A Fine-grained Approach for Power Consumption Analysis and Prediction

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Abstract: Power consumption has became a critical concern in modern computing systems for various reasons including financial savings and environmental protection. With battery powered devices, we need to care about the available amount of energy since it is limited. For the case of supercomputers, as they imply a large aggregation of heavy CPU activities, we are exposed to a risk of overheating. As the design of current and future hardware is becoming more and more complex, energy prediction or estimation is as elusive as that of time performance. However, having a good prediction of power consumption is still an important request to the computer science community. Indeed, power consumption might become a common performance and cost metric in the near future. A good methodology for energy prediction could have a great impact on power-aware programming, compilation, or runtime monitoring. In this paper, we try to understand from measurements where and how power is consumed at the level of a computing node. We focus on a set of basic programming instructions, more precisely those related to CPU and memory. We propose an analytical prediction model based on the hypothesis that each basic instruction has an average energy cost that can be estimated on a given architecture through a series of micro-benchmarks. The considered energy cost per operation includes all of the overhead due to context of the loop where it is executed. Using these precalculated values, we derive an linear extrapolation model to predict the energy of a given algorithm expressed by means of atomic instructions. We then use three selected applications to check the accuracy of our prediction method by comparing our estimations with the corresponding measurements obtained using a multimeter. We show a 9.48% energy prediction on sorting.

Key-words: power consumption, energy, multimeter, prediction, profiling

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Résumé : Ce travail concerne la prédiction de la consommation énergetique d'un programme à partir d'un décompte des différentes instructions élémentaires du code source. Nous nous intéressons principalement aux nids de boucles et à une classe d'instructions assez représentative de celles les plus utilisées habituellement.

Mots-clés : energy, complexité, multimètre, statistique

I. INTRODUCTION

While keep striving to provide faster computers, hardware designers have to contend with power and heat constraints [1]. For decades, computers got faster by increasing the speed of the central processing unit, now commonly made up with several cores. However, high processor frequency means higher heat potential. This concern is central when it come to supercomputers [2], [3], for which we have a large aggregation of heavy CPU activities, thus a genuine risk of overheating. The cost associated to the required energy, also for cooling, can become financially prohibitive for larger systems. Beyond petascale, the way to exascale is marked by energy concerns, and power consumption is becoming a metric. A clear illustration of the fact that energy has come to the spotlight is the so-called *Green500* project, which aims at providing a yearly ranking of the most energy-efficient supercomputers in the world.

For embedded systems or portable devices, which are battery powered, energy is obviously critical since available on a limited basis. The pervasiveness of portable devices will magnify and exacerbate this issue.

Cloud computing is another area where energy is an important concern. Indeed, computing and storage devices are continuously requested by different users. Such intensive use of resources implies a significant power consumption at various levels. One way to address the problem is through the concept of *federated clouds*, where different clouds are virtually merged in order to provide a flexible system to end users. Based on this configuration, we need to find the less (energy/time) costly scheduling from both users and providers standpoints.

Fig. 1. Cloud computing illustration

Based on Ohm's Law [4], the *dissipated power* is approximately proportional to the square of the CPU voltage and the CPU frequency, which gives

$$P = CV^2 f, \qquad (1)$$

where C is *capacitance*, V is *voltage*, and f is *frequency* [5]. It is important to note that those parameters can be changed dynamically at runtime [6], which offers an opportunity for energy-aware scheduling. Network and memory activities also count, but the most common focus is on the pure CPU side.

Energy reduction is an important research topic, which is being investigated at all levels of system abstraction, from the physical layout to software design. There have been several contributions on energy saving focused on scheduling/processors [3], [6], [7], [8], [9], data organizations [10], [11], compilation [12], [13], [14], and the algorithmic level [15], [16], [6]. Power management in sensors network, where energy is really critical, is addressed in [17]. The research at the architecture level has led to new and advanced low energy architectures. Current and future generation processors have their clock frequency that can be dynamically modified, and some of them are equipped with a sensor to measure the temperature. In addition, the upper threshold temperature beyond which the fan is automatically triggered can be dynamically adjusted too. However, all these features need to be skillfully monitored. This could be done statically at compile time, or dynamically at runtime.

