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# A type-logical account of quantification in event semantics

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**Abstract.** It has been argued that Davidson’s event semantics does not combine smoothly with Montague’s compositional semantics. The difficulty, which we call the *event quantification problem*, comes from a possibly bad interaction between event existential closure, on the one hand, and quantification, negation, or conjunction, on the other hand. The recent literature provides two solutions to this problem. The first one is due to Champollion [2, 3], and the second one to Winter and Zwarts [13]. The present paper elaborates on this second solution. In particular, it provides a treatment of quantified adverbial modifiers, which was absent from [13].

## 1 Introduction

It is well known that combining Davidsonian event semantics [5] with Montague’s treatment of quantification [10] may give rise to unexpected semantic interpretations. To understand the potential problem, consider the standard interpretations of proper names and transitive verbs, which allow one to give a semantic interpretation to simple sentences like (2).

- (1) a.  $\llbracket \text{John} \rrbracket = \lambda p. p \mathbf{j} : (\mathbf{e} \rightarrow \mathbf{t}) \rightarrow \mathbf{t}$   
b.  $\llbracket \text{Mary} \rrbracket = \lambda p. p \mathbf{m} : (\mathbf{e} \rightarrow \mathbf{t}) \rightarrow \mathbf{t}$   
c.  $\llbracket \text{kissed} \rrbracket = \lambda p x. p (\lambda y. \mathbf{kissed} \ x \ y) : ((\mathbf{e} \rightarrow \mathbf{t}) \rightarrow \mathbf{t}) \rightarrow \mathbf{e} \rightarrow \mathbf{t}$
- (2) John kissed Mary.

Adapting lexical entry (1-c) to the Davidsonian approach consists in providing the binary relation **kissed** with an additional event argument of type  $\mathbf{v}$ ,<sup>3</sup> which results in lexical entry (3-a). This allows adverbial modifiers to parallel adnominal modifiers (see lexical entry (3-b)). Then, in

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<sup>3</sup> We follow a Davidsonian approach as opposed to a neo-Davidsonian approach. We also distinguish the type of events ( $\mathbf{v}$ ) from the type of entities ( $\mathbf{e}$ ). These choices, which are rather arbitrary, will not affect our purpose.

order to interpret a sentence as a truth value rather than as a set of events, one has to apply an *existential closure* operator (3-c).

- (3) a.  $\llbracket \text{kissed} \rrbracket = \lambda p x e. p (\lambda y. \mathbf{kissed} e x y) :$   
 $((\mathbf{e} \rightarrow \mathbf{t}) \rightarrow \mathbf{t}) \rightarrow \mathbf{e} \rightarrow \mathbf{v} \rightarrow \mathbf{t}$   
 b.  $\llbracket \text{passionately} \rrbracket = \lambda p e. (p e) \wedge (\mathbf{passionate} e) : (\mathbf{v} \rightarrow \mathbf{t}) \rightarrow \mathbf{v} \rightarrow \mathbf{t}$   
 c. E-CLOS =  $\lambda p. \exists e. p e : (\mathbf{v} \rightarrow \mathbf{t}) \rightarrow \mathbf{t}$

Using the above apparatus, we obtain the semantic interpretation of sentence (4) by computing the value of expression (5), which results in formula (6).

- (4) John kissed Mary passionately.  
 (5)  $\llbracket \text{John} \rrbracket (\lambda x. \text{E-CLOS} (\llbracket \text{passionately} \rrbracket (\llbracket \text{kissed} \rrbracket \llbracket \text{Mary} \rrbracket x)))$   
 (6)  $\exists e. (\mathbf{kissed} e \mathbf{j m}) \wedge (\mathbf{passionate} e)$

Consider now sentence (7), which includes a quantified noun phrase.

- (7) John kissed every girl.

The standard interpretation of this quantified noun phrase is based on the following lexical interpretations:

- (8) a.  $\llbracket \text{girl} \rrbracket = \lambda x. \mathbf{girl} x : \mathbf{e} \rightarrow \mathbf{t}$   
 b.  $\llbracket \text{every} \rrbracket = \lambda p q. \forall x. (p x) \rightarrow (q x) : (\mathbf{e} \rightarrow \mathbf{t}) \rightarrow (\mathbf{e} \rightarrow \mathbf{t}) \rightarrow \mathbf{t}$

Then, using expression (9) to compute the semantic interpretation of sentence (7) results in a counterintuitive interpretation (formula (10)).

