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#### ▶ To cite this version:

Nicolas Brodu, Joshua Dijksman, Robert Behringer. Quantitative DEM of dense granular packings with a multiple contacts force model. MGMAS 2014 - Modeling Granular Media Across Scales, Jul 2014, Montpellier, France. hal-01024663

#### HAL Id: hal-01024663 https://inria.hal.science/hal-01024663

Submitted on 16 Jul2014

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# Quantitative DEM of dense granular packings with a multiple contacts force model

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Modeling Granular Media across scales, Montpellier, July 2014

Founded by: NASA grant NNX10AU01G, NSF grant DMR12-06351, and ARO grant W911NF-1-11-0110

## MOTIVATION

### 1. 3D Experiments

Access to the micro-structure, 3D force vectors Used as a reference for a comparison with DEM

### 2. DEM

Usual DEM + Hertz interactions not good enough Interactions between multiple contacts

## **ACCESSING THE MICRO-STRUCTURE**

X-rays / micro-ct Fine resolution Most materials Costly

### **Confocal:** emulsions

Microscopic Costly Difficult to control applied stresses

### This work: refractive index matching

Macroscopic grains Easy to control, tri-axial shearing Cheap **Submersed** 

Next slides on:

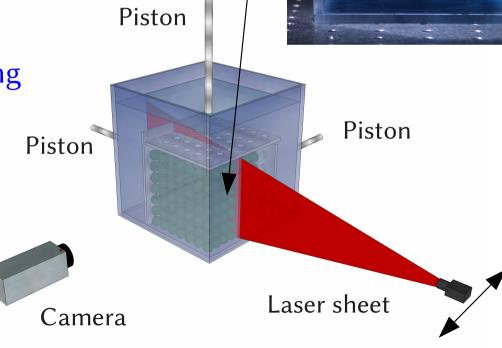
- 1. Structure
- 2. Forces in 3D

Mukhopadhyay et al. Phys. Rev. E 84, 011302, 2011 Dijksman *et al.* Rev. Sci. Intstrum, 2012

