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► **To cite this version:**

Hossein Aghighi, John Trinder, Yuliya Tarabalka, Samsung Lim. Dynamic Block-Based Parameter Estimation for MRF Classification of High-Resolution Images. IEEE Geoscience and Remote Sensing Letters, IEEE - Institute of Electrical and Electronics Engineers, 2014, 11 (10), pp.1687-1691. <hal-01016505>

HAL Id: hal-01016505

<https://hal.inria.fr/hal-01016505>

Submitted on 30 Jun 2014

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Dynamic Block-Based Parameter Estimation for MRF Classification of High-Resolution Images

Hossein Aghighi, *Student Member, IEEE*, John Trinder, Yuliya Tarabalka, *Member, IEEE*, and Samsung Lim

Abstract—A Markov random field is a graphical model that is commonly used to combine spectral information and spatial context into image classification problems. The contributions of the spatial versus spectral energies are typically defined by using a smoothing parameter, which is often set empirically. We propose a new framework to estimate the smoothing parameter. For this purpose, we introduce the new concepts of dynamic blocks and class label co-occurrence matrices. The estimation is then based on the analysis of the balance of spatial and spectral energies computed using the spatial class co-occurrence distribution and dynamic blocks. Moreover, we construct a new spatially weighted parameter to preserve the edges, based on the Canny edge detector. We evaluate the performance of the proposed method on three data sets: a multispectral DigitalGlobe WorldView-2 and two hyperspectral images, recorded by the AVIRIS and the ROSIS sensors, respectively. The experimental results show that the proposed method succeeds in estimating the optimal smoothing parameter and yields higher classification accuracy values when compared with state-of-the-art methods.

Index Terms—Classification, Markov random field (MRF), smoothing parameter, support vector machine (SVM).

I. INTRODUCTION

THE latest and upcoming generations of optical imaging sensors capture data with very high spectral and spatial resolutions. This raises new opportunities for remote sensing applications and challenges, where both spectral and spatial image contents have to be analyzed. Markov random fields (MRFs) are probabilistic models that are commonly used to incorporate spatial information via a neighborhood system for image classification problems [1]. In the MRF framework, the maximum *a posteriori* (MAP) decision rule is commonly formulated as the minimization of an energy function comprising spatial and spectral terms. One of the theoretical challenges consists in the proper choice of the balance between

the contributions of these two energy terms, which is controlled by a weight or a *smoothing parameter*. It has been demonstrated that a too large value of the smoothing parameter results in oversmoothing of the classification map and that a too small value does not fully utilize the available spatial information [2].

In order to estimate the smoothing parameter, Derin and Elliott used the least squares approach in terms of a second-order neighborhood system [3]. Later on, several heuristic methods have been proposed to improve parameter estimation and classification accuracy, such as iterative conditional estimation [4], genetic algorithms [5], Ho–Kashyap optimization method [6], and simulated annealing [2]. Jia and Richards [7] used the normalization value of the spatial and spectral components in the range (0, 1) to determine weighting coefficient estimation.

Recently, Tolpekin and Stein [8] followed by Li *et al.* [2] have proposed to estimate the smoothing parameter based on the analysis of the local energy balance. They concluded that the smoothing parameter is affected by class separability, scale factor information, neighborhood system size, configuration of class labels, and choice of the power-law index. Although their method proposed an efficient way for estimating the smoothing weight, it introduced another parameter, which was set as the constant empirical value in [8] and [2]. Because this parameter depends on the configuration of class labels in the image, it can be estimated based on the spatial frequency distribution of each pair of classes in each specific image, what was not done in [8] and [2]. Moreover, the existing methods suffer from the equal-class covariance matrix assumption.

This letter presents a novel and robust framework for smoothing parameter estimation under the Gaussian class-conditional density assumption, which overcomes the limitations of the use of constant empirical values. A contextually adaptive smoothing parameter estimation method is proposed on the basis of the balance of spatial and spectral energies and the global spatial frequency distribution of co-occurrence class label. The class labels are estimated by introducing three new concepts called the dynamic blocks, class-label co-occurrence matrix of the blocks (CLCMB) and global class-label co-occurrence matrix of the blocks (GCLCMB), which comprise the second contribution of this letter. The third contribution of this letter is a new edge probability index to preserve the information and location of edges while performing spatial regularization.