- (9)  $\llbracket \text{John} \rrbracket (\lambda x. \text{E-CLOS} (\llbracket \text{kissed} \rrbracket (\llbracket \text{every} \rrbracket \llbracket \text{girl} \rrbracket x)))$   
 (10)  $\exists e. \forall x. (\mathbf{girl} x) \rightarrow (\mathbf{kissed} e \mathbf{j} x)$

According to formula (10), there should be a single kissing event involving John and every girl. This requirement appears because the existential closure operator takes wide scope over the universally quantified noun phrase. The problem with this analysis becomes more apparent when we consider the interaction of events with quantifiers that are not upward-monotone, as in the following sentences.

- (11) a. John kissed no girl.  
 b. John kissed less than five girls.  
 c. John kissed exactly one girl.

Consider the standard lexical interpretation of the *no* quantifier, together with a semantic analysis akin to expression (9).

- (12) a.  $\llbracket \text{no} \rrbracket = \lambda pq. \forall x. (px) \rightarrow \neg(qx) : (e \rightarrow t) \rightarrow (e \rightarrow t) \rightarrow t$   
 b.  $\llbracket \text{John} \rrbracket (\lambda x. \text{E-CLOS} (\llbracket \text{kissed} \rrbracket (\llbracket \text{no} \rrbracket \llbracket \text{girl} \rrbracket) x))$

This leads to the following problematic interpretation:

- (13)  $\exists e. \forall x. (\text{girl } x) \rightarrow \neg(\text{kissed } e \text{ } \mathbf{j} \text{ } x)$

According to formula (13), sentence (11-a) would be true if John kissed a girl, but there is another event where John did not kiss any girl. Indeed, since in the latter event John kissed no girl, the sentence might be incorrectly analyzed as true in this situation. The same kind of problem can also be shown with sentences (11-b) and (11-c).

A similar problem may arise with negation.

- (14) a. John did not kiss Mary.  
 b.  $\llbracket \text{not} \rrbracket = \lambda px. \neg(px) : (e \rightarrow t) \rightarrow e \rightarrow t$   
 c.  $\llbracket \text{John} \rrbracket (\llbracket \text{not} \rrbracket (\lambda x. \text{E-CLOS} (\llbracket \text{kissed} \rrbracket \llbracket \text{Mary} \rrbracket) x)))$   
 d.  $\neg(\exists e. \text{kissed } e \text{ } \mathbf{j} \text{ } \mathbf{m})$   
 e.  $\text{E-CLOS} (\lambda e. \llbracket \text{John} \rrbracket (\llbracket \text{not} \rrbracket (\lambda x. \llbracket \text{kissed} \rrbracket \llbracket \text{Mary} \rrbracket) x e)))$   
 f.  $\exists e. \neg(\text{kissed } e \text{ } \mathbf{j} \text{ } \mathbf{m})$

Using a standard interpretation of negation (lexical entry (14-b)), expression (14-c) leads to a correct semantic interpretation of sentence (14-a), namely, formula (14-d). There is, however, another possible analysis of sentence (14-a), which is expressed by expression (14-e). This leads to formula (14-f), where the existential quantifier over events takes scope over negation. According to this fallacious interpretation, sentence (14-a) might be true in a situation where John kissed Mary, provided there is another event where he did not kiss Mary.

Besides quantification and negation, conjunction is also known to interact badly with event existential closure. Consider the following sentence, whose interpretation is meant to be distributive:

- (15) John kissed Mary and [then] Sue.

The standard interpretation of distributive coordination is given by the following lexical entry:

- (16)  $\llbracket \text{and} \rrbracket = \lambda pqr. (pr) \wedge (qr) : ((e \rightarrow t) \rightarrow t) \rightarrow ((e \rightarrow t) \rightarrow t) \rightarrow (e \rightarrow t) \rightarrow t$

Nevertheless, the semantic analysis given by expression (17-a) yields an interpretation (formula (17-b)) akin to a collective reading. According to this problematic interpretation, Mary and Sue would be the patients of the same kissing event.

