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Cécile Amblard, Stephane Girard, Ludovic Menneveau

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Algebraic properties of copulas defined from matrices

Cécile Amblard^{*}, Stéphane Girard, Ludovic Mennetau

We propose a new family of copulas, defined by:

$$S_\phi(u, v) = {}^t\phi(u)A\phi(v), \quad (u, v) \in [0, 1]^2,$$

where ϕ is a function from $[0, 1]$ to \mathbb{R}^p and A is a $p \times p$ matrix. Let us remark that if $p = 2$ and A is a diagonal matrix, then S_ϕ reduces to the family proposed in [1]. As a consequence, S_ϕ can be seen as an extension of this former family to arbitrary matrices.

First, we shall give sufficient conditions on A and ϕ to obtain copulas. Then, we shall establish the dependence and symmetry properties of this family of copulas. Finally, we shall study the stability properties of S_ϕ with respect to the operator $*$ (presented for instance in [2], p. 194) as well as other algebraic properties.

References

- [1] C. Amblard, S. Girard. Estimation procedures for a semiparametric family of bivariate copulas, *Journal of Computational and Graphical Statistics*, vol 14(2), pp 1–15 (2005).
- [2] R.B. Nelsen, *An introduction to copulas*, Lecture Notes in Statistics, Springer (1999).

¹Cécile Amblard
Université Grenoble 1
e-mail: Cecile.Amblard@imag.fr
²Stéphane Girard
INRIA Grenoble Rhône-Alpes
e-mail: Stephane.Girard@inria.fr
³Ludovic Mennetau
Université Montpellier 2
e-mail: mennet@math.univ-montp2.fr