The outline of this letter is as follows: Section II explains the framework of the proposed method and details of each step. In Section III, the data description and the experimental results are presented and discussed. Finally, conclusions are drawn in Section IV.

Manuscript received November 18, 2013; revised January 13, 2014; accepted February 3, 2014.

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Digital Object Identifier 10.1109/LGRS.2014.2305913

Fig. 2(b)]. Then, the sum of the selected values for each block is calculated and assigned to the central pixel in that block [see Fig. 2(c)]. In the next steps, the blocks are categorized based on the class labels of their central pixels [see Fig. 2(d)]. The blocks of each class are then sorted in descending order based on their probability sums [see Fig. 2(c)], and an equal proportion of blocks with the highest sums is selected for each class. These selected blocks are assumed to be reliably classified.

Next, the mean and covariance of each class are estimated using the SVM probability vectors for the central pixels of the selected blocks of each class. Then, the estimated means and covariances are used to compute $\Delta U_{\alpha\beta}^l$, i.e.,

$$\Delta U_{\alpha\beta}^l = \frac{1}{2} (\mu_\beta - \mu_\alpha)' \Sigma^{-1} (\mu_\beta - \mu_\alpha) \quad (5)$$

where Σ is computed using the average of the covariances for each pair of classes instead of using the same covariance matrix for all the classes [8]. The final output of this step is a square matrix of size M , which shows the Mahalanobis distance for each pair of classes. Moreover, the class code of the pixels of the selected blocks is extracted and used to calculate the CLCMB and the GCLCMB (see Section II-D).

D. CLCMB and GCLCMB

According to the concept of dynamic blocks, a new concept is defined and is called the class-label co-occurrence matrix of the blocks (CLCMB) [11]. CLCMB is a square matrix of size M that provides information about the spatial frequency distribution of each pair of classes in the selected blocks of each class; a similar concept with a different methodology was introduced in [12]. Let N_b be the number of selected blocks for a class ω_i . Since the second-order neighboring system is chosen, each central pixel (y_i) is surrounded by $N_s = 8$ pixels (y_j). The CLCMB index is calculated for the blocks of each class ω_i as

$$CLCMB_{\omega_i, \omega_j} = \sum_{b=1}^{N_b} \sum_{s=1}^{N_s} \delta(\ell_c, \omega_i) \delta(\ell_s, \omega_j). \quad (6)$$

Here, $CLCMB_{\omega_i, \omega_j}$ is the CLCMB for class ω_i with class ω_j . In this equation, ℓ_c is the class label of the central pixel of block b , and ℓ_s is the class label of its surrounding pixels s . The neighboring conditions in MRF say that: 1) a site cannot be a neighbor with itself $i \notin N_i'$; 2) the neighborhood relationship is mutual ($i \in N_j \iff j \in N_i$) [10]. Therefore, the CLCMB is converted to the global class-label co-occurrence matrix of the blocks (GCLCMB), which is a square matrix of size M and shows the global spatial frequency distribution of each pair of classes in the image, based on the selected blocks, i.e.,

$$GCLCMB_{\omega_i, \omega_j} = CLCMB_{\omega_i, \omega_j} + CLCMB_{\omega_j, \omega_i}. \quad (7)$$

The local posterior energy of the central pixel (1) is penalized by the frequency of the neighboring pixel labels as a spatial energy term (3). Thus, by globally analyzing an image, the probability that the true label (α) for a given pixel is misclassified as a false label (β) due to the spatial energy is the same as the global joint probability distribution of each pair of those classes in the image, which is computed by GCLCMB. Therefore, $\psi_{\alpha\beta}$ for each pair of classes ($\psi_{\alpha\beta}$) is the element

of the GCLCMB matrix, which belongs to classes α and β . In the next step, $\Delta U_{\alpha\beta}^l$ and $\psi_{\alpha\beta}$ are used to compute $\lambda_{\alpha\beta}$ for each pair of classes using (4). Finally, the average of $\lambda_{\alpha\beta}$ for all of the classes is computed and is called the optimized smoothing parameter (λ^*), i.e.,

$$\lambda^* = \frac{\sum_{\alpha=1}^M \sum_{\beta=1}^M \lambda_{\alpha\beta}}{M(M-1)}. \quad (8)$$