- (17) a.  $\llbracket \text{John} \rrbracket (\lambda x. \text{E-CLOS} (\llbracket \text{kissed} \rrbracket (\llbracket \text{and} \rrbracket \llbracket \text{Mary} \rrbracket \llbracket \text{Sue} \rrbracket) x))$   
 b.  $\exists e. (\mathbf{kissed} e \mathbf{j m}) \wedge (\mathbf{kissed} e \mathbf{j s})$

To obtain the right interpretations of sentences like (7), (11-a)-(11-c), (14-a), and (15), the event existential closure operator need to take narrow scope. For sentence (7), this is illustrated by expression (18), which is interpreted as in formula (19).

- (18)  $\llbracket \text{John} \rrbracket (\lambda x. \llbracket \text{every} \rrbracket \llbracket \text{girl} \rrbracket (\lambda y. \text{E-CLOS} (\llbracket \text{kissed} \rrbracket (\lambda p. p y) x)))$

- (19)  $\forall x. (\mathbf{girl} x) \rightarrow (\exists e. \mathbf{kissed} e \mathbf{j x})$

In many works, expressions such as (18) result from some covert movement operation. This explains why most approaches that combine event semantics and quantification either rely on syntactic devices that control the scope of the quantifiers [9], or depart significantly from standard assumptions in compositional semantics [1, 8]. Following Champollion [2, 3] and Winter and Zwarts [13], we see this enrichment of standard systems as problematic. Accordingly, we refer to the problem of combining standard compositional semantics and event semantics as the *event quantification problem*.

## 2 Two solutions to the event quantification problem

The recent literature provides two solutions to the event quantification problem. The first one is due to Champollion [2, 3]. It consists in interpreting sentences as generalized quantifiers over events  $((v \rightarrow t) \rightarrow t)$  rather than as sets of events  $(v \rightarrow t)$ . This allows the existential closure to occur at the lexical level. Accordingly, the lexical entries in (3) are adapted as follows.

- (20) a.  $\llbracket \text{kissed} \rrbracket = \lambda p x f. p (\lambda y. \exists e. (\mathbf{kissed} e x y) \wedge (f e)) :$   
 $((e \rightarrow t) \rightarrow t) \rightarrow e \rightarrow (v \rightarrow t) \rightarrow t$   
 b.  $\llbracket \text{passionately} \rrbracket = \lambda p f. p (\lambda e. (f e) \wedge (\mathbf{passionate} e)) :$   
 $((v \rightarrow t) \rightarrow t) \rightarrow (v \rightarrow t) \rightarrow t$   
 c.  $\text{CLOS} = \lambda p. p (\lambda e. \mathbf{true}) : ((v \rightarrow t) \rightarrow t) \rightarrow t$

The semantic interpretation of sentence (7) is then obtained by computing the value of expression (21). This expression is akin to expression (9). Nevertheless, this time, the computation yields the correct interpretation (formula (19)).

$$(21) \quad \llbracket \text{John} \rrbracket (\lambda x. \text{CLOS} (\llbracket \text{kissed} \rrbracket (\llbracket \text{every} \rrbracket \llbracket \text{girl} \rrbracket) x))$$

The second solution, which is due to Winter and Zwarts [13], is expressed in the framework of Abstract Categorical Grammar [7]. It takes advantage of the so-called *tectogrammatic level* [4] for the treatment of scope interactions. Following the type-logical tradition, Winter and Zwarts distinguish, at the abstract syntactic level, the category of noun phrases,  $NP$ , from the category of quantified noun phrases,  $(NP \rightarrow S) \rightarrow S$ . They also distinguish the category  $S$  of sentences interpreted as truth values ( $\mathbf{t}$ ) from the category  $V$  of sentences interpreted as sets of events ( $\mathbf{v} \rightarrow \mathbf{t}$ ).<sup>4</sup> This results in abstract syntactic structures specified by a signature akin to the following one.

$$(22) \quad \begin{array}{l} \text{a. } \text{JOHN} : NP \\ \text{b. } \text{GIRL} : N \\ \text{c. } \text{KISSED} : NP \rightarrow NP \rightarrow V \\ \text{d. } \text{EVERY} : N \rightarrow (NP \rightarrow S) \rightarrow S \\ \text{e. } \text{PASSIONATELY} : V \rightarrow V \\ \text{f. } \text{E-CLOS} : V \rightarrow S \end{array}$$