In order to guide the design of energy efficient programs or power aware schedulers, it is important to have a clear methodology for power consumption modeling and estimation. In [18], an analytical model, based on a mathematical programming formulation, is provided for energy optimization related to fully featured SDRAM. In this work, we consider the problem at source code level. Our hypothesis is that, although the correlation between hardware mechanisms, the energy cost of each basic CPU operation can be estimated and used as a parameter for a macroscopic prediction. The main advantage is that, from an inventory of the basic operations contained in a given source code, its power consumption can be estimated by a linear approximation. We measure the energy directly from the electricity entry of the computer using a commercial multi meter, which is more general than focusing only on information related to the CPU.

The rest of the paper is organized as follows. The next section provided an overview of the related work. Our energy measurement methodology is explained in section III, and data are provided for a given machine. In section IV, we present our prediction model, followed in section V by an experimental validation. Section VI provides potential perspectives for this work, and section VII concludes the paper.

II. RELATED WORK

There are many techniques in the literature that aim to improve the energy efficiency of computing resources. Most of them are based on Dynamic Voltage and Frequency Scaling (DVFS) [19], [20], [21]. DVFS techniques assume that applications dominated by memory accesses or involving heavy I/O activities can be executed at lower CPU frequency with only a marginal impact on their execution time. In this case, the goal of a DVFS scheduler is to identify each execution phase of

an application, quantify its workload characteristics, and then switch the CPU frequency to the most appropriate power/performance mode. There are also some works [22], [23], [24], [25] that consider the temperature of the computing node to make schedule decisions based on the amount of energy that is sufficient to consider decreasing the temperature. Moreover, number of researches explore software optimization at compiling level [26], [27], [28] in order to both improve performance and reduce energy.

In [19], DVFS decisions are based on memory workload prediction in order to avoid loss of performance. Experimental results on the NAS parallel benchmark and codes with large amounts of data communications and memory accesses show that the proposed approach can save 20% of energy with 4% of performance loss.

In [20], the power consumption of a chemistry application is studied in order to investigate potential energy savings and performance losses when using DVFS technique, mainly relying on CPU stall cycles caused by memory accesses and I/O operations. Experiments show that even when the CPU activity is high, e.g. frequently computing integrals, it is more energy efficient than computing the integrals at the beginning and store them on disk for subsequent reuses.

In [24], a DVFS and temperature aware load balancing technique is presented to constrain core temperatures. The approach lets each core working at the maximum available frequency until a temperature threshold is reached. Experiments in a cluster with dedicated air conditioning unit show that a cooling saving of 57% can be achieved with 20% of timing penalty.

In [25], two energy-conscious task consolidation heuristics (ECTC and MaxUtil) are used to maximize resource utilization for power saving. The cost of the ECTC heuristics is computed considering the energy consumption to run a group of parallel tasks. The MaxUtil heuristic tries to increase the consolidation density. Simulation results show that the proposed heuristics can lead to an energy saving of 18%(ECTC) and 13%(MaxUtil).

In [27], *coarse-grained* compiler optimization strategies are applied in order to minimize the energy consumption. First the registers are renamed in order to reduce output dependencies. Then, the instruction that minimizes the inter-instruction cost is selected for scheduling. The results show that the proposed optimization strategies can cut power consumption by 9%, leading to 4.54% saving on the total energy dissipation.

A distributed compiler approach is presented in [28]. The idea is to use distributed compilers to apply code transformations or highlighting parts of the source code that could not be optimized. The energy minimization is based on the number of cycles that is required to execute a given application. The results show a reduction of 40% in the number of cycles only employing some compiler optimization techniques.

