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Multi-channel audio source separation using multiple deformed references

Nathan Souviraà-Labastie, Anaik Olivero, Emmanuel Vincent, *Senior Member, IEEE*, and Frédéric Bimbot

Abstract—We present a general multi-channel source separation framework where additional audio references are available for one (or more) source(s) of a given mixture. Each audio reference is another mixture which is supposed to contain at least one source similar to one of the target sources. Deformations between the sources of interest and their references are modeled in a linear manner using a generic formulation. This is done by adding transformation matrices to an excitation-filter model, hence affecting different axes, namely frequency, dictionary component or time. A nonnegative matrix co-factorization algorithm and a generalized expectation-maximization algorithm are used to estimate the parameters of the model. Different model parameterizations and different combinations of algorithms are tested on music plus voice mixtures guided by music and/or voice references and on professionally-produced music recordings guided by cover references. Our algorithms improve the signal-to-distortion ratio (SDR) of the sources with the lowest intensity by 9 to 15 decibels (dB) with respect to original mixtures.

Index Terms—Source separation, GEM algorithm

I. INTRODUCTION

IN audio signal processing, source separation consists in recovering the different audio sources that compose a given observed audio mixture. It has been a hot topic over the past decade and this field of research now offers a wide variety of new possible applications for end-users and professionals. One of those concerns the remastering, restoration and remixing of movie soundtracks or musical recordings. Sound engineers may want to upmix the recordings to a higher number of channels, to remove some sources, to generate a karaoke version, or to substitute some sources by other sources, for instance in order to replace the original soundtrack of a movie with a new one. For these purposes, one needs high source separation quality, which is not yet achievable by blind source separation methods [1]. Taking additional information into account is necessary to improve the separation [2], [3]. In informed source separation methods [4], detailed information about the original sources is transmitted along with the mixture to be separated. Such methods are the ones that provide the best quality but they cannot be applied in the scenario considered hereafter, since the original sources are never observed.

Guided source separation is based on the use of any kind of additional information and has recently been more and

more focused on. It is well adapted to scenarios where the original sources are not available but high separation quality is nevertheless required. The additional information can be of different types : spatial and spectral information about the sources [5], [6], language structure [7], visual information [8], information about the recording/mixing conditions [9], musical scores [10]–[13], or user input [14]–[21]. For instance, the user can provide relevant information by drawing the fundamental frequency curve [18], by uttering the same sentence [16], by humming the melody [14], or even by selecting specific areas in the spectrogram of the mixture [17]. On top of this, interactive approaches allow the user to give feedback during the separation [19]–[22].

In this paper, we focus on methods that guide the separation process by a *reference signal* that is similar to one of the target sources [10], [14]–[16], [23]–[27]. Such a framework can be referred to as *reference guided source separation*, and it has recently been used in several scenarios : the restoration of music pieces guided by isolated piano sounds [10], the separation of music and sound effects from speech guided by several versions of the same movie in different languages [23], the separation of musical instruments guided by a multitrack cover version of a song [24], [25], and the denoising of speech guided by the same sentence pronounced by the same speaker [26] or by a different speaker [16]. Symbolic information such as a text [16] or a musical score [12] can also be used to generate reference signals.

Here, we propose a general model for *multi-channel reference guided source separation* that enables the joint use of multiple, multi-channel, deformed reference signals. Our preliminary experiments on music/voice separation [27] and cover guided music separation [25] showed that the use of references is relevant in the single-channel case. Here, we extend this approach to the multi-channel case using a Generalized Expectation-Maximization (GEM) algorithm inspired from [5]. Several initialization procedures and model configurations are investigated as well as the use of multiple references for each source. Different types of data and references are used to assess the relevance of our approach.

The paper is organized as follows. Section II introduces the general model of reference guided source separation. Section III presents the different algorithms and initialization procedures that are compared in the experiments. Section IV provides a first series of experiments with pitch shifted references. Sections V and VI are respectively dedicated to experiments on music/voice separation and on cover-guided music separation.

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II. GENERAL FRAMEWORK

In this section, we describe the proposed reference guided source separation model. Key concepts are first presented in order to facilitate understanding before we give a detailed description of the model. We also discuss different configurations of our model that can handle different types of available data and possible extensions of our framework.

A. Overview of practical scenarios

What we mean by reference signals ranges from different recordings of the true sources to noisy versions of the true sources and also include imitations. The references usually rely on several and very different deformations like time misalignment, time warping, changes of speaker/singer/instrument, additional overlapping sources, equalization, changes of melody/pronunciation, change of recording conditions, and/or pitch shifting. If there is no deformation at all, the reference is then the true source and as already mentioned this is a very restricted scenario. In this sense, we can say that a reference signal is by nature deformed. Hereafter, we consider that there is one target mixture that contains several target sources (sources to be recovered) and several other reference mixtures that contain one (or more) source(s) that are similar enough to the unknown sources of the target mixture. Hence, the sources in the reference mixtures are usually not reconstructed.

In this framework, the deformations between the reference signals and the target sources are modeled in a generic linear manner by transformation matrices. Each deformation acts on a specific axis, namely frequency, dictionary component or time. Time-alignment between all these signals is a main concern as it is often needed to provide suitable reference signals. We introduce the notion of multiple multi-channel mixtures to distinguish between phase aligned signals that constitute channels of the same mixture (*e.g.*, different recordings of the true source), and power aligned signals (at a frame level) that constitute different mixtures (*e.g.*, approximate imitation). Typically, power alignment is performed by a transformation matrix on the time axis. Examples of initialization and estimation of this time alignment are given in Section V.

B. Input representation

The observations are M audio mixtures $\mathbf{x}^m(t)$ indexed by m . Each mixture $\mathbf{x}^m(t)$ is multi-channel and contains I^m channels.

Each mixture is assumed to be the sum of the spatial images $\mathbf{y}_j(t)$ of one or more sources indexed by $j \in \mathcal{J}_m$:

$$\mathbf{x}^m(t) = \sum_{j \in \mathcal{J}_m} \mathbf{y}_j(t) \text{ with } \mathbf{x}^m(t), \mathbf{y}_j(t) \in \mathbb{R}^{I^m}. \quad (1)$$

In the Short-Time Fourier Transform (STFT) domain, this can be written as

$$\mathbf{x}_{fn}^m = \sum_{j \in \mathcal{J}_m} \mathbf{y}_{j,fn} \text{ with } \mathbf{x}_{fn}^m, \mathbf{y}_{j,fn} \in \mathbb{C}^{I^m}, \quad (2)$$

where $f = 1, \dots, F$ and $n = 1, \dots, N$ are respectively the frequency and the time indexes of the STFT. We consider that $\mathbf{x}^1(t)$ is the mixture to be separated, and $\mathbf{x}^m(t)$ for $m > 1$ are

other mixtures containing the reference signals used to guide the separation process.

We assume that the STFT coefficients of the source spatial images $\mathbf{y}_{j,fn}$ have a zero-mean Gaussian distribution [5] :

$$\mathbf{y}_{j,fn} \sim \mathcal{N}_{\mathbb{C}}(0, v_{j,fn} \mathbf{R}_{j,f}) \quad (3)$$

whose covariance factors into a scalar power spectrum $v_{j,fn} \in \mathbb{R}_+$ and a spatial covariance matrix $\mathbf{R}_{j,f} \in \mathbb{C}^{I^m \times I^m}$.

1) *Spatial parameters*: The spatial covariance matrices model the spatial characteristics of the sources, such as phase and intensity difference between channels. We only consider time-invariant spatial covariance matrices as the sound sources considered in our experimental scenarios are generally spatially stable over time. $\mathbf{R}_{j,f}$ can be non-uniquely represented as $\mathbf{R}_{j,f} = \mathbf{A}_{j,f} \mathbf{A}_{j,f}^H$ where $\mathbf{A}_{j,f} \in \mathbb{C}^{I^m \times R_j}$ and R_j is the rank of matrices $\mathbf{R}_{j,f}$ and $\mathbf{A}_{j,f}$ [5]. As spectral modeling is the focus of this paper, these aspects are not further detailed.

