



# Stability of Asynchronously Communicating Systems

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**Abstract:** Recent software is mostly constructed by reusing and composing existing components. Software components are usually stateful and therefore described using behavioral models such as finite state machines. Asynchronous communication is a classic interaction mechanism used for such software systems. However, analyzing communicating systems interacting asynchronously via reliable FIFO buffers is an undecidable problem. A typical approach is to check whether the system is bounded, and if not, the corresponding state space can be made finite by limiting the presence of communication cycles in behavioral models or by fixing buffer sizes.

In this paper, we focus on infinite systems and we do not restrict the system by imposing any arbitrary bounds. We introduce a notion of stability and prove that once the system is stable for a specific buffer bound, it remains stable whatever larger bounds are chosen for buffers. This enables us to check certain properties on the system for that bound and to ensure that the system will preserve them whatever larger bounds are used for buffers. We also prove that computing this bound is undecidable but show how we succeed in computing these bounds for many typical examples using heuristics and equivalence checking.

**Key-words:** Communicating Systems, Labelled Transition Systems, Unbounded Buffers, Verification

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## Stabilité des systèmes communicants de façon asynchrone

**Résumé :** Le logiciel moderne est principalement construit par réutilisation et composition de composants existants. Les composants logiciels sont souvent décrits par des modèles comportementaux tels que des machines à états. La communication asynchrone est un mécanisme de communication classique pour les systèmes logiciels. Cependant, analyser des systèmes communicants interagissant de façon asynchrone au travers de buffers FIFO est un problème indécidable. Une approche habituelle est de vérifier si le système est borné, et s'il ne l'est pas, l'espace d'états correspondant peut être rendu fini en limitant la présence de cycles de communication dans les modèles ou en fixant une taille arbitraire aux buffers.

Dans ce rapport, nous nous focalisons sur des systèmes infinis et nous n'imposons aucune restriction au système. Nous introduisons une notion de stabilité et prouvons que lorsque le système est stable pour une borne spécifique, il reste stable pour des bornes plus élevées. Cela permet de vérifier que certaines propriétés sont satisfaites par le système pour cette borne, et assure que ces propriétés seront préservées pour des tailles supérieures pour les buffers. Nous avons aussi prouvé que calculer cette borne n'est pas décidable mais nous sommes capables en pratique de trouver cette borne pour de nombreux exemples en utilisant des heuristiques et la vérification d'équivalence.

**Mots-clés :** Systèmes communicants, systèmes de transitions étiquetées, buffers non bornés, vérification

## 1 Introduction

Most software systems are now constructed by reusing and composing existing components or peers. This is the case in many different areas such as component-based systems, cloud applications, Web services, or cyber-physical systems. Software entities are often stateful and therefore described using behavioral models. Moreover, asynchronous communication via FIFO buffers is a classic communication model used for such distributed, communicating systems. A crucial problem in this context is to check whether a new system consisting of a set of interacting peers respects certain properties. Analyzing asynchronously communicating software has been studied extensively in the last 30 years and is known to be undecidable in general [6]. A common approach to circumvent this issue is to bound the state space by restricting the cyclic behaviors or imposing an arbitrary bound on buffers. Bounding buffers to an arbitrary size during the execution is not a satisfactory solution: if at some point buffers' sizes change (due to changes in memory requirements for example), it is not possible to know how the system would behave compared to its former version and new unexpected errors can show up.

In this paper, we do not want to impose any arbitrary bounds for buffer sizes. Hence, our focus is on systems that are likely to be unbounded and therefore result in infinite state spaces. It was shown recently that certain properties of distributed systems interacting asynchronously through unbounded buffers can be checked using the *synchronizability* property: [3] relies on this property to check whether a choreography is realizable and [28] uses it for verifying the compatibility of communicating systems. A set of peers is synchronizable if and only if the system generates the same sequences of messages under synchronous and unbounded asynchronous communication, considering only the ordering of the send actions and ignoring the ordering of receive actions. Focusing only on send actions makes sense for verification purposes because: (i) send actions are the actions that transfer messages to the network and are therefore observable, (ii) receive actions correspond to local consumptions by peers from their buffers and can therefore be considered to be local and private information. Synchronizability can be verified by checking the equivalence of the synchronous and 1-bounded asynchronous compositions of the given system. In the 1-bounded asynchronous composition, each peer is equipped with one input buffer bounded to size 1. Thus, this property can be verified using equivalence checking techniques on finite state spaces, although the system consisting of peers interacting asynchronously via unbounded buffers can result in infinite state spaces.

Figure 1 gives an example where peers are modelled using Labelled Transition Systems (LTSs). Transitions are labeled with either emissions (exclamation marks) or receptions (question marks). Initial states are marked with incoming half-arrows. This simple system is synchronizable because the synchronous system consists of sequences of interactions `request`, `result`, and `ack`, and this order is the same in the 1-bounded asynchronous system considering only send actions.

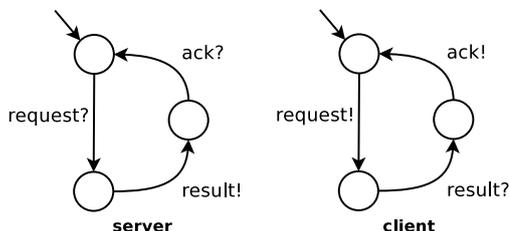


Figure 1: Motivating Example (1)

Let us now focus on a slightly extended version of this example where in addition the server

stores every request answered in a database (log) as depicted in Figure 2. This system is not synchronizable because the client can submit a second request in the 1-bounded asynchronous system before the server sends the log message to the database, and this behavior is not possible in the synchronous composition. So what can we do for non-synchronizable systems? This second example is typically unbounded, because the database peer has no obligation to consume from its buffer which can infinitely receive log messages. So far, and to the best of our knowledge, existing approaches cannot analyze such infinite-state systems.

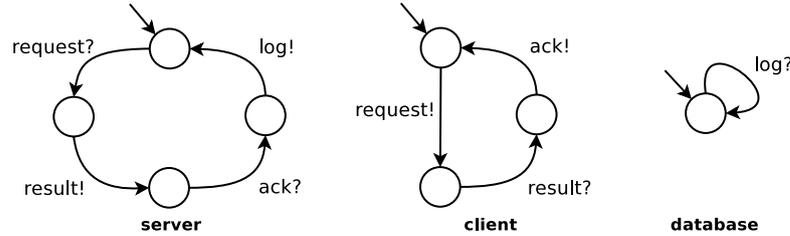


Figure 2: Motivating Example (2)

In this paper, we propose a new approach for analyzing a set of peers described using LTSs, communicating asynchronously via reliable (possibly unbounded) FIFO buffers. By reliability, we mean that there is no loss of messages. We do not want to restrict the system by imposing any arbitrary bounds on cyclic behaviors or buffers. We introduce a notion of stability for the asynchronous version of the system, which can be seen as a generalization of the synchronizability property. A system is stable if asynchronous compositions exhibit the same observable behavior from some buffer bound. We prove that once the system is stable for a specific buffer bound, it remains stable whatever larger bounds are chosen for buffers. This enables one to check temporal properties on the system for that bound and ensures that the system will preserve them whatever larger bounds are used for buffers. We also prove that computing this bound is undecidable, but we show how we succeed in computing such bounds in practice for many examples.

Going back to the former example (Fig. 2), we can use our approach to detect that when each peer is equipped with a buffer bound fixed to 2, the observable behavior of this system is stable. This means that we can check properties, such as the absence of deadlocks, on the 2-bounded asynchronous version of the system and the results hold for any asynchronous version of the system where buffer bounds are greater or equal to 2.

We implemented our approach in a tool that first encodes the peer LTSs and their compositions into process algebra, and then uses heuristics and equivalence checking techniques for verifying whether the system satisfies the stability property. If this is the case, we return the smallest bound respecting this property. Otherwise, our check stops when we reach a certain maximal bound, and we return an inconclusive result. Equivalence checking techniques are used for checking the stability properties and heuristics aim at guiding the approach towards the smallest bound satisfying stability. All the steps of our approach are fully automated (no human intervention). We applied our tool support to about 250 examples of communicating systems, many of them taken from the literature on this topic. We report in this paper on these experiments, which show that a large number of these examples are stable.

Our contributions with respect to existing results on formal verification of asynchronously communicating systems are the following:

- A general framework for verifying systems interacting asynchronously via reliable FIFO buffers;

- The introduction of the stability property for such systems and a proof showing that stability once acquired for a specific bound  $k$  is preserved for upper bounds;
- A proof demonstrating that computing this bound  $k$  is undecidable;
- A fully automated tool support that implements the presented approach and was applied to many examples for evaluation purposes.

The organization of the rest of this paper is as follows. Section 2 defines our models for peers and their synchronous/asynchronous compositions. Section 3 presents the stability property and our results on stable systems. Section 4 describes our tool support and experiments we carried out to evaluate our approach. Finally, Section 5 reviews related work and Section 6 concludes.

