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# Automated Code Generation for Lattice Quantum Chromodynamics and beyond

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**Abstract.** We present here our ongoing work on a Domain Specific Language which aims to simplify Monte-Carlo simulations and measurements in the domain of Lattice Quantum Chromodynamics. The tool-chain, called Qiral, is used to produce high-performance OpenMP C code from LaTeX sources. We discuss conceptual issues and details of implementation and optimization. The comparison of the performance of the generated code to the well-established simulation software is also made.

## 1. Introduction

Quantum Chromodynamics (QCD) is a fundamental theory within Standard Model used to describe strong interactions inside a nuclei. As the coupling constant for this force is large, the perturbation theory cannot be used in most cases. Instead, a number of non-perturbative methods have been developed, with the most prominent of them being Lattice QCD (LQCD). It is formulated in discrete space-time, with the matter fields residing on sites and the interaction fields (gluons) live on links. This setup allows us to simulate it on a computer by means of Monte-Carlo simulations. Such analysis already provided many insights into the nature of strong interactions and delivered a number of precise results to confront experimental data. With the arrival of teraflop installations, LQCD is now regarded as the most reliable method of solving QCD, as the simulations can be systematically improved. It has also been extended to help solve theories other than QCD.

The most time-consuming part of these simulations is the frequent inversion of an immense matrix (Hopping Matrix), which encodes interactions within the simulated system. To do this efficiently, thousands of people over the globe are working for years, inventing new methods for the inversion. At the same time, new Lagrangians appear, which, while preserving physical properties, have different mathematical ones which are supposed to make Monte-Carlo simulations faster and more reliable.

The Hopping Matrix is actually a representation of a tensor called Wilson-Dirac operator. The matrix is always sparse and structured, so the iterative methods are definitely considered. Therefore, the procedure of the application of this operator, resulting in a vector-matrix product, appears as a critical computation kernel that should be optimized as much as possible. Due to the size of the matrix, it has to be recalculated on every iteration. Therefore, in the simplest case, evaluating the Wilson-Dirac operator involves each node and 8 neighbors. Such configuration is really hindering in terms of computation, as memory access is very far from sequential and standard methods fail miserably. For current and future generation of supercomputers the hierarchical memory structure makes it next to impossible for a physicist to write an efficient code.

But even for computer scientists, the rapid change in parallel architectures makes the design of an optimized LQCD simulation a real challenge. This requires to design, select and combine iterative methods and preconditioners adapted to the problem and the target architecture, to optimize data layout and organize parallelism between nodes, cores, accelerators and SIMD units. In order to harness all resources of the hardware, orchestrating the work on many cores and accelerators, using different levels of parallelism, complex memory hierarchies and interconnect networks takes a large part of the tuning time, often at the expense of the exploration of new algorithms/preconditioners. Indeed, testing new methods can only be achieved with large enough data sets, requiring efficient parallel codes. Several codes and libraries have been designed for Lattice QCD and many works have been published on code optimization for Lattice QCD, among them the studies on Blue Gene/Q [4], Intel Xeon Phi [6] or clusters of GPUs [5]. They offer some degree of flexibility, but usually only focus at a small subset of existing architectures. However, designing new iterative methods, combining existing ones, changing data layout within these frameworks and tools is difficult and requires a significant code rewriting effort. This clearly hinders the adaptation of code to the new parallel machines, limiting performance and the expected scientific results.

This paper proposes a domain-specific language (DSL), QIRAL, for the description of Lattice QCD simulations, and its compiler to generate parallel code. A DSL can help to separate the high level aspects of the simulation from machine-dependent issues. The contribution of QIRAL is to address this twofold challenge:

- Propose to physicists a domain-specific language expressive enough to enable the description of different models and algorithms, and more importantly, expressive enough to enable

algorithmic exploration by composing different algorithms and preconditioners as well as the design of new algorithms.

- Generate from this description efficient codes for parallel machines. Explicit parallelism and data layout are automatically generated and can be guided by the user. The code generated by QIRAL targets shared memory parallel machines, corresponding to one node of larger Lattice QCD simulations. This code uses OpenMP and a library for efficient SIMD operations.