2) *Spectral parameters*: The power spectrogram of each source j is denoted as $V_j = [v_{j,fn}]_{fn} \in \mathbb{R}_+^{F \times N}$. Each V_j is split into the product of an excitation spectrogram V_j^e and a filter spectrogram V_j^ϕ . The excitation spectrogram (resp. the filter spectrogram) is decomposed by Nonnegative Matrix Factorization (NMF) into a matrix of spectral patterns $W_j^e \in \mathbb{R}_+^{F \times D^e}$ (resp. $W_j^\phi \in \mathbb{R}_+^{F \times D^\phi}$) and a matrix of temporal activations $H_j^e \in \mathbb{R}_+^{D^e \times N}$ (resp. $H_j^\phi \in \mathbb{R}_+^{D^\phi \times N}$). D^e (resp. D^ϕ) denotes the number of spectral patterns used in the NMF decomposition of the excitation (resp. filter) part. This results in the following decomposition :

$$V_j = V_j^e \odot V_j^\phi = W_j^e H_j^e \odot W_j^\phi H_j^\phi \quad (4)$$

where \odot denotes pointwise multiplication. The four matrices are as follows:

- W_j^e is a spectral dictionary that can be designed as a set of inharmonic, harmonic and/or wideband spectra [5]. Alternatively, such a dictionary can be learned on training data or estimated from the test mixture.
- H_j^e are the corresponding temporal activations which encode, *e.g.*, the musical score in the form of a piano roll [11]–[13], or the f_0 track [18].
- W_j^ϕ is a dictionary of spectral envelopes associated with, *e.g.*, different phonemes in the case of speech [16] or body resonances in the case of a musical instrument [10].
- H_j^ϕ are the corresponding temporal activations which encode, *e.g.*, the phoneme sequence for speech or instrument timbre changes for music such as muted/unmuted trumpet.

C. Proposed model with multiple deformed references

We proposed to consider three different cases for the settings of the matrices W_j^e , H_j^e , W_j^ϕ and H_j^ϕ . As a first case, they can be *fixed* and remain unchanged during the estimation. As a second case, they can be set as *free* parameters, which means that they will be adapted to the corresponding mixture m ($j \in \mathcal{J}^m$) during the estimation process. Finally, as the third case, these matrices can also be *shared* (*i.e.*, jointly estimated) between a given source $j \in \mathcal{J}^m$ and one (or more)

reference source(s) $j' \in \mathcal{J}^{m'}$ with $m' \neq m$ (e.g., $m = 1$ as in Section V). In this last case, the deformations between sources j and j' are modeled by transformation matrices $T_{jj'}$. We propose to model the sharing of spectral and temporal properties between one source V_j and its references $V_{j'}$ as follows :

1) *Transformation matrices for the excitation part*: For the excitation part, the transformation matrices are denoted as $T_{jj'}^{fe} \in \mathbb{R}_+^{F' \times F}$, $T_{jj'}^{de} \in \mathbb{R}_+^{D^e \times D^e}$ and $T_{jj'}^{te} \in \mathbb{R}_+^{N \times N'}$. Depending on the actual deformation between the target source and the reference sources, three different configurations are possible. One may share either the spectral patterns as shown in (5), the temporal activation as shown in (6), or both as shown in (7). This is modeled by one of the three following equations :

$$V_{j'}^e = T_{jj'}^{fe} W_j^e H_{j'}^e \quad (5)$$

$$V_{j'}^e = W_j^e H_j^e T_{jj'}^{te} \quad (6)$$

$$V_{j'}^e = T_{jj'}^{fe} W_j^e T_{jj'}^{de} H_j^e T_{jj'}^{te} \quad (7)$$

During the estimation process, each transformation matrix can be considered either as a *fixed* or a *free* parameter. In practice, frequency deformations of the excitation $T_{jj'}^{fe}$ can be used to model, e.g., differences of reading speed on analog devices or spectral dimensionality change due to different sampling rates. $T_{jj'}^{te}$ is used to time-align the signal spectra and represents the time warping path between the two signals. $T_{jj'}^{de}$ can be used to model changes in the excitation dictionary, such as pitch shifting¹. It only appears when the corresponding W_j, H_j are *shared*, otherwise it would be redundant.

2) *Transformation matrices for the filter part*: For the filter part, the transformation matrices between the target source and the reference sources are denoted as $T_{jj'}^{f\phi} \in \mathbb{R}_+^{F' \times F}$, $T_{jj'}^{d\phi} \in \mathbb{R}_+^{D^\phi \times D^\phi}$ and $T_{jj'}^{t\phi} \in \mathbb{R}_+^{N \times N'}$. In the same way as above, three different configurations are possible, which lead to share either the spectral patterns as shown in (8), the temporal activation as shown in (9), or both as shown in (10) :

$$V_{j'}^\phi = T_{jj'}^{f\phi} W_j^\phi H_{j'}^\phi \quad (8)$$

$$V_{j'}^\phi = W_j^\phi H_j^\phi T_{jj'}^{t\phi} \quad (9)$$

$$V_{j'}^\phi = T_{jj'}^{f\phi} W_j^\phi T_{jj'}^{d\phi} H_j^\phi T_{jj'}^{t\phi} \quad (10)$$

Similarly to transformation above, the matrices can be either *fixed* or *free*. Frequency deformations of the filter part $T_{jj'}^{f\phi}$ can be used to model, e.g., changes in vocal tract length [16] or a different equalization. $T_{jj'}^{d\phi}$ models changes in the filter dictionary, such as the change of some phonemes in the case of a speaker with a different accent (e.g., one phoneme often uttered in place of another), and it only appears when the corresponding W and H are *shared*. $T_{jj'}^{t\phi}$ models the temporal deformation of the filter, and it is used to time-align the signals.

Fig. 1 gives an illustration of a possible use of this model. It corresponds to a speech reference modeled by (30) and the related speech source that is uttered by a different speaker. More details can be found in Section V-B3a.

¹It can be noticed that pitch shifting and reading speed have two different effects, especially for inharmonic sounds.

D. Comparison with previous approaches

The proposed framework generalizes the state-of-the-art approaches in [10], [16], [27] as they exploit similar models. Our framework can also model the same kind of signals as used in [10], [14], [23]–[26] even if the models can be quite different. Finally, it makes it possible to investigate some new scenarios that have been put forward in [27], like music source separation for a verse guided by another verse.

E. Extensions of our approach

As previously mentioned, we consider here that $j \in \mathcal{J}^1$ and $j' \in \mathcal{J}^{m'}$ with $m' \neq 1$. These notations are supposed to represent the classical reference guided source separation scenario. Relaxing this constraint opens the way to more possibilities.

Modeling the relationship between sources of the same mixture (i.e., $j, j' \in \mathcal{J}^m$) could be of interest to model delays between sources of the same mixture like a canon in music. Modeling "circular" relationships (e.g., using $T_{jj'}, T_{j'j''}, T_{j''j}$) would allow joint separation of all mixtures. But it requires the use and the estimation of one more matrix. More generally, considering the mixture to be separated as central is a good way to avoid having additional matrices and potential smoothing effects on the sources of interest.

Another possible extension would be the sharing of transformation matrices, for instance when different instruments undergo the same transformation (tonality or pitch shift) or when the excitation and the filter part are subject to the same time deformation².

F. Additional constraints

When using an excitation-filter model, the estimation of the filter part usually requires additional smoothness constraints, as in [5], [28], to guarantee that the filter part actually represents the resonances of the vocal tract or the musical instrument. In this work, we do not use any explicit constraint for our excitation-filter model in order not to overload the framework. However, we found experimentally that the estimated filters in the presence of reference-based constraints are smooth. Fig. 2 shows examples of estimated filters for the experiment in Section V. One possible explanation is that using more than one source to estimate a given filter (while the excitation is different for each source) yields a more robust estimate than using only one source. However, it is hard, if not impossible, to provide some theoretical guarantee of this behavior.

If needed, explicit frequency smoothness constraints can be included in the previously presented model either by constraining the matrices W_j^ϕ as the product of smooth frequency-localized patterns and spectral envelope coefficients as in [5], [28] or by introducing probabilistic priors on the coefficients of W_j^ϕ as in [29]. Similarly, time continuity constraints may be imposed on H_j^ϕ or H_j^e . Such refinements of the proposed general framework are outside the scope of the current article and are not discussed hereafter.

²The shared transformation matrices would then be estimated in a similar manner as the shared parameters in (14) or (16).