## 2 Communicating Systems

We use Labeled Transition Systems (LTSs) for modeling peers. This behavioral model defines the order in which a peer executes the send and receive actions.

**Definition 1** *A peer is an LTS  $\mathcal{P} = (S, s^0, \Sigma, T)$  where  $S$  is a finite set of states,  $s^0 \in S$  is the initial state,  $\Sigma = \Sigma^! \cup \Sigma^? \cup \{\tau\}$  is a finite alphabet partitioned into a set of send messages, a set of receive messages, and the internal action, and  $T \subseteq S \times \Sigma \times S$  is a transition relation.*

We write  $m!$  for a send message  $m \in \Sigma^!$  and  $m?$  for a receive message  $m \in \Sigma^?$ . We use the symbol  $\tau$  for representing internal activities. A transition is represented as  $s \xrightarrow{l} s' \in T$  where  $l \in \Sigma$ . This can be directly extended to  $s \xrightarrow{\sigma} s'$ ,  $\sigma \in \Sigma^*$ , where  $\sigma = l_1, \dots, l_n$ ,  $s \xrightarrow{l_1} s_1, \dots, s_i \xrightarrow{l_{i+1}} s_{i+1}, \dots, s_{n-1} \xrightarrow{l_n} s' \in T$ . In the following, for the sake of simplicity, we will denote this by  $s \xrightarrow{\sigma} s' \in T^*$ .

We assume that peers are deterministic on observable messages meaning that if there are several transitions going out from one peer state, and if all the transition labels are observable, then they are all different from one another. Observable determinism can be easily obtained in peers using standard determinization algorithms [21]. Nondeterminism can also result from internal choices when several transitions (at least two) outgoing from a same state are labeled with  $\tau$ . It is worth observing that these internal transitions are important when checking the synchronizability property [3, 28], which partly relies on synchronous communication. In such a case, internal transitions outgoing from a same state express an internal choice whereas transitions labeled with observable messages outgoing from a same state stand for an external choice semantics.

Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , we assume that each message has a unique sender and a unique receiver:  $\forall i, j \in 1..n, i \neq j, \Sigma_i^! \cap \Sigma_j^! = \emptyset$  and  $\Sigma_i^? \cap \Sigma_j^? = \emptyset$ . Furthermore, each message is exchanged between two different peers:  $\Sigma_i^! \cap \Sigma_i^? = \emptyset$  for all  $i$ . We also assume that each emission has a reception counterpart in another peer (closed systems):  $\forall i \in 1..n, \forall m \in \Sigma_i^! \implies \exists j \in 1..n, i \neq j, m \in \Sigma_j^?$ .

The synchronous composition of a set of peers corresponds to the system where a communication occurs when one peer can send a message and another peer is in a state in which that message can be received.

**Definition 2 (Synchronous Composition)** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$  with  $\mathcal{P}_i = (S_i, s_i^0, \Sigma_i, T_i)$ , the synchronous composition is the labeled transition system  $LTS_s = (S_s, s_s^0, \Sigma_s, T_s)$  where:*

- $S_s = S_1 \times \dots \times S_n$
- $s_s^0 \in S_s$  such that  $s_s^0 = (s_1^0, \dots, s_n^0)$
- $\Sigma_s = \cup_i \Sigma_i$
- $T_s \subseteq S_s \times \Sigma_s \times S_s$ , and for  $s = (s_1, \dots, s_n) \in S_s$  and  $s' = (s'_1, \dots, s'_n) \in S_s$

(interact)  $s \xrightarrow{m} s' \in T_s$  if  $\exists i, j \in \{1, \dots, n\}$  where  $i \neq j : m \in \Sigma_i^! \cap \Sigma_j^?$  where  $\exists s_i \xrightarrow{m^!} s'_i \in T_i$ ,  
and  $s_j \xrightarrow{m^?} s'_j \in T_j$  such that  $\forall k \in \{1, \dots, n\}, k \neq i \wedge k \neq j \Rightarrow s'_k = s_k$

(internal)  $s \xrightarrow{\tau} s' \in T_s$  if  $\exists i \in \{1, \dots, n\}, \exists s_i \xrightarrow{\tau} s'_i \in T_i$  such that  $\forall k \in \{1, \dots, n\}, k \neq i \Rightarrow s'_k = s_k$

In the asynchronous composition, the peers communicate with each other asynchronously via FIFO buffers. Each peer  $\mathcal{P}_i$  is equipped with an unbounded input message buffer  $Q_i$ . A peer can either send a message  $m \in \Sigma^!$  to the tail of the receiver buffer  $Q_j$  at any state where this send message is available, read a message  $m \in \Sigma^?$  from its buffer  $Q_i$  if the message is available at the buffer head, or evolve independently through an internal transition. We recall that we focus on send actions in this paper. We consider that reading from the buffer is private non-observable information, which is encoded as an internal transition in the asynchronous system.

**Definition 3 (Asynchronous Composition)** Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$  with  $\mathcal{P}_i = (S_i, s_i^0, \Sigma_i, T_i)$ , and  $Q_i$  being its associated buffer, the asynchronous composition is the labeled transition system  $LTS_a = (S_a, s_a^0, \Sigma_a, T_a)$  where:

- $S_a \subseteq S_1 \times Q_1 \times \dots \times S_n \times Q_n$  where  $\forall i \in \{1, \dots, n\}, Q_i \subseteq (\Sigma_i^?)^*$
- $s_a^0 \in S_a$  such that  $s_a^0 = (s_1^0, \epsilon, \dots, s_n^0, \epsilon)$  (where  $\epsilon$  denotes an empty buffer)
- $\Sigma_a = \cup_i \Sigma_i$
- $T_a \subseteq S_a \times \Sigma_a \times S_a$ , and for  $s = (s_1, Q_1, \dots, s_n, Q_n) \in S_a$  and  $s' = (s'_1, Q'_1, \dots, s'_n, Q'_n) \in S_a$

(send)  $s \xrightarrow{m^!} s' \in T_a$  if  $\exists i, j \in \{1, \dots, n\}$  where  $i \neq j : m \in \Sigma_i^! \cap \Sigma_j^?$ , (i)  $s_i \xrightarrow{m^!} s'_i \in T_i$ ,  
(ii)  $Q'_j = Q_j m$ , (iii)  $\forall k \in \{1, \dots, n\} : k \neq j \Rightarrow Q'_k = Q_k$ , and (iv)  $\forall k \in \{1, \dots, n\} : k \neq i \Rightarrow s'_k = s_k$

(consume)  $s \xrightarrow{\tau} s' \in T_a$  if  $\exists i \in \{1, \dots, n\} : m \in \Sigma_i^?$ , (i)  $s_i \xrightarrow{m^?} s'_i \in T_i$ , (ii)  $m Q'_i = Q_i$ ,  
(iii)  $\forall k \in \{1, \dots, n\} : k \neq i \Rightarrow Q'_k = Q_k$ , and (iv)  $\forall k \in \{1, \dots, n\} : k \neq i \Rightarrow s'_k = s_k$

(internal)  $s \xrightarrow{\tau} s' \in T_a$  if  $\exists i \in \{1, \dots, n\}, (i) s_i \xrightarrow{\tau} s'_i \in T_i, (ii) \forall k \in \{1, \dots, n\} : Q'_k = Q_k, and (iii) \forall k \in \{1, \dots, n\} : k \neq i \Rightarrow s'_k = s_k$

We use  $LTS_a^k = (S_a^k, s_a^0, \Sigma_a^k, T_a^k)$  to define the bounded asynchronous composition, where each message buffer is bounded to size  $k$ . The definition of  $LTS_a^k$  can be obtained from Def. 3 by allowing send transitions only if the message buffer of the receiving peer has less than  $k$  messages in it. Otherwise, the sender is blocked, *i.e.*, we assume reliable communication without message losses.

### 3 Stability

In this section, we introduce successively the synchronizability property, the stability property, the proof of undecidability for the stability property, and several results on stable systems.

#### 3.1 Synchronizability

The composition of finite peer LTSs can result into an infinite state system if these peers communicate asynchronously over unbounded buffers. This makes the exhaustive analysis of all executed communication traces impossible and verification tasks in this setting are undecidable [6]. This issue can be avoided for systems that are synchronizable [3]. The synchronizability property checks whether the sequences of send actions generated by the peer composition remain the same under synchronous and asynchronous communication semantics. This enables one to analyze asynchronous systems, even those generating an infinite state space, using the synchronous version of the given system (which has a finite state space). This property was used recently for analyzing properties on communicating systems [28] and is checked using branching equivalence [33], which is the finest equivalence notion in presence of internal behaviors.

