

# Modeling and control of pedestrian behaviors: An environment optimization approach

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# Modeling and control of pedestrian behaviors: An environment optimization approach

E. Cristiani, F. S. Priuli, A. Tosin



Istituto per le Applicazioni del Calcolo - Consiglio Nazionale delle Ricerche

New Trends in Optimal Control  
(NetCo 2014)

June 23-27, 2014, Tours (France)

1 Modeling pedestrian rationality

2 Controlling pedestrian rationality

## Background assumptions

no panic – known environment – given target

- **Basic**<sup>1</sup>: Path is computed once at the initial time, assuming that the environment is empty.
- **Rational**<sup>2</sup>: Path is recomputed continuously, taking into account the *current* pedestrian distribution.
- **Highly rational**<sup>3</sup>: Path is computed once, taking into account the pedestrian distribution at *current and later* time. **Highly rational crowd** → **Nash equilibrium**.
- **$\theta$ -rational**: Path is recomputed continuously, taking into account the pedestrian distribution at current and later time up to a time  $t + \theta$ .

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<sup>1</sup>Bellomo & Dogbé, 2008; Cristiani et al., 2011; Helbing & Molnár, 1995; Xia et al., 2009

<sup>2</sup>Hughes, 2002

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# Choice of the behavior

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# A multi-purpose approach

## First goal

Creating a unique model such that the degree of rationality can be freely tuned.

We consider a macroscopic first-order model based on a nonlinear nonlocal anisotropic conservation law

$$\frac{\partial}{\partial t} \rho(x, t) + \operatorname{div}(\rho(x, t) v[\rho](x, t)) = 0$$

with

$$v[\rho](x, t) = v_b^* + v_i$$

and

$$v_i = v_i[\rho(\cdot, t)](x) = \int_{\mathcal{S}(x)} \mathcal{F}(y - x) \rho(y, t) dy$$

This model is 2D and fundamental-diagram free

# Basic behavior + minimum time problem

## Perceived dynamics

$$\dot{y}(t) = v_b(t), \quad t > 0.$$


At the initial time we solve once

## Eikonal equation

$$\begin{cases} |\nabla\phi(x)| - 1 = 0, & x \in \Omega \\ \phi(x) = 0, & x \in Target \end{cases}$$

Then, the optimal behavioral velocity field is taken in feedback form as

$$v_b^*(x) = -\frac{\nabla\phi(x)}{|\nabla\phi(x)|}, \quad x \in \Omega.$$

$v_b^*$  is time-independent coherently with the fact that pedestrians are insensitive to the evolution of the crowd. 

# Rational behavior + minimum time problem

## Perceived dynamics

$$\dot{y}(t) = v_b(t) + v_i[\rho(\cdot, \tau)](y), \quad t > \tau.$$


At any given time  $t = \tau$  we solve

## Modified eikonal equation

$$\begin{cases} |\nabla\phi_\tau(x)| - v_i[\rho(\cdot, \tau)](x) \cdot \nabla\phi_\tau(x) - 1 = 0, & x \in \Omega \\ \phi_\tau(x) = 0, & x \in \text{Target} \end{cases}$$

Then, the optimal behavioral velocity field is taken in feedback form as

$$v_b^*(x) = -\frac{\nabla\phi_\tau(x)}{|\nabla\phi_\tau(x)|}, \quad x \in \Omega.$$

At any fixed time, the HJB equation is independent of the conservation law for  $\rho$ . 

# Highly rational behavior + minimum time problem


## Perceived dynamics

$$\dot{y}(t) = v_b(t) + v_i[\rho(\cdot, t)](y), \quad t > 0.$$

We solve once the following forward-backward equation

## Mean-field equation

$$\begin{cases} \partial_t \rho(t, x) + \operatorname{div}[\rho(x, t)(v_b^*(x, t) + v_i[\rho(\cdot, t)](x))] = 0 & t \rightarrow \\ \max_{v_b \in B_1(0)} \{-(1, v_b + v_i[\rho(\cdot, t)](x)) \cdot \nabla_{x,t} \phi(x, t) - 1\} = 0 & \leftarrow t \\ v_b^*(x, t) \in \arg \max_{v_b \in B_1(0)} \{-(1, v_b + v_i[\rho(\cdot, t)](x)) \cdot \nabla_{t,x} \phi(t, x) - 1\} \end{cases}$$

The HJB and the CL are fully coupled. 