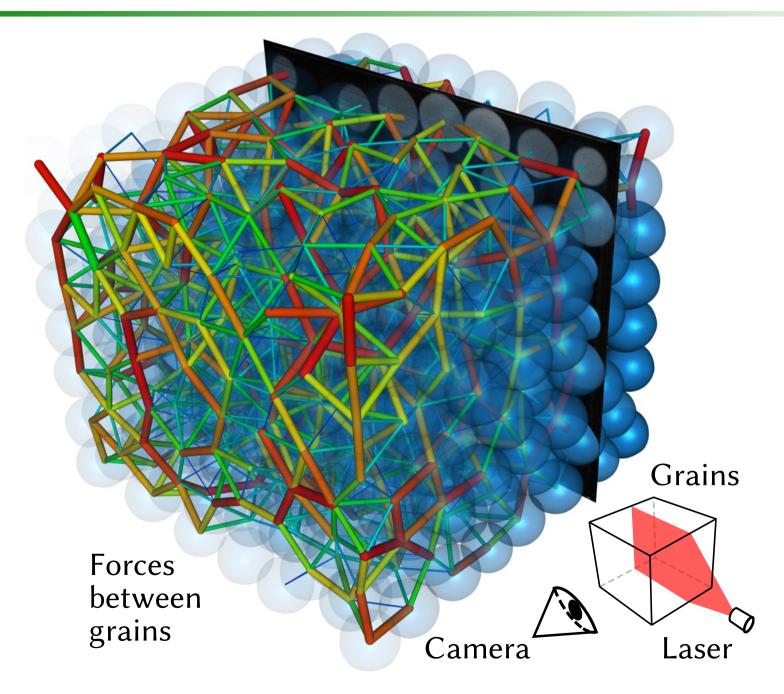
> Hydrogel grains index-matched

+ fluorescent dye

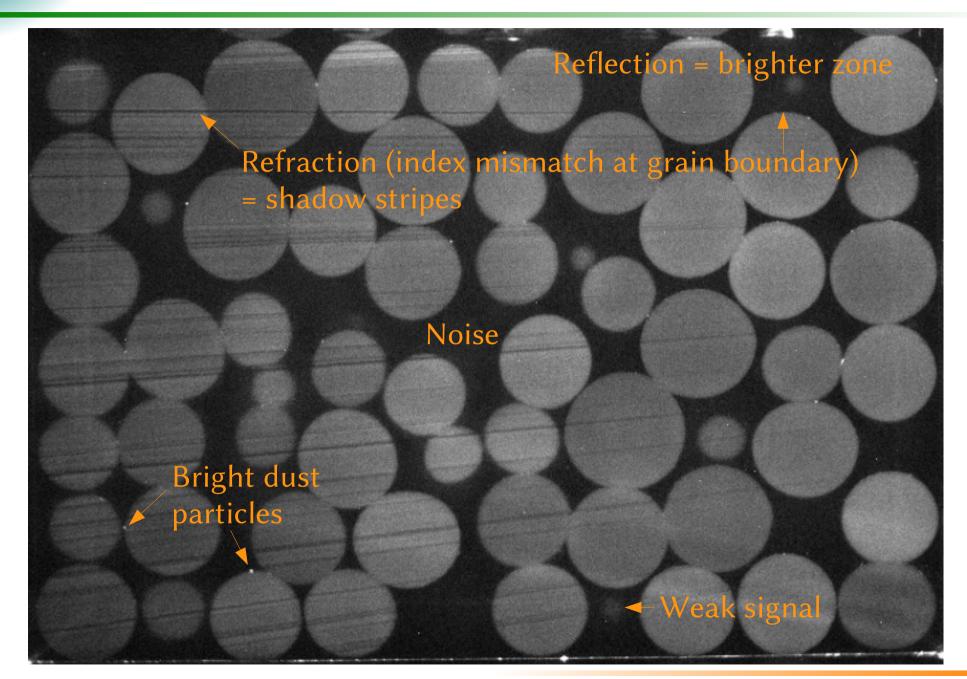




## What we get

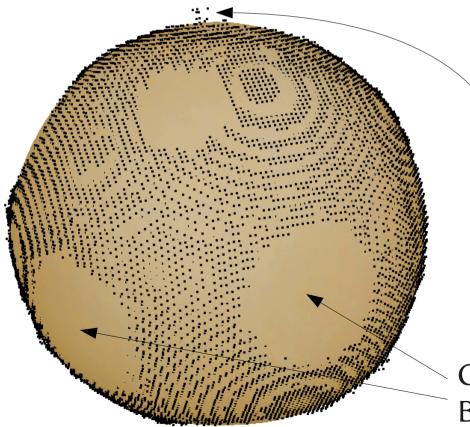


## TYPICAL IMAGE



## FROM 2D IMAGES TO 3D GRAINS

Step 1: Stack the images into 3D voxelsStep 2: Detect border voxels and assign them to unique grainsStep 3: Fit an analytic surface to these bordersStep 4: Use these surfaces to get accurate forces