**Definition 4 (Branching Bisimulation)** *Given two LTSs  $LTS_1$  and  $LTS_2$ , they are branching bisimilar, denoted by  $LTS_1 \equiv_{br} LTS_2$ , if there exists a symmetric relation  $R$  (called a branching bisimulation) between the states of  $LTS_1$  and  $LTS_2$  satisfying the following two conditions:*

- *The initial states are related by  $R$ ;*
- *If  $R(r, s)$  and  $r \xrightarrow{\delta} rt$ , then either  $\delta = \tau$  and  $R(rt, s)$ , or there exists a path  $s \xrightarrow{\tau^*} s_1 \xrightarrow{\delta} st$ , such that  $R(r, s_1)$  and  $R(rt, st)$ .*

For the sake of simplicity and consistency, the relation  $R$  is replaced by  $\equiv_{br}$  in the rest of this paper, *i.e.*,  $R(r, s)$  is noted  $r \equiv_{br} s$ .

**Definition 5 (Branching Synchronizability)** *A set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$  is branching synchronizable if  $\forall k \geq 1$ ,  $LTS_s \equiv_{br} LTS_a^k$ .*

It was proved that  $LTS_s \equiv_{br} LTS_a^1$  is a sufficient and necessary condition for branching synchronizability [28].

The synchronizability property is quite strong and there are many non-synchronizable systems, see *e.g.*, Fig. 2. If the set of peers is not synchronizable, there is no standard solution for formally analyzing those systems.

#### 3.2 Stability

In this section, we show that systems consisting of a finite set of peers involving cyclic behaviors and communicating over FIFO buffers may stabilize from a specific buffer bound  $k$ . We call this property *stability* and we say that the corresponding systems are *stable*. The class of systems which are not synchronizable yet stable corresponds to systems whose asynchronous compositions remain the same from some buffer bound when we observe send actions only (we ignore receive actions and buffer contents). Stability results do not hold if we consider that receptions are also observable. Focusing only on send actions makes sense for verification purposes because: (i) send actions are the actions that transfer messages to the network and are therefore observable,

(ii) receive actions correspond to local consumptions by peers from their buffers and can therefore be considered to be local and private information.

Since stable systems produce the same behavior from a specific bound  $k$ , they can be analyzed for that bound to detect for instance the presence of deadlocks or to check whether they satisfy any kind of temporal properties. Stability ensures that these properties will be also satisfied for larger bounds. The stability definition relies on branching equivalence checking, and this equivalence preserves properties written with ACTL\X logic [27].

Contrarily, some systems are not stable. Unstability is due to some particular cycle inclusion in the peer behaviors that makes the asynchronous composition exhibit new behaviors every time the buffer bound is increased. In the rest of this section, we will first define the stability property. We will show how stability is established and what can be deduced for such systems. We will also present other results such as the non-decidability of the stability problem.

**Definition 6 (Stability)** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , we say that this system is stable if and only if  $\exists k$  such that  $LTS_a^k \equiv_{br} LTS_a^q$  ( $\forall q > k$ ).*

Before presenting our main results, we first introduce a few definitions that will be used in the following deduction. First, a border state of  $LTS_a^k$  is considered as a boundary between  $LTS_a^k$  and  $LTS_a^{k+1}$  if the latter has more behaviors than the former due to larger buffers. This means that the transitions after any border state in  $LTS_a^{k+1}$  cannot exhibit in  $LTS_a^k$  due to limited buffer size. Precisely, for a border state of  $LTS_a^k$ , the first condition of Definition 7 means that during the trace from the initial state to a border state, there is no state whose buffer contains more than  $k$  messages. The second condition states that a border state has a successor state in  $LTS_a^{k+1}$  that is not reachable in  $LTS_a^k$  due to limited buffer size. Then the new behavior, which leads to a state whose buffers contain  $k+1$  messages that are not contained in  $LTS_a^k$ , must begin after this border state.

**Definition 7 (Border State)** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , given a state  $s^k = (s_1^k, Q_1^k, \dots, s_n^k, Q_n^k) \in S_a^k$ , if it satisfies the following two conditions, we call it a  $k$ -border state, simply a border state if there is no ambiguity:*

- $\forall s'^k \in S_a^k, s'^k \xrightarrow{\sigma} s^k \in T_a^{k*}$ , where  $s'^k = (s'_1{}^k, Q_1'^k, \dots, s'_n{}^k, Q_n'^k)$  we have  $\forall i \in \{1, \dots, n\}$ ,  $|Q_i'^k| < k+1$  and  $|Q_i^k| < k+1$ ;
- $\exists s''^k \xrightarrow{m^1} s'^k \in T_a^{k+1}$ , where  $s''^k$  has one peer whose buffer contains  $k+1$  messages.

A single  $k$ -message state defined as follows is a state where only one buffer contains  $k$  messages.

**Definition 8 (Single  $k$ -message State)** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$  and a state  $s^k = (s_1^k, Q_1^k, \dots, s_n^k, Q_n^k) \in S_a^k$ , if  $\exists i \in \{1, \dots, n\}, |Q_i^k| = k, \forall j \in \{1, \dots, n\}, j \neq i, |Q_j^k| < k$ , and there exists a border state  $s^{k-1}$  such that  $s^{k-1} \xrightarrow{m^1} s^k \in T_a^k, m^? \in \Sigma_i^k$ , then  $s^k$  is a single  $k$ -message state, denoted by  $SG(s^k)$ .*

In the left part of Figure 3, the small ellipsis represents  $LTS_a^{k-1}$  and the bigger one is  $LTS_a^k$ . Here,  $s^k \in S_a^k$  is a single  $k$ -message state and  $s^{k-1} \in S_a^{k-1}$  is the corresponding border state.

Next we define a special state  $s^k$  in  $LTS_a^k$  such that it contains only one buffer with  $k$  messages, whose precedent state is a border state. Furthermore, from this border state, there are two branches. One is to reach  $s^k$  with one emission. The other one is to reach another state  $s^{k-1}$  through a reception followed by the same emission such that  $s^{k-1}$  contains at most  $k-1$  messages in its buffers. Then we will show  $s^k \equiv_{br} s^{k-1}$  and that these two branches will converge in the future, *i.e.*, there will form a confluent diamond.

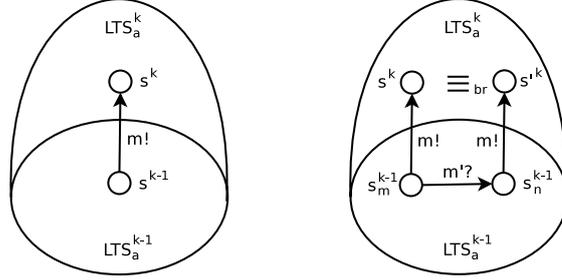


Figure 3: A single k-message state (left part) and a loose k-message state (right part).

**Definition 9 (Loose k-message State)** Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$  and a state  $s^k$  such that  $SG(s^k)$ , i.e.,  $\exists s_m^{k-1} \xrightarrow{m!} s^k \in T_a^k$ ,  $m? \in \Sigma_i^?$ ,  $i \in \{1, \dots, n\}$ , where  $s_m^{k-1}$  is a border state, then  $s^k$  is called a loose k-message state, denoted by  $LS(s^k)$ , if the following conditions are satisfied

1.  $\exists m!? \in \Sigma_i^?$ , such that  $s_m^{k-1} \xrightarrow{m!?} s_n^{k-1} \xrightarrow{m!} s'^k$ , where  $s_m^{k-1} \xrightarrow{m!?} s_n^{k-1}$ ,  $s_n^{k-1} \xrightarrow{m!} s'^k \in T_a^k$ ;
2. for  $s^k$  and  $s'^k$ , we have  $s^k \equiv_{br} s'^k$

In the right part of Figure 3,  $s^k \in S_a^k$  is a loose k-message state which is a single k-message state satisfying the above two conditions.

**Theorem 1** Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , the following holds for each single k-message state  $s^k \in S_a^k$ .

$$LS(s^k) \Leftrightarrow \exists s^{k-1} \in S_a^{k-1} \text{ such that } s^{k-1} \equiv_{br} s^k$$

**Proof .**

$\Rightarrow$  Suppose that for a single k-message state  $s^k = (s_1^k, Q_1^k, \dots, s_n^k, Q_n^k) \in S_a^k$ ,  $|Q_i^k| = k$ ,  $i \in \{1, \dots, n\}$ ,  $LS(s^k)$  holds. Then in  $LTS_a^k$ ,  $\exists m? \in \Sigma_i^?$ , such that  $s_0^k \xrightarrow{\sigma} s_m^k \xrightarrow{m!} s^k$ , where  $s_0^k \xrightarrow{\sigma} s_m^k \in T_a^{k*}$ ,  $s_m^k \xrightarrow{m!} s^k \in T_a^k$ . From Definition 9, we know that  $s_m^k$  is a border state and that  $\exists m!? \in \Sigma_i^?$ ,  $s_0^k \xrightarrow{\sigma} s_m^k \xrightarrow{m!?} s_n^k \xrightarrow{m!} s'^k$ , where  $s_m^k \xrightarrow{m!?} s_n^k$ ,  $s_n^k \xrightarrow{m!} s'^k \in T_a^k$ . This implies that there must be a corresponding part in  $LTS_a^{k-1}$ :  $s_0^{k-1} \xrightarrow{\sigma} s_m^{k-1} \xrightarrow{m!?} s_n^{k-1} \xrightarrow{m!} s'^{k-1}$ , where  $s_0^{k-1} \xrightarrow{\sigma} s_m^{k-1} \in T_a^{k-1*}$ ,  $s_m^{k-1} \xrightarrow{m!?} s_n^{k-1}$ ,  $s_n^{k-1} \xrightarrow{m!} s'^{k-1} \in T_a^{k-1}$ ,  $s'^{k-1} = (s_1'^{k-1}, Q_1'^{k-1}, \dots, s_n'^{k-1}, Q_n'^{k-1})$ ,  $|Q_j'^{k-1}| < k$ ,  $\forall j \in \{1, \dots, n\}$ . The reason is that the maximum number of messages in all states between  $s_0^{k-1}$  and  $s'^{k-1}$  is smaller than  $k$ . Now from the second condition of Definition 9, we know that beginning from the state  $s^k$  in  $LTS_a^k$  and from  $s'^{k-1}$  in  $LTS_a^{k-1}$ , we have exactly the same branching structure. This implies  $s^k \equiv_{br} s'^{k-1}$ .