# $\theta$ -rational behavior + minimum time problem

## Perceived dynamics

$$\dot{y}(t) = v_b(t) + v_i[\rho^\theta(\cdot, t)](y),$$

$$\rho^\theta(x, t) := \rho(x, t), t \in [\tau, \tau + \theta], \quad \rho^\theta(x, t) := \rho^\theta(x, \tau + \theta), t > \tau + \theta.$$

At any given time  $t = \tau$  we solve

## Mean-field equation /2

$$\begin{cases} \partial_t \rho^\theta + \operatorname{div}[\rho^\theta (v_b^{*,\theta} + v_i[\rho^\theta])] = 0 & \text{in } (\tau, \tau + \theta) \times \Omega & t \rightarrow \\ \max_{v_b \in \overline{B_1(0)}} \left\{ - \left( 1, v_b + v_i[\rho^\theta(\cdot, t)](x) \right) \cdot \nabla_{x,t} \phi^\theta(x, t) - 1 \right\} = 0 & \leftarrow t \\ v_b^{*,\theta}(x, t) \in \arg \max_{v_b \in \overline{B_1(0)}} \left\{ - \left( 1, v_b + v_i[\rho^\theta(\cdot, t)](x) \right) \cdot \nabla_{x,t} \phi^\theta(x, t) - 1 \right\} \end{cases}$$

# Inducing unconscious rationality

## Second goal

Forcing people to behave more rationally than they would naturally do

By means of the models described above we can describe

## The natural behavior

The expected behavior according to their real limited predictive ability (f.e., the basic one)

## The target behavior

A particularly efficient behavior one would like they to assume (f.e., the rational or highly rational one)

## Key idea

But people are hardly controlled... So we want to get the target behavior still *keeping* the natural one

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# Environmental optimization

## Environmental control

We assume that one can introduce in the domain **additional controlled obstacles**, hoping they improve the dynamics (**Braess' paradox**)

## Environmental cost

The natural behavior in the new environment should be as close as possible to the target behavior in the original environment in terms of

- evacuation times;
- exits usage (if more than one);
- maximal densities (related to overcompression and then injuries);
- ...

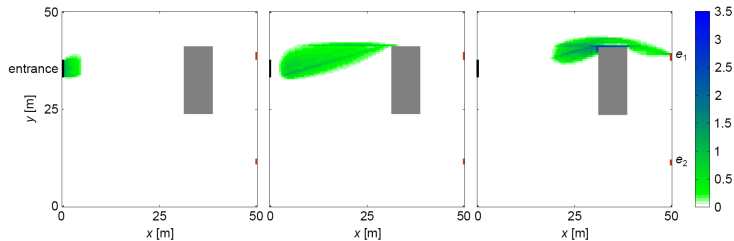
## Minimization strategy (rectangular obstacles)

Exhaustive search, compass search + simulated annealing.

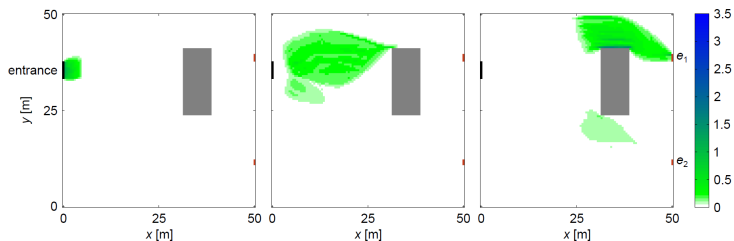


# Room with fixed obstacle

natural = basic [ $t_{\text{evac}} = 120.6$ ]

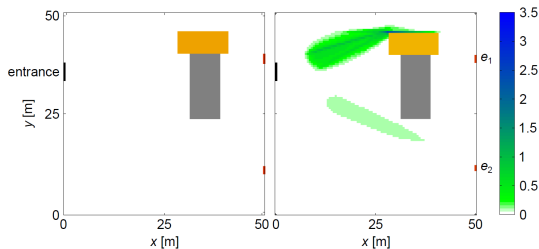


target = rational [ $t_{\text{evac}} = 95.8$ ]

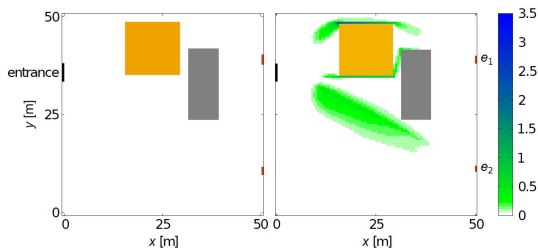


# Room with fixed obstacle

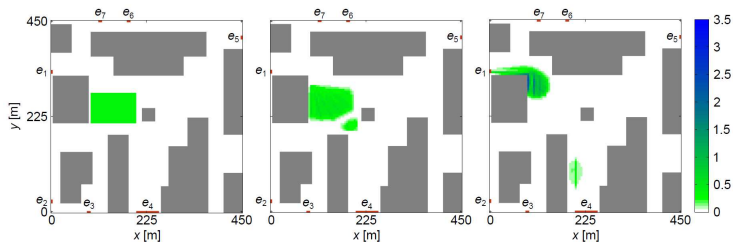
natural behavior with manual guess [ $t_{\text{evac}} = 125.5$ ]