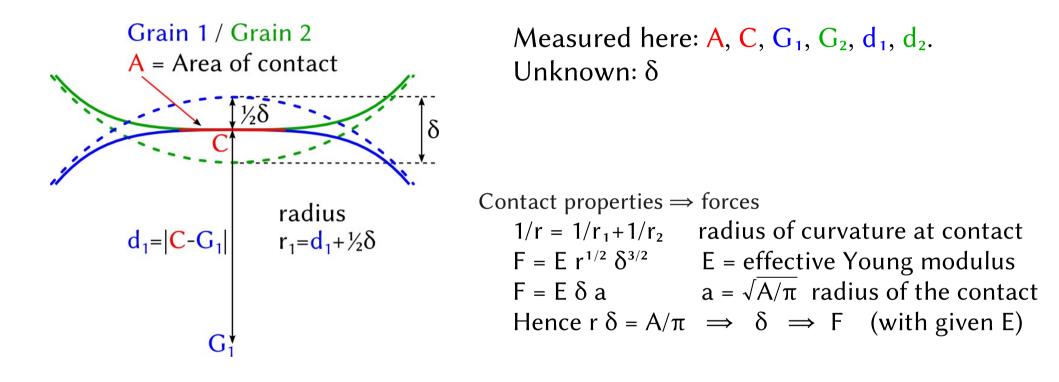


Outliers completely eliminated

Contacts = no border between grains BUT surface area is well defined

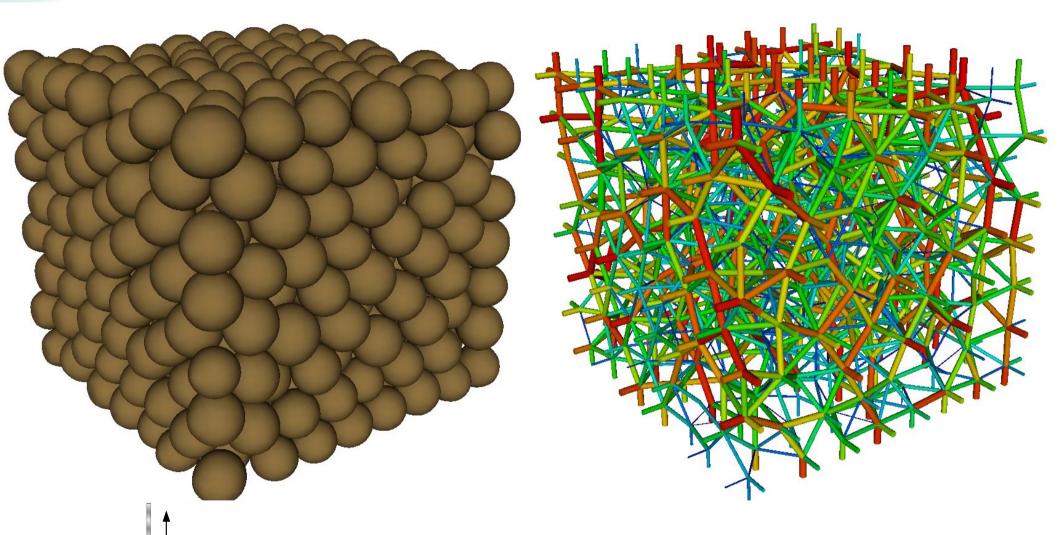
## INFERRING FORCES IN FULL 3D

Analytic shape descriptions  $\Rightarrow$  contact properties



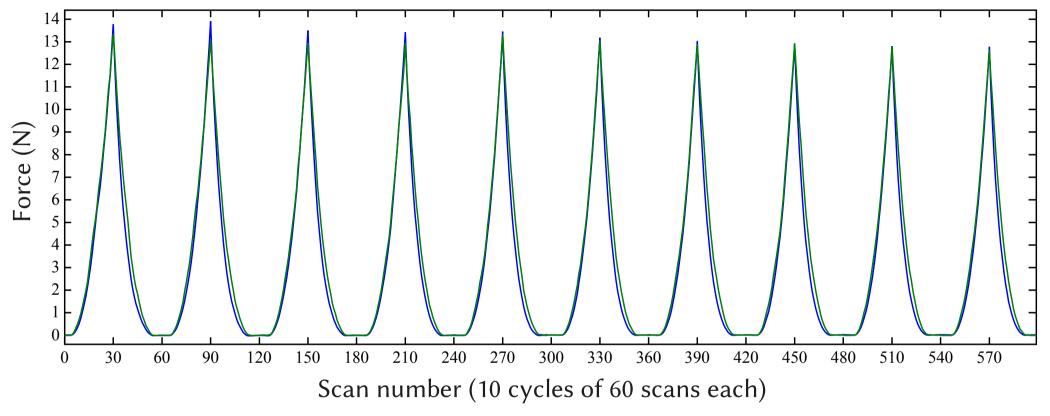
⇒ Vector forces in full 3D, with orientation, position, norm
+ grain centers of mass, stress tensor, etc.