$\Leftarrow$  Now suppose that in  $LTS_a^k$ , we have a single k-message state  $s^k = (s_1^k, Q_1^k, \dots, s_n^k, Q_n^k) \in S_a^k$ ,  $|Q_i^k| = k$ ,  $i \in \{1, \dots, n\}$ , such that  $LS(s^k)$  does not hold. From Definition 9, we show that the violation of each one of the two conditions implies  $\nexists s^{k-1} \in S_a^{k-1}$ , such that  $s^k \equiv_{br} s^{k-1}$ .

1. If the first condition is not satisfied, i.e.,  $\nexists m!? \in \Sigma_i^?$ , such that  $s_m^k \xrightarrow{m!?} s_n^k \xrightarrow{m!} s'^k$ , where  $s_m^k \xrightarrow{m!?} s_n^k$ ,  $s_n^k \xrightarrow{m!} s'^k \in T_a^k$ . This implies that the reception of  $m!$  that is contained in the buffer  $Q_i^k$  cannot be executed between the border state  $s_m^k$  and the state just before  $m!$ . If  $m!?$  is executed after  $m!$  preceding the border state, then there is no equivalent state in  $LTS_a^{k-1}$  with respect to  $s^k$  since the part after the border state cannot be reached in

$LTS_a^{k-1}$ . Otherwise, if  $m!?$  is before the border state, *e.g.*, suppose  $s_h^k \xrightarrow{l!/?} s_m^k \xrightarrow{m!} s^k$ , where  $s_h^k \xrightarrow{l!/?} s_m^k, s_m^k \xrightarrow{m!} s^k \in T_a^k$ , we have  $s_h^k \xrightarrow{m!/?} s_p^k \xrightarrow{l!/?} s_q^k \xrightarrow{m!} s_r^k$ , where  $s_h^k \xrightarrow{m!/?} s_p^k, s_p^k \xrightarrow{l!/?} s_q^k, s_q^k \xrightarrow{m!} s_r^k \in T_a^k$ . In this case, we can deduce that  $m!?$  should execute before  $l!/?$ . In other words,  $\nexists s^k \xrightarrow{m!/?} s \in T_a^k$ . This means that we cannot reach  $s_r^k$  from  $s^k$ , *i.e.*, there is no confluent diamond. Thus, there is no branching equivalent state in  $LTS_a^{k-1}$  for  $s^k$ .

2.  $\exists m!? \in \Sigma_g^?, s_m^k \xrightarrow{m!/?} s_n^k \xrightarrow{m!} s'^k$ , where  $s_m^k \xrightarrow{m!/?} s_n^k, s_n^k \xrightarrow{m!} s'^k \in T_a^k, s^k \not\equiv_{br} s'^k$ . It is clear that we have also  $s^k \not\equiv_{br} s_n^k$  since  $m!$  is before  $s^k$  but after  $s_n^k$ . Thus, there is no branching equivalent state in  $LTS_a^{k-1}$  for the state  $s^k$ .

From above, if a single  $k$ -message state is not a loose one, then  $\nexists s^{k-1} \in S_a^{k-1}$  such that  $s^{k-1} \equiv_{br} s^k$ .

Thus, we have proved this theorem for both directions. ■

Here is the main result of this paper. If we are able to find a bound  $k$  such that the  $k$ -bounded and the  $(k+1)$ -bounded asynchronous systems are branching equivalent, then we prove that the system remains stable, meaning that the observable behavior is always the same for any bound greater than  $k$ . The main interest of the stability property is that the  $k$ -bounded version of the system can be analyzed using existing model checking tools and this result ensures that these properties are preserved when buffer bounds are increased or if buffers are unbounded.

**Theorem 2** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , if  $\exists k \in \mathbb{N}$ , such that  $LTS_a^k \equiv_{br} LTS_a^{k+1}$ , then the system is stable. In other words:  $LTS_a^k \equiv_{br} LTS_a^{k+1} \Rightarrow LTS_a^k \equiv_{br} LTS_a^q, \forall q > k$ .*

**Proof .**

We prove this theorem by induction. The idea is to show  $LTS_a^k \equiv_{br} LTS_a^q, \forall q > k$  from  $LTS_a^k \equiv_{br} LTS_a^{k+1}$ . We rewrite  $q > k$  by  $q = k + m, m \geq 1$ . Now the base case  $m = 1$  is true from the hypothesis, *i.e.*,  $LTS_a^k \equiv_{br} LTS_a^{k+1}$ . To prove that this is also true for  $\forall m > 1$ , we suppose  $LTS_a^k \equiv_{br} LTS_a^{k+1} \equiv_{br} \dots \equiv_{br} LTS_a^{k+m}, m \geq 1$  and we show  $LTS_a^k \equiv_{br} LTS_a^{k+m+1}$ . To do this, we consider two cases according to whether the maximum number of messages in all buffers is smaller than  $k + m + 1$  or not in the asynchronous composition, which are formally represented as follows:

1. In  $LTS_a^{k+m+1}, \forall s^{k+m+1} = (s_1^{k+m+1}, Q_1^{k+m+1}, \dots, s_n^{k+m+1}, Q_n^{k+m+1}) \in S_a^{k+m+1}$ , we have  $\forall i \in \{1, \dots, n\}, |Q_i^{k+m+1}| \leq k + m$ ;
2. In  $LTS_a^{k+m+1}, \exists s^{k+m+1} = (s_1^{k+m+1}, Q_1^{k+m+1}, \dots, s_n^{k+m+1}, Q_n^{k+m+1}) \in S_a^{k+m+1}$ , such that  $\exists i \in \{1, \dots, n\}, |Q_i^{k+m+1}| = k + m + 1$ .

Now we show that in each of the two cases, we can deduce  $LTS_a^k \equiv_{br} LTS_a^{k+m+1}$ .

- The first case implies that in the asynchronous composition of this set of peers  $LTS_a$ , the buffer of any peer contains at most  $k+m$  messages in all states of  $LTS_a$ . Hence,  $LTS_a^{k+m+1}$  is exactly the same LTS as  $LTS_a^{k+m}$ . This follows  $LTS_a^{k+m+1} \equiv_{br} LTS_a^{k+m}$ . From the assumption  $LTS_a^k \equiv_{br} LTS_a^{k+m}$ , we have  $LTS_a^k \equiv_{br} LTS_a^{k+m+1}$ .
- In the second case, since there exists a buffer containing  $k + m + 1$  messages, there are new states in  $LTS_a^{k+m+1}$  that are not in  $LTS_a^{k+m}$ . Now from the inductive hypothesis, we have  $LTS_a^{k+m-1} \equiv_{br} LTS_a^{k+m}$ . Then from Theorem 1, we can deduce that for each single

( $k+m$ )-message state  $s^{k+m}$  in  $LTS_a^{k+m}$ , we have  $LS(s^{k+m})$ , i.e.,  $\exists s^{k+m-1} \in S_a^{k+m-1}$ , such that  $s^{k+m-1} \equiv_{br} s^{k+m}$ . From Definition 9, we know that the only difference between the path from  $s_a^0$  to  $s^{k+m-1}$  and that from  $s_a^0$  to  $s^{k+m}$  is that the former has one more reception that has however no impact on the execution after  $s^{k+m-1}$  since  $s^{k+m-1} \equiv_{br} s^{k+m}$ . So when we reach  $s^{k+m+1} \in S_a^{k+m+1}$  from  $s^{k+m}$  through  $\sigma \in \Sigma_a^+$ , then we also have the state  $s'^{k+m} \in S_a^{k+m}$  that is reached from  $s^{k+m-1}$  through  $\sigma$ . This follows  $s'^{k+m} \equiv_{br} s^{k+m+1}$ . Thus, we show that for each state in  $LTS_a^{k+m+1}$ , we have a branching equivalent state in  $LTS_a^{k+m}$ . Hence, we have  $LTS_a^{k+m} \equiv_{br} LTS_a^{k+m+1}$ . From  $LTS_a^k \equiv_{br} LTS_a^{k+m}$ , we prove  $LTS_a^k \equiv_{br} LTS_a^{k+m+1}$ .