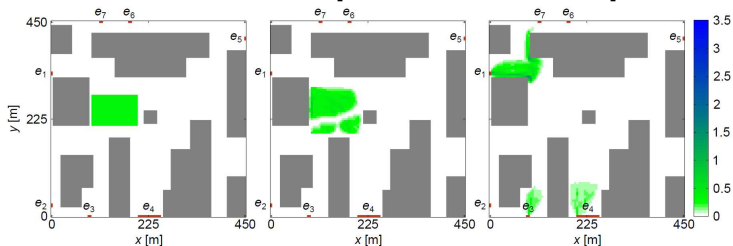
natural behavior with best obstacle [ $t_{\text{evac}} = 99.0$ ]



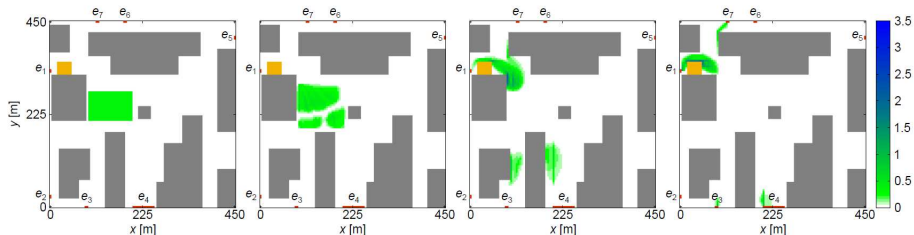
natural = basic [92%, 0, 8%, 0]

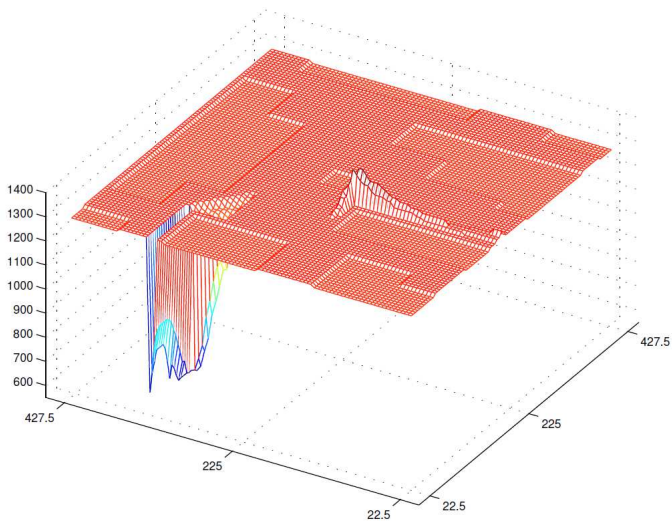


target = rational [61%, 10%, 15%, 14%]

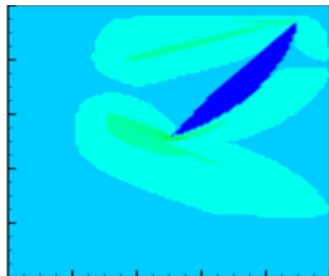
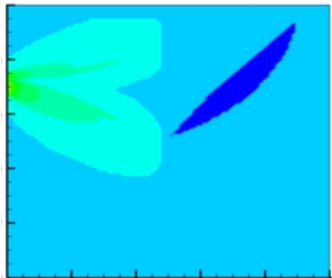


natural behavior with best obstacle [60%, 12%, 18%, 10%]

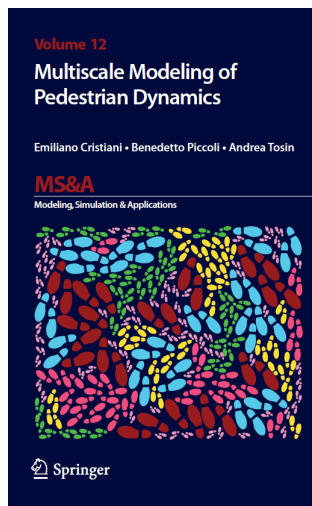




Obstacles with free shape (with D. Peri)



# Multiscale Modeling of Pedestrian Dynamics



Thank you

**THANK YOU**

(pay attention when you leave the room, I'm watching you...)