## UNI-AXIAL COMPRESSION CYCLES



Top plate moves by 1mm increments A full scan is taken between increments Forces = struts joining the grain centers Blue = weakest, Red = strongest

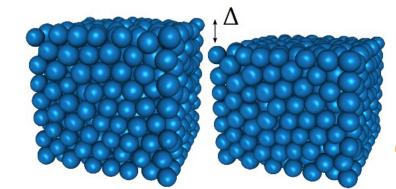
## VALIDATION ON COMPRESSION CYCLES



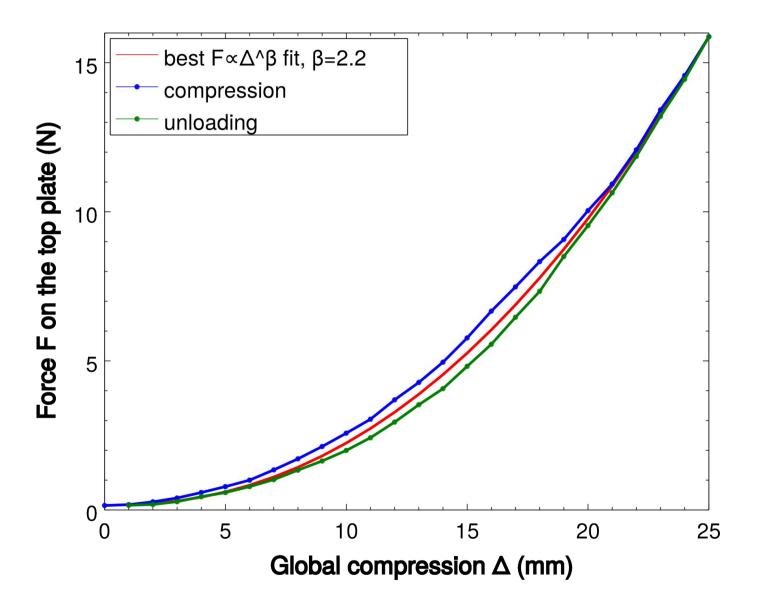
Blue = force measured on the top plate sensor Green = force inferred from the images + measure of E≈23 kPa

Full experiment:

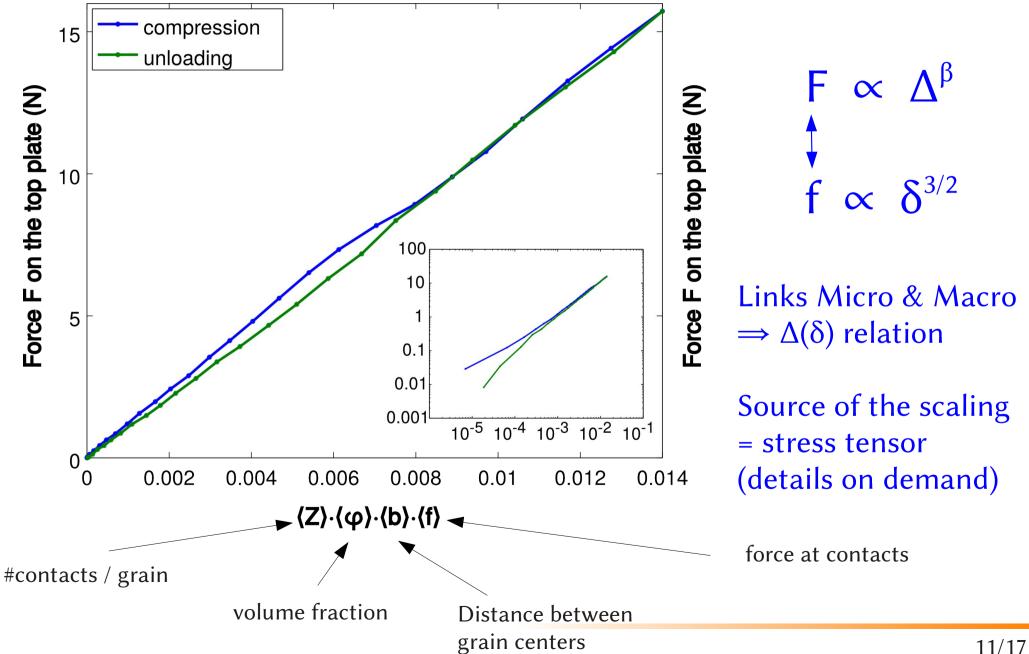
Maximal compression of  $\Delta \approx 13\%$  the initial height Average force at min compression  $\approx 10^{-2}$  N 20 cycles = 1200 scans, >1M contacts (=good stats!).