With a higher level description of the Lattice QCD formulation we achieve multiple goals. It becomes easier to try new algorithmic ideas, the high level code is easier to maintain and develop. This makes numerical simulation accessible to a large number of users, not necessarily high performance computing experts. We show on several architectures, from Nehalem-EX with 128 cores to the Xeon Phi accelerator that the code generated with QIRAL competes in terms of parallel efficiency and performance with tmLQCD, while QIRAL provides an easier framework for the writing of algorithms and the adaptation to new architectures.

This paper is organized as follows: first we describe the DSL in Section 2, describe the high-level compiler in Section 3. Then the optimizations for locality, parallelism and SIMDization are presented in Section 4. Benchmarks, comparing with tmLQCD and describing strong scalability are shown in Section 5.

The whole project, under the name PetaQCD [1], was partly funded by a grant from ANR, through the program COSINUS-2008, from 2009 up to 2011.

## 2. The QIRAL Domain-Specific Language

As one of the purposes of the QIRAL DSL is to give scientists a familiar tool to describe the problem in scope, it makes sense to take an existing system of symbolic notation as the basic language. There are two such systems in most disciplines,  $\text{\LaTeX}$  and Mathematica. While we are not attached to a particular one, we chose to use  $\text{\LaTeX}$ -like syntax where certain additional macros have been defined. Therefore the QIRAL description can be processed either using the QIRAL compiler to produce program source code or alternatively, by the  $\text{\LaTeX}$  typesetter to produce its documentation. This means we revive the principle of *literate programming* coined by Donald Knuth [7]. For instance, the algorithm in Figure 3 is a QIRAL program included into this document as processed by  $\text{\LaTeX}$ . The description of the language given in the following complements a description previously presented by the authors [2].

QIRAL is a language for describing linear algebra objects and operations, with a specialization in manipulation of sparse matrices defined through tensor products and direct sums of dense matrices as they appear in Lattice QCD. It is well-adapted to the particular features of Lattice QCD, or, rather, any realistic field theory. All interactions in such theories are local, therefore it is well-suited for the so-called stencil computation, involving a point and its nearest neighbours only. It assumes that the underlying manifold is a 4D space-time, cut into a cartesian mesh (the lattice). The Dirac operator, used for this inversion, is a sparse but regularly structured matrix that can be seen as a diagonal of dense matrices. This operator describes interaction between matter fields and guides the evolution of the system. The matter fields are represented by spinors, which are complex matrices having four spin and three color. Hence for a  $24^3 \times 48$  lattice, the Dirac operator is a matrix of  $(24^3 \times 48 \times 12)^2$  complex values. Due to locality of the interaction, the resulting matrix is sparse, and QIRAL takes advantage of this structure to reduce the unnecessary computation.

Elements of the language are declarations, equations, algorithms and the goal. Declarations declare symbols and functions with their type. Basic types are boolean, integers, real ( $\mathbb{R}$ ), complex ( $\mathbb{C}$ ) vectors ( $\mathbf{V}$ ), matrices ( $\mathbf{M}$ ), indices and index sets. Vectors and matrices are defined over index sets either defined through the notation  $\mathbf{V1}[is]$ , where  $is$  is the possibly multi-dimensional index set for vector  $\mathbf{V1}$ , or deduced through type inference. A particular element

of a vector is accessed by the use of an index: `V1[I1]`. Figure 1 shows the declaration of the constants used for Lattice QCD, and the definition of Dirac operator as a matrix. The two other matrices,  $P_e$  and  $P_o$  are projections, keeping only black or white elements of the lattice, like a 4D checkerboard.

Equations are used to define variables or functions. Figure 2 describes nearly all properties and definitions on the constant and functions used for the simulation. For instance, the function “invertible” is defined only for some expressions.