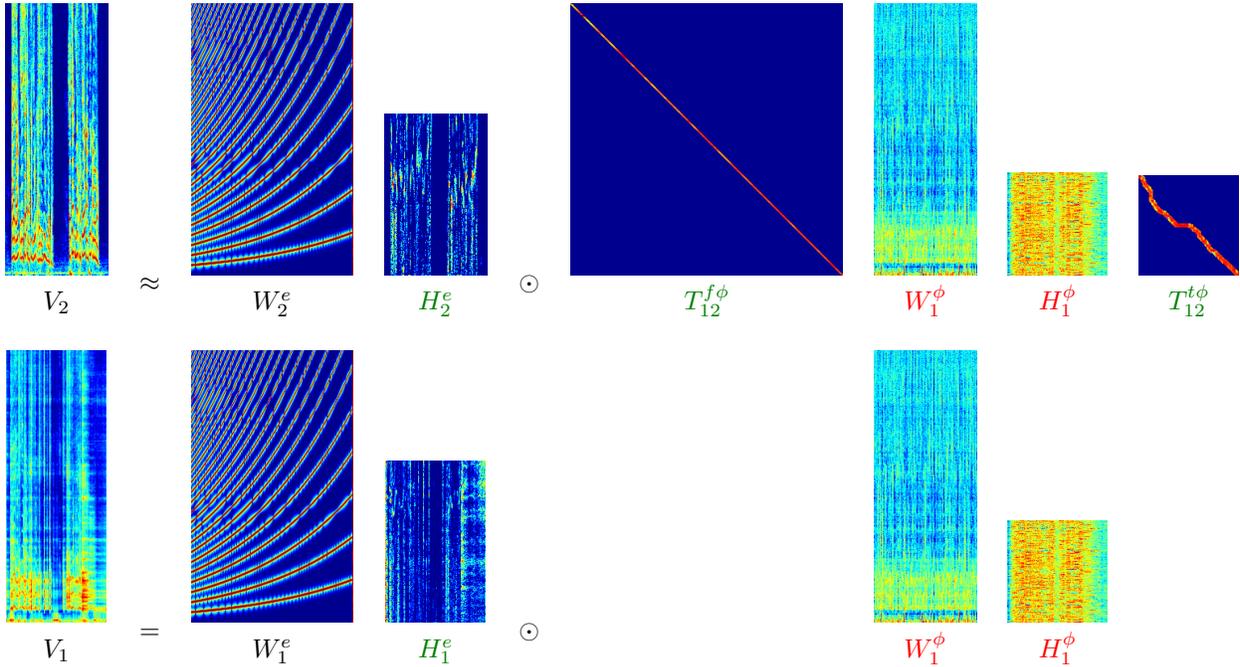


Fig. 1. Example estimated decomposition of the spectral power of a reference mixture ($m' = 2$) containing a single source ($j' = 2$) similar to source $j = 1 \in \mathcal{J}^1$. The excitation parameters are not *shared* whereas the filter follows (10) with $T_{12}^{d\phi}$ set to identity. The parameters of the target source ($j = 1$) are also displayed.

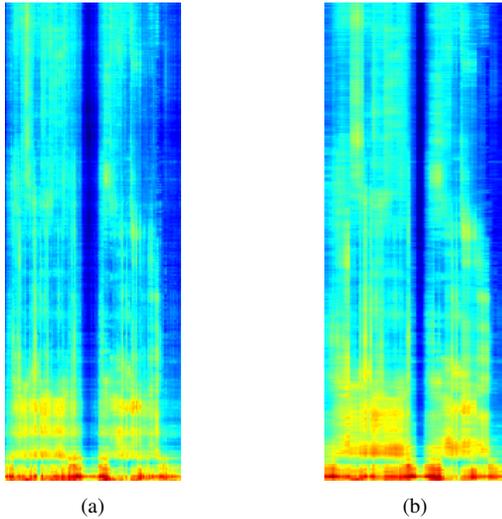


Fig. 2. Examples of estimated filter parts V^ϕ for a speech source (2a) and its reference (2b) in the experiment in Section V.

III. PARAMETER ESTIMATION

In this section, we present two methods for parameter estimation in the maximum likelihood (ML) sense. The ML objective can be written as :

$$\hat{\theta} = \operatorname{argmax}_{\theta} \sum_{m=1}^M \lambda^m \log p(\mathbf{x}^m | \theta) \quad (11)$$

where θ is the set of parameters to be estimated, *i.e.*, the spatial covariance matrices $\mathbf{R}_{j,fn}$, and the matrices W , H and T that are either *free* or *shared*. $\lambda^m \in \mathbb{R}_+$ are weight parameters that can balance potentially different durations or frequency

resolutions between mixtures 1 and m , or put more emphasis on the references which are expected to be the most relevant. The reader can refer to [30] for a discussion on their influence on the results.

First, we introduce a multiplicative update (MU) algorithm to deal with single-channel mixtures. Then, a GEM algorithm is used to estimate the parameters in the multi-channel case. Finally, we discuss different initialization procedures.

A. Multiplicative updates for nonnegative matrix partial co-factorization (NMPcF) for the single-channel case

In the single-channel case, maximizing the log-likelihood is equivalent to minimizing the Itakura-Saito (IS) divergence [31]:

$$\hat{\theta} = \operatorname{argmin}_{\theta} \sum_{m=1}^M \lambda^m \sum_{f,n=1}^{F,N} d_{IS}(X_{fn}^m | V_{fn}^m) \quad (12)$$

where $X^m = [|\mathbf{x}_{fn}^m|^2]_{fn}$ and $V^m = \sum_{j \in \mathcal{J}^m} V_j$ are respectively the observed and estimated power spectrograms, and $d_{IS}(a|b) = a/b - \log(a/b) - 1$ is the IS divergence. Other divergences are worth considering but they are not extendable to the multi-channel case whereas Itakura-Saito is. A common way to estimate the parameters is the use of a multiplicative gradient descent approach [31] in which each parameter is updated at each iteration without increasing criterion (12) [32]. The update of one parameter consists in multiplying it by the ratio of the negative and positive parts of the derivative of the criterion with respect to this parameter.

According to their status (*free* or *shared*) different MU can be derived for each parameter. For *free* parameters, (12) leads to the classical MU of NMF. An example of such update is

given in (13) for the parameter W_j^e . For *shared* parameters, (12) leads to the MU of NMPcF. An example of such update is given in (14)³ for the parameter W_j^e . $V^{\cdot[-p]}$ denotes the matrix with entries $(V_{ij})^{-p}$.

B. Generalized Expectation-Maximization (GEM) algorithm for the multi-channel case

In the multi-channel case, the spatial information can make the separation clearly more tractable, especially when sources have different directions of arrival. In the case of reference guided source separation, the relevance of multi-channel data remains even though the mixtures have different numbers of channels and even though no assumptions are made on the similarity between directions of arrival of the sources and their references.

Following the general framework in [5], we introduce R_j independent Gaussian random variables $s_{jr,fn}$ ($r = 1, \dots, R_j$) distributed as $s_{jr,fn} \sim \mathcal{N}(0, v_{j,fn})$ for every source j and time-frequency bin (f, n) . An additive isotropic noise source \mathbf{b}_{fn}^m of diagonal covariance $\Sigma_{\mathbf{b}_{fn}^m} = \sigma_f^2 \mathbf{I}_{I^m} \in \mathbb{C}^{I^m \times I^m}$ is also added for each mixture m . With these changes, (2) becomes :

$$\mathbf{x}_{fn}^m = \mathbf{A}_{fn}^m \mathbf{s}_{fn}^m + \mathbf{b}_{fn}^m \quad (17)$$

where $\mathbf{A}_{fn}^m \in \mathbb{C}^{I^m \times R^m}$ (resp. $\mathbf{s}_{fn}^m \in \mathbb{C}^{R^m}$) results from the concatenation ($R^m = \sum_{j \in \mathcal{J}^m} R_j$) of the mixing matrices $\mathbf{A}_{j,fn}$ (resp. of all the sub-sources $s_{jr,fn}$) of all the sources $j \in \mathcal{J}^m$.

EM is a natural algorithm to handle such a parameter estimation in the ML sense in the presence of *observed* data $\mathbf{X} = \{\mathbf{X}^m\}_m = \{x_{fn}^m\}_{m,fn}$ and *unobserved* data $\mathbf{S} = \{\mathbf{S}^m\}_m = \{s_{fn}^m\}_{m,fn}$, that form a complete set $\mathbf{Z} = \{\mathbf{X}, \mathbf{S}\}$. The algorithm proceeds by alternating an E-step that computes the expected value of the complete-data log-likelihood $\mathbb{E}_{\mathbf{Z}|\theta^c} [\log p(\mathbf{Z}|\theta)] \triangleq Q(\theta, \theta^c)$ given the observation and the current set of parameters θ^c , and an M-step that chooses a θ that maximizes the quantity $Q(\theta, \theta^c)$. In the case of GEM, the M-step only seeks to find a θ that increases Q . A detailed derivation is given in Appendix A. The quantity Q can be written up to a constant as :

$$\begin{aligned} Q(\theta, \theta^c) \stackrel{c}{=} & - \sum_{m,fn} \frac{\lambda^m}{\sigma_f^2} \text{tr} \left[\mathbf{R}_{\mathbf{x}_{fn}^m} - \mathbf{A}_f^m \mathbf{R}_{\mathbf{x}_{fn}^m} \mathbf{A}_f^{mH} \right. \\ & \left. - \mathbf{R}_{\mathbf{x}_{fn}^m} \mathbf{A}_f^{mH} + \mathbf{A}_f^m \mathbf{R}_{\mathbf{s}_{fn}^m} \mathbf{A}_f^{mH} \right] \\ & - \sum_{m,j \in \mathcal{J}^m, fn} \lambda^m R_j d_{IS}(\xi_{j,fn} | v_{j,fn}), \quad (18) \end{aligned}$$

with: $\mathbf{R}_{\mathbf{x}_{fn}^m} \triangleq \hat{\mathbf{R}}_{\mathbf{x}_{fn}^m} = \mathbb{E}[\mathbf{x}_{fn}^m \mathbf{x}_{fn}^{mH}]$, $\mathbf{R}_{\mathbf{x}_{fn}^m} \mathbf{A}_f^{mH} \triangleq \hat{\mathbb{E}}[\mathbf{x}_{fn}^m \mathbf{s}_{fn}^{mH}]$, $\mathbf{R}_{\mathbf{s}_{fn}^m} \mathbf{A}_f^{mH} \triangleq \hat{\mathbb{E}}[\mathbf{s}_{fn}^m \mathbf{s}_{fn}^{mH}]$ and $\xi_{j,fn} \triangleq \frac{1}{R_j} \sum_{r=1}^{R_j} \hat{\mathbb{E}}[|s_{jr,fn}|^2]$.