## Non-Hertzian Packing response



### A SCALING HOLDS



## DEM of the "same" system

### For 3D spheres Grain i Grain j $v_i$ $v_j$ $v_j$ $v_j$

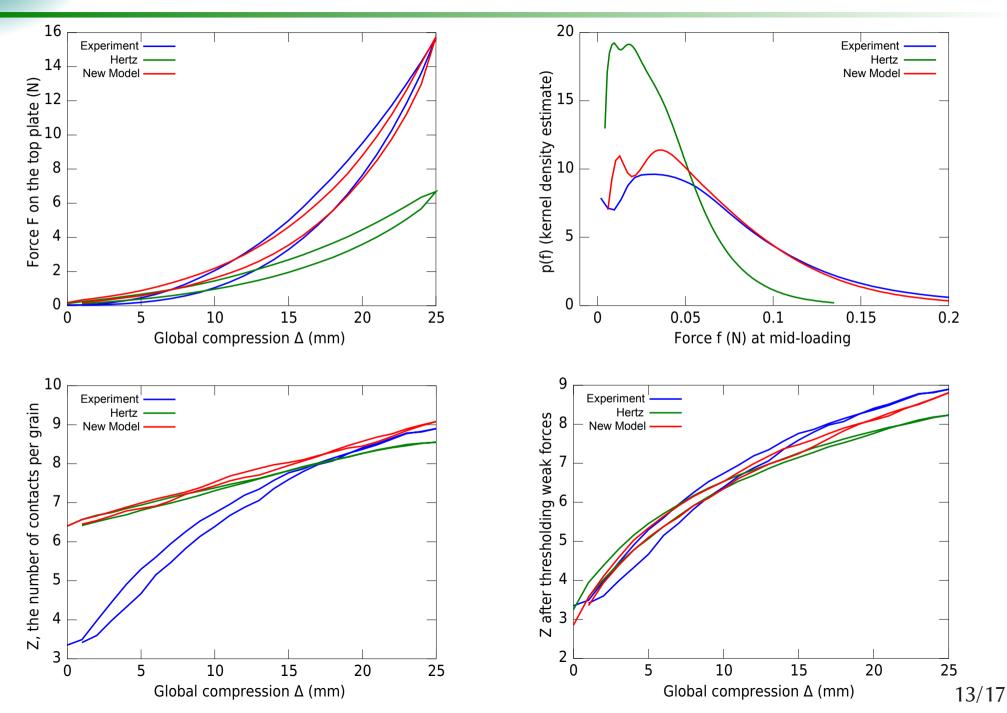
### Standard DEM simulation

- Overlapping non-deformable spheres, overlap =  $\delta$
- + Force model F = F( $\delta$ ) (either linear, Hertz, hysteretic...)
- + Solid Dynamics (friction, solid bodies)
- + Newton's law for integrating the new positions after an elementary dt
- = Trajectories of all particles + all contact properties

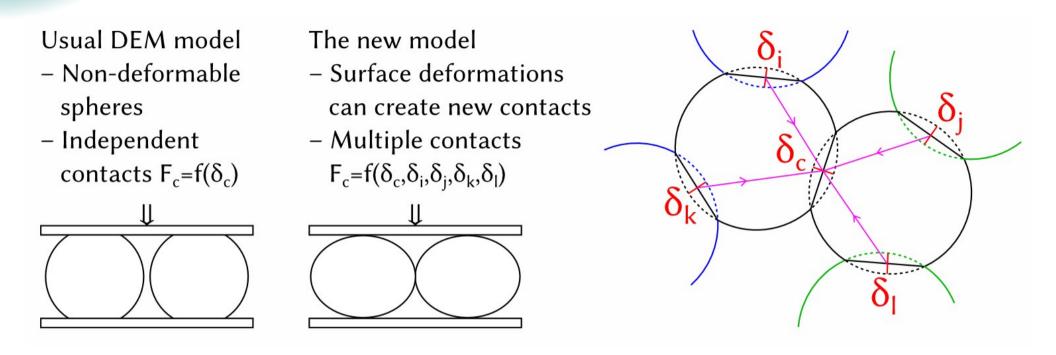
### As close as we can get to the experimental setup

