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Soluble Microbial Products and Suspended Solids influence in membrane fouling dynamics and interest of punctual relaxation and/or backwashing

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Abstract

To favour the control of membrane fouling on line by relaxation and backwash sequencing, two major fouling origins are considered: the former is due to retention of large particles on the membrane surface forming a growing deposit that can be controlled by tangential shear stresses, the second is due to the retention of the largest soluble polymers forming a thin layer on the membrane surface including pore blocking and inducing a progressive reduction of the deposit porosity, the influence of this second fouling origin can only be reduced by backwashing. A simple model was developed to represent (i) the accumulation of two types of compounds and its consequences and the evolution with time of the hydraulic resistance of the system and (ii) the role of relaxation and backwashing to reduce the fouling impact. Some simulations were

presented according to the values of the three model parameters. Simulations were also compared to experimental data obtained on biological suspensions.

Keywords: Membrane fouling, Soluble Microbial Products, Total Suspended Solids, fouling modelling, backwashing, relaxation

Nomenclature

d	Cake particles diameter (m)
J_p	Permeate flux ($L \cdot m^{-2} \cdot h^{-1}$)
$k_\varepsilon, k_1, k_2, k_3, b$	Constants
m_c	Specific cake mass ($g \cdot m^{-2}$)
m_s	Critical specific cake mass ($g \cdot m^{-2}$)
R_0	Clean membrane resistance (m^{-1})
R_c	Cake resistance (m^{-1})
R_s	Resistance due to SMP deposit (m^{-1})
R_t	Total resistance (m^{-1})
S	Soluble microbial products concentration ($gCOD \cdot L^{-1}$)
t_f	Filtration time
t_r	Relaxation time
t_B	Backwashing time
TMP	Total Trans-Membrane Pressure (Pa)
TMP_0	Initial Trans-Membrane Pressure (Pa)
X	Total suspended solids concentration ($gCOD \cdot L^{-1}$)
α	Cake specific resistance (mkg^{-1})
β	Shear parameter ($m^2 \cdot g^{-1}$)
ε	Cake porosity
ε_0	Initial cake porosity
η_1, η_2, η_3	Constants
μ	Permeate viscosity (Pa.s)
ρ_s	Cake density ($kg \cdot m^{-3}$)
σ	Soluble polymers fraction rejected by the membrane

1. Introduction

Membrane bioreactors are now a mature technology for the treatment of industrial or urban wastewaters. The total rejection of biomass by the membrane allows a significant improvement of water quality (absence of SS and advanced disinfection) with respect to that obtained with

conventional systems. Moreover because the membrane rejection does not depend on biomass concentration in the bioreactor, it is possible to intensify the biological processes by increasing sludge retention time or decreasing the reactor volume. Nevertheless major drawbacks still hinder MBR development, that are membrane fouling, high energy requirements and lack of simple tools to optimize online MBR control. Depending on numerous factors, membrane fouling in MBR appears as a combination of complex phenomena [1]. It is directly related to the filtration phase during which largest compounds retained by the membrane cut-off accumulate on the membrane surface [2]. It also depends on physical-chemical interactions between smaller compounds and the membrane material (pore blocking, adsorption notably). The only tool to quantify online the intensity of fouling is the monitoring of the Trans-Membrane Pressure (TMP). Many works have been trying to study the TMP dynamics. Based on an experimental observation highlighting a two step TMP increase: a slow increase followed by a TMP jump, Sarjo et al. (2008) [3] and Ognier et al. (2004) [4] have proposed models assuming that a progressive pore blocking would lead to a local flux increase and consequently to an increase of membrane fouling. Other studies assumed that TMP increase would go through three stages [5]: an initial stage of short-term TMP rising due to soluble microbial products (SMP) deposition or bioflocs adsorption leading to a pore blocking, a second stage of long-term TMP rising either linearly or weakly exponential due to the development of cake formed by either the suspended solids SS or SMP, and a third stage of sudden TMP rising also know as the TMP jump due to inhomogeneous fouling. Different mechanisms explaining the TMP jump have been proposed and modelled such as the area loss model [6], the pore narrowing model [7], the pore loss model [8] and the critical suction pressure model [9].

Even though, TMP measurement is a global evaluation of instantaneous fouling intensity. It does not allow any differentiation of the relative importance of the different fouling processes and it is then difficult to optimize the operation and energy requirements. In practice, the filtration step is then essentially controlled using two criteria: average TMP variation during defined time periods and the maximal TMP value allowed.

In association with the monitoring of such criteria, the operator has different options to minimize fouling dynamics during operation including parietal shear stresses as tangential flow circulation, gas injection (air for aerobic process) close to the membrane surface to detach a large part of the

compounds accumulated onto the membrane surface, backwash to eject compounds blocking the pores to partially deconstruct the deposit/biofilm onto the membrane surface, and chemical cleaning to desorb compounds linked to materials, even destroying biofilm structure.

Numerous models were developed to give a better understanding and quantification of the different fouling modes including the role of parietal shear stresses to minimize deposit influence [10, 11, 12]. Such models also took into account the biological functioning conditions to include the role of SS, EPS and SMP concentrations in both reversible and irreversible fouling [13]. However, very few of them develop simulations by including the role of periodic relaxation and backwash on the instantaneous modification of the different fouling origin and their relative intensity [13, 14]. It is precisely the objective of this work to develop a simple model including mass balance when operating a filtration with air injection and periodic backwash. The simple model is confronted to experimental data obtained under several operating conditions and simulations are analyzed to point out the specific role of some fundamental criteria.

2. Model hypothesis

When filtering the mixed liquor suspended solids on membranes, the fouling dynamics is assumed to be due to three main phenomena as represented in Figure 1 [1, 15, 16]: (i) deposition of soluble polymers onto the membrane surface with the formation of a thin layer leading to some pore blocking and significantly that reducing the membrane open area and the membrane permeability, (ii) accumulation of particles onto the membrane surface to form a deposit which can also play the role of a porous filter able to retain some soluble fractions that progressively modified the deposit structure and its permeability, and (iii) the adsorption of smallest molecules that enter inside the pores and interact with the membrane material to induce pore's constriction and again reducing membrane permeability.

Nevertheless, many works studying fouling in membrane bioreactors, proved that the internal fouling is minor compared to the surface fouling [2, 17] and especially in the case of high suspended solids concentration or when using ultrafiltration [2, 18]. Based on these studies and aiming the development of simple model, the resistance due to pore constriction has been neglected in the proposed model.

Even if suspended solids are totally retained by the membrane to form an external deposit, sufficient and effective shear stresses would avoid significant membrane clogging, which make them no longer the main cause of fouling intensity [12, 19]. The transfer resistance is then due to a thin film development on the membrane surface (a biofilm in case of bioreactors) that contributes to a drastic decrease of membrane permeability notably if the pore blocking phenomenon is associated to thin layer formation. In fact, during cross flow filtration, the large soluble polymer compounds, as SMP or soluble EPS in bioreactors, retained by the membrane have lower value of critical flux and are most likely transported to the membrane surface by the imposed flux [20]. This phenomenon characterizes the first fouling phase making concentration of such soluble fraction an important parameter controlling initial fouling dynamics. Most of the soluble foulants interacting with the membrane material and causing pore blocking were characterized as SMP in MBR by Wu et al. (2008) [21].