| <b>Constant:</b>   | <b>Constant:</b>                                  |
|--|---|
|  | $dx, dy, dz, dt \in Index$                        |
| <b>Constant:</b>   | $D = \{dx, dy, dz, dt\}$                          |
| $Dirac, P_e, P_o, \gamma_5 \in M,$   | $isPeriodic(L) = true$                            |
| $L, S, C, even \in Indexset,$  | $U[s \otimes d]^\dagger = U[(s + d) \otimes -d]$  |
| $\gamma \in Index- > M,$   | $U[s \otimes -d]^\dagger = U[(s + -d) \otimes d]$ |
| $U \in Index- > M,$  | $Preconditioner1(Dirac) = P_e$                    |
| $\kappa, \mu, \in \mathbb{R},$   | $Preconditioner2(Dirac) = P_o$                    |
| $D \in Indexset$   | $\gamma[d]^\dagger = \gamma[d]$                   |
| <b>Variable:</b> $s \in Index, d \in Index$  | $diagonal(\gamma_5) = true$                       |
|  | $\gamma_5 * \gamma_5 = I_S$                       |
|  | $\gamma_5 * \gamma[d] = -\gamma[d] * \gamma_5$    |
|  | $invertible(I_S + c * \gamma_5) = true$           |
|  | $invertible(I_S - c * \gamma_5) = true$           |
|  | $invertible(-(c * I_S) + i * \gamma_5) = true$    |
| $Dirac = I_{L \otimes C \otimes S}$  | $\gamma_5^\dagger = \gamma_5$                     |
| $+ 2 * i * \kappa * \mu * I_{L \otimes C} \otimes \gamma_5$  | $type(\gamma[d]) = S \times S$                    |
| $+ -\kappa * \sum_{d \in D} ((J_L^{-d} \otimes I_C) * \bigoplus_{s \in L} U[s \otimes d]) \otimes (I_S - \gamma[d])$ | $type(U[s \otimes d]) = C \times C$               |
| $+ -\kappa * \sum_{d \in D} ((J_L^d \otimes I_C) * \bigoplus_{s \in L} U[s \otimes -d]) \otimes (I_S + \gamma[d])$   | $type(\gamma_5) = S \times S$                     |
| $P_e = P_{even,L} \otimes I_{C \otimes S}$   | $vol(S) = 4$                                      |
| $P_o = P_{!even,L} \otimes I_{C \otimes S}$  | $vol(C) = 3$                                      |

Figure 1: Definitions of the Dirac matrix on a Lattice  $L$  in QIRAL, and the two projections for even and odd elements ( $P_e$  and  $P_o$  respectively) of this lattice.

Figure 2: Identities of constants used for Lattice QCD.

Algorithms are given as possible definitions for statements or expressions. For instance, the conjugate gradient algorithm in Figure 3 provides the code that computes expressions of the form  $x = A^{-1} * b$ , when  $A$  and  $b$  are given. It outputs the value of  $x$ , i.e. solves the linear system  $Ax = b$ .

The initial statement, in the **Match** clause, is then defined (and replaced) by the pseudo-code. The **Var** keyword declares the type of local variables. This algorithm is written using the “algorithm2e” package in L<sup>A</sup>T<sub>E</sub>X, and is not specific to Lattice QCD. The user has the possibility to write new algorithms for Lattice QCD or any other algorithm found in common literature. The QIRAL compiler finds automatically how to compute for instance  $A * p$  when  $A$  is instantiated with the Dirac operator.

Most often the validity of an algorithm depends on prerequisites, special properties the inputs

**Input** :  $A \in M, b \in V$   
**Output** :  $x \in V$   
**Constant**:  $\epsilon \in \mathbb{R}$   
**Match** :  $x = A^{-1} * b$   
**Var** :  $r, p, Ap, z \in V, \alpha, \beta, n_r, n_z, n_{z1} \in \mathbb{R}$   
 $r = b$  ;  
 $z = A^\dagger * r$  ;  
 $p = z$  ;  
 $x = 0$  ;  
 $n_z = (z | z)$  ;  
 $n_r = (r | r)$  ;  
**while** ( $n_r > \epsilon$ ) **do**  
     $Ap = A * p$  ;  
     $\alpha = n_z / (Ap | Ap)$  ;  
     $x = x + \alpha * p$  ;  
     $r = r - \alpha * Ap$  ;  
     $z = A^\dagger * r$  ;  
     $n_{z1} = (z | z)$  ;  
     $\beta = n_{z1} / (n_z)$  ;  
     $p = z + \beta * p$  ;  
     $n_z = n_{z1}$  ;  
     $n_r = (r | r)$  ;

Figure 3: Conjugate Gradient, normal residual method (CGNR).