Dabbagh et al. [29] propose a methodology to estimate the energy of operations that can be implemented in hardware. Considering the *backpropagation* algorithm, the proposed approach was able to estimate the energy consumption with an error rate of 5.44%.

In [30], a methodology for measuring the energy efficiency of an application is presented. The aim is to analyze the impact of the application design on its energy efficiency and the environment where the application is developed. The results show that the software abstraction design and the use of some frameworks and libraries must be considered when the goal is to minimize energy, especially for large applications. In other words, in many cases, the use of external frameworks and libraries incurs a high cost in terms of energy consumption.

The closest work to ours are [29] and [30]. Each of these works use the source code to estimate the energy consumption. Our work differs from these approaches in the following ways. First, we argue that the memory and I/O workload must be seriously considered to estimate the energy consumption of an application. Second, we included other kernel operations such as memory accesses (read, write and allocation), register comparison, and I/O and the effect of the CPU frequency in the execution of these operations. Tracking the energy cost per basic instruction, we end up with an analytical model to predict the energy performance of a given source code.

III. Energy Measurement

Our goal in this section is to validate our hypothesis that each basic CPU operation consumes a fixed amount of energy that can be calculated for a given architecture. The machine we have considered is an Intel(R) Core(TM) 2 Quad CPU Q6600, 2.40GHz with 4 GB of RAM running Fedora Linux (kernel version 3.9.8). The power and energy consumption of the machine is measured using the WattsUp power meter [31] with a sampling rate of $1Hz$. This approach of performing measurements directly at the electrical level is expected to cover all sources of power consumption compared to methods that are based on data provided by the thermal sensor of the CPU. Due to the low measuring resolution of the multi meter (slot of 1 second), a large number of executions are needed in order obtain meaningful measurements. In addition, since the raw data provided by the power meter are the distribution of the *electrical power* over the time, we obtain the corresponding energy by just summing up those data. This summation corresponds to the discretization of the required integral

of the power over the targeted time interval.

$$E(t_0, t_1) = \int_{t_0}^{t_1} P(t)\mathrm{d}t \approx \sum_{t=t_0}^{t_1} P(t)\Delta t \approx \sum_{t=0}^{n} P(t_0+k),$$
(2)

where n is the largest integer such that $t_0 + n \leq t_1$. We consider $\Delta t = 1$ because, as previously explained, the WattsUp power meter works by slots of 1 second. In order to capture possible fluctuations when estimating the energy, we perform several measurements (typically 10) and we take the average value.

We evaluate nine basic instructions {*addition, multiplication, division, memory read, memory write, memory copy, print, comparison, malloc*} in order to estimate their energy consumption under different CPU frequencies. For each of them, we apply the aforementioned method to estimate the associated power consumption. The following code is for the *addition* case, we use a similar code for other basic measurements.

```
void floating_point_addition()
{
    register float s;
    int i,n;
    start_energy_counters();
    for(n = 0; n < NB_REPEAT; n ++)
    {
        s = 0.25;
        for (i = 0; i < LENGTH; i++)
            s += 0.3141516;
    }
    get_consumed_energy();
}
```

The outer loop is there just to magnify the computing load (by `NB_REPEAT` times). Having a total of `NB_REPEAT`×`LENGTH` operations offer a more flexible way to sufficiently increase the computing time, otherwise we could stand below one second, means less than what the multi meter can really measure. In any case, the total energy is divided by `NB_REPEAT`×`LENGTH` to get the cost for a single operation.
For the case of memory reads and writes, we use inline assembly instructions in order to make sure the *load* (resp. *store*) instructions are really executed. We will come back later on this particular case regarding the impact of the level of cache. Taking into account the CPU frequency, our profiling is performed following the model described by Algorithm 1. It is important to note here that we compile our code without any optimization.