Figures 2, 3 and 4 give some illustrations of the control actions that can be taken online in response to the evolution of the main cleaning process. A parietal shear stress (Figure 2) favours the reduction of the deposit thickness by inducing an external particle detachment and a laminar movement of deposit that contributes to some deconstruction of the external deposit. During a relaxation period (the parietal shear stress is maintained but the filtration strength on particles is stopped), the parietal shear stresses is intensified (Figure 3) but the membrane surface fouling (thin film of soluble compound accumulated on the membrane surface and pore blocking) is not modified. At the opposite, when starting backwash (Figure 4), the compounds blocking physically the pores are ejected and the thin layer deposit (including biofilm) can be deconstructed. The only phenomenon not concerned by the preceding modes of permeability regeneration is the internal adsorption of small molecules inside the pores that necessitates chemical cleaning for their detachment. This internal phenomenon appears generally as the less intensive one [22].

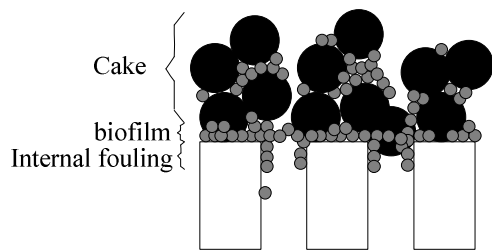


Figure 1: Different fouling mechanisms

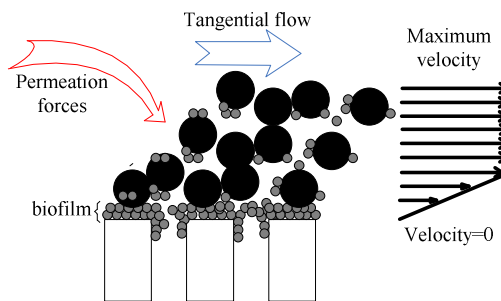


Figure 2: Shear forces effect on cake's destruction during tangential filtration

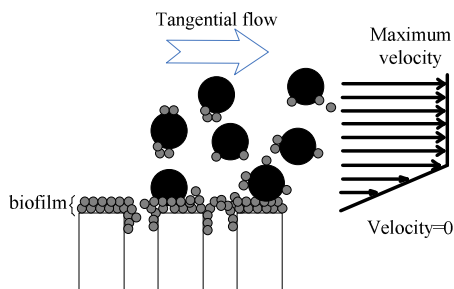


Figure 3: Relaxation effect on membrane cleaning

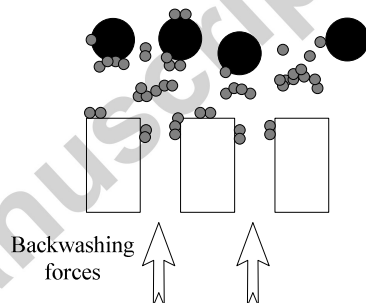


Figure 4: Back-washing effect on membrane cleaning

3. Fouling model development

In this section, a simple model to describe and to quantify the most important fouling mechanisms is proposed. It includes the respective role of each hydraulic cleaning method, notably relaxation and backwash. More particularly, this model highlights the effect of particles and large soluble compounds on cake's building and pore blocking and their consequences on fouling intensity and reversibility according to the different modes of hydraulic cleaning such as parietal shear stresses, relaxation and backwash.

The proposed model is based on two foulant families totally retained by the membrane cut-off but differing in sizes. While particles (Suspended Solids) are retained on the membrane surface to form a cake, the largest soluble compounds presenting a size in the range of the membrane pore size distribution are retained both inside the particle cake (reducing its porosity and permeability)

and on the membrane surface by blocking the membrane pores and forming a thin layer (Figure 5). The prediction of the dynamics of the hydraulic resistance of the system can then be largely improved by taking into account such combined phenomena [23].

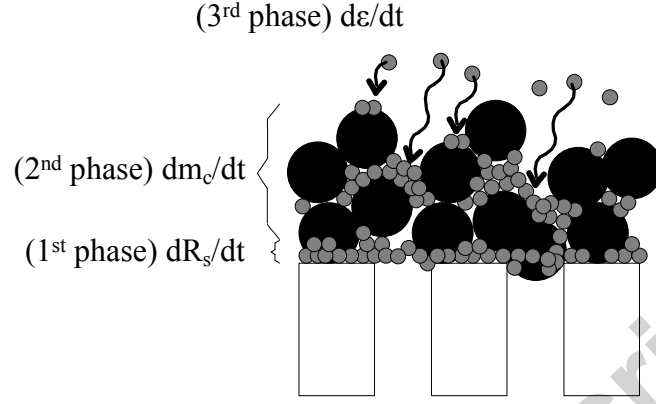


Figure 5: The three fouling mechanisms considered in the proposed model

During filtration phase, the model is given by the following set of equations:

$$TMP = \mu \cdot J_p \cdot R_t \quad (eq.1)$$

where TMP (Pa) is the trans-membrane pressure, μ (Pa.s) is the permeate viscosity, J_p ($L \cdot m^{-2} \cdot h^{-1}$) is the permeate flux and R_t (m^{-1}) is the total fouled membrane resistance that can be expressed as:

$$R_t = R_0 + R_s + R_c \quad (eq.2)$$

In eq. 2, R_0 stands for the membrane intrinsic resistance, R_s is the resistance of the first thin fouling layer and R_c is the cake's resistance.

One has:

$$R_0 = \frac{TMP_0}{\mu J_p} \quad (eq.3)$$

with TMP_0 (Pa) the initial value of the trans-membrane pressure.

Depending on the actual value of m_c , the dynamics of R_s is modelled as:

$$\frac{dR_s}{dt} = k_1 \cdot J_p \cdot \sigma \cdot S \quad (eq.4) \quad \text{if } m_c \leq m_s$$

$$\frac{dR_s}{dt} = 0 \quad (\text{eq.5}) \quad \text{if } m_c > m_s$$

where m_s (g.m^{-2}) is the specific mass of the first thin fouling layer.

Finally, the cake resistance is given by:

$$R_c = \alpha m_c \quad (\text{eq.6})$$

where α (m.kg^{-1}) is the cake's specific resistance and m_c (g.m^{-2}) is the deposit mass per area unit which dynamics is described by:

$$\frac{dm_c}{dt} = J_p \cdot (\sigma \cdot S + X) \cdot (1 - \beta(m_c - m_s)) \quad (\text{eq.7})$$

In this last equation, S (gCOD.L^{-1}) is the total SMP concentration, X (gCOD.L^{-1}) is the suspended solids concentration, σ is the SMP fraction rejected by the membrane barrier and β ($\text{m}^2.\text{g}^{-1}$) is the shear parameter.