This proves the theorem. ■

### 3.3 Undecidability

Before showing the undecidability of checking the stability of a system, we first present a sufficient and necessary condition for a system that is stable.

**Theorem 3** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , this system is stable iff the following condition is satisfied, denoted by  $\mathcal{C}$ :*

$$\exists k \in \mathbb{N}, \forall s^k \in S_a^k. [\neg SG(s^k) \vee LS(s^k)].$$

**Proof .**

$\Rightarrow$  Suppose that the given set of peers is stable. Next we show that the stability of the set of peers implies that the condition  $\mathcal{C}$  is satisfied. Since this set of peers is stable, from Theorem 2, we deduce  $\exists k \in \mathbb{N}$ , such that  $LTS_a^k \equiv_{br} LTS_a^{k-1}$ . There are two cases for this:

1.  $LTS_a^k = (S_a^k, s_a^0, \Sigma_a^k, T_a^k)$  and  $LTS_a^{k-1} = (S_a^{k-1}, s_a^0, \Sigma_a^{k-1}, T_a^{k-1})$  have exactly the same structure, i.e.,  $S_a^k = S_a^{k-1}, \Sigma_a^k = \Sigma_a^{k-1}, T_a^k = T_a^{k-1}$ ;
2.  $LTS_a^k$  and  $LTS_a^{k-1}$  do not have the same structure but are branching equivalent, i.e.,  $S_a^k \neq S_a^{k-1}$  and  $T_a^k \neq T_a^{k-1}$ .

We demonstrate that any one of the two cases must satisfy the condition  $\mathcal{C}$ .

- In the first case, we can deduce that in  $LTS_a^k$ , for each peer, its buffer contains at most  $k-1$  messages in all states, i.e.,  $\forall s^k = (s_1^k, Q_1^k, \dots, s_n^k, Q_n^k) \in S_a^k, \forall i \in \{1, \dots, n\}, |Q_i^k| < k$ . This follows that there is no single  $k$ -message state in  $LTS_a^k$ , i.e.,  $\forall s^k \in S_a^k, \neg SG(s^k)$ . Hence, the condition  $\mathcal{C}$  is satisfied.
- Now consider the second case, where  $LTS_a^k$  and  $LTS_a^{k-1}$  are not exactly the same one. Hence, we can deduce  $\exists s^k = (s_1^k, Q_1^k, \dots, s_n^k, Q_n^k) \in S_a^k, \exists i \in \{1, \dots, n\}, |Q_i^k| = k$  in  $LTS_a^k$ . In other words, there exists at least one single  $k$ -message state. Furthermore, since  $LTS_a^k \equiv_{br} LTS_a^{k-1}$ , for all states in  $LTS_a^k$ , there must be a corresponding branching equivalent state in  $LTS_a^{k-1}$ , including all single  $k$ -message states. Thus, from Theorem 1, we can deduce that  $\forall s^k \in S_a^k$ , we have either  $\neg SG(s^k)$  or  $LS(s^k)$ . This means that the condition  $\mathcal{C}$  is satisfied.

So if the set of peers is stable, then the condition  $\mathcal{C}$  should be satisfied.

$\Rightarrow$  Now suppose that the condition  $\mathcal{C}$  is satisfied. Thus, we consider three cases: all states are not single  $k$ -message states, formally described by the first case in the following; all states are loose  $k$ -message states, which is not possible since the initial state has no message in all buffers; some of the states are single  $k$ -messages states that should be loose ones, formally presented by the second case below:

1.  $\exists k \in \mathbb{N}, \forall s^k \in S_a^k$ , we have  $\neg SG(s^k)$ ;
2.  $\exists k \in \mathbb{N}, \forall s^k \in S_a^k$  such that  $SG(s^k)$ , we have  $LS(s^k)$ .

Now we show that any one of these two conditions implies that the system is stable.

- The first condition means that in  $LTS_a^k$ , there is no single k-message state, *i.e.*, the maximum number of messages in buffers is smaller than  $k$  for any state. It can thus be deduced that  $LTS_a^k$  and  $LTS_a^{k-1}$  have exactly the same structure, which follows  $LTS_a^k \equiv_{br} LTS_a^{k-1}$ . From Theorem 2, this is a stable set of peers.
- The second condition means that all single k-message state in  $LTS_a^k$  are loose ones. From Theorem 1, it can be deduced that  $\forall s^k \in S_a^k$ , there is a corresponding state  $s^{k-1} \in S_a^{k-1}$ , such that  $s^k \equiv_{br} s^{k-1}$ . It is clear that  $\forall s^k \in S_a^k$ , we have at least one corresponding branching equivalent state in  $LTS_a^k$ . This follows that  $LTS_a^k \equiv_{br} LTS_a^{k-1}$ . Hence, this set of peers is stable from Theorem 2.

Hence, if the condition  $\mathcal{C}$  is satisfied, then the system is stable. ■

Next we show that checking the stability of the system is undecidable by showing that verifying the condition  $\mathcal{C}$  is an undecidable problem. Yet there are many cases in which stability is satisfied and the corresponding bound can be computed in those cases using heuristics and equivalence checking (see Section 4).

**Theorem 4** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , it is undecidable whether the corresponding asynchronous system is stable.*

**Proof .**

From Theorem 3, we know that  $\mathcal{C}$  is a sufficient and necessary condition to check that a system is stable. We show that the problem of checking this condition is undecidable. The idea is to demonstrate that the boundedness problem [6] is its subproblem. The communication of a set of peers with FIFO buffers is said to be bounded iff  $\exists k \in \mathbb{N}$  such that for any reachable state  $s = (s_1, Q_1, \dots, s_n, Q_n) \in S_a$ , we have  $\forall i \in \{1, \dots, n\}, |Q_i| < k$ . Now recall that to check whether the condition  $\mathcal{C}$  is violated, the following two conditions should be both checked one after another:

- $\forall k \in \mathbb{N}, \exists s^k \in S_a^k$ , such that  $SG(s^k)$ ;
- $\neg LS(s^k)$ .

Now we show that the first condition is equivalent to the boundedness problem. If this condition is satisfied, it can be deduced that  $\nexists k \in \mathbb{N}$ , such that  $\forall s = (s_1, Q_1, \dots, s_n, Q_n) \in S_a$ , we have  $\forall i \in \{1, \dots, n\}, |Q_i| < k$ . So this system is not bounded. On the other hand, if the condition is not satisfied, *i.e.*,  $\exists k \in \mathbb{N}$ , there does not exist a reachable state such that it is a single k-message state. This means that  $\forall s^k = (s_1^k, Q_1^k, \dots, s_n^k, Q_n^k) \in S_a^k$ , we have  $\neg SG(s^k)$ . From Definition 8, to have  $\neg SG(s^k)$ , consider three cases for  $s^k$ : 1) at least two buffers contain  $k$  messages, *i.e.*,  $\exists i_1, \dots, i_m \in \{1, \dots, n\}, |Q_{i_j}^k| = k, j \in \{1, \dots, m\}, m \geq 2$ ; 2) no buffer contains  $k$  messages, *i.e.*,  $\forall i \in \{1, \dots, n\}, |Q_i^k| < k$ ; 3) there does not exist a border state  $s^{k-1}$  such that  $s^{k-1} \xrightarrow{m!} s^k \in T_a^k$ , where  $SG(s^k)$ . For the first case, if this is true, there must be at least one  $s^k$  such that  $SG(s^k)$  since to reach a state where more than one buffer has  $k$  messages, we have to first reach such a state  $s^k$ ,  $SG(s^k)$ . This follows that the first case is not possible with the assumption without single k-message states. Then the second case means that the maximum number of messages in

buffers is smaller than  $k$ . And for the third case, even in  $s^k$ , there exists a buffer containing  $k$  messages, this state cannot be reached in  $LTS_a^k$  since there is no border state before it. From above, we analyze all three cases for a state  $s^k$  such that  $\neg SG(s^k)$ . We can see that  $\neg SG(s^k)$  implies that  $s^k$  is bounded by  $k$ . This follows that if  $\forall s^k \in S_a^k$ , we have  $\neg SG(s^k)$ , then the system is bounded. So we have shown that this first condition is equivalent to the boundedness problem, which is thus a subproblem of checking  $\mathcal{C}$ : consequently, if the former is undecidable, which was proved in [6], then so is the latter. ■

### 3.4 Other Results

In the rest of this section, we present a few additional results on the stability of communicating systems.

**Proposition 1** *A set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$  is stable if it is synchronizable.*

**Proof .**

From Definition 5, a system is synchronizable meaning that all its asynchronous compositions are branching equivalent whatever is the bound for buffers. This means that  $\forall k, q \in \mathbb{N}$ , we have  $LTS_a^k \equiv_{br} LTS_a^q$ . Now from Definition 6, it follows that this system is stable. ■

The opposite is false because stability ensures branching equivalence of the asynchronous systems from a specific bound  $k$ , which means that systems for lower bounds and for its synchronous version behave differently.