Table I provides the results of energy consumption for a single *addition* (the overall energy is divided by the total number of additions performed). We display the measurement for each of the 10 executions. The goal is to give a picture of the variations, which we expected to be very slight. Indeed, it is, like with other basic

put the machine in the idle state;
foreach *available CPU frequency* f **do**
    set the frequency of the CPU's core to f;
    foreach *benchmark* b **do**
        for $i = 1$ **to** 10 **do**
            execute b;
        end
        consolidate the data of b;
    end
    sleep 5 seconds;
    consolidate the data for frequency f;
end
Algorithm 1: Generic energy profiling algorithm

operations as the whole set of measurements will reveal.

N	Time (s)	Power (W)	Energy (nJ)
1	28.24	97.01	273
2	28.23	97.09	274
3	28.24	97.24	274
4	28.23	97.28	274
5	28.23	97.48	275
6	28.23	97.06	273
7	28.23	96.92	273
8	28.23	96.88	273
9	28.23	97.12	274
10	28.23	97.05	273

TABLE I
EXECUTION TIME, AVERAGE POWER CONSUMPTION AND ENERGY FOR THE ADDITION OPERATION AT CPU FREQUENCY OF 1.6 GHz.

Tables [II-V] show the results of our energy measurements related to the selected set of basic instructions, using four different values for the CPU frequency (1.6 Ghz, 1.8 Ghz, 2.13 Ghz, and 2.4 Ghz). For each measurement, we first obtain a set of values similar to Table I, then we calculate the mean and the standard deviation. For memory operations (read, write, copy, and malloc), the energy provided is per MB (read, written, copied, or allocated). Figure Fig. 2 depicts an aggregated view of our measurements.

Instruction	Energy (nJ)	STD (10^{-9})	Time (s)
Addition	274	0.50	28.23
Multiplication	334	0.64	34.54
Division	372	0.55	38.53
Memory Read	191	0.42	19.88
Memory Write	207	0.58	21.52
Memory Copy	525	1.85	51.69
Print	172	5.14	17.60
Comparison	221	0.46	23.11
Malloc	3882	8.53	389.23

TABLE II
ENERGY CONSUMPTION AND EXECUTION TIME FOR EACH INSTRUCTION AND CPU FREQUENCY OF 1.6 GHZ.

Instruction	Energy (nJ)	STD (10^{-9})	Time (s)
Addition	247	1.26	24.19
Multiplication	301	0.81	29.61
Division	337	0.65	33.02
Memory Read	173	0.55	17.03
Memory Write	192	0.70	18.89
Memory Copy	479	1.52	44.11
Print	160	6.97	15.40
Comparison	202	0.54	19.79
Malloc	3610	87.22	337.00

TABLE III
ENERGY CONSUMPTION AND EXECUTION TIME FOR EACH
INSTRUCTION AND CPU FREQUENCY OF 1.8 GHZ.

Instruction	Energy (nJ)	STD (10^{-9})	Time (s)
Addition	227	2.01	21.17
Multiplication	297	64.00	27.82
Division	308	1.54	28.89
Memory Read	158	1.07	14.91
Memory Write	176	1.48	16.55
Memory Copy	443	3.13	38.64
Print	142	1.22	13.00
Comparison	184	1.43	17.30
Malloc	3304	18.22	292.19

TABLE IV
ENERGY CONSUMPTION AND EXECUTION TIME FOR EACH
INSTRUCTION AND CPU FREQUENCY OF 2.13 GHZ.

Instruction	Energy (nJ)	STD (10^{-9})	Time (s)
Addition	209	2.38	18.81
Multiplication	254	2.01	23.01
Division	285	1.41	25.68
Memory Read	146	1.45	13.25
Memory Write	164	1.41	14.83
Memory Copy	415	4.60	34.36
Print	132	5.68	11.60
Comparison	171	1.56	15.40
Malloc	3075	31.47	259.67

TABLE V
ENERGY CONSUMPTION AND EXECUTION TIME FOR EACH
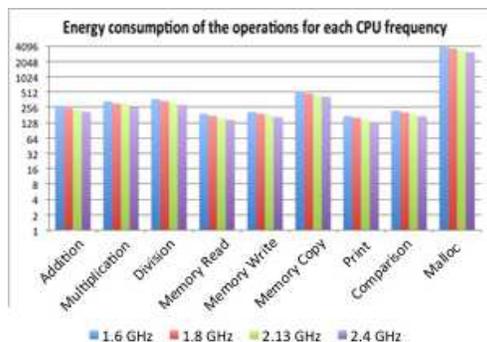INSTRUCTION AND CPU FREQUENCY OF 2.4 GHZ.