The dynamics of the cake porosity ε is:

$$\frac{d\varepsilon}{dt} = -k_\varepsilon \left(\frac{\varepsilon}{\varepsilon + b} \right) \quad (\text{eq.8})$$

while:

$$k_\varepsilon = k_2 \cdot J_p \cdot \sigma \cdot S \quad (\text{eq.9})$$

$$\alpha = \frac{180(1-\varepsilon)}{\rho_s d^2 \varepsilon^3} \quad (\text{eq.10})$$

$$\frac{d\alpha}{dt} = -k_3 \frac{(2\varepsilon_0 - 2k_\varepsilon t - 3)}{(\varepsilon_0 - k_\varepsilon t)^4} \quad (\text{eq.11})$$

$$k_3 = \frac{180k_\varepsilon}{\rho_s d^2} \quad (\text{eq.12})$$

with d the cake particle mean diameter and ρ_s is the cake density.

When filtration is operated at constant permeate flux, the Trans-membrane pressure increases with time to compensate the hydraulic resistance increase due to the accumulation of compounds on/in the membrane material. The TMP variation is then based on Darcy's law and expressed with the resistance in series model (eq. 1). The total resistance of the clogged membrane is thus

expressed by eq. 2. The intrinsic membrane resistance R_0 can be quantified in filtering demineralised water (eq. 3).

R_s is the hydraulic resistance due to the presence of the SMP thin layer on the membrane, leading to some pore blocking and membrane porosity decrease. Only a backwashing is supposed able to cancel such phenomena and the corresponding resistance.

The evolution over time of the hydraulic resistance R_s due to the largest soluble compounds accumulation onto the membrane surface, including pore blocking, is given by equation 4. Such accumulation is supposed to depend only on the largest soluble compounds concentration in the suspension (σS) and on the permeate flux, until reaching a critical thickness corresponding to a critical mass m_s identified as the specific mass of deposit remaining on the membrane surface when relaxation is operated. When the accumulated deposit m_c becomes greater than the critical m_s value, the parietal shear stresses are supposed to restrain this resistance increase as expressed by the equation 5.

The dynamic of deposit formation is based on the model proposed by Charfi et al. (2014) [24]. The dynamic of particle accumulation on the membrane surface was supposed to be linked to a mass balance between the flux of particle brought onto the membrane by the filtration phenomenon and the intensity of particle detachment due to parietal shear stresses represented by the coefficient β . To improve this first model, the specific cake's mass m_c variation is supposed to be due to simultaneous accumulation of particles also able to retain largest polymer that contribute to the deposit building. The specific cake mass dynamic is then expressed by the equation 7. The resulting cake's resistance is given by equation 6.

The accumulation of large soluble compounds inside the particle deposit induces a porosity decrease of this cake layer [25]. As expressed in equations 8 and 9, the cake porosity ε decrease is supposed to depend on the concentration of rejected soluble polymers ($\sigma.S$) present in the

suspension and the permeate flux J_p . The function $\left(\frac{\varepsilon}{\varepsilon + b}\right)$ appearing in equation 8, can be

understood as a limiting function which prevents obtaining a negative value of ε whatever be the operation time. The Kozeny-Carman relation (eq. 10) is considered to express the cake specific resistance [26]. The porosity decrease leads to the specific cake resistance increase which is expressed by the equation 11.

Taking into account the relations 8 and 10, the constant k_3 is given by the equation 12. The parameter k_3 is then proportional to k_e which means that the effect of the parameter k_3 on the model output would be the same as the parameter k_e . As a consequence, the time evolution of the cake resistance can be only represented by the parameter k_e .

4. Cleaning phases

The relaxation, found effective in removing the cake formed on the membrane surface [21] but not the pore clogging [27]. Based on these two ideas, the equation 13 has been proposed to describe fouling layer mass variation during a relaxation phase. The cake deposit represented by the mass m_c is supposed composed by two superposed layers, (i) the external layer which can be detached by the tangential shear stress, and (ii) the thin layer represented by m_s directly in contact with the membrane surface which is not sensitive to tangential flow, only to backwashing. Then the influence of tangential flow to detach deposit is supposed proportional to the difference ($m_c - m_s$), when this difference is great the detachment is important, when $m_c = m_s$, the detachment by tangential flow is null.

During a phase of relaxation the filtration is stopped and the cake is only depending on the shear stresses (Figure 3). Such forces detach mainly external particles from the deposit and induce a laminar moving of deposit whose intensity is depending on the local position of particles. Then m_c quickly decreases (eq. 13) till it reaches m_s . Fouling intensity, and thus TMP, then decrease. The variation of m_c during the relaxation phase can be written as follows:

$$\frac{dm_c}{dt} = -\beta(m_c - m_s) \quad (eq.13)$$

During this phase, the cake's porosity ε is kept constant, and so is the cake's specific resistance α and the thin layer resistance R_s .

During a phase of backwash (Figure 4), the cake deposit including m_s is supposed largely deconstructed assuming that the external fouling and pore blocking are then totally reversible. Nevertheless the cleaning efficiency of backwash is depending on the own resistance (compactness) of deposit (that can be different for m_s and m_c) and on the backwash intensity. Therefore, in order to take into account the cleaning efficiency of the cake and the polymer layer, the parameters η_1 and η_2 were respectively introduced (eq. 14, eq. 15). The backwash effect on

the cake's porosity is expressed by the parameter η_3 (eq. 16). If a total reversibility can be reached and if internal adsorption remains negligible, the total resistance will then decrease till reaching the membrane intrinsic resistance (R_0). The cake mass, the resistance of the thin polymer deposit and the cake's porosity variation over backwash are expressed in the eq. 14, eq. 15 and eq. 16 respectively.

$$\frac{dm_c}{dt} = -\eta_1 m_c \quad (eq.14)$$

$$\frac{dR_s}{dt} = -\eta_2 R_s \quad (eq.15)$$

$$\frac{d\varepsilon}{dt} = -\eta_3 \varepsilon \quad (eq.16)$$

5. Influence of the model criteria on fouling intensity

Numerical simulations have been carried out to qualify the interest of the proposed model and to highlight the fouling phenomena according to the specific values of the different model parameters.

5.1- Effect of k_2 and ($J_p \cdot \sigma \cdot S$) on cake porosity variation

The cake porosity variation is supposed to be proportional to k_2 and ($J_p \cdot \sigma \cdot S$) (equations 8 and 9) and their respective importance on fouling dynamics can be represented through the only parameter k_e due to their relation of proportionality. The influence of such a parameter is highlighted in figures 6 and 7. The greater k_e value, the quicker the cake's porosity decrease, while the membrane resistance increases inducing a TMP increase.