E. Edge Probability Map

Each image band may provide different or even conflicting information based on its wavelength. Hence, extraction of an accurate edge map for very high resolution multispectral images and hyperspectral images is a challenging topic [9], [13]. Therefore, a one-band gradient from the B -band image is computed by using the Canny edge detector for all bands (B) and with (n_t) hysteresis threshold levels between (0.1 and 1) [14]. By a summation for all bands and all threshold levels, the edge probability map is computed [15]. The resulting map is convolved with the Gaussian kernel to decrease the smoothness effects near boundary regions [14]. In order to relate the edge probability of each pixel to the smoothing parameter, a new spatially weighted parameter $w_{(i)}$ is constructed, i.e.,

$$w_{(i)} = 1 - \frac{1}{B \times n_t} \sum_{i=1}^B \sum_{j=1}^{n_t} G_{(i,j)}, \quad 0 < w_{(i)} \leq 1 \quad (9)$$

where $G_{(i,j)}$ is the binary edge map generated by using the Canny edge detector on each band at each hysteresis threshold. Therefore, to preserve the small structures and edges in the classified map, a new spatial energy component for edge for the adaptive MRF is proposed. Thus

$$U_{\text{spatial}}^E(y_i) = \sum_{y_j \in N_i} w_{(i)} (1 - \delta(\ell_i, \ell_j)) \quad (10)$$

where superscript E refers to the edge probability map.

III. RESULTS AND DISCUSSION

In order to evaluate the performance of the proposed smoothing parameter estimation method, several experiments were conducted using a multispectral satellite image, medium-resolution and very high resolution airborne hyperspectral images.

- 1) Mildura region image: A multispectral WorldView-2 (WV-2) image from 2010-05-21 comprising 521×521 pixels, which is located between 142.071 E, 34.188 S and 142.083 E, 34.197 S. The image of the area is very complex and comprises a variety of garden and building roof colors. Seven major land use and land cover types were chosen: gardens, farms, grass, trees, bare soil, roads, and buildings.
- 2) The Indian Pines image: A hyperspectral image of an agricultural area, which is recorded by the AVIRIS sensor. The image comprises 145×145 pixels with 20 m/pixel spatial resolution and 200 spectral bands. Its reference map contains 16 classes.

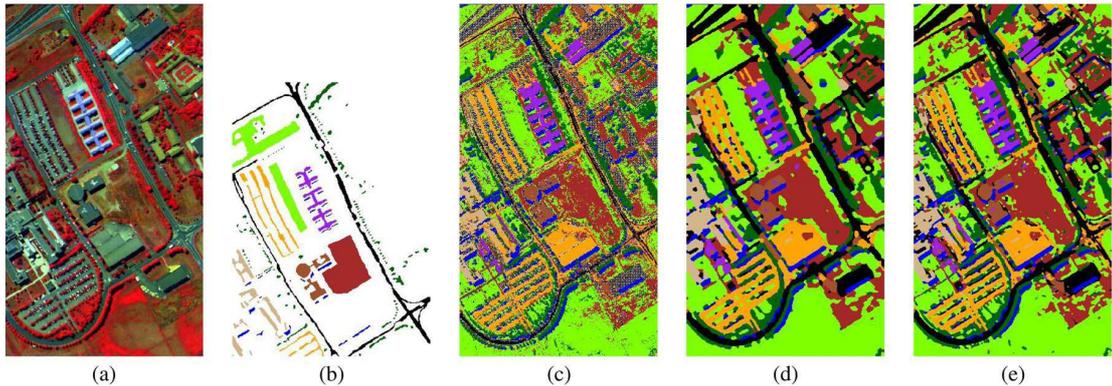


Fig. 3. University of Pavia. (a) Three-band color composite. (b) Reference data. (c) SVM pixelwise classification map. (d) SVMRF-NE classification map. (e) SVMRF-E classification map.

TABLE I
ESTIMATED λ^* FOR SVMRF METHODS

Studying area	Mildura region	Indian pines	Pavia University
λ^*	0.913	0.9657	0.9605

- 3) The University of Pavia image: A very high spatial resolution hyperspectral image of an urban area, which is acquired by the ROSIS sensor comprises 610×340 pixels and 103 spectral channels [see Fig. 3(a)]. Nine classes of interest are considered [see Fig. 3(b)].