Fig. 2. Atomic power consumption of basis operations

Let make some important observations:

- our hypothesis is general, but the energy per basic instruction is of course machine dependent. The corresponding values should be seen as energy parameters useful for any macroscopic estimation.
- for *arithmetic operations*, our measurements somehow follow the intuition. Indeed, the more the operation is complex from the hardware point of view, the more it consumes energy.
- the previous observations seems to be also true for memory accesses (read and write). For memory copy, we use the *memcpy()* routine. We see that the result is slightly larger than *read + write*, which makes sense since copying a memory location necessary involves reading and writing.
- *printing* seems to consume less energy than any other operation from our selected subset. This also makes sense as the CPU is not really involved.
- *memory allocation* is the most energy consuming. However, the fact that it is done once before using the corresponding memory space will impact less energy in practice for time consuming programs.
- the energy is lower with higher CPU frequencies, probably due to the reduction of the execution time. However, in case of time consuming processing, keeping the CPU at high frequency will incur a higher energy for cooling, which we do not count in this work. Because of the energy for cooling, since the energy variation related to CPU frequency is marginal, switching to lower CPU frequencies on memory and I/O operations should be globally rewarding over a long period of processing time.

IV. PREDICTION MODEL

For a given source code for which we could get an inventory of basic instructions, our prediction of the energy is given by

$$E(f) = \sum_{i=1}^{p} N_i e_i(f) + E_{cooling}(f, t_{max}), \quad (3)$$

where $e_i(f)$ is the energy of the corresponding atomic operation at frequency f as previously calculated, and N_i is the number of such instructions. These numbers can be obtained either from a profiling, a code analysis framework [32], or a complexity estimation. For a more rigorous estimation, one could proceed with the corresponding assembly code. The second term, $E_{cooling}(f, t_{max})$ is the energy for cooling, which depends on

- how CPU temperature changes during the execution (this depends on the code and the CPU frequency)

- the temperature threshold (t_{max}) beyond which the cooling system is activated, typically the *fan* for standard machines.

We do not consider the second term in this paper. We keep it, together with the corresponding study, in our list of perspectives. We think this concern is more relevant for programs with longer execution times.

The linear model defined by (3) could be refined by taking into account the following considerations

- the use of *fuse multiply-add* instructions, which may correlate the energy for *additions* and *multiplications*
- the level of cache where we read or write data, as this has a significant impact on the execution time, thus on the overall energy
- the effect of *instructions pipeline*, which clearly stands against an additive energy consumption model

The last two aspect are quite elusive, and could be addressed with rough estimations, unless a more rigorous analysis is made possible by the availability of key hardware and system information.

V. VALIDATION AND TECHNICAL DISCUSSION

In this section, we consider three case studies to illustrate and validate our power estimation approach. For each application, the number of basic operations is obtained from a direct complexity analysis of the corresponding algorithm. The reader should keep this in mind when reading the formulas provided for energy estimation. We denote by $e_a(f)$, $e_m(f)$, $e_d(f)$, $e_c(f)$, $e_l(f)$, and $e_s(f)$, the energy consumed at CPU frequency f for a single *addition*, *multiplication*, *division*, *comparison*, *load*, and *store* respectively. We recall that the corresponding values are provided in Tables II, III, IV, and V.