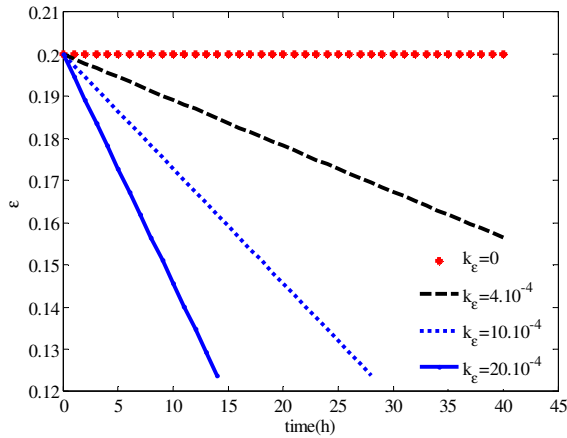


Figure 6: Cake's porosity variation with time according to k_{ϵ}

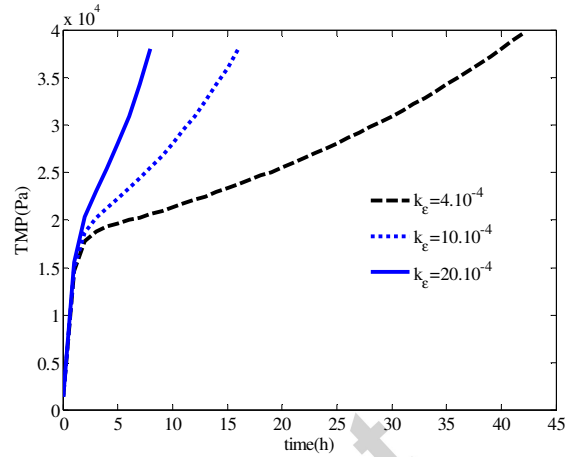


Figure 7: TMP variation with time according to parameter k_{ϵ}

5.2- Effect of k_1 and $(J_p \cdot \sigma \cdot S)$ on R_s resistance

As expressed in the equation 4, the variation with time of R_s is directly proportional to the criterion k_1 and $(J_p \cdot \sigma \cdot S)$. This effect of the variation of one of these criteria is shown in Figures 8 and 9, the higher is the value of the considered criterion (the illustration is given for k_1) the higher are the thin layer resistance and the TMP increase.

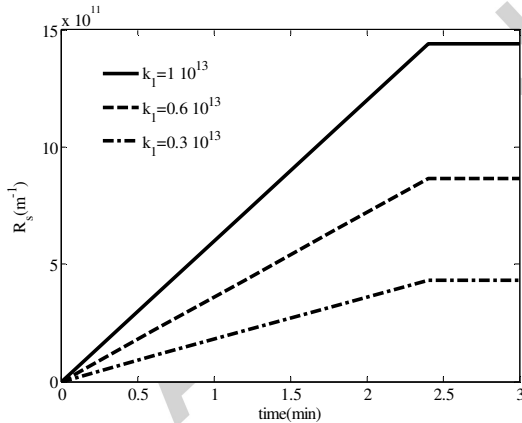


Figure 8: Effect of k_1 parameter on the thin polymer layer resistance evolution

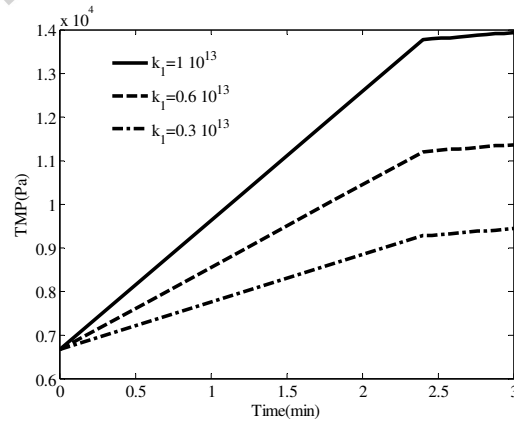


Figure 9: Effect of k_1 parameter on TMP evolution with time

5.3- Specific effect of $(J_p \cdot \sigma \cdot S)$ on simultaneous evolutions of R_s and R_c

The role of both cake resistance and thin layer resistance on total fouling resistance increase during long term experiment are illustrated in Figure 10. It illustrates notably the role of the soluble polymers on the fouling dynamics and the fouling resistance intensity. In fact the more the soluble polymer convective flow is important due to SMP concentration increase, the quicker

the total resistance increases. Figure 11 shows that during short-term experiment the thin layer resistance R_s is dominant compared to the cake resistance R_c . This phenomenon is more significant for high SMP concentration. This dynamic is then determining according to conventional time of filtration cycles when practising periodic relaxation and backwashing.

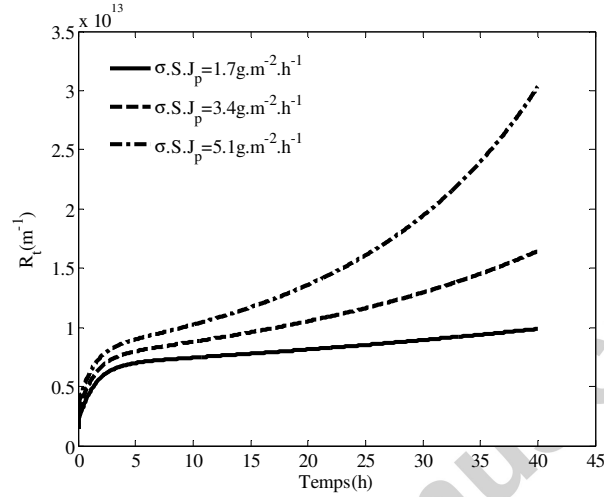


Figure 10: Effect of soluble polymer convective flow on the total fouling resistance for long term

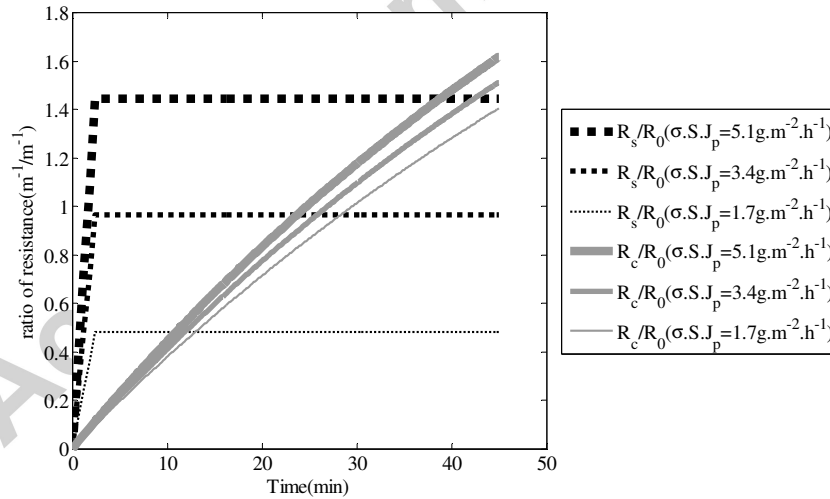


Figure 11: Comparison of the importance of specific hydraulic resistance due to polymer layer and cake deposit for different SMP convective flows in short-term filtration

6- Influence of the model criteria on membrane regeneration

The model was developed to optimise the filtration cycle including periodic hydraulic cleaning such as relaxation and backwash. According to equations 13, 14 and 15, simulations were carried

out to analyse the role of the frequency and the intensity of cleaning on the residual resistance of cake deposit and thin polymer layer.