- Hertz + same material properties
- Grains are replaced by spheres of the same volume with the same center of mass
- Same box size and piston motion

### COMPARISON WITH DATA



## DEALING WITH MULTIPLE CONTACTS



### Correlation between contacts (ex [Gonzalez/Cuitiño])

- $-\delta_c$  = the deformation at contact c.
- Other contacts i,j,k,l have an extra influence on c

### New model

- A different expression for the correlations
- Surfaces are deformed **before** the grains touch: new contacts can be created
- Backed up by data!

## INDUCED DISPLACEMENTS

### Sphere-based ideas in the literature

- Point force on full sphere solution [Bondareva 1969]
- Gonzales / Cuitiño, approximating Zhapanska's solution for two spheres in contact

Problem:

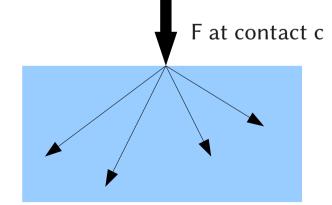
Dense granular material is more like an interconnected medium with pores

Very complex boundary (+inner) conditions.

 $DEM \Rightarrow$  Decoupling of the grains. Contact model = recoupling.

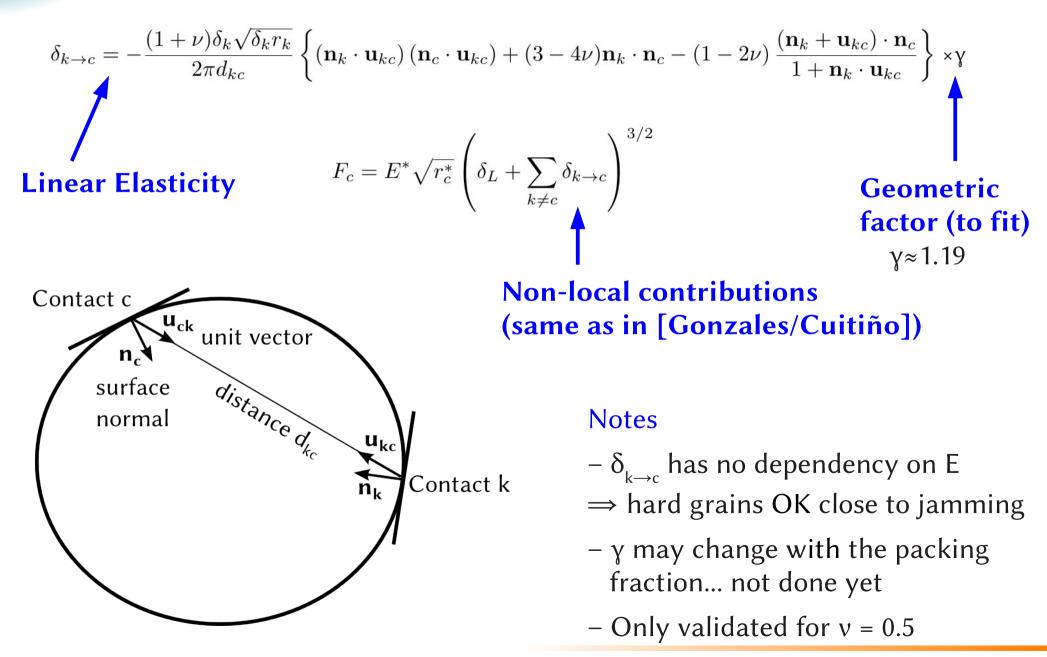
### Here: Linear Elasticity on infinite half space

- Point force applied on elastic material
- Half-plane approximation = consistent with Hertz
- Geometric factor introduced in the model to compensate for the holes



Displacement  $\delta$  induced by F at distance d in the continuous elastic medium 15/17

## THE MODEL



## QUESTIONS?