In order to compare the accuracy of classified maps, the same sets of test pixels for each image were selected by the stratified random method [16]. The training set contained 50 pixels per class, and the test set comprised 1000 pixels for all the classes for the WV-2 image. Table III gives the number of training and test pixels for each class for the AVIRIS and ROSIS data sets, respectively.

In this letter, multiclass one-versus-one SVM classification was adopted as a nonlinear classifier through the use of a Gaussian radial basis function kernel [9]. The optimal SVM parameters C and γ were chosen by fivefold cross validation [9]. The *SVMLIB* library was used to estimate the probability for individual classes for each pixel and produce the classification map [see Fig. 3(c)]. Then, the results of SVM classification were used to estimate smoothing parameter λ^* for each data set (see Table I).

To estimate the efficiency of the parameter estimation method, we applied both nonedge-based SVMRF and edge-based SVMRF methods with different values of smoothing parameter λ , varying from 0.1 to 0.99. The resulting overall accuracy values for the three data sets are reported in Table II, from which it can be concluded that parameter λ^* estimated by the proposed dynamic block-based method yielded the highest overall accuracy values for the three images.

Table III gives overall (OA), average (AA), and class-specific accuracy values, as well as the kappa coefficient (K) [7] for the SVM, SVMRF-NE, and SVMRF-E methods [9], for the Indian Pines and the University of Pavia images, respectively. Fig. 3(c)–(e) shows the corresponding classification maps for the University of Pavia image. It can be seen that the classification maps obtained by applying the MRF-based method with the optimal smoothing parameter contain more homogeneous regions and look less noisy than the SVM classification map.

TABLE II
OVERALL ACCURACY ASSESSMENT OF THE CLASSIFIED MAPS FOR SVMRF METHOD WITH DIFFERENT SMOOTHING PARAMETERS AND SVM FOR WV-2, AVIRIS, AND ROSIS IMAGES

Smoothing Parameter	Mildura region		Indian pines		Pavia University	
	SVMRF		SVMRF		SVMRF	
	NE	E	NE	E	NE	E
0.1	73.9	74.5	87.8	85.5	85.3	85.2
0.2	73.8	74.9	89.1	87.7	87.4	86.9
0.3	73.8	76.5	90.5	89.1	88.6	85.9
0.4	74.2	76.8	90.9	90.3	89.2	89.2
0.5	74.5	77.7	91.1	90.3	89.6	89.5
0.6	74.7	77.4	91.6	91.0	90	89.9
0.7	75.2	77.5	91.6	92.0	90.4	90.4
0.8	76.8	78	91.6	92.1	91	91.7
0.9	77.4	78.8	91.6	92.2	91.4	93.9
0.99	76.3	76.2	91.3	91.7	84.8	92.1
λ^*	77.7	82.5	91.8	92.3	91.5	94.1
SVM	73.5	73.5	82.2	82.2	84.8	84.8

We compared the performance of our classification system using the proposed smoothing parameter estimation method with the classification methods described in [9] and [17], which used similar data sets and methods. The results of this study indicate that the accuracy values obtained for the Indian Pines image are comparable with those obtained in previous works. However, the overall accuracy values of our method for the University of Pavia image are improved by 6.5% and 8.4%, when compared with the results of Tarabalka *et al.* [9], for SVMRF-E and SVMRF-NE methods, respectively.

The overall accuracy of the proposed SVMRF-E framework is higher than that of the SVMRF-NE method for all three data sets. We evaluated the statistical significance of the improvement of classification results in terms of accuracy, when the proposed edge probability index was included in the classification, by using McNemar's test with the 5% significance level for each pair of the classification maps of each data set [17]. According to the calculated χ^2 and z values, the null hypothesis (H_0) of no significant difference between two map accuracy values is rejected for both Indian Pines and University of Pavia images. This means that the use of the proposed edge probability index is beneficial for MRF-based hyperspectral image classification. The results of the Pavia University and Indian Pines image classification were then compared with those of Tarabalka *et al.* [9]. Although using both fuzzy no-edge/edge index [9] and the edge probability map similarly increased