The next result concerns computability of the smallest buffer bound for stable systems.

**Proposition 2** *Given a stable set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , the minimal bound  $k$  satisfying the stability property is computable.*

**Proof .**

Since this set of peers is stable, from Theorem 2, we know that  $\exists k \in \mathbb{N}$ ,  $LTS_a^k \equiv_{br} LTS_a^{k+1}$ . This means that  $k$  is finite. Furthermore, it is clear that the construction of  $LTS_a^k$ ,  $LTS_a^{k+1}$  and their equivalence checking is computable. Hence, the minimal bound  $k$  for the stability property is also computable. ■

The computability of the stability property will be illustrated on real-world examples in Section 4 by using equivalence checking and heuristics.

Beyond these results on stability, a common approach is to identify classes of systems where stability is guaranteed. This is the case of synchronizable systems (Prop. 2) and also of *finite systems*. By finite systems, we mean systems where peers interact over unbounded FIFO buffers and whose asynchronous compositions are finite. This is the case for instance for acyclic peers, for systems with a single cyclic peer where cycles do not involve only emissions, or for systems with peers exhibiting *independent cycles*, *i.e.*, cycles that are not included one from another [24]. Apart from these obvious cases, two candidates are (i) systems involving peers exhibiting cycles of emissions, and (ii) well-formed systems. Unfortunately, we show in the rest of this section that we cannot take any conclusions regarding stability for these classes of systems.

Let us start with systems where peers can infinitely send messages. We establish that the existence of a cycle of emissions in one peer has no impact on whether the system is stable or not, which is however a sufficient condition for unboundedness [6].

**Proposition 3** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , if a peer  $\mathcal{P}_i \in \{\mathcal{P}_1, \dots, \mathcal{P}_n\}$  exhibits a cycle of emissions  $\phi = s_i^k \xrightarrow{m_i!} s_i^{k+1} \dots \xrightarrow{m_n!} s_i^k$  such that it can infinitely send messages, this does not imply that the system is stable.*

**Proof .**

We prove this result by demonstrating that a system with a cycle of emissions in one peer that is able to infinitely send messages may be stable or not. Suppose first that for this system, in  $LTS_a$ ,  $\forall \sigma \in \Sigma_a^*, s_a^0 \xrightarrow{\sigma} s^{n-1} \xrightarrow{m_i!} s^n, s_a^0 \xrightarrow{\sigma} s^{n-1} \in T_a^*, s^{n-1} \xrightarrow{m_i!} s^n \in T_a$ , where  $m_i!$  is one send message in  $\phi$ , then  $\exists \sigma' \in \Sigma_a^*, s_a^0 \xrightarrow{\sigma'} s^{m-1} \xrightarrow{m_i!} s^m \xrightarrow{m_i?} s^{m+1}, s_a^0 \xrightarrow{\sigma'} s^{m-1} \in T_a^*, s^{m-1} \xrightarrow{m_i!} s^m, s^m \xrightarrow{m_i?} s^{m+1} \in T_a$ , where  $P_1(\sigma) = P_1(\sigma')$ . Here we denote the projection of  $\sigma$  on send messages by  $P_1(\sigma)$ . This means that whenever a message in this cycle is emitted, there exists at least one execution with the same sequence of emissions, where the corresponding peer is ready to receive it. In this case, the system may be stable.

Now suppose that in this system,  $\exists \sigma \in \Sigma_a^*, s_a^0 \xrightarrow{\sigma} s^{n-1} \xrightarrow{m_i!} s^n, s_a^0 \xrightarrow{\sigma} s^{n-1} \in T_a^*, s^{n-1} \xrightarrow{m_i!} s^n \in T_a$ , where  $m_i!$  is one send message in  $\phi$ , for which  $\nexists \sigma' \in \Sigma_a^*, s_a^0 \xrightarrow{\sigma'} s^{m-1} \xrightarrow{m_i!} s^m \xrightarrow{m_i?} s^{m+1}$ , such that  $s_a^0 \xrightarrow{\sigma'} s^{m-1} \in T_a^*, s^{m-1} \xrightarrow{m_i!} s^m, s^m \xrightarrow{m_i?} s^{m+1} \in T_a$ , where  $P_1(\sigma) = P_1(\sigma')$ . This means that  $\exists \sigma'' \in \Sigma_a^*, s_a^0 \xrightarrow{\sigma''} s^{m-1} \xrightarrow{m_i!} s^m \xrightarrow{\sigma''} s^t \xrightarrow{m_i?} s^{t+1}$ , where  $s_a^0 \xrightarrow{\sigma''} s^{m-1}, s^m \xrightarrow{\sigma''} s^t \in T_a^*$  and  $s^{m-1} \xrightarrow{m_i!} s^m, s^t \xrightarrow{m_i?} s^{t+1} \in T_a$ . Next we show that there is at least one send message in the sequence  $\sigma''$ . This can be proved by assuming that all messages in  $\sigma''$  are receive messages, which in turn implies  $\exists s_a^0 \xrightarrow{\sigma''} s^m \xrightarrow{m_i!} s^n \xrightarrow{m_i?} s^{n+1}$  and thus a contradiction. So it is clear that in  $\sigma''$ , we must have at least one send message. This follows that  $\forall k \in \mathbb{N}$ , in  $LTS_a^{k+1}$ ,  $\exists s^0 \xrightarrow{\sigma} s^m \xrightarrow{m_i!} s^n \xrightarrow{m(i+1) \bmod n!} s^{n+1} \dots \xrightarrow{m(i+j) \bmod n!} s^{n+j}$ , whose corresponding part in  $LTS_a^k$  is  $s^0 \xrightarrow{\sigma} s^m \xrightarrow{m_i!} s^n \xrightarrow{m(i+1) \bmod n!} s^{n+1} \dots \xrightarrow{m(i+j-1) \bmod n!} s^{n+j-1}$ . This follows  $LTS_a^k \not\equiv_{br} LTS_a^{k+1}$  and the system is thus not stable. ■

The example shown in Figure 4 has a cycle of emissions. This system is not synchronizable because there is a deadlock before entering this cycle in its synchronous composition, which is however not the case for its asynchronous one. This means that there is no branching equivalence between the synchronous and asynchronous compositions. However, it is stable from bound 1, *i.e.*,  $LTS_a^1 \equiv_{br} LTS_a^k, k > 1$ .

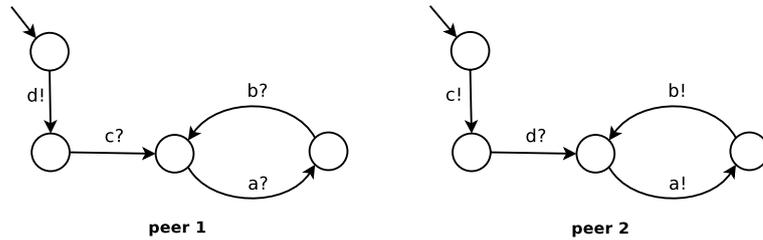


Figure 4: A Stable System Exhibiting a Cycle of Emissions

Figure 5 depicts another example with a cycle of emissions that is not stable. For this example, if we first execute  $a!$  and  $b!$  before  $c!$ , then to read the receive message from the buffer of peer 2, we have to wait for  $c!$ . Hence, consider the execution where  $c$  is still not sent. We have that  $\forall k, LTS_a^{k+1}$  always exhibits a new observable behavior compared to  $LTS_a^k$ . The reason is

that the cycle of emissions in peer 1 can infinitely send  $a$  and  $b$ , which is only constrained by the size of buffer in Peer 2. This follows that this system is not stable.

Another result concerns well-formed systems [3]. A system consisting of a set of peers is well-formed iff whenever the size of the buffer,  $Q_i$ , of the  $i$ -th peer is non-empty, the system can move to a state where  $Q_i$  is empty.

**Definition 10 (Well-formed System)** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , it is well-formed if  $\forall s = (s_1, Q_1, \dots, s_n, Q_n) \in S_a, \forall Q_i$ , such that  $|Q_i| > 0$ , then  $\exists s \xrightarrow{\sigma} s' \in T_a^*$ , where  $s' = (s_1', Q_1', \dots, s_n', Q_n') \in S_a, |Q_i'| = 0$ .*

**Proposition 4** *The well-formedness of a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$  can be checked with the following CTL temporal formula on its asynchronous composition  $LTS_a$ :*

$$AG(|Q_i| > 0) \Rightarrow EF(|Q_i| = 0)$$

We show that a well-formed system is not mandatorily stable, *i.e.*, well-formedness is not a sufficient condition for stability.