Starting from (18), one can demonstrate that $\mathbb{T}(\mathbf{X}, \mathbf{S}) = \{\mathbf{R}_{\mathbf{x}_{fn}^m}, \mathbf{R}_{\mathbf{x}_{fn}^m} \mathbf{A}_f^{mH}, \mathbf{R}_{\mathbf{s}_{fn}^m} \mathbf{A}_f^{mH}\}_{m,fn}$ is the set of *natural (sufficient) statistics* [33] for \mathbf{Z} . This leads to the following two steps of our GEM algorithm.

³ In (14) and (16), we assume that V_j^e and V_j^ϕ follow models (7) and (10). In practical scenarios, the number of *shared* parameters and transformation matrices will generally be smaller, as exemplified in Sections V and VI.

1) *E-step*: This step consists in computing the conditional expectations of the natural statistics given θ^c :

$$\hat{\mathbf{R}}_{\mathbf{s}_{fn}^m} = \Omega_{\mathbf{s}_{fn}^m} \hat{\mathbf{R}}_{\mathbf{x}_{fn}^m} \Omega_{\mathbf{s}_{fn}^m}^H + (\mathbf{I}_R - \Omega_{\mathbf{s}_{fn}^m} \mathbf{A}_f^m) \Sigma_{\mathbf{s}_{fn}^m} \quad (19)$$

$$\hat{\mathbf{R}}_{\mathbf{x}_{fn}^m} = \hat{\mathbf{R}}_{\mathbf{x}_{fn}^m} \Omega_{\mathbf{s}_{fn}^m}^H \in \mathbb{C}^{I^m \times R^m} \quad (20)$$

with :

$$\Sigma_{\mathbf{s}_{fn}^m} = \text{diag}([\phi_{r,fn}]_{r=1}^{R^m}) \in \mathbb{R}_+^{R^m \times R^m} \quad (21)$$

$$\Sigma_{\mathbf{x}_{fn}^m} = \mathbf{A}_f^m \Sigma_{\mathbf{s}_{fn}^m} \mathbf{A}_f^{mH} + \Sigma_{\mathbf{b}_{fn}^m} \in \mathbb{C}^{I^m \times I^m} \quad (22)$$

$$\Omega_{\mathbf{s}_{fn}^m} = \Sigma_{\mathbf{s}_{fn}^m} \mathbf{A}_f^{mH} \Sigma_{\mathbf{x}_{fn}^m}^{-1} \in \mathbb{C}^{R^m \times I^m} \quad (23)$$

where $\phi_{r,fn} = v_{j,fn}$ if $r \in \mathcal{R}_j$ (i.e., r is a sub-source of j).

2) *M-step*: The *free* parameters that compose the set θ are here updated in order to increase the quantity Q . The update for the spatial parameters is [5] :

$$\mathbf{A}_f = \left[\sum_n \hat{\mathbf{R}}_{\mathbf{x}_{fn}^m} \right] \left[\sum_n \hat{\mathbf{R}}_{\mathbf{s}_{fn}^m} \right]^{-1}. \quad (24)$$

If none of the parameters are *shared*, the resulting GEM algorithm processes the different mixtures separately, and behaves as in [5]. The sharing of spectral parameters induces a single change in the algorithm routines that occurs during the M-step updates of these *shared* spectral parameters. Examples of MU are given for *free* parameters in (15) and for *shared* parameters in (16)³. They generalize the update (30) in [5] with $\hat{\xi}_j = [\hat{\xi}_{j,fn}]_{fn} \in \mathbb{R}_+^{F \times N}$ where $\hat{\xi}_{j,fn} = \frac{1}{R_j} \sum_{r=1}^{R_j} \hat{\mathbf{R}}_{\mathbf{s}_{fn}^m}(r, r)$.

C. Parameter initialization

The results of both MU and EM depend on initialization. With respect to blind source separation, reference guided separation provides better initial values for the parameters W and H taking advantage of the provided references. The other parameters, i.e., the transformation matrices T , are beforehand roughly estimated (see Section V). For instance, we can use MU to minimize the following criterion :

$$\hat{\theta}_{\text{ref}} = \underset{\theta_{\text{ref}}}{\text{argmin}} \sum_{m=2}^M \lambda^m \sum_{f,n=1}^{F,N} d_{IS}(X_{fn}^m | V_{fn}^m) \quad (25)$$

where θ_{ref} is the set of W and H parameters that occur in the reference signals. This is especially efficient when there is a single dominant source in each reference signal. At the end of this stage, only the parameters of the mixture to be separated that are not shared with any reference signals remain weakly initialized if no prior information about them is available.

In the experiments, we will distinguish the following successive initialization and algorithmic stages :

- *Init* : for all sources, we define the status (i.e., *fixed*, *free* or *shared*) of their spectral parameters (i.e., W , H and T) and we initialize them in the best way according to prior information. The exact initialization is specified below in Sections V and VI depending on the considered scenario.
- *NMF* : the *shared* and *free* W , H of the reference mixtures are updated using MU, i.e., the method described in this Section III-C,

MU-free :

$$W_j^e \leftarrow W_j^e \odot \frac{[V_j^\phi \odot V^{m \cdot [-2]} \odot X^m][H_j^e]^T}{[V_j^\phi \odot V^{m \cdot [-1]}][H_j^e]^T} \quad (13)$$

MU-shared :

$$W_j^e \leftarrow W_j^e \odot \frac{\lambda^m [V_j^\phi \odot V^{m \cdot [-2]} \odot X^m][H_j^e]^T + \sum_{j'} \lambda^{m'} [T_{jj'}^{fe}]^T [V_j^\phi \odot V^{m' \cdot [-2]} \odot X^{m'}][T_{jj'}^{de} H_j^e T_{jj'}^{te}]^T}{\lambda^m [V_j^\phi \odot V^{m \cdot [-1]}][H_j^e]^T + \sum_{j'} \lambda^{m'} [T_{jj'}^{fe}]^T [V_j^\phi \odot V^{m' \cdot [-1]}][T_{jj'}^{de} H_j^e T_{jj'}^{te}]^T} \quad (14)$$

EM-free :

$$W_j^e \leftarrow W_j^e \odot \frac{[V_j^\phi \odot V_j^{[-2]} \odot \hat{\Xi}_j][H_j^e]^T}{[V_j^\phi \odot V_j^{[-1]}][H_j^e]^T} \quad (15)$$

EM-shared :

$$W_j^e \leftarrow W_j^e \odot \frac{\lambda^m R_j [V_j^\phi \odot V_j^{[-2]} \odot \hat{\Xi}_j][H_j^e]^T + \sum_{j'} \lambda^{m'} R_{j'} [T_{jj'}^{fe}]^T [V_j^\phi \odot V_j^{[-2]} \odot \hat{\Xi}_j][T_{jj'}^{de} H_j^e T_{jj'}^{te}]^T}{\lambda^m R_j [V_j^\phi \odot V_j^{[-1]}][H_j^e]^T + \sum_{j'} \lambda^{m'} R_{j'} [T_{jj'}^{fe}]^T [V_j^\phi \odot V_j^{[-1]}][T_{jj'}^{de} H_j^e T_{jj'}^{te}]^T} \quad (16)$$

- *Plain-NMF* : we apply the algorithm described in Section III-A to the target mixture only ($M = 1$ in (12)),
- *NMPcF* : we apply the algorithm described in Section III-A to all mixtures,
- *GEM* : we apply the algorithm described in Section III-B to all mixtures.

During the experiments, different combinations of these four stages are tried in the above order. In all cases, the final source estimates are obtained using an adaptive Wiener filter $\hat{s}_{fn}^m = \Omega_{s_{fn}^m} \mathbf{x}_{fn}^m$ and multiplied by the structured A_f^m to obtain the corresponding spatial images $\mathbf{y}_{j,fn}^m$.