This signature comes with a lexicon that specifies the surface realization of the abstract syntactic structures:

$$(23) \quad \begin{array}{l} \text{a. } \text{JOHN} := \mathbf{John} \\ \text{b. } \text{GIRL} := \mathbf{girl} \\ \text{c. } \text{KISSED} := \lambda xy. y + \mathbf{kissed} + x \\ \text{d. } \text{EVERY} := \lambda x f. f (\mathbf{every} + x) \\ \text{e. } \text{PASSIONATELY} := \lambda x. x + \mathbf{passionately} \\ \text{f. } \text{E-CLOS} := \lambda x. x \end{array}$$

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<sup>4</sup> Following Montague's homomorphism requirement, these two abstract categories should indeed be distinguished since they correspond to different semantic types. The fact that they share the same surface realizations may be considered as a mere contingency. Alternatively, we may relax the homomorphism requirement, e.g. as in [12], who treats indefinite NPs as ambiguous between predicates and quantifiers.

In this setting, the only abstract structure corresponding to sentence (7) is the following well-typed expression (whose derivation and surface realization are given in Appendix A).

$$(24) \quad \text{EVERY GIRL } (\lambda x. \text{E-CLOS } (\text{KISSED } x \text{ JOHN}))$$

Then, using the semantic interpretation given here below, the evaluation of expression (24) yields the expected result, i.e., formula (19).

$$(25) \quad \begin{array}{l} \text{a. } \text{JOHN} := \mathbf{j} : \mathbf{e} \\ \text{b. } \text{GIRL} := \lambda x. \mathbf{girl} \ x : \mathbf{e} \rightarrow \mathbf{t} \\ \text{c. } \text{KISSED} := \lambda x y e. \mathbf{kissed} \ e \ x \ y : \mathbf{e} \rightarrow \mathbf{e} \rightarrow \mathbf{v} \rightarrow \mathbf{t} \\ \text{d. } \text{EVERY} := \lambda p q. \forall x. (p \ x) \rightarrow (q \ x) : (\mathbf{e} \rightarrow \mathbf{t}) \rightarrow (\mathbf{e} \rightarrow \mathbf{t}) \rightarrow \mathbf{t} \\ \text{e. } \text{PASSIONATELY} := \lambda p e. (p \ e) \wedge (\mathbf{passionate} \ e) : \\ \hspace{20em} (\mathbf{v} \rightarrow \mathbf{t}) \rightarrow (\mathbf{v} \rightarrow \mathbf{t}) \\ \text{f. } \text{E-CLOS} := \lambda p. \exists e. p \ e : (\mathbf{v} \rightarrow \mathbf{t}) \rightarrow \mathbf{t} \end{array}$$

Signature (22) compels the existential closure operator (E-CLOS) to take scope below the quantified noun phrase (EVERY GIRL). This is because the abstract syntactic category assigned to EVERY ( $N \rightarrow (NP \rightarrow S) \rightarrow S$ ) is given in standard terms of the abstract category  $S$  (interpreted as truth-values) rather than  $V$  (interpreted as sets of events). Consequently, each of the derived sets of events (i.e., each expression of type  $V$ ) must first be “closed” (i.e., turned into an expression of type  $S$ ) before quantification can apply.

This solution is easily transferable to the cases of negation and conjunction. It suffices to express their abstract categories in term of  $S$ .<sup>5</sup>

$$(26) \quad \begin{array}{l} \text{a. } \text{NOT} : (NP \rightarrow S_{\circ}) \rightarrow (NP \rightarrow S) \\ \text{b. } \text{AND} : NP \rightarrow NP \rightarrow (NP \rightarrow S) \rightarrow S \end{array}$$

Thus, boolean negation and conjunction are still treated by using the boolean  $S$ -based types, rather than the Davidsonian  $V$ -based types.

Unlike Champollion, Winter and Zwarts do not consider the case of quantified adverbial modifiers such as *everyday* or *everywhere*. The present paper aims to fill this gap.

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<sup>5</sup> The reason for distinguishing between type  $S$  and type  $S_{\circ}$ , which is merely syntactic, is explained in Appendix B.

