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Modeling spontaneous metastasis following surgery: an *in vivo-in silico* approach

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Abstract

Rapid improvements in the detection and tracking of early-stage tumor progression aim to guide decisions regarding cancer treatments as well as predict metastatic recurrence in patients following surgery. Mathematical models may have the potential to further assist in estimating metastatic risk, particularly when paired with in vivo tumor data that faithfully represent all stages of disease progression. Herein we describe mathematical analysis that uses data from mouse models of spontaneous metastasis developing after surgical removal of orthotopically implanted primary tumors. Both presurgical (primary tumor) and postsurgical (metastatic) growth was quantified using bioluminescence and was then used to generate a mathematical formalism based on general laws of the disease (i.e. dissemination and growth). The model was able to fit and predict pre-/post-surgical data at the level of the individual as well as the population. Our approach also enabled retrospective analysis of clinical data describing the probability of metastatic relapse as a function of primary tumor size. In these data-based models, inter-individual variability was quantified by a key parameter of intrinsic metastatic potential. Critically, our analysis identified a highly nonlinear relationship between primary tumor size and postsurgical survival, suggesting possible threshold limits for the utility of tumor size as a predictor of metastatic recurrence. These findings represent a novel use of clinically relevant models to assess the impact of surgery on metastatic potential and may guide optimal timing of treatments in neoadjuvant (presurgical) and adjuvant (postsurgical) settings to maximize patient benefit.

Précis: A data-based mathematical model that assesses the impact of surgery on metastatic development may have clinical uses to individualize adjuvant therapies that can extend cancer remission.

Introduction

1 Surgical removal of an early-stage localized tumor remains one of the most
2 effective strategies in reducing the probability of systemic metastatic disease spread
3 (1). Improved technologies of early cancer detection aim to classify primary tumor
4 stage to identify whether potential treatment modalities – such as presurgical
5 ‘neoadjuvant’ or postsurgical ‘adjuvant’ – should be considered to complement
6 surgery and reduce metastatic potential. However the relationship between primary
7 tumor growth and eventual metastasis remains enigmatic (2). Metastatic seeding was
8 initially thought to occur only during late stages of primary tumor growth and invasion
9 (3), however, recent evidence suggests systemic dissemination is a much earlier
10 event (4). Indeed even the direction of tumor spread, initially thought to occur uni-
11 directionally from primary to secondary sites, has been replaced by more complex
12 and dynamic theories of interaction. These include models where primary and
13 secondary lesions grow (and evolve) in parallel (2) and the possibility that cell seeding
14 can be bi-directional, with metastasis potentially ‘re-seeding’ back to original primary
15 location (5,6).

16 To assist in understanding this complexity, mathematical modeling has been used
17 to determine the relationship between primary (localized) and secondary (metastatic)
18 tumor dissemination and growth. Early studies used statistical analyses only (7,8),
19 while later work included experimentally-derived data to validate models using
20 biological information that aimed to more faithfully represent the metastatic process
21 (9). In 2000, Iwata and colleagues used imaging data from one patient with metastatic
22 hepatocellular carcinoma to introduce a more formalistic and biologically-based
23 approach that relied on the description of the temporal dynamics of a population of
24 metastatic colonies, with equations written at the organ or organism scale (10). In

25 parallel, several studies have sought to include additional variables when modeling
26 tumor growth, such as angiogenesis (11), stem cell behavior (12), tumor-immune
27 interactions (13) and microenvironment influences (14), among numerous others. To
28 date, the majority of mathematical studies in cancer modeling have focused on
29 primary tumor and relatively few have investigated the metastatic development (15-
30 22).