**Proposition 5** *Given a set of peers  $\{\mathcal{P}_1, \dots, \mathcal{P}_n\}$ , its well-formedness does not imply that this set of peers is stable.*

**Proof .**

This can be proved by demonstrating that a well-formed system can be unstable. We illustrate this through the example depicted in Figure 5. Suppose that one peer in the system contains a cycle  $\phi = s_i^k \xrightarrow{\sigma} s_i^k$ , where  $\sigma \in \Sigma_a^+$  and  $\sigma$  contains at least one send message. In this example, one such cycle is  $\sigma = a!.b!$  in peer 1. Furthermore, there is at least one receive message corresponding to one send message in  $\phi$ , denoted by  $m_k?$ , in another peer with a preceding send message  $m_t!$ , such as  $a?$  or  $b?$  in peer 2, that is the reception of the emission  $a!$  or  $b!$  in peer 1, with a preceding emission  $c!$ . Suppose further that the execution of the cycle  $\phi$  is totally independent of the send message  $m_t!$ , *i.e.*,  $\phi$  can continue to execute regardless of the emission of  $m_t!$ , and that there is no constraint on  $m_t!$ , *i.e.*,  $m_t!$  can be emitted at any moment. This is the case for our example, where the cycle  $a!.b!$  is independent of  $c!$  whose execution is however possible at any moment. For such a system, we can deduce that it is not stable due to the cycle of emissions in peer 1 that can infinitely send messages, which generates new observable behaviors in  $LTS_a^{k+1}$  compared to  $LTS_a^k, \forall k \in \mathbb{N}$ , when  $c!$  is still not executed. Furthermore, this system is well-formed because the execution of  $c!$  is possible at any moment in peer 2, then all messages in its buffer can be eventually read (cycle of receptions) until the buffer is empty. ■

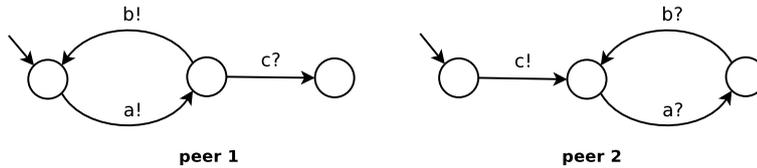


Figure 5: A Well-formed yet Unstable System

## 4 Tool Support

In this section, we present successively methodological aspects, an encoding into process algebra that is used here for computing peer compositions, heuristics for computing the smallest bound satisfying the stability property, and some experimental results.

### 4.1 Method

First of all, we introduce some methodological aspects that put in practice the results on systems stability we have presented in the former section. Figure 6 overviews the main steps of the overall approach. Given a set of peer LTSs, we first check whether this system is synchronizable [3]. If this is the case, it means that the observable behavior for the synchronous and asynchronous composition always remains the same whatever buffer size is chosen. Therefore, in such a case, the synchronous product can be used for analysis purposes.

If the set of peers is not synchronizable, we compute an initial bound  $k$  using one of the heuristics we will introduce below (Section 4.3). For that bound, we verify whether the  $k$ -bounded asynchronous system is branching equivalent to the  $(k + 1)$ -bounded system. If it is the case, the system is stable for bound  $k$ . Then, we decrement  $k$  for searching the smallest  $k$  satisfying the stability property. Thus, we can analyze properties of interest for that system (buffers bounded to the smallest  $k$ ) and, if they are satisfied, we claim that these properties are preserved for any upper bound.

If for a specific  $k$ , the equivalence check between the  $k$ -bounded asynchronous system and the  $(k + 1)$ -bounded system returns false, we modify  $k$  (using, *e.g.*, binary search or incremental update of the former bound) and apply the check again. We repeat the process up to a certain arbitrary bound  $kmax$  that makes the approach abort if attained. If we reach that bound, the test is inconclusive. The only solution in that situation is to bound arbitrarily the system and analyze the system for that specific bound.

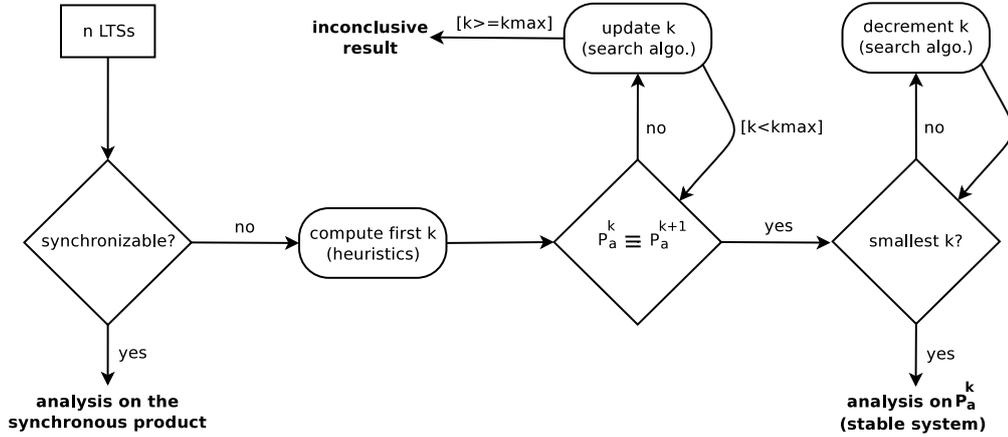


Figure 6: Methodological Aspects

### 4.2 Process Algebra Encoding

In order to automate these different checks, we use an encoding into process algebra and equivalence checking. In particular, we encode the set of peer LTSs into the LNT process algebra [10],

one of the input languages of the CADP toolbox [17]. Each peer LTS is represented in LNT using several processes. Each state in the peer LTS is encoded by one process, whose body corresponds to a choice between all the possible transitions outgoing from that state. Each branch of this choice first executes the action labelling the corresponding transition (message emission or reception, or internal action) followed by a call to the process encoding the target state of that transition. We also define in LNT FIFO buffers and classic operations to manipulate them. Finally, synchronous and bounded asynchronous compositions are generated using parallel composition and hiding operators. More precisely, in the asynchronous composition case, all peers and buffers are composed in parallel. Each peer reads from its buffer and sends messages to other peer buffers. Receptions corresponding to message consumptions for peers from their buffers are hidden.

In a second step, from this encoding, we use CADP compilers and exploration tools to generate synchronous and asynchronous composition LTSs. These LTSs are finally compared with CADP equivalence checking tools [4] for checking the stability property. The whole process is fully automated thanks to some Python scripts we wrote and SVL verification scripts [16] that are automatically generated. Python scripts are particularly used for generating the LNT code and for searching the smallest bound  $k$  satisfying stability. SVL scripts automate the compilation from LNT to LTSs and call the equivalence checking tools.

### 4.3 Heuristics and Search Algorithms

In our experimental results, we use five strategies for searching the smallest bound  $k$  from which the set of peers interacting asynchronously become stable. Since the calculation of this bound is undecidable, all computations are bound by an arbitrary upper bound  $kmax$ . Each strategy consists of the computation of an initial bound  $k$  and an algorithm calculating the next bound to attempt.

- Our first strategy (#1) is *brute force*, *i.e.*, we start from bound  $k$  equal to one and we increment it by one until obtaining a positive result for the equivalence check or reaching  $kmax$ .
- A second strategy (#2) computes the longest sequence of emissions in all peer LTSs, then starts from this number and uses a binary search algorithm. For example, if the stability check for the first  $k$  is true (false, resp.), the next  $k$  to explore is midway between 1 and  $k$  (between  $k$  and  $kmax$ , resp.).

The intuition behind the longest sequence of emissions is that in that case all peers can at least send all their messages even if no peer consumes any message from its buffer. Experiments show that in most cases, the searched bound  $k$  is greater than or equal to this computed size.

- A third strategy (#3) uses again the longest sequence of emissions for the initial  $k$ , but then progresses by incrementing or decrementing the bound till reaching  $kmax$  or the smallest  $k$  satisfying stability. Precisely, if the stability check for the first  $k$  is true (false, resp.), the next bound to explore is  $k - 1$  ( $k + 1$ , resp.).

The problem of the longest sequence of emissions is when several peers have the same partner as recipient of their messages. In such a case, the partner buffer can get full even if the sending peers still want to emit other messages to it.

- A fourth strategy (#4) computes the maximum between the longest sequence of emissions in all peers and the highest number of emissions destined to a same peer, and then uses

the binary search algorithm (as for #2) for computing the next bounds. The second part of the maximum function corresponds to the case in which the buffer size prevents some peers to send messages because that buffer is already full. This case is somehow the counterpart of the longest sequence of emissions but from the receiver point of view.

- A fifth strategy (#5) uses the same initial  $k$  computation as presented for strategy #4, and then increments or decrements the bound till completion of the process as in strategy #3.

In the rest of this section, for the sake of evaluation of our approach, we will present experimental results and use them for comparing the strategies introduced above.

#### 4.4 Experimental Results

We used a Mac OS laptop running on a 2.53 GHz Intel dual core processor with 4 GB of RAM and carried out experiments on about 250 examples of communicating systems. Table 1 presents experimental results for some real-world examples. We also present at the end of the table a few hand-crafted examples for showing how our approach scales (the examples from the literature are quite small). The table gives for each example the number of peers (P), the total number of states (S) and transitions (T) involved in these peers, the bound  $k$  if the system is stable (0 if the system is synchronizable and  $kmax$  if this upper bound is reached during the analysis process), the size of the  $k$ -bounded asynchronous system (minimized modulo branching reduction), and the time for applying the whole process for each strategy introduced beforehand. In the  $LTS_a^k$  column, we give the size of the 1-bounded asynchronous composition for synchronizable systems and the size of the  $kmax$ -bounded asynchronous composition for non-stable systems. During our experiments, we used a bound  $kmax$  arbitrarily fixed to 10, which enabled us to keep computation times within a few hours during our experiments.