### 3 Quantified adverbial modifiers

Consider sentence (27) together with a plausible semantic interpretation (formula (28)).

(27) John kissed Mary everyday.

(28)  $\forall x. \underline{(\mathbf{day} x)} \rightarrow (\exists e. (\mathbf{kissed} e \mathbf{j m}) \wedge \underline{(\mathbf{time} e x)})$

In formula (28), the underlined subformulas are derived from the semantic interpretation of *everyday*. In a compositional setting, this makes it necessary that the lexical semantics of *everyday* acts both inside and outside of the scope of the existential closure.

The solution to this puzzle is in accordance with the type-logical tradition. It consists in distinguishing the category of adverbial modifiers from the category of quantified adverbial modifiers. Similarly to the treatment of noun phrases, the category of quantified adverbial modifiers is obtained from the category of non-quantified adverbial modifiers by type-shifting. This results in the following type assignment.

(29)  $\text{EVERYDAY} : ((V \rightarrow V) \rightarrow S) \rightarrow S$

Then, the abstract structure corresponding to sentence (27) may be expressed as follows.

(30)  $\text{EVERYDAY} (\lambda q. \text{E-CLOS} (q (\text{KISSED MARY JOHN})))$

Finally, using lexical entry (31), one may compute compositionally the interpretation of sentence (27).

(31)  $\text{EVERYDAY} := \lambda q. \forall x. (\mathbf{day} x) \rightarrow (q (\lambda p e. (p e) \wedge (\mathbf{time} e x))) : ((\mathbf{v} \rightarrow \mathbf{t}) \rightarrow (\mathbf{v} \rightarrow \mathbf{t})) \rightarrow \mathbf{t} \rightarrow \mathbf{t}$

It is to be noted that our approach is consistent with the treatment of quantified adverbial prepositional phrases such as *in every room*. Consider the category and the semantic interpretation assigned to the preposition *in*.

(32) a.  $\text{IN} : NP \rightarrow V \rightarrow V$   
 b.  $\text{IN} := \lambda x p e. (p e) \wedge (\mathbf{location} e x)$

We may then derive an abstract structure of the appropriate type, corresponding to the prepositional phrase *in every room*.

(33)  $\lambda q. \text{EVERY ROOM} (\lambda x. q (\text{IN } x)) : ((V \rightarrow V) \rightarrow S) \rightarrow S$



We give a toy-grammar that summarizes our approach in appendix B. This grammar allows one to handle examples such as sentence (34).

(34) John did not kiss Mary for one hour.

Sentences such as (34) are known to exhibit a scope ambiguity that yields two different semantic interpretations. In the present case, these two interpretations may be paraphrased as follows.

- (35) a. For one hour, it was not the case that John kissed Mary.  
 b. It was not the case that John kissed Mary for one hour.

Using our toy-grammar, these two interpretations may be obtained by computing the semantic interpretations of the two following abstract structures whose surface realization is sentence (34).

- (36) a.  $\text{FOR}_o (\text{ONE HOUR})$   
            $(\lambda q. \text{NOT} (\lambda x. \text{E-CLOS}_o (q (\text{KISSED}_o \text{MARY } x))) \text{JOHN})$   
 b.  $\text{NOT} (\lambda x. \text{FOR}_{oo} (\text{ONE HOUR})$   
            $(\lambda q. \text{E-CLOS}_o (q (\text{KISSED}_o \text{MARY } x))))$   
           JOHN

The abstract constants marked with small circles ( $\text{FOR}_o$ ,  $\text{E-CLOS}_o$ ,  $\text{KISSED}_o$ , etc.) involve a syntactic treatment of negation, which avoids ill-formed strings like \**John did not kissed Mary*. For more details see Appendix B.

We conclude that the ambiguity of sentence (34), which is treated in Champollion’s system as an ordinary case of scope ambiguity, is similarly treated here, by following an adaptation of the system proposed by Winter and Zwarts.

A final remark has to do with sentences like the following.

(37) John did not kiss Mary deliberately.

This sentence presents an ambiguity similar to the one of sentence (34):

- (38) a. It was deliberate that John did not kiss Mary.  
 b. It was not deliberate that John kissed Mary.