31 This dearth in metastatic data stems largely from the complexity of studying
32 metastasis itself. Metastasis starts with localized primary tumor growth which then
33 invades and intravasates into the bloodstream which, in turn, spreads systemically
34 until extravating into tissue at a distant (hospitable) site (23,24). While clinical
35 (retrospective) data has value (2,7,20,25,26), mouse tumor models have typically
36 aimed to mimic (and distinguish between) several stages of the metastatic process. In
37 certain mouse models, metastasis can derive from a tumor that is implanted
38 ectopically or orthotopically into a primary or metastatic site ('ectopic', 'orthotopic' or
39 'ortho-metastatic' models, respectively (27)) and can involve various immune states
40 (i.e., human xenograft or mouse isograft). Although more rarely performed, models
41 can also include surgical resection of the primary tumor which allows for progression
42 of clinically relevant spontaneous metastatic disease. These can include surgery
43 following ectopic implantation (i.e., 'ecto-surgical', such as tumors grown in the ear or
44 limb that are later amputated), or orthotopic implantation and resection (i.e., 'ortho-
45 surgical'), which more faithfully represent patient disease. To date, no studies have
46 utilized data from ortho-surgical metastasis models for mathematical analysis.

47 Herein we describe a mathematical approach developed using data derived from
48 two ortho-surgical metastasis models representing competent and incompetent
49 immune systems with luciferase-tagged human breast (LM2-4^{LUC+}) and mouse kidney
50 (RENCA^{LUC+}) cell lines. We first defined a mathematical formalism from basic laws of

51 the disease (dissemination and growth). Then we confronted the mathematical
52 outputs to longitudinal measurements of primary tumor size, metastatic burden and
53 survival using a population approach (nonlinear mixed-effects) for statistical
54 estimation of the parameters. Minimally parameterized models of each experimental
55 system were generated and used to fit and predict pre-/post-surgical data at the
56 individual and population levels. Next we used clinical datasets to assess metastatic
57 relapse probability from primary tumor size and show that, in both cases (preclinical
58 and clinical), one specific parameter (μ) allowed quantification of inter-
59 animal/individual variability in metastatic propensity. Critically, our models confirm a
60 strong dependence between presurgical primary tumor size and postsurgical
61 metastatic growth and survival. However, quantitative analysis revealed a highly
62 nonlinear pattern in this dependency and identified a range of tumor sizes (either
63 large or small) where variation of tumor size did not significantly impact on survival.
64 These represent potential threshold limits for the utility of primary size as a predictor
65 of metastatic disease (i.e., if small, then surgical cure; if large, then surgical
66 redundancy). These findings represent the first time clinically relevant surgical models
67 have been integrated with data-based mathematical models to inform the quantitative
68 impact of presurgical primary tumor size on subsequent metastatic disease.

69 Quick guide to equations and assumptions

70 The metastatic modeling approach we employed follows the formalism initiated by
71 Iwata et al. (10), which was further developed/expanded in recent works in two key
72 ways: 1) effect of systemic therapies (28,29), and 2) use in a (non-surgical) *in vivo*
73 human xenograft model involving orthotopic primary tumors (PTs) and metastasis
74 (21). Metastatic development is reduced to two main components:

- 75 1) Growth: includes presurgical primary (g_p) and secondary (g) tumor growth rates
76 2) Dissemination: includes metastatic dissemination rate (d).

77 A schematic description of the model is depicted in Figure 1. More complex
78 considerations on the biology (1,30) and modeling (31) of the metastatic process have
79 been considered elsewhere.

80 Growth dynamics

81 The PT volume $V_p(t)$ solves the following equations

$$\begin{cases} \frac{dV_p}{dt} = g_p(V_p) \\ V_p(t = 0) = V_i \end{cases} \quad (1)$$

82 The initial condition for the PT, denoted by V_i , was determined either by the number of
83 injected cells (preclinical case) or the initial tumor size at inception (clinical case,
84 $V_i = 1$ cell). Metastases were assumed to start from one cell. For each case, the
85 optimal structure resulting from our investigations was to assume the same structural
86 law for the PT and the metastases, although with possibly different parameter values.