Figure 12 shows the relaxation efficiency determined for different ratios of relaxation time by filtration time (t_r/t_f), and different shear stress conditions.

According to the model, remember the thin layer deposit R_s is not removed by relaxation. According to the relaxation conditions, R_c can be totally removed or not: More efficient relaxation cleaning is obtained for high shear stress and frequent cleaning (Figure 12). The relaxation efficiency is then determined as the ratio of the removed cake resistance at the end of the relaxation time by the cake resistance at the end of the filtration time.

It is also important to notice that the case considering $t_r/t_f=1$ is not profitable and thus a compromise between the different operational conditions is to be found.

Figure 13 shows some simulations describing the effect of relaxation when operating under different relaxation times and intensities. The considered parameter values for the simulations are reported in Table 1.

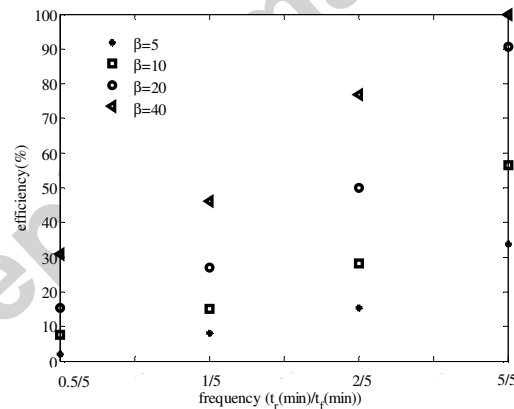


Figure 12: Relaxation efficiency versus its frequency

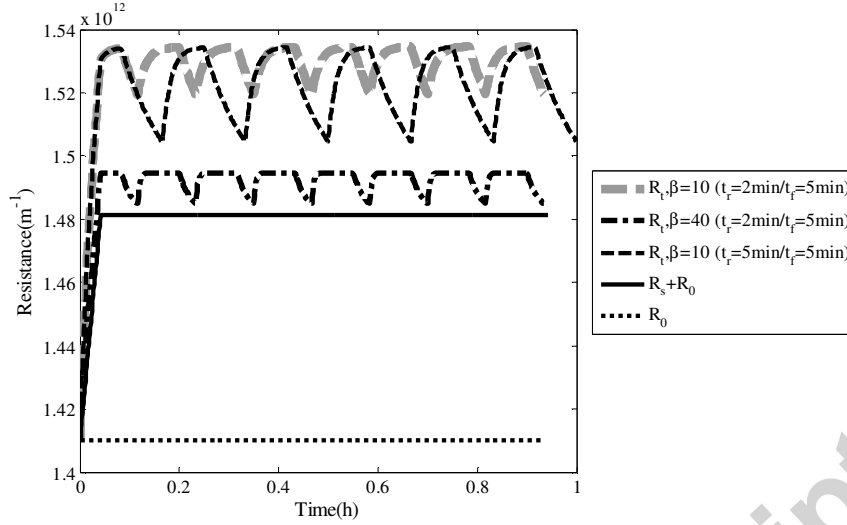


Figure 13: Relaxation effect on membrane fouling (t_r : filtration time, t_r : relaxation time)

Table 1: operational conditions considered to study relaxation effect

ε_0	0.2
d	10^{-5} m
k_1	$0.1 \cdot 10^{13}$
J_p	$17 \text{ L}\cdot\text{m}^{-2}\cdot\text{h}^{-1}$
$\sigma\cdot S$	$0.1 \text{ g}\cdot\text{L}^{-1}$
X	$1 \text{ g}\cdot\text{L}^{-1}$

Figure 13 shows the total resistance evolution for different relaxation conditions. To obtain a complete removal of R_c , Figure 13 points out a possible solution, $\beta=40\text{m}^2\cdot\text{g}^{-1}$ associated with a cleaning frequency of 2min relaxation every 5min of filtration. Of course the optimisation of the relaxation should correspond to the highest water production per day for example.

The backwash is considered as a more efficient cleaning procedure since it allows the thin layer removal and the re-opening of blocked pores. Two parameters controlling the backwash operation are highlighted in Figure 14: the backwash frequency and the cleaning efficiency η_1 which controls the kinetic of the cake's removal. The parameter η_1 is proportional to the backwash flow and the easiness of deposit deconstructing. More efficient cleaning is then obtained for high η_1 and frequent backwash. Under the conditions considered in these simulations

(Table 2), the total recovering of the initial membrane resistance R_0 is obtained for η_1 equal to 300h^{-1} and a backwash frequency of 1min every 30min of filtration.

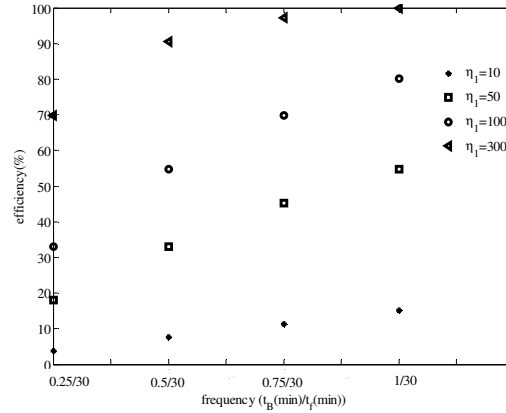


Figure 14: Back-washing efficiency versus its frequency

Table 2: Operational conditions considered to study backwash effect

ε_0	0.2
d	10^{-5} m
k_1	$0.1 \cdot 10^{13}$
β	$5\text{m}^2 \cdot \text{g}^{-1}$
J_p	$17 \text{L} \cdot \text{m}^{-2} \cdot \text{h}^{-1}$
$\sigma \cdot S$	$0.1 \text{g} \cdot \text{L}^{-1}$
X	$1 \text{g} \cdot \text{L}^{-1}$

7- Model validation

To validate the model including the hydraulic cleaning phases, simulations were compared to experimental data obtained when operating with a submerged MBR treating synthetic solution of biodegradable pollutants. The reactor was fed with a synthetic substrate composed with sodium acetate (CH_3COONa) as the exogenous easy biodegradable organic matter resource in MBR influent, Ammonium chloride (NH_4Cl) as nitrogen matter in influent. Other salts such as ammonium phosphate ($(\text{NH}_4)_2\text{HPO}_4$) was also added to insure no nutriment limitation but also pH regulation. This synthetic substrate was diluted in tap water. The concentration of ammonium nitrogen in influent was set at $125 \text{mgN-NH}_4/\text{L}$.