Nevertheless, sentences like (37) cannot be treated like sentence (34) because the adverb is not quantificational. Following Davidson, we assume that adverbs like *deliberately*, unlike standard manner adverbs, have a modal element to their meaning, and accordingly modify full propositions rather than events. Like Champollion, we believe that the treatment of

modal adverbs and other modal operators is orthogonal to the main tenets of event semantics.

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## Appendix A

Derivation of expression (24):

$$\frac{\vdash \text{EVERY} : N \rightarrow (NP \rightarrow S) \rightarrow S \quad \vdash \text{GIRL} : N}{\vdash \text{EVERY GIRL} : (NP \rightarrow S) \rightarrow S} \quad (1)$$

$$\frac{\frac{\vdash \text{KISSED} : NP \rightarrow NP \rightarrow V \quad x : NP \vdash x : NP}{x : NP \vdash \text{KISSED } x : NP \rightarrow V} \quad \vdash \text{JOHN} : NP}{x : NP \vdash \text{KISSED } x \text{ JOHN} : V} \quad (2)$$

$$\frac{\frac{\vdash \text{E-CLOS} : V \rightarrow S \quad x : NP \vdash \text{KISSED } x \text{ JOHN} : V}{x : NP \vdash \text{E-CLOS} (\text{KISSED } x \text{ JOHN}) : S} \quad \vdots (2)}{\vdash \lambda x. \text{E-CLOS} (\text{KISSED } x \text{ JOHN}) : NP \rightarrow S} \quad (3)$$

$$\frac{\frac{\vdash \text{EVERY GIRL} : (NP \rightarrow S) \rightarrow S \quad \vdash \lambda x. \text{E-CLOS} (\text{KISSED } x \text{ JOHN}) : NP \rightarrow S}{\vdash \text{EVERY GIRL} (\lambda x. \text{E-CLOS} (\text{KISSED } x \text{ JOHN})) : S} \quad \vdots (1) \quad \vdots (3)}$$

Surface realization of expression (24):

$$\begin{aligned} & \text{EVERY GIRL } (\lambda x. \text{E-CLOS} (\text{KISSED } x \text{ JOHN})) \\ &= (\lambda x f. f (\mathbf{every} + x)) \text{ GIRL } (\lambda x. \text{E-CLOS} (\text{KISSED } x \text{ JOHN})) \\ &= (\lambda f. f (\mathbf{every} + \text{GIRL})) (\lambda x. \text{E-CLOS} (\text{KISSED } x \text{ JOHN})) \\ &= (\lambda x. \text{E-CLOS} (\text{KISSED } x \text{ JOHN})) (\mathbf{every} + \text{GIRL}) \\ &= \text{E-CLOS} (\text{KISSED} (\mathbf{every} + \text{GIRL}) \text{ JOHN}) \\ &= (\lambda x. x) (\text{KISSED} (\mathbf{every} + \text{GIRL}) \text{ JOHN}) \\ &= \text{KISSED} (\mathbf{every} + \text{GIRL}) \text{ JOHN} \\ &= (\lambda xy. y + \mathbf{kiss} + x) (\mathbf{every} + \text{GIRL}) \text{ JOHN} \\ &= (\lambda y. y + \mathbf{kiss} + \mathbf{every} + \text{GIRL}) \text{ JOHN} \\ &= \text{JOHN} + \mathbf{kiss} + \mathbf{every} + \text{GIRL} \\ &= \mathbf{john} + \mathbf{kiss} + \mathbf{every} + \text{GIRL} \\ &= \mathbf{john} + \mathbf{kiss} + \mathbf{every} + \mathbf{girl} \end{aligned}$$

## Appendix B

This appendix presents a toy grammar that covers the several examples that are under discussion in the course of the paper. It mainly consists of three parts:

- a set of abstract syntactic structures, specified by means of a higher-order signature;
- a surface realization of the abstract structures, specified by means of a homomorphic translation of the signature;
- a semantic interpretation of the abstract structures, specified by means of another homomorphic translation;

### B.1 Abstract Syntax

The signature specifying the abstract syntactic structures is given in Table 1. It uses a type system built upon the following set of atomic syntactic categories:

- $N$ , the category of *nouns*;
- $N_u$ , the category of *nouns that name units of measurement*;
- $NP$ , the category of *noun phrases*;
- $NP_\tau$ , the category of *noun phrases that denote time intervals*;
- $S$  and  $S_o$ , the category of *sentences* (positive and negative);
- $V$  and  $V_o$ , the category of *“open” sentences* (positive and negative).