87 Preclinical : Human breast (LM2-4^{LUC+}) metastasis model

88 Growth dynamics were defined by

- 89 1) Gomp-Exp (32) growth model (see expression below)

90 2) Growth parameters for PT and metastases treated identically ($g = g_p$)

91 In a previous study quantifying the descriptive power of several growth kinetics
92 models using data from the same breast animal model (33), the Gompertz model
93 accurately described primary tumor growth curves, in accordance with a large body of
94 literature (see references in (33)). However, a limitation of this model is that the tumor
95 doubling time could become arbitrarily small for small volumes, a feature that we
96 considered biologically irrelevant for small volumes at metastatic initiation (of the
97 order of the cell). A lower bound to this doubling time might be expressed by the *in*
98 *vitro* doubling time of the cell line, which can be experimentally determined.
99 Consequently, we adopted the Gomp-Exp model (32), defined by

$$g_p(v) = g(v) = \min\left(\lambda v, \left(\alpha - \beta \ln\left(\frac{v}{V_0}\right)\right) v\right) \quad (2)$$

100 Under this model, growth is divided between two phases: an initial exponential
101 phase, followed by a Gompertz growth phase. Parameter λ is the maximal
102 proliferation rate, taken here to be equal to the value inferred from *in vitro* proliferation
103 assays (see supplementary Figure 1A and Table 2). The second term in the min
104 function is the Gompertz growth rate, defined by two parameters. Parameter α is the
105 intrinsic relative (specific) growth rate at the size V_0 of one cell. Parameter β is the
106 exponential decay rate of the relative (specific) growth rate.

107 **Preclinical : Mouse kidney (RENCA^{LUC+}) metastasis model**

108 Growth dynamics were defined by

109 1) Exponential growth model.

110 2) Growth parameters for PT and metastases treated differently.

111 In mathematical terms, this is expressed by

$$g_p(v) = \alpha_p v, \quad g(v) = \alpha v \quad (3)$$

112 **Clinical : Human metastatic breast data**

113 Growth dynamics were defined by

114 1) Gompertz growth model

115 2) Growth parameters for PT and metastases treated identically ($g_p = g$)

116 **Metastatic dissemination**

117 The formation of new metastases was assumed to occur at a PT volume-
118 dependent rate $d(V_p)$ having the following parametric expression

$$d(V_p) = \mu V_p \quad (4)$$

119 where parameter μ is an intrinsic parameter of metastatic aggressiveness. This critical
120 coefficient is the daily probability for a given tumor cell to successfully establish a
121 metastasis. Therefore it is the product of several probabilities: 1) the probability of
122 having evolved the necessary genetic mutations to ensure the phenotypic abilities
123 required at each step of the metastatic process, 2) the survival probability of all
124 adverse events occurring in transit including survival in the blood or immune escape,
125 among others, and 3) the probability to generate a functional colony at the distant site.
126 Following reported observations (34), we assumed that all the metastases were
127 growing at the same volume (v)-dependent rate $g(v)$ and that they all started from the
128 same volume corresponding to the volume of one cell. The population of metastases
129 was then formalized by means of a time (t)-dependent volume distribution $\rho(t, v)$
130 solving the following problem (10):

$$\begin{cases} \partial_t \rho(t, v) + \partial_v (\rho(t, v) g(v)) = 0 & t \in (0, +\infty), v \in (V_0, +\infty) \\ g(V_0) \rho(t, V_0) = d(V_p(t)) & t \in (0, +\infty) \\ \rho(0, v) = 0 & v \in (V_0, +\infty) \end{cases}$$

$$N(t) = \int_{V_0}^{+\infty} \rho(t, v) dv = \int_0^t d(V_p(s)) ds = \mu \int_0^t V_p(s) ds, \quad (5)$$