Id	Description	P	S / T	$k$	$LTS_a^k$  S / T	Time (in seconds)				
						#1	#2	#3	#4	#5
(1)	Estelle specification [22]	2	7/9	5	28/54	148	264	164	250	146
(2)	News server [28]	2	9/9	3	14/22	105	212	100	204	101
(3)	Client/server [6]	2	6/10	0	3/4	40				
(4)	CFSM system [22]	2	6/7	$kmax$	393/802	295	125	246	133	247
(5)	Promela program (1) [23]	2	6/6	1	3/4	59	85	83	81	81
(6)	Promela program (2) [24]	2	8/8	$kmax$	275/616	268	124	271	127	278
(7)	Web Services [14]	3	13/12	0	7/7	53				
(8)	Trade system [13]	3	12/12	0	30/46	53				
(9)	Online stock broker [15]	3	13/16	$kmax$	168/379	a few hours				
(10)	Train station [31]	4	18/18	2	19/26	134	234	164	238	196
(11)	Factory job manager [8]	4	20/20	0	12/15	65				
(12)	Bug report repository [18]	4	12/12	1	7/8	98	276	172	266	219
(13)	Cloud application [20]	4	8/10	$kmax$	26,754/83,200	427	338	406	249	403
(14)	Sanitary agency [30]	4	35/41	3	44/71	170	239	169	247	166
(15)	Booking system [26]	5	45/53	1	27/35	117	361	210	hours	213
(16)	Hand-crafted example	5	396/801	4	17,376/86,345	272	hours	240	376	239
(17)	—	6	16/18	5	202/559	325	826	241	793	238
(18)	—	7	38/38	6	1,716/6,468	481	952	490	919	481
(19)	—	10	48/47	8	14,904/57,600	729	968	370	943	361
(20)	—	14	85/80	4	19,840/113,520	602	1,722	621	1,694	601
(21)	—	16	106/102	3	22,400/132,400	960	2,042	565	1,944	572
(22)	—	20	128/116	4	80,640/522,480	861	2,557	896	2,735	853

Table 1: Experimental results

All the examples included in the table involve cyclic behaviors. The examples from the literature correspond to quite simple systems (up to 5 peers). Four examples are synchronizable, seven examples are stable, and four examples are not stable. To sum up, out of the 15 real-world examples presented in the table, 11 can be analyzed using existing verification techniques and properties are satisfied for any buffer size. For these real-world examples, LTSs are quite small and computation times reasonable (up to a few minutes). Computation times may be less satisfactory for non-stable systems whose intermediate state spaces grow gradually with the size of the buffer bounds, until we stop once  $kmax$  is reached, see online stock broker for instance (9). However, it depends on the system and in some cases the computation time remains reasonable, see CFSM system (4). It is worth observing that some examples that are presented as unbounded and then impossible to analyze in the literature are actually stable, see, *e.g.*, Estelle specification (1).

As far as hand-crafted examples are concerned, we observe that the LTS sizes and computation times increase mainly with the size of the peer LTSs, the number of peers, and the size of buffer bounds. Yet we are able to check stable systems involving a large number of peers in a reasonable time (less than 15 minutes for the last example with 20 peers using #1, #3, or #5). This time remains quite low for peers exhibiting many states and transitions (about 4 minutes for the first hand-crafted example (16) using #1, #3, or #5).

Now let us compare the five strategies we used in our experiments. It turns out that strategy #2 and #4 are not very efficient in terms of performance for two main reasons. First, if the equivalence check for the initial  $k$  returns false, the binary search algorithm computes a second value for  $k$ , which can be quite high. This results in calculating asynchronous systems with large buffer bounds, which requires more computation time than for lower  $k$  values as computed with the other strategies. Second, in some cases, binary search takes time before converging to the result, and this causes additional equivalence computations. The advantage of binary search is that for non-stable systems,  $k$  increases quite fast and quickly reaches  $kmax$ , see CFSM system (4).

Strategies #3 and #5 are much better than strategies #2 and #4 but also better in most cases than strategy #1. This gain is not clear for small examples and examples requiring a small buffer bound, but it becomes obvious for examples involving more peers and for those requiring larger buffer bounds. These two strategies (#3 and #5) are particularly satisfactory when the initial  $k$  finely approximates the expected result. In such cases, we can have up to a factor 2 gain in terms of computation time, see the fourth hand crafted example (19) for illustration purposes.

## 5 Related Work

One of the first results on analyzing communicating state machines was proposed by Brand and Zafropulo [6]. They defined the unspecified receptions compatibility notion for interaction protocols described using Communicating Finite State Machines (CFSMs). This work focuses on the verification of  $n$  interacting processes executed in parallel and exchanging messages via FIFO buffers. When considering unbounded buffers, the authors showed that the resulting state spaces may be infinite, and the problem becomes undecidable. Gouda *et al.* [19] presents sufficient conditions to compute a bound  $k$  from which two finite state machines communicating through 1-directional channels are guaranteed to progress indefinitely. Jeron and Jard [22] propose a sufficient condition for testing unboundedness, which can be used as a decision procedure in order to check reachability for CFSMs.

Abdulla *et al.* [1] propose some verification techniques for CFSMs. They present a method for

performing symbolic forward analysis of unbounded *lossy* channel systems. In [23], the authors present an incomplete boundedness test for communication channels in Promela and UML RT models. They also provide a method to derive *upper bound* estimates for the maximal occupancy of each individual message buffer. Cécé and Finkel [9] focus on the analysis of infinite half-duplex systems and present several (un)decidability results. For instance, they prove that a symbolic representation of the reachability set is computable in polynomial time and show how to use this result to solve several verification problems. Poizat *et al.* [29] propose the notions of bounded analysis and bounded decomposition for Symbolic Transition Systems, which can be used to test boundedness of systems and to generate finite simulations for them so that standard model-checking techniques may be applied for verification purposes.

Darondeau and colleagues [11] identify a decidable class of systems consisting of non-deterministic communicating processes that can be scheduled while ensuring boundedness of buffers. [12] proposed a causal chain analysis to determine upper bounds on buffer sizes for multi-party sessions with asynchronous communication. Bouajjani and Emmi [5] consider a bounded analysis for message-passing programs, which does not limit the number of communicating processes nor the buffers' size. However, they limit the number of communication cycles. They propose a decision procedure for reachability analysis when programs can be sequentialized. By doing so, program analysis can easily scale while previous related techniques quickly explode. Recently, Ouederni *et al.* [28] presented a sufficient condition for checking compatibility of a set of asynchronously communicating components with unbounded message buffers. They exploit the synchronizability property introduced in [3], but if systems are non-synchronizable, they cannot be analyzed with this approach.

Last but not least, communicating systems have been intensively studied in the context of choreographies and realizability/conformance checking in the last 10 years. In [7], the authors tackle the choreography conformance issue from a theoretical point of view, and propose notions of contract refinement and choreography conformance for services that communicate through message queues. [18] proposes techniques to check whether a set of peers interacting asynchronously can realize a choreography with finite buffers, and if so, for what buffer sizes. [25] studies several notions of realizability and investigates decidability results for choreographies involving services interacting via buffers, which do not assume that messages arrive in the same order in which they have been sent. As mentioned earlier in this paper, Basu *et al.* proposed to check choreography conformance and realizability verifying the synchronizability property [3]. The realizability problem for Message Sequence Charts (MSCs) has also been studied, see *e.g.*, [32, 2]). [2] for instance presents some decidability results on bounded MSC graphs, which are graphs obtained from MSCs using bounded buffers.

Compared to all these results, we do not impose any bound on the number of peers, cycles, or buffer bounds. Another main difference is that we do not want to ensure or check boundedness of the systems under analysis. Contrarily, we are particularly interested in unbounded (yet possibly stable) systems. We also go one step farther than synchronizable systems, since we propose verification techniques for systems that do not satisfy this property.

## 6 Conclusion

We have presented in this paper a framework for formally analyzing systems communicating via (possibly unbounded) FIFO buffers. This work focuses on cyclic systems modelled using finite state machines. We have introduced the stability property, which shows several systems become stable from a specific buffer bound  $k$  when focusing on send messages. Computing this bound is undecidable in the general case, but for many systems we can compute it using heuristics

and search algorithms. Experiments showed that many real-world examples satisfy this stability property and this can be identified in a reasonable time using equivalence checking. Model checking techniques can then be used on the asynchronous version of the system with buffers bound to the smallest  $k$  satisfying stability. If a stable system satisfies a specific property for that  $k$ , the property will be satisfied too if buffer bounds are increased or if buffers are unbounded.

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