Table 3: The feed solution composition

COD (mg/L)	NH ₄ ⁺ (mg/L)	P (mg/L)
250	125	2.5

The experiments were carried out in a 60 litres lab-scale membrane bioreactor treating biodegradable organic and nitrogen pollutants. The functioning conditions are indicated in Table 4. Even if the feeding solution, the HRT and the SRT are similar for the first six experiments, the MLSS and the SMP concentrations determined show a discard. In fact, to favor rapid increasing of biomass concentration in the reactor, no sludge extraction was practiced during experiment 1, and to analyze the membrane fouling dynamics, aeration intensity was decreased in experiments 4 to 6 and a stratification of MLSS concentration was observed in the bioreactor with a lower concentration in its upper part where the membrane module was set. The values of MLSS and SMP concentrations indicated in Table 4 were then values measuring in the suspension flowing through the membrane module.

Table 4: Biological conditions of MBR functioning

	COD (mg/L)	NH ₄ ⁺ (mg/L)	P (mg/L)	HRT (h)	SRT (days)	MLSS (X) (g/L)	SMP rejected (S) (g/L)
Experiment1	250	125	2.5	10	40	2.1	0.19
Experiment2	250	125	2.5	10	40	1.57	0.16
Experiment3	250	125	2.5	10	40	1.54	0.16
Experiment4	250	125	2.5	10	40	0.67	0.21
Experiment5	250	125	2.5	10	40	1	0.19
Experiment6	250	125	2.5	10	40	0.6	0.10
Experiment7	250	125	2.5	10	60	2.09	0.11

The system was equipped with submerged polymeric flat sheet membranes (Microdyn-Nadir, Germany) developing a filtering surface of 0.34 m² and presenting an effective pore diameter of 0.04 μm. Two measures were adopted to minimize membrane fouling: (i) continuous fine air

bubble injection throughout the membrane module by an air diffuser situated just below the membrane module, (ii) introduction of periodic relaxation and backwash periods during each filtration cycle composed by 8.75min of continuous filtration ($17 \text{ L.m}^{-2}.\text{h}^{-1}$, LMH), 0.25min of relaxation, 0.75min of backwashing ($8.82 \text{ L.m}^{-2}.\text{h}^{-1}$) and 0.25min of relaxation.

COD was measured in permeate and in supernatant obtained after 2 hours of mixed liquor suspension settling. The concentration of large polymer rejected by the membrane barrier is estimated at 93%, of the supernatant COD concentration (S). The concentration of particles (X) was assimilated as the mixed liquor suspended solids concentration MLSS. This concentration is expressed in terms of gCOD/L based on the measured TSS concentration and the fact that the growth of 1g of biomass involves the consumption of 1.42g of O_2 (eq. 17).

$$X (\text{gCOD} / \text{L}) = X (\text{gTSS} / \text{L}) \times 1.42 (\text{gCOD} / \text{gTSS}) \quad (\text{eq.17})$$

The permeate viscosity μ and the cake density ρ_s were assumed to be constant ($\mu=10^{-3} \text{ Pa.s}$, $\rho_s=10^3 \text{ kg.m}^{-3}$) as well as the intrinsic membrane resistance R_0 and the permeate flux J_p ($R_0=1.41 \cdot 10^{12} \text{ m}^{-1}$ and $J_p=17 \text{ L.m}^{-2}.\text{h}^{-1}$). A first validation has been conducted using data of continuous filtration (without membrane cleaning).

Using the least squares method programmed with matlab R2008b, model parameters were optimized in order the simulated data to fit the experimental ones. Three parameters have been optimized using three TMP data series obtained under similar experimental conditions as shown in Table 4. The optimized parameters were the cake's particles mean size (d), the shear parameter (β) and the parameter of the porosity decrease (k_ϵ). Regarding the possible existence of different parameters sets leading to the same fitting quality, we refers to as "parameter identifiability". The theoretical identifiability study is usually difficult to realize. It is why a numerical approach has been rather used which consists in running a large number of optimizations while varying the initial conditions for the parameters to be identified. The application of this procedure in the present case revealed a unique combination of optimized parameters.

For The optimal values of these parameters, reported in Tables 5 and 7, an uncertainty study was conducted to estimate standard deviations. The optimal values have been used to fit the experimental data for the slow TMP increase phase plotted in Figure 15. To evaluate the fitting

operation efficiency, the coefficients of determination R^2 have been calculated and are displayed in Figures 15 and 16. When fitting short term data (Figure 15), R^2 values were superior to 96% for all of the three studied cases. The model describes very well the TMP evolution for this phase mainly controlled by the suspended solids deposition on the membrane surface. However when fitting with all of the experiment data (Figure 16), R^2 values were slightly inferior to those obtained with the initial phase. This discard is probably due to other fouling mechanisms, actually not modelled and which would contribute to the TMP jump such as the membrane's pores clogging, for instance due to the adsorption of soluble compounds inside the membrane's pores.

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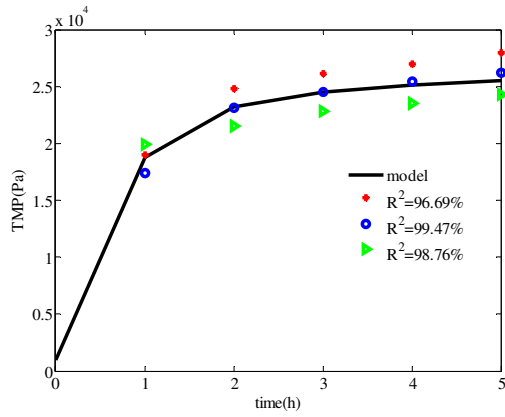


Figure 15: Model fitting with the initial TMP increase data

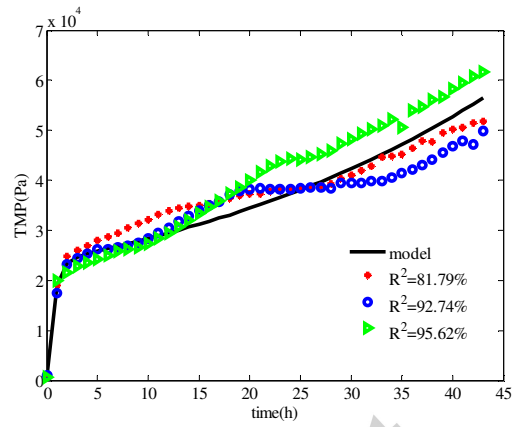


Figure 16: Model fitting with both the first and second fouling phases data

Table 5: Model parameters for continuous filtration (Experiment 1)

Theoretical parameters		Unit
ϵ_0	0.2	-
β	$0.055 \pm 1.99\%$	$\text{m}^2 \cdot \text{g}^{-1}$
k_2	$2.5 \cdot 10^{-4} \pm 4.14\%$	$\text{m}^2 \cdot \text{h} \cdot \text{g}^{-1}$
k_ϵ	$8 \cdot 10^{-4} \pm 4.14\%$	
d	$1.3 \cdot 10^{-5} \pm 1.03\%$	M
experimental conditions		
X	2.98	$\text{gCOD} \cdot \text{L}^{-1}$
$\sigma \cdot S$	0.19	$\text{gCOD} \cdot \text{L}^{-1}$

The model was also adjusted with experimental data obtained under different operational conditions (Figure 17). Even when changing the suspension characteristics the model gives a simulation closed to the experimental TMP evolution (with R^2 superior to 90%).