$$M(t) = \int_{V_0}^{+\infty} v \rho(t, v) dv = \int_0^t d(V_p(t-s)) V(s) ds$$

131 The first equation is a continuity equation expressing conservation of the number of
132 metastases when they grow. The second equation is a Neumann boundary condition
133 on the flux of entering metastases at size $V = V_0$. The third equation describes the
134 initial condition (no metastases at the initial time). From the solution of this problem
135 two main macroscopic quantities can be derived, the metastatic burden $M(t)$ and the
136 number of metastases $N(t)$. In the convolution formula for $M(t)$ (35), $V(s)$ represents
137 a solution to the Cauchy problem (1) with g instead of g_p and V_0 as initial condition.
138 This formula allows fast simulation of the model using the fast Fourier transform
139 algorithm (35), which was essential for estimation of the parameters that required a
140 very large number of model evaluations.

141 **Materials and methods**

142 **Preclinical Methodology**

143 **Cell lines**

144 The human LM2-4^{LUC+} cells are a luciferase-expressing metastatic variant of the
145 MDA-MB-231 breast cancer-cell line derived after multiple rounds of *in vivo* lung
146 metastasis selection in mice, as previously described (see (36) (37)). Mouse kidney
147 RENCA^{LUC+} cells expressing luciferase were a kind gift from R.Pili, Roswell Park
148 Cancer Institute and described previously (38). LM2-4^{LUC+} and RENCA^{LUC+} were
149 maintained in Dulbecco's modified Eagle's medium (Corning, Cat. #MT10-013-CV)
150 and in RPMI (Roswell Park Memorial Institute) medium (Corning, Cat. #MT15-041-
151 CV), respectively, with 5% heat-inactivated fetal bovine serum (Corning, Cat. #MT35-
152 010-CV). Cells were authenticated by STR profile comparison to ATCC parental cell
153 database (for LM2-4^{LUC+}) or confirmation of species origin (for RENCA^{LUC+}) (DDC
154 Medical, USA). All cells were incubated at 37°C and 5% CO₂ in a humidified
155 incubator.

156 **Cell Proliferation assay**

157 LM2-4^{LUC+} cells were plated in 35mm plates (5x10⁵ cells per plate) and were
158 manually counted using trypan blue staining every 24 hours for 72 hours total (cellgro,
159 Cat. #25-900-CI).

160 **Photon-to-cell ratio**

161 LM2-4^{LUC+} cells were trypsinized and counted. 5x10⁶ cells were serial diluted 2 fold
162 down to 9.77x10³ cells and processed with Bright-Glo Luciferase Assay System
163 (Promega, Cat. #E2610) following manufacture's protocol.

164 **Ortho-surgical models of metastasis**

165 Animal tumor model studies were performed in strict accordance with the
166 recommendations in the Guide for Care and Use of Laboratory Animals of the
167 National Institutes of Health and according to guidelines of the institutional Animal
168 Care and Use Committee (IACUC) at Roswell Park Cancer Institute (Protocol: 1227M,
169 to JMLE).

170 The optimization and use of animal models of breast and kidney metastasis
171 orthotopic primary tumor implantation and surgical resection have been extensively
172 detailed elsewhere (39). Briefly, LM2-4^{LUC+} cells (2×10^6 cells in 50 μ L) and RENCA^{LUC+}
173 (4×10^4 cells in 5 μ L) were implanted, respectively, into the right inguinal mammary fat
174 pad (right flank) or kidney (subcapsular space) of 6-8 week old female CB-17 SCID or
175 Balb/c mice(39). Primary breast tumor size was assessed regularly with Vernier
176 calipers using the formula $\text{width}^2(\text{length} \times 0.5)$ and in both tumor models animals were
177 monitored bi-weekly for bioluminescence to quantify tumor growth (40). See
178 Supplementary preclinical methodology section for more details.