**Input** :  $A, P_e, P_o \in M, b \in V$   
**Output** :  $x \in V$   
**Match** :  $x = A^{-1} * b$   
**Constant**:  $D_{11}, D_{12}, D_{21}, D_{22} \in M$   
**Var** :  $v_1, v_2, x_1, x_2 \in V$   
**Require** :  $\text{invertible}(P_e * A * P_e^t)$   
 $D_{21} = P_o * A * P_e^t$  ;  
 $D_{11} = P_e * A * P_e^t$  ;  
 $D_{22} = P_o * A * P_o^t$  ;  
 $D_{12} = P_e * A * P_o^t$  ;  
 $v_1 = P_e * b$  ;  
 $v_2 = P_o * b$  ;  
 $x_2 = (D_{22} - D_{21} * D_{11}^{-1} * D_{12})^{-1} * (v_2 - D_{21} * D_{11}^{-1} * v_1)$  ;  
 $v_1 = P_e * (2 * \kappa * b)$  ;  
 $x_1 = D_{11}^{-1} * (v_1 - D_{12} * x_2)$  ;  
 $x = P_e^t * x_1 + P_o^t * x_2$  ;

Figure 4: Definition of Schur complement method.

must have. These prerequisites are declared in a clause **Require** and is proved by the QIRAL compiler. The following example illustrates this prerequisite mechanism. Figure 4 describes the Schur complement method that is used as a preconditioner for the conjugate gradient and the conjugate residual. The condition  $\text{invertible}(P_e * A * P_e^t)$  is proved automatically by the compiler when  $A$  matches the matrix *Dirac*. To prove this, the property defined previously for the function “invertible” is used. If the compiler is not able to prove the requirements attached to an algorithm, the algorithm is not applied and an error is generated. Notice that on this preconditioning, the statements involve computation of inverse matrices. For the expression  $D_{11}^{-1}$ , the QIRAL compiler can prove automatically that  $D_{11}$  is diagonal (when  $A$  is the Dirac operator), and knows how to invert this matrix. For the computation of the expression  $(D_{22} - D_{21} * D_{11}^{-1} * D_{12})^{-1}$ , an iterative method has to be applied.

The goal defines the initial code and the list of algorithms to apply. The algorithms are composed from right to left.

**Input** :  $bb \in V$   
**Output** :  $xx \in V$   
**Templates:** CGNR schur  
 $xx[L \otimes C \otimes S] = \text{Dirac}^{-1} * bb[L \otimes C \otimes S]$  ;

For this goal here the preconditioner `schur` is applied on the initial statement, and then the CGNR algorithm. It is possible to chain multiple algorithms, used to apply preconditions before the solvers. The index set  $L \otimes C \otimes S$  represents the Cartesian product of these sets and the domain for the vector  $bb$ . At this level, there is no implicit data layout for vectors and matrices. The vector  $bb$  could be either a 4D array of structures, one dimension for each dimension of  $L$  and the structure representing elements indexed by  $C$  and  $S$ , or a 1D array of structures, or just a large 1D array of complex values. This is orthogonal to the expression of the algorithm.

The output of QIRAL compiler is a function in C and OpenMP pragmas representing the computation described in the goal, and taking as parameters  $bb$  and  $xx$ . All other constant values (in particular constant matrices) are assumed to be global.

### 3. Implementation Details

The QIRAL compiler is based on a rewriting system, Maude [3]. The different steps of this transformation are explained in this section.

#### 3.1. Algorithms composition and expression simplification

Algorithms are translated into rules of the rewriting system, while equations define the equational theory for the rewriting system. The first step consists in transforming L<sup>A</sup>T<sub>E</sub>X input into a Maude program. Additional modules, defining usual algebraic simplifications are added to this code.

The first step parses the L<sup>A</sup>T<sub>E</sub>X input and captures only what is described in predefined environments, for algorithms, definitions and the goal. Syntactic verification as well as type checking is performed. The output generated is a Maude module, with equations corresponding to definitions, rules corresponding to algorithms, and a unique Maude statement, corresponding to the goal.

The algorithms declared in the goal are applied, in turn, to the statements provided. These statements are terms for Maude. The **Match** clause is the left-hand side (lhs) of the rule, while the pseudo-code corresponds to a term that is the right-hand side (rhs) of the rule. Any statement matching the lhs will then be rewritten in the rhs. If a **Require** clause exists, it constitutes the condition for the rewriting. The first statement is provided by the goal, then algorithms are applied successively.