The reason for distinguishing between the categories of positive and negative (open) sentences is merely syntactic. Without such a distinction, the surface realization of a negative expression such as:

NOT (KISSED MARY) JOHN

would be:

\*John did not kissed Mary

Without this distinction, it would also be possible to iterate negation. This would allow the following ungrammatical sentences to be generated:

\*John did not did not kiss Mary  
\*John did not did not did not kiss Mary  
⋮

<i>Abstract Syntax</i>	
JOHN	$: NP$
MARY	$: NP$
SUE	$: NP$
THE-KITCHEN	$: NP$
ROOM	$: N$
GIRL	$: N$
HOUR	$: N_u$
KISSED	$: NP \rightarrow NP \rightarrow V$
KISSED <sub>o</sub>	$: NP \rightarrow NP \rightarrow V_o$
NOT	$: (NP \rightarrow S_o) \rightarrow (NP \rightarrow S)$
ONE	$: N_u \rightarrow NP_\tau$
A	$: N \rightarrow (NP \rightarrow S) \rightarrow S$
A <sub>o</sub>	$: N \rightarrow (NP \rightarrow S_o) \rightarrow S_o$
EVERY	$: N \rightarrow (NP \rightarrow S) \rightarrow S$
EVERY <sub>o</sub>	$: N \rightarrow (NP \rightarrow S_o) \rightarrow S_o$
NO	$: N \rightarrow (NP \rightarrow S) \rightarrow S$
NO <sub>o</sub>	$: N \rightarrow (NP \rightarrow S_o) \rightarrow S_o$
AND	$: NP \rightarrow NP \rightarrow (NP \rightarrow S) \rightarrow S$
AND <sub>o</sub>	$: NP \rightarrow NP \rightarrow (NP \rightarrow S_o) \rightarrow S_o$
PASSIONATELY	$: V \rightarrow V$
PASSIONATELY <sub>o</sub>	$: V_o \rightarrow V_o$
EVERYDAY	$: ((V \rightarrow V) \rightarrow S) \rightarrow S$
EVERYDAY <sub>o</sub>	$: ((V_o \rightarrow V_o) \rightarrow S) \rightarrow S$
IN	$: NP \rightarrow V \rightarrow V$
IN <sub>o</sub>	$: NP \rightarrow V_o \rightarrow V_o$
FOR	$: NP_\tau \rightarrow ((V \rightarrow V) \rightarrow S) \rightarrow S$
FOR <sub>o</sub>	$: NP_\tau \rightarrow ((V_o \rightarrow V_o) \rightarrow S) \rightarrow S$
FOR <sub>oo</sub>	$: NP_\tau \rightarrow ((V_o \rightarrow V_o) \rightarrow S_o) \rightarrow S_o$
E-CLOS	$: V \rightarrow S$
E-CLOS <sub>o</sub>	$: V_o \rightarrow S_o$

Table 1

## B.2 Surface Realization

The surface realization of the abstract syntactic structures is given in table 2. This realization is such that every abstract term of an atomic

type is interpreted as a string. Accordingly, abstract terms of a functional type are interpreted as functions acting on strings.

<i>Surface Realization</i>	
JOHN	:= <b><i>John</i></b>
MARY	:= <b><i>Mary</i></b>
SUE	:= <b><i>Sue</i></b>
THE-KITCHEN	:= <b><i>the + kitchen</i></b>
ROOM	:= <b><i>room</i></b>
GIRL	:= <b><i>girl</i></b>
HOUR	:= <b><i>hour</i></b>
KISSED	:= $\lambda xy. y + \mathbf{kissed} + x$
KISSED <sub>o</sub>	:= $\lambda xy. y + \mathbf{kiss} + x$
NOT	:= $\lambda fx. x + \mathbf{did} + \mathbf{not} + (f \epsilon)$
ONE	:= $\lambda x. \mathbf{one} + x$
A, A <sub>o</sub>	:= $\lambda xf. f(\mathbf{a} + x)$
EVERY, EVERY <sub>o</sub>	:= $\lambda xf. f(\mathbf{every} + x)$
NO, NO <sub>o</sub>	:= $\lambda xf. f(\mathbf{no} + x)$
AND, AND <sub>o</sub>	:= $\lambda xyf. f(x + \mathbf{and} + y)$
PASSIONATELY, PASSIONATELY <sub>o</sub>	:= $\lambda x. x + \mathbf{passionately}$
EVERYDAY, EVERYDAY <sub>o</sub>	:= $\lambda f. f(\lambda x. x + \mathbf{everyday})$
IN, IN <sub>o</sub>	:= $\lambda xy. y + \mathbf{in} + x$
FOR, FOR <sub>o</sub> , FOR <sub>oo</sub>	:= $\lambda xf. f(\lambda x. y + \mathbf{for} + x)$
E-CLOS, E-CLOS <sub>o</sub>	:= $\lambda x. x$