A. Selection sort

```
for (i = 0; i < n; i++) do
    i_min = i;
    for (j = i + 1; j < n; j++) do
        if(u[j] < u[i_min]) i_min = j;
    end
    x = v[i]; v[i] = v[i_min]; v[i_min] = x;
end
```
Algorithm 2: Main loop of the selection sort

Following our model and the complexity of Algorithm 2 (as it is written), we can estimate the energy as

$$E_{sort}(f) = \frac{n(n+1)}{2}(e_c(f) + 2e_l(f)) + 2ne_s(f). \quad (4)$$

Depending on the relative order of the values in the array to be sorted, the cost of the last step, where we swap

two components, will depend on how distant are i and i_min. Figure Fig. 3 displays the energy performances of the selection sort implemented from Algorithm 2.
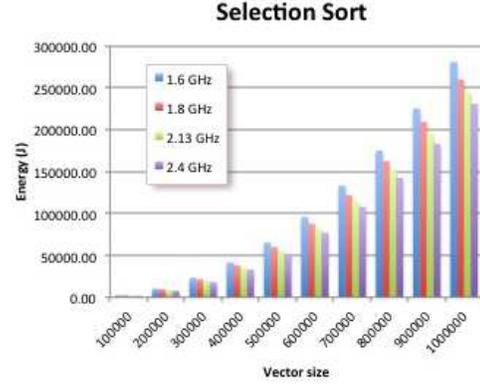

Fig. 3. Measured power consumption of the selection sort

Table VI provides both our predictions and the measurements for the selection sort on arrays of various sizes ($N \times 10^5$), at different CPU frequencies.

N	1.6 Ghz		1.8 Ghz		2.13 Ghz		2.4 Ghz	
1	3.0	2.6	2.7	2.4	2.5	2.2	2.3	2.0
2	12	10	11	9.6	10	8.9	9.3	8.1
3	27	23	25	22	22	20	21	18
4	48	42	44	38	40	35	37	33
5	75	65	68	60	62	55	58	52
6	108	96	97	87	90	82	83	77
7	148	133	134	122	122	113	113	108
8	193	175	175	163	160	151	148	143
9	244	225	222	209	202	195	187	183
10	301	281	274	260	250	244	231	231

TABLE VI
ENERGY PREDICTIONS VS PERFORMANCES (KJOULES) FOR THE
SELECTION SORT ALGORITHM

The average relative error is 9.48%, which is quite good, especially for sorting as the effective number of memory moves depends on the values of the array to be sorted. The impact of swapping is also values dependent.

B. Weighted means

```
s = 0;
for (i = 0; i < n; i++) do
    s = s + w[i] * v[i];
    u[i] = s/(i + 1);
end
```
Algorithm 3: Main loop of the weighted means

The energy of Algorithm 3 (as it is written), can be

estimated by

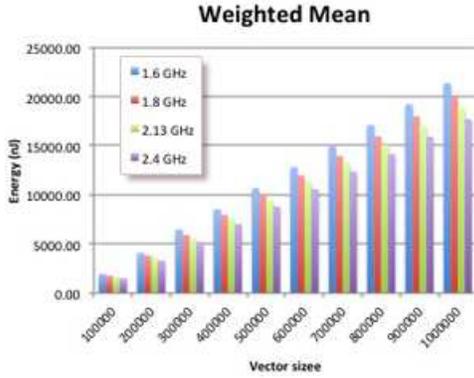$$E_{mean}(f) = n(2e_a(f) + e_m(f) + e_d(f) + 2e_l(f) + e_s(f)), \quad (5)$$

Fig. 4. Measured power consumption of the weighted means

$N_{\times 10^5}$	1.6 Ghz		1.8 Ghz		2.13 Ghz		2.4 Ghz	
1	1.8	1.9	1.7	1.8	1.6	1.6	1.4	1.5
2	3.7	4.1	3.3	3.8	3.1	3.6	2.8	3.3
3	5.5	6.5	5.0	5.9	4.7	5.6	4.2	5.2
4	7.4	8.5	6.7	8.0	6.2	7.5	5.7	7.0
5	9.2	10	8.4	10	7.8	9.4	7.1	8.8
6	11	13	10	12	9.3	11	8.5	11
7	13	15	12	14	11	13	9.9	12
8	15	17	14	16	13	15	11	14
9	17	19	15	18	14	17	13	16
10	19	21	17	20	16	19	14	18

TABLE VII
ENERGY PREDICTIONS VS PERFORMANCES (KJOULES) FOR THE
WEIGHTED MEANS CALCULATION

The average relative error is 18.36%. We think that instructions pipeline really applies here. However, we could reach 5.75% in some cases.