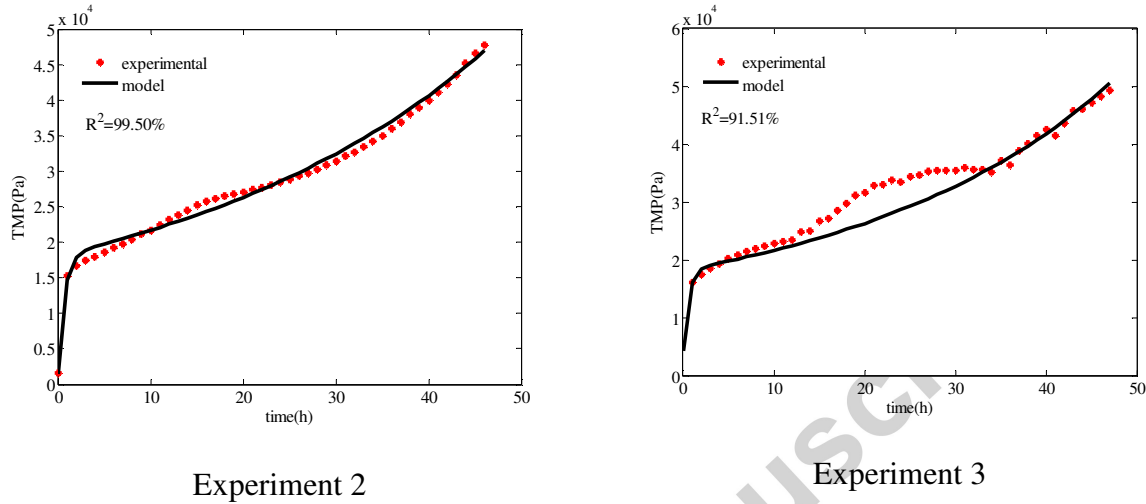


Figure 17: model fitting with data obtained in different experimental conditions

During experiment, a cyclic washing was adopted as indicated. A second validation has then been realized using data collected during filtration cycle.

The model simulations were compared with three series of TMP experimental data, Figures 18-20. These data were obtained under different concentrations of suspended solids and SMP (Table 5). Using the same parameters values for β and d than those obtained in the previous model (continuous filtration data), simulations were realized and are presented in figures 18A, 19A and 20A. The values of other parameters are shown in Table 5. The simulated TMP evolution fitted well the experimental data. For each of the experimental series, the theoretical evolution, during one filtration cycle, of the SMP layer, the cake layer and the total resistances are shown in figures 18B, 19B and 20B.

The experimental data presented in figures 18A and 20A were obtained under similar operating conditions (Table 5), except for soluble polymers concentration (S). The model allows a determination of the specific mass value of the first fouling layer formed mainly by soluble polymers responsible of the 1st fouling phase, 0.1 and 0.07 g/m² respectively, with corresponding resistances of $8.1 \cdot 10^{11}$ and $7.33 \cdot 10^{11} \text{ m}^{-1}$ respectively (Figures 18B and 20B). This confirms that

high SMP concentrations lead to thicker biofilm and then sharper fouling as mentioned by Pan et al. (2010) and Ho and Sung (2009) [28, 18].

When comparing the global evolution of the TMP in the cyclic and in the continuous filtration cases, the TMP increase is found to be 32 times higher in the continuous filtration case.

The figures 18B, 19B and 20B show that the relaxation effect in removing the cake layer is negligible comparing to the backwash which allows, in the studied cases, removing both of the cake layer and the thin SMP layer. Using higher shear stress (higher aeration) would improve the relaxation efficiency.

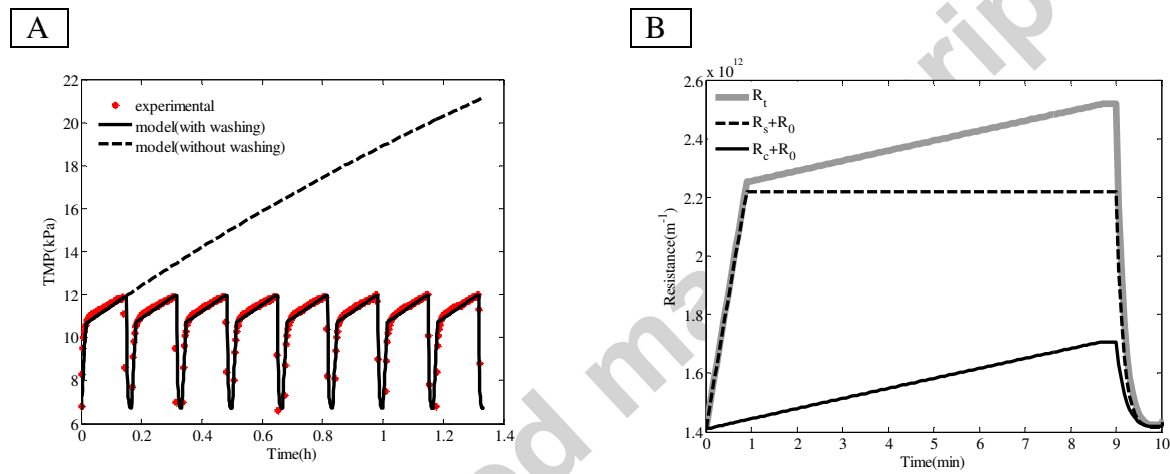


Figure 18: (A) Model fitting the experimental data obtained under low shear stress (Table 5, experiment 4) (B) Different layer resistances for one cycle

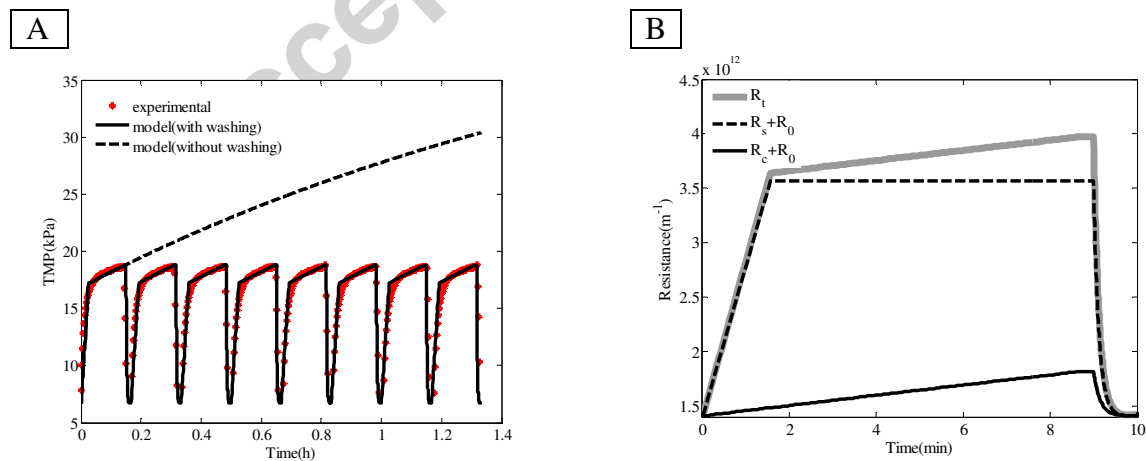


Figure 19: (A) Model fitting the experimental data obtained under low shear stress (Table 5, experiment 5) (B) Different layer resistances for one cycle