Definitions and properties are considered by Maude as defining the equational theory for the rewriting system. Actually, these equations are handled as automatic rewriting rules: Maude automatically applies all possible equations, rewriting their lhs into rhs, until the term is normalized. For instance, the property  $x * (y + z) = x * y + x * z$ , stating the distributivity of  $+$  over  $*$ , will only be used to distribute the operators, not to factorize terms.

The main objective of this formal rewriting is to eliminate all terms that are equal to zero. In Lattice QCD, the Dirac matrix used in the problem is sparse, but built from dense matrices with a regular structure. To obtain such simplifications, an additional module defines properties for the linear algebra operators, on complex, vectors and matrices: Addition is commutative and associative, multiplication is associative and distributes over the addition, binary subtraction is converted to unary minus, transposition distributes over the addition and multiplication, etc. Moreover, some properties are also defined for permutation and projection matrices, in particular to handle Schur preconditioning.

## 4. Code Optimizations

### 4.1. Improving Locality

Loops fusion is a transformation to reduce reuse distances, hence improving locality. To check if fusion is valid, a simple dependence analysis, based on dependence distance, is computed. The fusion method is applied on consecutive independent loops that share the same iterators, and is applied on all code until no more fusion is possible. This simple strategy is sufficient for Lattice QCD generated codes.

Following this fusion, the regions of arrays that are written/read by all loops, and the regions that are inputs/outputs of loops are computed. All arrays that are used only in one loop are scalar promoted. The resulting values are allocated on the stack, and aligned for further vectorization. This reduces memory consumption.

Both transformations are applied automatically.

### 4.2. Versioning Matrix Multiplication

The computation involve many multiplications of vectors by constant matrices, accounting for transformations on spin and color ( $S$  and  $C$  index sets respectively). These matrices are small, of size  $3 \times 3$  and  $4 \times 4$  respectively, and the latest have only 2 non-null elements per line, these elements being among  $\{1, -1, i, -i\}$ . Therefore specialization of these products is necessary in order to obtained better performance. These matrix-vector multiplications appear in expressions of the form  $(M_1 \otimes M_2) \cdot V$  with  $M_1$  and  $M_2$  the two matrices multiplied by a tensor product, and  $V$  is a 12 element vector. In this case the QIRAL compiler uses the identity

$$(M_1 \otimes M_2) * V = M_1 * V * M_2^t$$

where on the lhs,  $V$  is considered a matrix of size  $3 \times 4$  and  $*$  stands for the matrix product. Therefore, instead of using general matrix multiplication, QIRAL compiler finds these occurrences and calls versioned matrix multiplications. Specializing such multiplications for these particular sizes, in particular performing SIMDization, is essential for performance. These functions correspond to the hot-spot of the codes generated by QIRAL. The codes of these functions are hand-written in `libqiral` library as presented in Figure ??.

Other expressions can be replaced by library calls, and QIRAL changes expressions on vectors and matrices into BLAS calls (or specialized BLAS). The fact that the QIRAL compiler automatically identifies these functions in the code generated from the different algorithms facilitates the optimization process and is an asset of QIRAL. The optimization of these functions in `libqiral`, specializations of BLAS, can indeed be achieved by an expert in high-performance computing, independent of any Lattice QCD context.



## 5. Performance Results

Several iterative methods are written with QIRAL. Figure 5 presents some of these methods, for two architectures: CGNR, CRNE, MCR1 and MCR2 with some preconditioners: Schur and preMCR. We observe that while MCR2 exhibits the best time per iteration, the method takes

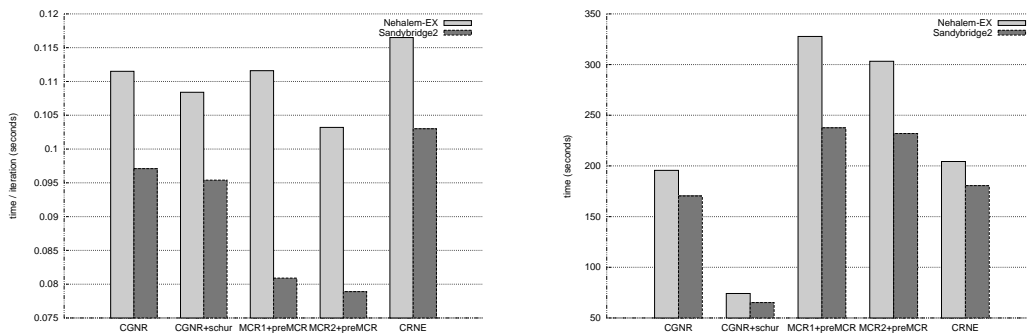


Figure 5: Comparison between different iterative methods, on Nehalem-EX and Sandybridge 2 architectures. Left figure: Time in seconds per iteration. Right figure: Total execution time.