IV. ELEMENTARY SCENARIO WITH PITCH SHIFTING

We first illustrate the method on single-source signals for which the reference is a pitch shifted version of these signals. This elementary example addresses one possible use of the transformation matrices of the excitation part T^{fe} and T^{de} .

A. Data

We used six guitar source signals of thirty seconds and generated several pitch shifted references for each of them (from one to four semitones). The pitch shifted examples are obtained using GuitarPitchShifter⁴.

B. Model and initialization

The source is hereafter numbered as $j = 1$ and the reference as $j = 2$. In this description, we remove the notion of mixture as only single-source signals are used. *Fixed* variables are in black (W_1^e, W_2^e), *free* variables are in green ($T_{12}^{f\phi}, T_{12}^{d\phi}$) and *shared* variables are in red ($H_1^e, W_1^\phi, H_1^\phi$). The source power spectrum V_1 is modeled as,

$$V_1 = W_1^e H_1^e \odot W_1^\phi H_1^\phi \quad (26)$$

and the reference power spectrum V_2 is modeled either as

$$V_2 = T_{12}^{fe} W_2^e H_1^e \odot W_1^\phi H_1^\phi \quad (27)$$

or

$$V_2 = W_2^e T_{12}^{de} H_1^e \odot W_1^\phi H_1^\phi. \quad (28)$$

The *fixed* excitation spectral patterns W_1^e and W_2^e are a set of harmonic components computed as in [5] (see also Fig. 1). Each component is a harmonic spectrum and two successive components are separated by one semitone. In order to represent the pitch shifting transformation, we investigate two alternative models:

- a dictionary component transformation T^{de} that will be, in the ideal case, a translation defined by the equation $y = x + b$, where b is the amount of shift in semitones,
- a frequency transformation T^{fe} that will be, in the ideal case, a homothety defined by the equation $y = \alpha x$, where $\alpha = 2^{b/12}$.

These *free* transformation matrices $T_{12}^{f\phi}$ and $T_{12}^{d\phi}$ are either initialized

- in an informed way, *i.e.*, the matrix elements within a one-tone range of the actual pitch shift are initialized with random values and the other elements are set to zero,
- or entirely with random values.

Examples of estimated transformation matrices are given in Fig. 3. As we work with MU, let us remind that zeros (dark blue in the figures) in the parameters remain unchanged over the iterations. All the elements of the other matrices ($H_1^e, W_1^\phi, H_1^\phi$) are initialized with random values.

C. Estimation and results

The estimation of the parameters of the joint model, *i.e.*, equations (26) and (27) or (26) and (28) is done using *NMPcF* (see Section III-A). An experiment without deformation in the reference model, *i.e.*, $V_2 = V_1$ is added as comparison, as well as an "oracle" setting, *i.e.*, $V_2 = T_{12}^{fe} W_2^e H_2^e \odot W_2^\phi H_2^\phi$ or $V_2 = W_2^e T_{12}^{de} H_2^e \odot W_2^\phi H_2^\phi$. These two complementary experiments should respectively provide lower and upper bounds to our approach. The results are given in terms of signal-to-noise ratio (SNR) between the magnitude spectra of the true source and reference signals ($\|\mathbf{x}_{fn}^1\|_{fn}$ and $\|\mathbf{x}_{fn}^2\|_{fn}$) and the estimated

⁴<http://www.guitarpitchshifter.com/matlab.html>

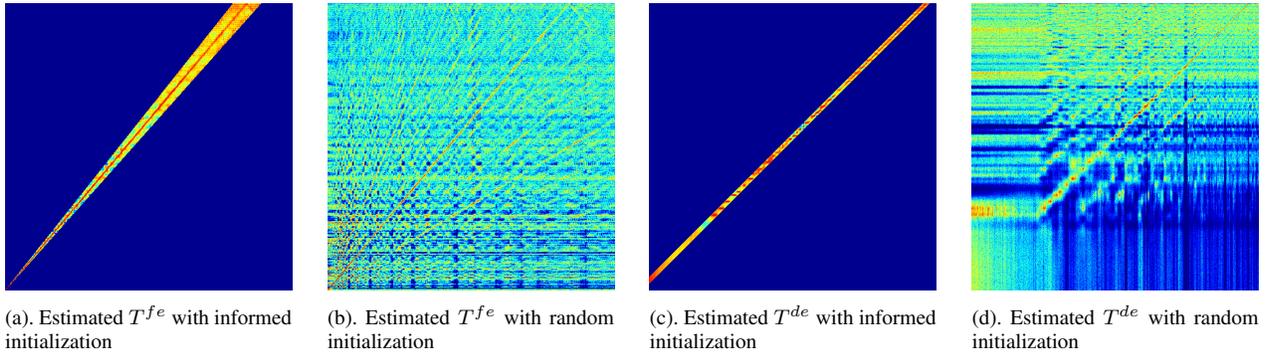


Fig. 3. Examples of different deformation matrices modeling the pitch shifting of a guitar sample.

Pitch shift (tone)	1/2		1		3/2		2	
Source/Reference	Src	Ref	Src	Ref	Src	Ref	Src	Ref
Oracle	10.3	9.6	10.3	9.6	10.2	9.4	10.2	9.6
T^f informed	9.1	7.9	8.8	7.6	8.5	7.5	8.5	7.3
T^f random	9.0	7.8	8.7	7.4	8.3	7.1	8.1	7.0
T^d informed	8.5	7.2	7.9	6.9	7.5	6.6	7.4	6.2
T^d random	9.3	6.9	8.7	6.5	8.5	6.2	8.3	5.5
No deformation	6.5	4.5	6.2	3.7	6.0	3.1	5.9	2.8

(A). AVERAGE SNR (DB).

Pitch shift (tone)	1/2		1		3/2		2	
Source/Reference	Src	Ref	Src	Ref	Src	Ref	Src	Ref
Oracle	0.09	0.10	0.09	0.10	0.09	0.10	0.09	0.11
T^f informed	0.13	0.19	0.15	0.20	0.15	0.21	0.15	0.22
T^f random	0.12	0.19	0.13	0.20	0.13	0.21	0.13	0.22
T^d informed	0.13	0.19	0.14	0.20	0.15	0.22	0.16	0.23
T^d random	0.13	0.20	0.14	0.21	0.15	0.23	0.16	0.24
No deformation	0.18	0.28	0.20	0.28	0.24	0.28	0.27	0.29

(B). AVERAGE IS DIVERGENCE.

TABLE I

SIGNAL-TO-NOISE RATIO (SNR) AND IS DIVERGENCE BETWEEN TRUE AND ESTIMATED SPECTRA FOR THE ELEMENTARY SCENARIO WITH PITCH-SHIFTED GUITAR SIGNALS AS DESCRIBED IN SECTION IV

spectra ($V_1^{[1/2]}$ and $V_2^{[1/2]}$) in Table Ia and in terms of the IS divergence (the terms of the sum in (12)) in Table Ib.

For both SNR and IS divergence, we observe that the distortion is much smaller after deformation modeling than before, for instance 9.1 dB and 7.9 dB SNR compared to 6.5 dB and 4.5 dB (first column in Table Ia). Nevertheless, the distortion remains slightly larger than what can be achieved in the oracle setting (e.g., 10.3 dB and 9.6 dB). These results show the ability of all our models to account for pitch shifting and effectively reduce the difference between the source signals and the corresponding models. It can also be noticed that the knowledge of the pitch shift value leads to a small improvement in terms of SNR for the reference. Such information can be provided by a sound engineer or a musician, for instance.

As the considered pitch shifting is a software effect, the use of T^{fe} is possible even though the guitar is inharmonic. In a different scenario where a given melody would be played by an inharmonic instrument in two different tonalities, the inharmonicity would require a specific inharmonic dictionary and the use of T^{de} instead of T^{fe} . Indeed, the partials of a given pitch would not be found by simple shifting of the partials of another pitch and pitched components must be shifted while attack components must not. Such a distinction for each component is not possible with T^{fe} .

V. VOICE/MUSIC SEPARATION

In this section, we describe a second use case of the proposed framework for source separation with deformed reference. We target the separation of speech and music from old recorded movies and TV series. Speech and/or music references are used to guide the separation.

After briefly describing the data, we recall how speech and music references are modeled in the proposed framework. We consider two distinct models for the music references depending on whether they are aligned a priori or not. We conduct experiments that compare these two models as well as different initialization procedures. Finally, we investigate the use of several references for a single source with the objective of making the separation more robust.

A. Data

The musical samples and the corresponding references are obtained using the MODIS audio motif discovery software in [34]. This software aims at clustering the segments of a long audio stream (here movies or TV series) that are similar enough according to a threshold. It is based on seeded discovery and template matching [35], but on a more fundamental level the audio segments are compared using a segmental variant of dynamic time warping (DTW) and common features. As long as it allows the discovery of non-exact repetitions, the discovered references are distorted compared to the source of interest (rhythm changes, fade in) and also contain additional sources (mainly sound effects).