TABLE III

NUMBER OF TRAINING AND TEST PIXELS AND CLASSIFICATION ACCURACY IN PERCENTAGE FOR EACH CLASS OF **THE INDIAN PINES** IMAGE AND **THE UNIVERSITY OF PAVIA** IMAGE, WHERE **OA**, **AA**, AND **K** REPRESENT THE **OVERALL ACCURACY**, **AVERAGE ACCURACY**, AND **KAPPA COEFFICIENT**; CLASSES 1–9 IN THE UNIVERSITY OF PAVIA IMAGE REPRESENT ASPHALT, MEADOWS, GRAVEL, TREES, PAINTED METAL SHEETS, BARE SOIL, BITUMEN, SELF-BLOCKING BRICKS, AND SHADOWS, AND CLASSES 1–16 FOR THE INDIAN PINES IMAGE REPRESENT ALFALFA, CORN-NO TILL, CORN-MIN TILL, CORN, GRASS/PASTURE, GRASS TREES, GRASS/PASTURE-MOWED, HAY-WINDROWED, OATS, SOYBEANS-NO TILL, SOYBEANS-MIN TILL, SOYBEANS-CLEAN TILL, WHEAT, WOODS, BLDF-GRASS-TREE-DRIVES, STON-STEEL TOWERS, RESPECTIVELY

	The University of Pavia					The Indian pines				
	No. of samp		SVM	SVMMRF		No. of samp		SVM	SVMMRF	
	Train	Test		NE	E	Train	Test		NE	E
OA	-	-	84.8	91.5	94.1	-	-	82.2	91.8	92.3
AA	-	-	88.0	93.1	94.3	-	-	85.1	95.3	95.7
K	-	-	0.803	0.892	0.922	-	-	0.797	0.905	0.912
1	50	6581	71.7	83.9	82.5	15	39	63.0	85.2	85.2
2	50	18599	86.4	93.1	97.5	100	1334	75.3	88.8	89.0
3	50	2049	74.8	81.9	83.4	100	734	70.8	79.8	84.2
4	50	3014	93.1	93.6	93.9	100	134	95.0	99.4	99.4
5	50	1295	99.2	99.7	98.6	100	397	96.4	97.4	98.1
6	50	4979	82.5	91.2	93.5	100	647	97.2	99.6	100
7	50	1280	95.6	98.4	100.0	15	11	92.3	100	100
8	50	3632	90.1	96.9	99.4	100	389	99.5	99.8	99.8
9	50	897	99.0	99.1	99.9	15	5	100	100	100.0
10	-	-	-	-	-	100	868	88.8	98.3	98.7
11	-	-	-	-	-	100	2368	69.4	85.0	84.7
12	-	-	-	-	-	100	514	88.5	98.5	98.5
13	-	-	-	-	-	100	112	99.3	99.3	99.3
14	-	-	-	-	-	100	1194	91.5	95.2	96.3
15	-	-	-	-	-	100	280	83.6	98.4	98.7
16	-	-	-	-	-	50	45	100	100	100

the *SVMMRF_E* classification accuracy for the Pavia University data set, a comparison of the two results reveals that the proposed edge probability map improved the overall accuracy by 2.6% (see Table II), while the use of the fuzzy no-edge/edge index in [9] improved the overall accuracy by only 0.7%. For the Indian Pines image, the use of no-edge/edge index in [9] yielded a decrease in overall accuracy of 0.2%, while the proposed edge probability map yielded the improvement of overall accuracy by 0.5%.

This nonsignificant difference between the *SVMMRF_E* and *SVMMRF_NE* classification maps of the Mildura image needs to be interpreted with caution. Because this image contains large spatial structures, the selected test points do not comprise region edges due to the small subpopulation of the region edge pixels in the image.

IV. CONCLUSION

In this letter, a novel robust framework for the smoothing parameter estimation for the spectral-spatial classification of very high spectral and spatial resolution remote sensing images has been presented. This method consists in performing SVM classification, followed by a new concept that is called dynamic blocks and two new indexes (CLCMB and GCLCMB) to estimate the smoothing parameter for MRF-based optimization. Furthermore, a new spatially weighted parameter based on the Canny filter is proposed, which helps in preserving edges

in the image scene. Experimental results have demonstrated that the proposed method can estimate the optimal smoothing parameter, and it yields accurate classification maps for images captured by different types of sensors.

ACKNOWLEDGMENT

The authors would like to thank DigitalGlobe for providing the DigitalGlobe WorldView-2 images, the Murray-Darling Basin Authority for providing the very high resolution aerial images, and the anonymous reviewers for comments that helped improve and clarify this manuscript.

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