more time to converge than CGNR and Schur. This shows that the best method cannot be determined only by benchmarking a single iteration, but it is necessary to run all iterations. Besides, the second plot of Figure 5 shows that the relative difference may vary according to the architecture. While the absolute best method is still the same (here CGNR combined with Schur), this stresses the fact that the algorithmic solution may be chosen depending on the target architecture.

In order to compare tmLQCD with the code generated by QIRAL, the same algorithm is used for both (CGNR and Schur preconditioning). Performance is displayed for all architectures as the total execution time multiplied by the number of cores. Due to the fact that tmLQCD is using MPI, there is no version for Xeon Phi. Besides, the tmLQCD code uses in-line assembly code with SSE3 instructions. Adapting this code for newer SIMD extensions is more difficult than adapting intrinsics as used by QIRAL. Indeed for intrinsics, part of the optimization work still relies on the compiler: register allocation, generation of FMAs, scheduling. The code generated by QIRAL has been quickly ported to these architectures, and then code tuning has focused on the library used by QIRAL (with versioned BLAS), using intrinsics and aggressive in-lining.

Figure 6 presents timing results on different architectures, comparing tmLQCD code with QIRAL generated code. For QIRAL, the “hand-optimized library” corresponds to the best version obtained, using intrinsics (AVX, AVX2, Xeon Phi) for Sandybridge, Haswell and Xeon Phi architectures. The Nehalem EX version does not use SSE SIMD intrinsics. This explains why QIRAL/Nehalem EX version is more than two times slower than tmLQCD. For Xeon Phi, the performance displayed corresponds to the use of all the 60 cores, and a linear speed-up can be observed by using an increasing number of cores. The ISPC compiler has been used to generate SIMD version of matrix multiplication of size  $3 \times 4$  on complexes. The compiler is still under heavy development and does not fully work for Xeon Phi. Figure 6 shows that the level of performance reached with ISPC is not competing with the level for hand-tuned intrinsics.

The strong scalability of the code generated by QIRAL is evaluated on Xeon Phi and Nehalem-EX architectures. Figure 6, right, shows efficiency results for different number of cores. Note that the size of the lattice is different for both architectures, reflecting the need for different granularity. The efficiency for the Xeon Phi is compared to the run on 4 cores, with 4 threads each. This explains why for some number of threads, the efficiency goes beyond 1. The code

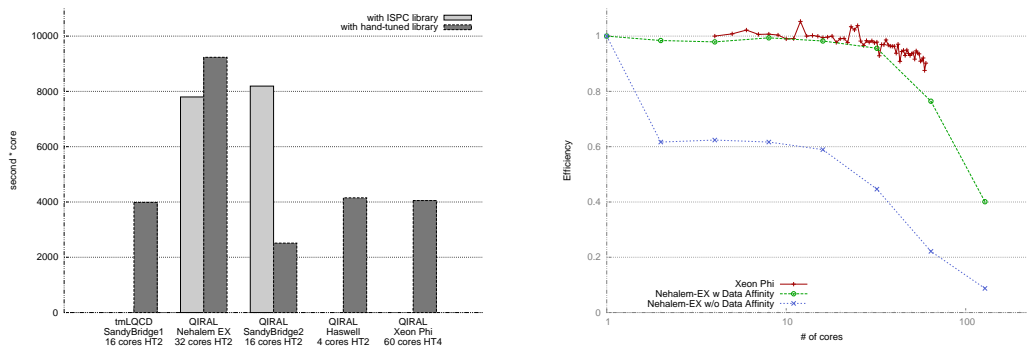


Figure 6: Left: Normalized performance for the inversion on different architectures, with QIRAL and tmLQCD codes. Performance is shown in sec\*core (ie “seconds times number of cores”), lower is better. The execution time is obtained by dividing this performance by the number of cores. The same method, a conjugate gradient with Schur preconditioning is used in all cases, with a lattice of size  $24^3 * 48$  and an error of  $10^{-14}$ . Right: Efficiency of the code generated by QIRAL on Xeon Phi and Nehalem EX, according to the number of cores used. For both architectures, the method used is the conjugate gradient with Schur preconditioning. The lattice size for the Xeon Phi is  $24^3 * 48$  and for the Nehalem-EX,  $64^3 * 128$ . On the Nehalem-EX the efficiency is measured with and without NUMA-aware memory allocation.

scales well up to the 60 cores (240 threads). For the Nehalem-EX machine, the efficiency is higher than 95% up to 32 cores, and then drops quickly. The reason is that a 128-core node is structured with 4 groups of 4 octo-cores, connected through a switch. Going through the switch has a high penalty in terms of performance.