Speech examples are taken from the database in [36] in which 16 different speakers uttered the same 238 sentences. We kept 4 musical examples and 4 sentences (two female and two male speakers) and mixed them at two different voice-to-music ratios : -6 dB (music as foreground and voice as background), and 12 dB (voice as foreground and music as background). Thus the original SDRs are -6 dB and 12 dB for the voice and 6 dB and -12 dB for the music. These levels are close to those effectively observed in movies and TV

series. We mixed such examples ourselves in order to obtain objective measures for the evaluation and to compare our estimated sources with the original ones using [37]. Combining those parameters leads to 32 original mixtures X^1 . For each mixture to be separated, we have one or more deformed music reference(s) (other discovered versions of the same music excerpt), and one or more deformed speech reference(s) (same sentence uttered by different speakers). The original mixtures and the references are about eight seconds long, they are sampled at 16 kHz and are single-channel ($\forall m, I^m = 1$). Some examples are available online⁵.

B. Tested models

In the different setups reported here, the speech sources are numbered as $j = 1$ or 2 , the music sources as $j = 3$ or 4 , and the other sources and background noise as $j = 5$ or 6 . *Fixed* variables are in black ($W_1^e, W_2^e, W_3^e, W_4^e, T_{34}^{t\phi}$). *Free* variables are in green ($H_1^e, H_2^e, T_{12}^{f\phi}, T_{12}^{d\phi}, T_{12}^{t\phi}, T_{34}^{te}, W_5, H_5, W_6, H_6$). *Shared* variables are in red or blue ($W_1^\phi, H_1^\phi, H_3^e, W_3^\phi, H_3^\phi$). Note that, in one particular setup, H_3^e, W_3^ϕ and H_3^ϕ are *free*. The *fixed* matrices T set to identity are removed from the notations.

1) *Signal to be separated*: The first signal is the mixture to be separated. It is composed of speech V_1 , music V_3 and noise V_5 :

$$\begin{aligned} V^1 &= V_1 + V_3 + V_5 \\ &= W_1^e H_1^e \odot W_1^\phi H_1^\phi + W_3^e H_3^e \odot W_3^\phi H_3^\phi + W_5 H_5 \end{aligned} \quad (29)$$

2) *Speech reference*: The second mixture is composed of the speech reference V_2 alone :

$$V^2 = V_2 = W_2^e H_2^e \odot T_{12}^{f\phi} W_1^\phi T_{12}^{d\phi} H_1^\phi T_{12}^{t\phi} \quad (30)$$

During the *NMPcF* and/or *GEM* stages, H_1^e and H_2^e are estimated separately to model the different intonations and pitches between the speakers. Conversely, the filter matrices W_1^ϕ and H_1^ϕ are jointly estimated to model similar phonetic content, as the two speech signals are composed of the same phonemes. $T_{12}^{t\phi}$ models the time alignment between the two utterances. $T_{12}^{f\phi}$ is constrained to be diagonal and it models both the equalization and the speaker's difference. $T_{12}^{d\phi}$ is also used to model the speaker difference and its initialization is discussed in Section V-F. This model is similar to the one used in [16], where a time-invariant filter is used to model the frequency deformations of V_2 , but here we consider in addition a transformation matrix $T_{12}^{d\phi}$ for the filter dictionary. Additional speech references are treated in the same way.

3) *Music reference*: The third signal is composed of the music reference V_4 , that is similar to V_3 , and of some noise V_6 . We consider two different models for this signal.

a) *non phase aligned reference*: This first model represents the reference signal as a third observed mixture V^3 :

$$V^3 = V_4 + V_6 = W_4^e H_3^e T_{34}^{te} \odot W_3^\phi H_3^\phi T_{34}^{t\phi} + W_6 H_6 \quad (31)$$

T_{34}^{te} and $T_{34}^{t\phi}$ model the alignment of short-term spectra between the two music examples.

b) *phase aligned reference*: In this second model, the music reference is aligned at the signal level with the mixture to be separated. This is achieved by windowing X^1 into time frames, aligning each time frame with X^2 by means of time-delay computation using the Generalized Cross Correlation with PHase Amplitude Transform (GCC-PHAT) algorithm [38], and reconstructing a time-aligned reference signal \tilde{X}^2 by overlap-and-add. Once aligned, it is considered within our general framework as a second channel of the first mixture ($I^1 = 2$). As a consequence, V^3 is not used in this model, and V_3 becomes a single music source with a *free* spatial parameter $A_3 \in \mathbb{C}^{2 \times 2}$ encoding the amplitude and phase differences between the target and the reference channel of the first mixture. H_3^e, W_3^ϕ , and H_3^ϕ are *free* parameters. As the other sources belong to one channel only, their spatial parameters are *fixed* to $A_1 = A_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$, and $A_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$.

C. Parameter initialization

We here give details about the *Init* and *NMF* stages previously mentioned in Section III-C. The weight parameter $\lambda^{m'}$ is set to $\frac{NF}{N'F'}$. The *fixed* excitation spectral patterns W_j^e for $j = 1, 2, 3, 4$ are a set of harmonic components computed as in [5]. We initialize the synchronization matrices $T_{12}^{t\phi}, T_{34}^{t\phi}$, and T_{34}^{te} with Dynamic Time Warping (DTW) [39] matrices computed on MFCC vectors [40] for speech sources and on chroma vectors for music sources. Following [16], we allow the temporal path to vary within an enlarged region around the estimated DTW path. Since the data are deformed and noisy (especially for music), we weight this enlarged path by coefficients of the similarity matrix (from which the DTW is obtained), in order to avoid obvious initialization errors. We invite the reader to refer to [16] for details on this strategy. The spectral transformation matrix $T_{12}^{f\phi}$ is initialized as the identity matrix. The others matrices ($H_1^e, H_2^e, W_5, H_5, W_6, H_6, W_1^\phi, H_1^\phi, H_3^e, W_3^\phi, H_3^\phi$) are initialized with random values. In the phase aligned music reference case, we proceed with the same initialization as for the previous setup, but without any T^{te} and $T^{t\phi}$ matrices for music. The music spatial parameter is initialized to $A_3 \approx \begin{pmatrix} 1 & -0.25 \\ 1 & 0.25 \end{pmatrix}$, where the first column accounts for the fact that the two channels are expected to be time and amplitude aligned and the second column accounts for residual differences.

The *NMF* stage can then be applied separately on the reference mixtures (30) and (31) (unaligned references), where the *shared* matrices ($W_1^\phi, H_1^\phi, H_3^e, W_3^\phi, H_3^\phi$) and the *free* parameters (H_3^e, W_6, H_6) are updated whereas matrices $T_{12}^{f\phi}, T_{12}^{d\phi}, T_{12}^{t\phi}, T_{34}^{te}$, and $T_{34}^{t\phi}$ are not. In the phase aligned music reference case, the parameters $H_3^e, W_3^\phi, H_3^\phi, W_6$, and H_6 are updated to fit the reference signal that is already phase aligned with the signal to be separated. In both cases, W_6 and H_6 are set once again to random values before applying *NMPcF* and/or *GEM*.

D. Algorithm combination

As a first experiment, we evaluate the effect of *NMF* initialization in the case of a single non phase aligned music

⁵http://speech-demos.gforge.inria.fr/source_separation/taslp2015/index.html

		-6 dB voice-to-music ratio						12 dB voice-to-music ratio					
		voice			music			voice			music		
		SDR	SAR	SIR	SDR	SAR	SIR	SDR	SAR	SIR	SDR	SAR	SIR
No phase alignment	<i>Init + NMPcF</i>	-0.6	2.3	-2.1	5.9	11.7	8.3	3.6	4.9	29.2	-6.8	6.8	-5.5
	<i>Init + NMF + Plain-NMF</i>	1.8	1.0	8.9	9.2	13.1	12.4	5.1	7.1	23.8	-3.9	3.1	-1.5
	<i>Init + NMF + NMPcF</i>	2.1	2.9	8.1	9.2	11.6	17.7	6.0	8.7	24.6	0.5	2.7	3.9
Phase alignment	<i>Init + NMF + GEM</i>	0.0	5.7	-3.3	1.8	-1.3	16.3	4.1	4.3	10.7	-8.7	-9.3	4.6
	<i>Init + NMPcF + GEM</i>	-1.1	3.9	-1.0	5.3	11.6	8.4	3.2	3.8	27.9	-7.3	6.7	-6.0
	<i>Init + NMF + NMPcF + GEM</i>	2.2	3.7	7.5	9.8	11.4	17.7	7.6	13.0	21.6	2.9	4.0	10.0

TABLE II

AVERAGE VOICE/MUSIC SEPARATION PERFORMANCE (dB) FOR DIFFERENT COMBINATIONS OF ALGORITHMIC STAGES IN THE CASE OF ONE MUSIC REFERENCE AND NO VOICE REFERENCE.

reference and no speech reference. The number of iterations is set to 10 for the *NMF*, *Plain-NMF*, and *NMPcF* stages, and to 100 for the *GEM* stage that is known to require more iterations. The separation performance results are evaluated in terms of signal-to-distortion ratio (SDR), signal-to-interference ratio (SIR) and signal-to-artifacts ratio (SAR) [37].

