{IP-8000}$ and $G_{BA-8000}$, respectively. Notice that, the improvement is more evident in the case of DUAL, as its maximum space occupancy per node is by far higher than that of LFR. Concerning DUAL, this behavior is confirmed also in the average case, where DUAL-DCP requires 0.81 and 0.92 times the average space occupancy per node of DUAL, in $G_{IP-8000}$ and $G_{BA-8000}$, respectively. On the contrary, our data show that the average space occupancy per node of LFR-DCP is slightly greater than that of LFR and that the use of DCP induces an overhead in the average space occupancy per node which is equal to 53% and 77%, in $G_{IP-8000}$ and $G_{BA-8000}$, respectively. This is due to the fact that the average space occupancy of LFR is quite low by itself and that, in this case, the space occupancy overhead needed to store the *ChainPath* is greater than the space occupancy reduction induced by the use of DCP. As a final remark, notice that, the use of DCP represents an improvement in the maximum space occupancy per node also with respect to the use of DLP (See Table 1).

Graph	Algorithm	MAX		AVG	
		Bytes	Ratio	Bytes	Ratio
$G_{IP-8000}$	DUAL	8 320 000	1	311 410	1
	DUAL-DLP	5 161 984	0.62	240 754	0.77
	DUAL-DCP	2 517 680	0.30	252 625	0.81
$G_{IP-8000}$	LFR	549 170	1	192 871	1
	LFR-DLP	421 862	0.77	204 675	1.06
	LFR-DCP	392 658	0.72	295 930	1.53

Table 1: Space occupancy per node of the implemented algorithms.

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