Table 2

## B.2 Semantic interpretation

The semantic interpretation of the abstract syntactic categories is given in Table 3. Besides the usual semantic types  $e$  and  $t$ , we also use  $v$ ,  $i$ , and  $n$ . These stand for the semantic types of events, time intervals, and scalar quantities, respectively.

The semantic interpretation of the abstract constants is then given in Table 5. This interpretation makes use of the non-logical constants given in Table 4.

<i>Semantic Types</i>
$N := e \rightarrow t$
$N_u := i \rightarrow n \rightarrow t$
$NP := e$
$NP_\tau := i \rightarrow t$
$V := v \rightarrow t$
$V_o := v \rightarrow t$
$S := t$
$S_o := t$

Table 3

<i>Non-Logical Constants</i>
$\mathbf{j, m, s, k} : e$
$\mathbf{room, girl, day} : e \rightarrow t$
$\mathbf{hour} : i \rightarrow n \rightarrow t$
$\mathbf{kissed} : v \rightarrow e \rightarrow e \rightarrow t$
$\mathbf{1} : n$
$\mathbf{passionate} : v \rightarrow t$
$\mathbf{time, location} : v \rightarrow e \rightarrow t$
$\mathbf{duration} : v \rightarrow i \rightarrow t$

Table 4

<i>Semantic Interpretation</i>
$\mathbf{JOHN} := \mathbf{j}$
$\mathbf{MARY} := \mathbf{m}$
$\mathbf{SUE} := \mathbf{s}$
$\mathbf{THE-KITCHEN} := \mathbf{k}$
$\mathbf{ROOM} := \lambda x. \mathbf{room} x$
$\mathbf{GIRL} := \lambda x. \mathbf{girl} x$
$\mathbf{HOUR} := \lambda xy. \mathbf{hour} x y$
$\mathbf{KISSED, KISSED}_o := \lambda xye. \mathbf{kissed} e x y$
$\mathbf{NOT} := \lambda px. \neg(p x)$
$\mathbf{ONE} := \lambda pt. p t \mathbf{1}$
$\mathbf{A, A}_o := \lambda pq. \exists x. (p x) \wedge (q x)$
$\mathbf{EVERY, EVERY}_o := \lambda pq. \forall x. (p x) \rightarrow (q x)$
$\mathbf{NO, NO}_o := \lambda pq. \forall x. (p x) \rightarrow \neg(q x)$
$\mathbf{AND, AND}_o := \lambda xyp. (p x) \wedge (p y)$
$\mathbf{PASSIONATELY,}$
$\mathbf{PASSIONATELY}_o := \lambda pe. (p e) \wedge (\mathbf{passionate} e)$
$\mathbf{EVERYDAY,}$
$\mathbf{EVERYDAY}_o := \lambda q. \forall x. (\mathbf{day} x) \rightarrow (q (\lambda pe. (p e) \wedge (\mathbf{time} e x)))$
$\mathbf{IN, IN}_o := \lambda xpe. (p e) \wedge (\mathbf{location} e x)$
$\mathbf{FOR, FOR}_o, \mathbf{FOR}_{oo} := \lambda pq. \exists t. (p t) \wedge (q (\lambda pe. (p e) \wedge (\mathbf{duration} e t)))$
$\mathbf{E-CLOS, E-CLOS}_o := \lambda p. \exists e. p e$

Table 5