C. Scalar product

```
s = 0;
for (i = 0; i < n; i++) do
│   s = s + u[i] * v[i];
end
    Algorithm 4: Main loop of the scalar product
```

The energy of Algorithm 4 can be estimated by
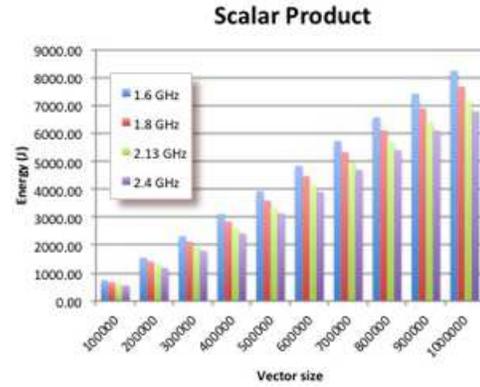
$$E_{scalar}(f) = n(e_a(f) + e_m(f) + 2e_l(f)), \quad (6)$$

Fig. 5. Measured power consumption of the scalar product

$N_{\times 10^5}$	1.6 Ghz		1.8 Ghz		2.13 Ghz		2.4 Ghz	
1	1.0	0.8	0.9	0.7	0.8	0.6	0.8	0.6
2	2.0	1.6	1.8	1.4	1.7	1.3	1.5	1.2
3	3.0	2.3	2.7	2.1	2.5	2.0	2.3	1.8
4	4.0	3.1	3.6	2.8	3.4	2.6	3.0	2.4
5	5.0	3.9	4.5	3.6	4.2	3.3	3.8	3.1
6	5.9	4.8	5.4	4.5	5.0	4.1	4.5	3.9
7	6.9	5.7	6.3	5.3	5.9	5.0	5.3	4.7
8	7.9	6.6	7.2	6.1	6.7	5.7	6.0	5.4
9	8.9	7.4	8.0	6.9	7.6	6.4	6.8	6.1
10	9.9	8.2	8.9	7.7	8.4	7.2	7.6	6.8

TABLE VIII
ENERGY PREDICTIONS VS PERFORMANCES (KJOULES) FOR THE
SCALAR PRODUCTS CALCULATION

The average relative error is 18.18%. The same observation as for weighted means calculation holds. The relative erros here range from 10.05% to 24.11%.

VI. DISCUSSIONS AND PERSPECTIVES

As we have previously mentioned, our energy prediction can be refined by investigating on other energy consuming aspects as well as on the hardware correlation between some pairs of instructions. The case of *fuse multiply-add* should be investigated following the methodology considered in this paper. The gap observed with the *scalar product* and the *weighted means* might be due to such transformation by the compiler. Network activities and disk accesses should be studied to, thus leading to an extension of our model to larger computing systems like the *Cloud* or *supercomputers*.

A more deeper but very important investigation could address the energy coming from CPU cooling. This requires to be able to model the variation of the CPU temperature during the execution of a given program, and also the electrical power used for cooling.

VII. CONCLUSION

Modern computing devices are provided to deliver very fast processing capabilities. Either because of the

limited amount of energy available for mobile devices and embedded systems, or because of the cost (financial and environmental) of the energy related to larger systems, we need to have a good control on power consumption. Among possible approaches, quantitative modeling of energy prediction is particularly attractive, as it could be used for power aware programming or compilation. The approach proposed in this paper is one way to derive such a model and we think, either by construction or from the satisfactory validation results, that it deserves a close attention.

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