The results are summarized in the top part of Table II. The best SDRs are indicated in bold for each column's part (delimited by double lines). A notable improvement (at least 2.5 dB) is observed when *NMF* is used beforehand, as compared to using *NMPcF* alone. The use of *NMPcF* instead of *Plain-NMF* then leads to an improvement when the source with a reference (here music) is as background. A similar behavior is observed in the experiment of Section VI.

E. Model comparison for music reference

As a second experiment, we evaluate the effect of phase alignment for the music reference. The results are shown in the bottom part of the Table II. Comparing the configurations chosen for the fourth and fifth lines with the first line shows that *GEM* decreases the separation performance if it is used directly after *NMF* or *NMPcF* alone. This highlights that the proper functioning of the *GEM* depends on the two previous steps. The best results are obtained when the signals are phase aligned and both *NMF* and *NMPcF* are used before *GEM*. In that case, the improvements compared to the non phase aligned case are marginal when the music is as foreground, but significant when the music is as background.

As a *GEM* iteration is in the order of ten times longer than a *NMPcF* iteration, the relevance of this costly last step can be discussed. Given the marginal improvements when music is in the foreground, additional *GEM* iterations are not necessary for this voice-to-music ratio. Conversely, when music is in the background, *GEM* increases the music SDR by 2.4 dB. This result is also greater by 1.3 dB compared to approaches that use multiple references (see Table III).

F. Multiple references for a single source

Experiments on the effect of using reference signals for different sources have been conducted in [27]. Complementary experiments are here conducted on the influence of the number of reference signals per source, *i.e.*, several j' for a single j . The number of speech (resp. music) references grows from 0 to 3 (resp. 2). We also evaluate the separation performance without any deformation modeling except time alignment,

referred hereafter as *Reference-based Wiener Filter (RbWF)*. Table III gathers all the results.

It can be emphasized that the use of multiple speech references leads to better result, especially when speech is in the background (in the order of 0.5 dB). Conversely, the use of two music references tends to smaller or equal results. This can be explained by the fact that the considered music references contain additional sources supposed to be taken into account by the matrices W_6 and H_6 in (31), and that leads to a more complicated situation for the algorithm. But for some particular examples, the second music reference leads to better results. Overall, the addition of more than one reference seems to improve separation when the new references carry complementary information.

Reference-based Wiener Filter (RbWF) results are obtained using an adaptive Wiener filter that reconstructs the different sources of the mixture based on the power spectrum ratio between the reference signals. As the references and the mixture are of different length, a time alignment (as previously described) is performed beforehand. These baseline measurements give the reader a better description of the quality of the reference. All the results show a significant difference compared to the case with one reference for each source, while the foreground music source results are comparable. This can be explained by the quality of the alignment pre-processing technique when the reference source predominates in the mixture signal. However, the proposed approach shows clear benefit when the reference source does not predominate.

VI. COVER GUIDED MUSIC SEPARATION

This last experimental part focuses on the task of professionally-produced music separation guided by covers [24]. A cover song is a replica of an original song with some differences due for instance to artist interpretation, singer/instrument changes, or new song structure. Such covers can be easily found, and they are usually close to the original song making them interesting for separation. As it provides high quality separation, such demixing enables the edition of the song by end-users (*e.g.*, for active listening) or professional users (*e.g.*, for upmixing).

Here we use multitrack recordings of cover songs to guide the separation. Each track is used as a reference for one corresponding source, so the number of tracks is the same as the number of sources to be separated. In [24], the multitrack cover signals are only used to initialize the source parameters W and H (*Plain-NMF*). Here, these parameters are shared

Number of speech references	Number of music references	-6 dB voice-to-music ratio						12 dB voice-to-music ratio					
		voice			music			voice			music		
		SDR	SAR	SIR	SDR	SAR	SIR	SDR	SAR	SIR	SDR	SAR	SIR
1	0	2.1	5.9	3.7	7.7	11.9	13.8	8.7	11.3	19.7	-2.2	3.5	-1.5
2	0	2.3	6.1	3.9	7.9	12.4	13.3	8.6	11.1	19.9	-2.5	3.8	-1.9
3	0	2.8	5.7	4.7	8.3	12.6	13.6	9.2	11.7	20.6	-2.2	4.1	-1.6
0	1	2.1	2.9	8.1	9.2	11.6	17.7	6.0	8.7	24.6	0.5	2.7	3.9
1	1	4.6	6.0	9.9	8.0	9.6	18.9	13.3	14.5	26.2	1.6	3.4	6.7
2	1	4.9	6.2	10.2	8.5	10.4	19.4	12.2	13.5	25.5	0.9	3.4	6.5
3	1	5.0	6.3	10.5	8.6	10.5	19.4	12.1	13.4	25.4	1.6	3.4	6.3
0	2	1.5	3.0	4.9	8.4	11.8	14.4	4.8	7.5	25.3	-2.2	3.9	-1.0
1	2	4.1	6.1	8.5	8.1	11.0	16.2	10.4	12.2	26.2	-0.6	3.4	1.2
2	2	4.6	6.3	9.4	8.3	11.1	16.5	10.3	12.2	26.2	-0.9	3.6	1.3
3	2	4.6	6.2	9.5	8.5	11.3	16.8	10.0	11.8	25.7	-0.5	3.7	1.2
<i>RbWF</i>	<i>RbWF</i>	3.0	4.1	7.2	9.0	13.3	12.0	5.5	7.5	24.8	-6.5	6.2	-5.4

TABLE III

AVERAGE VOICE/MUSIC SEPARATION PERFORMANCE (dB) FOR DIFFERENT NUMBERS OF SPEECH AND MUSIC REFERENCES. SPEECH REFERENCES ARE UTTERED BY DIFFERENT SPEAKERS THAT HAVE THE SAME GENDER AS IN THE MIXTURE TO BE SEPARATED. THE MUSIC REFERENCE IS NOT PHASE ALIGNED, AND ONLY 10 ITERATIONS OF *NMF* AND *NMPcF* ARE USED. THE BEST SDRs ARE INDICATED IN BOLD.

Title	Track names
I Will Survive	Bass, Brass, Drums, Electric Guitar, Strings, Vocal.
Pride and Joy	Bass, Drums, Electric Guitar, Vocal.
Rocket Man	Bass, Choirs, Drums, Others, Piano, Vocal.
Walk this Way	Bass, Drums, Electric Guitar, Vocal.

TABLE IV
COVER MULTITRACK DATASET

between the source and the reference hence the reference signals are used during the estimation stage too. Deformations are modeled in various ways using the general framework introduced in Section II.

A. Data and settings

In order to compare our results, we used the same data set and settings as in [24]. Both original and cover multitracks are available in order to evaluate the separation. They are also used in the mirror configuration, *i.e.*, considering the original as the reference and vice versa. Here, we make an exhaustive list of settings that differ from [24] and refer the reader to [24] for other common details.

The 30 second examples are chosen in a different way as in [24] and are typically composed of half of a verse and half of a chorus. The considered tracks of four songs are listed in Table IV. There is no second electric guitar for the song "Walk this Way" as it does not appear in the example that we selected. We use 50 iterations for *NMF* and *NMPcF* instead of 500 [24] and 10 iterations for *GEM* instead of 500 [24]. The number of components D is kept to 50. For the sake of clarity, the single-channel case is first investigated to show the effect of different deformation models, then stereo data are processed using the *GEM* algorithm presented in Section III-B.

B. Tested models

In this scenario, the mixture to be separated is an original song. The reference signals are the different tracks of a cover version of this original song. Each reference signal is related to one target source in the original song. The power spectrum

of each reference signal is modeled as $V_j = W_j H_j$ and its parameters are initialized using the *Init* and *NMF* stages in all the different settings reported in Table V.

Conversely, different settings are considered for the power spectrum model of the sources to be separated: WH , $T^f WH$, and $WT^d H$ (see Table V). The general framework introduced in Section II is then used by inverting j and j' in (7) for instance. This is because the initialization of the T^f and T^d matrices is weak and would have disturbed the *NMF* stage.

C. Initialization

Parameters W and H are randomly initialized before being updated to fit the reference signal. Here, this is done by the so-called *Init* and *NMF* steps similarly to what was done in [24]. When used, T^f is initialized as an identity matrix. Along the same lines, we tested several initializations of T^d starting from the identity matrix and changing the weight of the off-diagonal coefficients. The best initial value was the sum of an identity matrix and a random matrix drawn from a rectified Gaussian distribution. When stereo data and the *GEM* algorithm are used, the (full-rank) spatial parameters are initialized beforehand using the reference for each source as in [24].