## 6. Conclusion

The contribution of this paper is a new domain-specific language, QIRAL, for the automatic code generation of OpenMP codes for Lattice QCD simulations. QIRAL language offers to physicists the possibility to implement iterative methods and preconditioners, literally “from the book” using  $\text{\LaTeX}$ , or design new ones, and test them on large parallel shared memory machines or on accelerators such as the Xeon Phi. The language enables the composition of preconditioners and iterative methods, and the compiler checks automatically the validity of application for each method. This makes possible a more systematic exploration of the algorithmic space: indeed, it removes from the physicists the burden of long and stressful validations of their new code since it will be automatically generated, then safer, and the time-to-market for a viable product will be much shorter. The QIRAL compiler generates OpenMP parallel code using BLAS or specialized versions of BLAS functions. Further hand-tuning is possible on the code generated by QIRAL, and we have shown that the performance on various multi-core architectures and on Xeon Phi accelerator it compares or outperforms the performance of a hand-tuned Lattice QCD application, tmLQCD.

Among the perspectives of this work, the automatic generation of a communication code for multi-node computation would enable to run Lattice QCD simulations on a larger scale. Besides, the fine tuning of the library functions used by QIRAL on different architectures, in particular their SIMDization, could be improved.

## 7. The bibliography

- [1] J. Angles D'Auriac, D. Barthou, D. Becirevic, R. Bilhaut, F. Bodin, P. Boucaud, O. Brand-Foissac, J. Carbonell, C. Eisenbeis, P. Gallard, G. Grosdidier, P. Guichon, P. Honore, G. Le Meur, P. Pene, L. Rilling, P. Roudeau, A. Seznec, A. Stocchi, and F. Touze. Towards the petaflop for Lattice QCD simulations the PetaQCD project. In J. G. . M. Lokaajicek, editor, *J. of Physics Conf. Series*, volume 219, page 052021, Prague, Tchèque, République, 2010. IOP Publishing. LAL 09-58, LPSC09233.
- [2] D. Barthou, G. Grosdidier, M. Kruse, O. Pène, and C. Tadonki. QIRAL: A High Level Language for Lattice QCD Code Generation. *CoRR*, abs/1208.4035, 2012.
- [3] M. Clavel, F. Durán, S. Eker, P. Lincoln, N. Martí-Oliet, J. Meseguer, and C. Talcott. The Maude 2.0 System. In R. Nieuwenhuis, editor, *Rewriting Techniques and Applications (RTA 2003)*, number 2706 in Lecture Notes in Computer Science, pages 76–87. Springer-Verlag, June 2003.
- [4] J. Doi. Peta-scale lattice quantum chromodynamics on a Blue Gene/Q supercomputer. In *Proceedings of the International Conference on High Performance Computing, Networking, Storage and Analysis, SC '12*, pages 45:1–45:10, Los Alamitos, CA, USA, 2012. IEEE Computer Society Press.
- [5] B. Joó and M. A. Clark. Lattice QCD on GPU clusters, using the QUDA library and the Chroma software system. *Int. J. High Perform. Comput. Appl.*, 26(4):386–398, Nov. 2012.
- [6] B. Jo, D. Kalamkar, K. Vaidyanathan, M. Smelyanskiy, K. Pamnany, V. Lee, P. Dubey, and I. Watson, William. Lattice QCD on Intel Xeon Phi Coprocessors. In J. Kunkel, T. Ludwig, and H. Meuer, editors, *Supercomputing*, volume 7905 of *Lecture Notes in Computer Science*, pages 40–54. Springer Berlin Heidelberg, 2013.
- [7] D. E. Knuth. Literate programming. *The Computer Journal*, 27:97–111, 1984.