179 **Mathematical Methodology: Fit procedures**

180 **Preclinical data: primary tumor and metastatic burden dynamics**

181 Three fit procedures were investigated: 1) fitting the population average time
182 series, 2) individual fits of each mouse's primary tumor (PT) and metastatic burden
183 (MB) kinetics and 3) a mixed-effect population approach. Due to the high variability in
184 the data, the first approach was not considered relevant. The second approach
185 showed that the model was able to describe individual dynamics but, due to the
186 relative scarcity of the data in a given animal, led to very poor identifiability of the
187 coefficients, in particular the metastatic dissemination parameter μ . The third
188 approach was considered the most appropriate to our case. Indeed, nonlinear mixed-
189 effect modeling (41) is a statistical technique specifically tailored for sparse serial
190 measurements in a population. It assumes that inter-animal variability can be

191 described by a parametric distribution on the model's parameters (here assumed to
192 be lognormal, consistently with other works (20,42)). Multiple strategies were tested in
193 order to find the appropriate formalism to fit the data. These included fitting PT and
194 MB separately or together. The strategy fitting PT and MB was ultimately selected
195 because it resulted in more accurate fits and allowed for possible correlations
196 between the primary and secondary tumors growth parameters in a same animal.

197 One of the model parameters for Gomp-Exp growth was the *in vitro* proliferation
198 rate, which was determined by an exponential fit to an *in vitro* proliferation assay.
199 Maximization of the likelihood function under nonlinear mixed-effect formalism was
200 solved using the function *nlmefitsa* implemented in Matlab (43), which is based on the
201 stochastic approximation of expectation maximization (SAEM) algorithm. Specific
202 assumptions were: log-transformation of the parameters (i.e. log-normal population
203 distribution), proportional error model and full covariance matrix. For individual fits,
204 weighted least squares minimization corresponding to individual likelihood
205 maximization was performed using the function *fminsearch* of Matlab (Nelder-Mead
206 algorithm), following previously reported methods (33).

207 **Clinical data: Calculation of metastatic relapse probability**

208 Our methodology for fitting the clinical data followed the same format as (44),
209 although here the model was simplified (only parameter μ was allowed to vary among
210 individuals) and PT size at diagnosis was considered to be uniformly distributed within
211 each size range. Parameters for the growth of the primary and secondary tumors
212 were fixed (not subject to optimization) and corresponded to a maximal volume of
213 10^{12} cells (≈ 1 kg) and a doubling time of 7.5 months at 1 g, consistently with clinical
214 values reported in the literature (8,25).

215 The data reported in (26) consisted of metastatic relapse probabilities during the
216 next 20 years post-surgery, for patients stratified by PT size (see Table 1). Diameter
217 data from PT sizes at diagnosis were converted into volumes under the assumption of

218 a spherical shape and then converted to number of cells using the conversion rule 1
 219 $\text{mm}^3 \simeq 10^6$ cells (45). Parameter μ was assumed log-normally distributed in the
 220 population, with mean μ^m and standard deviation μ^σ .

221 The probability of having a metastatic relapse in the next 20 years for a primary
 222 tumor diagnosed with a given size was assumed to be equal to the probability of
 223 already having one distant tumor at the time of diagnosis. For a given volume range
 224 of PT sizes at diagnosis (V^k, V^{k+1}) , $k \in \{1, \dots, 7\}$, we considered the diagnosis volume
 225 V_D^k as a random variable uniformly distributed in (V^k, V^{k+1}) . Then, we computed the
 226 corresponding age of the tumor at diagnosis (i.e. the time elapsed from the first
 227 cancer cell) from the assumption of Gompertzian growth with the parameter values
 228 previously mentioned. This quantity was denoted $T_D(V_D^k)$. Under our formalism, the
 229 probability of having a disseminated metastasis at time $T_D(V_D^k)$ then writes

$$\mathbb{P}(\text{Met}^k; \mu^m, \mu^\sigma) = \mathbb{P}\left(\mu \int_0^{T_D(V_D^k)} V_p(t) dt > 1\right) \quad (6)$$

230 where Met^k stands for the event of having one metastasis at diagnosis when the PT
 231 volume is in (V^k, V^{k+1}) . For any volume range and value of μ^m and μ^σ , this formalism
 232 allowed us to compute a probability to be compared to the respective empirical
 233 proportion of relapsing patients reported in (26), by simulating the two random
 234 variables involved (V_D^k and μ). We then determined the best-fit parameters by
 235 minimizing the sum of squared errors to the data, using the function *fminsearch* from
 236 Matlab.