D. Results

Separation performance is evaluated in terms of signal-to-distortion ratio improvement (SDRI) that is the difference between the output SDR [37] and the input SDR. The input SDR is defined as the power ratio between a source to be estimated and the mixture to be separated. The samples that we selected lead to an input SDR of the same order (-8.44 dB instead of -7.60 dB in [24]). The results are summarized in Table V. Some examples are also available online⁵.

1) *Single-channel results*: First, we reproduced the experiments in [24] with the differences previously presented. A similar SDRI mean is obtained (8.74 dB instead of 8.98 dB) in the case when the parameters are not shared. Compared to the initialization (10.06 dB), this configuration leads in fact to

	Source model	Instruments Number of tracks Input SDR	Average 20	Bass 4	Drums 4	Guitar 3	Vocal 4	Choirs 1	Others 1	Piano 1	Brass 1	Strings 1
Mono		<i>Reference-based Wiener Filter</i>	-8.44	-7.42	-7.17	-9.98	-4.18	-12.34	-9.75	-12.48	-18.64	-10.55
	<i>WH</i>	<i>Init + NMF</i>	9.93	9.27	8.90	9.59	9.42	13.40	9.88	10.34	16.30	9.51
	<i>WH</i>	<i>Init + NMF + Plain-NMF</i> [24]	10.06	9.33	9.02	9.71	9.60	13.70	9.79	10.80	16.25	9.80
	<i>WH</i>	<i>Init + NMF + NMPcF</i>	8.74	6.94	8.95	8.53	8.14	11.36	9.66	10.51	11.54	10.11
	<i>T^fWH</i>	<i>Init + NMF + NMPcF</i>	10.27	9.26	9.28	9.82	10.24	13.23	10.27	11.11	15.67	10.62
	<i>T^fWH</i>	<i>Init + NMF + NMPcF</i>	10.09	8.79	9.22	9.88	9.78	12.29	10.47	12.94	14.66	10.65
	<i>WT^dH</i>	<i>Init + NMF + NMPcF</i>	10.64	9.23	9.94	10.80	10.73	13.01	10.07	11.36	15.80	10.61
	Best	<i>Init + NMF + NMPcF</i>	10.85	9.42	10.25	10.11	10.79	14.42	10.05	11.47	18.09	10.83
<i>WH</i>	<i>Init + Oracle</i>	15.48	14.48	15.35	15.36	15.29	16.21	13.27	16.22	21.58	15.74	
Stereo	<i>WH</i>	<i>Init + NMF + NMPcF + GEM</i>	10.41	8.99	9.12	10.05	9.98	15.31	10.96	11.95	16.79	10.76
	<i>T^fWH</i>	<i>Init + NMF + NMPcF + GEM</i>	10.16	8.64	8.86	8.87	10.02	15.50	10.90	12.78	17.27	10.05
	<i>WT^dH</i>	<i>Init + NMF + NMPcF + GEM</i>	10.50	9.01	9.66	9.95	10.35	13.48	10.22	11.78	17.88	10.61

TABLE V

AVERAGE SDRI (dB) FOR THE SEPARATION OF MUSIC RECORDINGS USING MULTITRACK COVERS AS REFERENCES. VALUES IN BOLD INDICATE THE MODEL CHOSEN FOR EXPERIMENT REFERRED AS **BEST**.

a decrease of the average SDRI. This can be explained by the high similarity between the covers and the original tracks, as shown by the *Reference-based Wiener Filter (RbWF)* results in Table V⁶. Conversely, sharing the parameters during the final estimation guarantees not to draw away too much from the starting point while getting closer to a solution that fits better to the original tracks. In our case, a marginal improvement is observed (10.27 dB average SDRI). This small improvement is not surprising as we considered no deformation between the references and the sources that we estimate.

More appropriate models that use deformations (T^f or T^d) have been tried with promising results. Better overall results (10.64 dB) are obtained when using a T^d in the source model, whereas T^f slightly decreases the average result. Moreover, the improvement is not uniformly observed, and some sources are more enhanced using T^f instead of T^d .

We conduct a final experiment (**Best**) where, for each source, the best source model (values in bold font) is chosen. The *Init + NMF* setting is not taken into account in this choice as it would avoid the benefit of the update of the other parameters during the *NMPcF*. We observe for this selection an overall increase of the performance (10.85 dB), hence showing the potential of using suitable deformation models for specific sources. As we selected the different models based on their optimal results, this last experiment is of course not representative of an unsupervised scenario. However, it is realistic in the considered context where an expert user may be able to select the best model by listening to the results. Further experiments are needed to understand which parameters should be accessible to the user, maybe depending on its level of expertise.

2) *Multi-channel results*: The stereo settings reported in [24] yield a SDRI of 10.05 dB. Here, the model without deformation shows a small improvement (from 10.27 dB to 10.41 dB) when 10 additional *GEM* iterations are added and similar results are observed for the models with deformation. The EM algorithm usually requires more iterations that were not achievable in a reasonable computation time here. Indeed here each reference is considered as a mixture which requires a

specific E-step in the EM algorithm presented in Section III-B.

VII. CONCLUSION

In this paper, we have presented a general framework for using audio information in order to separate a given mixture. This model is general enough to take different types of audio references into account and to accommodate for their possible deformations in the frequency domain and/or in the temporal domain. After having presented an elementary scenario with pitch shifted example, we have provided extensive experiments on two realistic scenarios : voice and music separation in the context of movie soundtracks, and cover-guided music separation.

Our experiments show that the use of reference for a given source improves the general sound quality of the estimated source (from 9 to 15 dB). Different temporal alignment methods appear to be adapted to different situations and signals. Moreover, our experiments show that having at least one reference per source is of prime importance.

Other algorithmic approaches can also be investigated like stacked NMF (column-wise concatenation of mixture and time-warped references) with other advantages and disadvantages. A more general perspective of this study will be the design of some automatic processes that choose the best configuration of our general model for a given mixture. Our model can also be improved by adding well-chosen constraints on the parameters. For instance, smoothness constraints on the spectral transformation matrices $T_{j'j}^{f,\phi}$ should help the model to derive a more relevant spectral deformation between the target sources and the references.

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⁶These results were obtained following the definition of the *RbWF* in Section V-F except that no time alignment was performed.

APPENDIX A

Here we give a detailed derivation of the expected value of the complete-data log-likelihood (18).

$$\begin{aligned}
Q(\theta, \theta^c) &\triangleq \mathbb{E}_{\mathbf{Z}|\theta^c} [\log p(\mathbf{Z}|\theta)] = \sum_m \lambda^m \mathbb{E}_{\mathbf{Z}|\theta^c} [\log p(\mathbf{X}^m, \mathbf{S}^m|\theta)] \\
&= \sum_m \lambda^m \mathbb{E}_{\mathbf{X}^m, \mathbf{S}^m|\theta^c} [\log p(\mathbf{X}^m|\mathbf{S}^m)] + \sum_m \lambda^m \mathbb{E}_{\mathbf{S}^m|\theta^c} [\log p(\mathbf{S}^m|\theta)] \\
&= \sum_{m,f,n} \lambda^m \mathbb{E}_{\mathbf{x}_{fn}^m, \mathbf{s}_{fn}^m|\theta^c} \left[\log \mathcal{N}_{\mathbb{C}} \left(\mathbf{x}_{fn}^m | \mathbf{A}_{fn}^m \mathbf{s}_{fn}^m, \mathbf{\Sigma}_{\mathbf{b}_{fn}^m} \right) \right] + \sum_{m,j \in \mathcal{J}^m, f,n} \lambda^m \sum_{r=1}^{R_j} \mathbb{E}_{s_{jr,fn}|\theta^c} [\log \mathcal{N}_{\mathbb{C}} (s_{jr,fn} | 0, v_{j,fn})] \\
&\stackrel{c}{=} - \sum_{m,fn} \frac{\lambda^m}{\sigma_f^2} \text{tr} \left[\mathbf{R}_{\mathbf{x}_{fn}^m} - \mathbf{A}_{fn}^m \mathbf{R}_{\mathbf{x}\mathbf{s}_{fn}^m} \mathbf{H} - \mathbf{R}_{\mathbf{x}\mathbf{s}_{fn}^m} \mathbf{A}_{fn}^m \mathbf{H} + \mathbf{A}_{fn}^m \mathbf{R}_{\mathbf{s}_{fn}^m} \mathbf{A}_{fn}^m \mathbf{H} \right] - \sum_{m,j \in \mathcal{J}^m, f,n} \lambda^m R_j d_{IS}(\xi_{j,fn} | v_{j,fn})
\end{aligned}$$

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