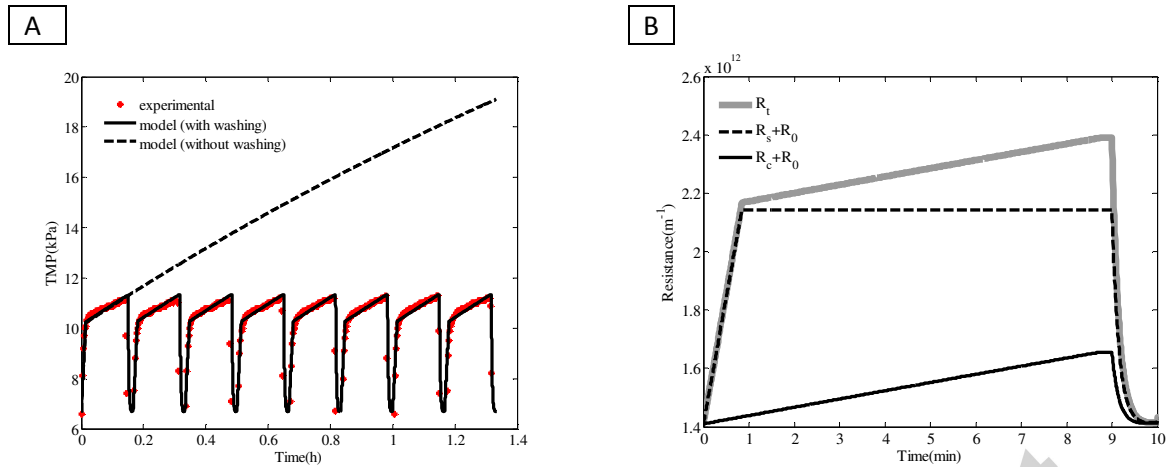


Figure 20: Model fitting the experimental data obtained under low shear stress (Table 5, experiment 6) (B) Different layer resistances for one cycle

Table 6: Model parameters for cyclic filtration under low shear stress (aeration $3\text{m}^3/\text{h}$)

	Experiment 4	Experiment 5	Experiment 6	Unit
Theoretical parameters				
ε_0	0.2	0.2	0.2	-
β	0.055	0.055	0.055	$\text{m}^2 \cdot \text{g}^{-1}$
d	$1.3 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	m
k_1	$1.5 \cdot 10^{13}$	$2.5 \cdot 10^{13}$	$3 \cdot 10^{13}$	
m_s	0.1	0.24	0.07	$\text{g} \cdot \text{m}^{-2}$
k_2	$2.5 \cdot 10^{-4}$	$2.5 \cdot 10^{-4}$	$2.5 \cdot 10^{-4}$	
k_ε	$8.92 \cdot 10^{-4}$	$8 \cdot 10^{-4}$	$4.25 \cdot 10^{-4}$	
η_1	400	400	400	
η_2	400	400	400	
η_3	0.055	0.048	0.025	
Experimental conditions				
X	0.95	1.42	0.85	$\text{gCOD} \cdot \text{L}^{-1}$
$\sigma \cdot S$	0.21	0.19	0.10	$\text{gCOD} \cdot \text{L}^{-1}$

8. Effect of shear stress

Other TMP experimental data have been obtained when increasing the shear stress through increasing aeration to $6\text{m}^3\text{h}^{-1}$. Our model has also been confronted to these data (Figure 21). As it may be seen, it was possible to describe the TMP variation by the cake formation model. The

shear stress increase enhances the soluble polymers dragging which conducts to the 1st fouling phase disappearance corresponding to the first SMP deposit layer.

For these data, the optimized parameters are shown in Table 6. Since the shear stress has been increased, the shear parameter β value increases considerably from 0.055 (low shear stress experiments) to $9.48\text{m}^2.\text{g}^{-1}$ leading to the decrease of particles size from 13 to $2.33\mu\text{m}$. This is clearly in accordance with the fact that the particles breakdown due to the shear forces has been observed in MBR [17, 18].

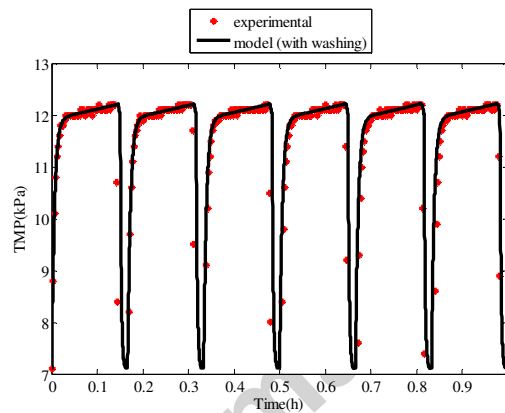


Figure 21: Model fitting the experimental data obtained under high shear stress (aeration $6\text{m}^3/\text{h}$)

Table 7: Model parameters for cyclic filtration under high shear stress (aeration $6\text{m}^3/\text{h}$)

	Experiment 7	Unit
Theoretical parameters		
ε_0	0.2	-
B	$9.48 \pm 0.73\%$	$\text{m}^2.\text{g}^{-1}$
D	$2.33 \cdot 10^{-6} \pm 0.36\%$	m
η_1	400	
η_3	0.012	
experimental conditions		
X	2.96	gCOD.L^{-1}
σ_S	0.11	gCOD.L^{-1}

9. Conclusions

In this paper a new simple model has been presented to describe fouling dynamics when operating in a MBR. The model assumes that membrane fouling goes through three phases. The first phase is characterized by a TMP increase due to film development on the membrane surface, including pore blocking, due to the retention of the largest soluble compounds. The second phase is characterized by an increase of the TMP due to a cake building involving both suspended solids and SMP. Then, the latter stage reflects the progressive decrease of the cake porosity due to the SMP retention inside the cake structure including progressively a sharp TMP jump. Then, two hydraulic ways of membrane permeability regeneration have been defined. Subsequently, model simulations were compared to experimental data obtained in lab-scale MBR pilot and gave satisfactory fitting results. To conclude, the definition of fouling levels and its associated phenomenon are a valuable tool for tuning the right filtration parameters including the determination of relaxation and backwashing cycles.

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Highlights

- A simple tool simulating the fouling dynamics during the filtration and cleaning phases, is proposed
- MBR fouling goes through three phases: film deposit, cake deposit and cake pores decrease
- Simulating the cake porosity decrease let appear the TMP jump
- The model offers a valuable tool for tuning the right filtration parameters