237 **Results**

238 **Quantitative and differential modeling of metastasis in ortho-** 239 **surgical models**

240 To mimic clinical progression of spontaneous systemic metastatic disease, two
241 models involving orthotopic tumor implantation and surgical resection (ortho-surgical)
242 were employed. These included a xenograft breast model (LM2-4^{LUC+} cells implanted
243 into the mammary fat pad) and an isograft kidney model (RENCA^{LUC+} implanted into
244 the subcapsular kidney space) (38) (see Methods). Presurgical primary tumor (PT)
245 and postsurgical metastatic burden (MB) were tracked by bioluminescence (BL)
246 emission, expressed in photons/second (p/s) (Figure 2A).

247 In the breast model, simultaneous BL and gross tumor volume measurements
248 (caliper) were performed. The former only quantifies living cells whereas the latter
249 computes a total volume indifferently of its composition. Volume and BL emission
250 were significantly correlated (supplementary Figure 1B), as observed by others (46).
251 Determination of the signal corresponding to one cell was required in our modeling for
252 the value assigned to V_0 . Based on linear regression between BL emission and tumor
253 volume, we established that $BL = 2.19 \cdot 10^6 V + 7.89 \cdot 10^7$, where BL is the
254 bioluminescence in p/s and V is the volume in mm^3 . This relationship, evaluated at V
255 $= 10 \text{ mm}^3 \approx 10^7$ cells gives 1 cell ≈ 10.08 p/s, which was approximated to 10 p/s.
256 Using this value gave reasonable fits to the PT growth data (supplementary Figure 2).

257 **Validation and calibration of the mathematical model**

258 We assessed the ability of the models to describe and predict the experimental
259 data of postsurgical MB dynamics. Several model designs were evaluated to define
260 the optimal structure and methodology that would allow accurate and reliable data
261 description. Specifically, for each *in vivo* experimental system, multiple structural
262 expressions and parametric dependences between the growth rate of the PT and MB

263 were tested. We refer to supplementary Figures 3 and 4 for direct comparison of
264 goodness-of-fit and identifiability under different modeling setups. Population and
265 individual fits of the best models to the data are shown in Figures 2B-C (and
266 supplementary Figure 5), and Figure 3, respectively. The parameter values inferred
267 from the population fits are reported in Table 2. The mathematical models – combined
268 with the population distribution of the parameters inferred from the nonlinear mixed-
269 effects statistical procedure – were able to give reasonable descriptions of the
270 presurgical PT and postsurgical MB growth. Importantly, these combinations could
271 quantify the dynamics of the process as well as the inter-animal variability. The latter
272 was better characterized by the metastatic potential parameter μ (large coefficients of
273 variation in Table 2). The models could also fit individual dynamics of longitudinal data
274 of pre-surgical PT and post-surgical MB (see Figure 3 for some representative
275 examples of growth dynamics in particular mice and supplementary Figures 6 and 7
276 for fits of all mice).

277 In addition to their descriptive power, the models were able to predict growth
278 dynamics in external data sets that were not employed for estimation of the
279 parameters (Figure 2D-E). These results emphasize the ability of our general
280 modeling structure to capture MB growth dynamics. Additionally, the modeled post-
281 surgical MB could also be related to empirical survival by means of a lethal burden
282 threshold, which was estimated to be 4×10^9 p/s (supplementary Figure 8).

283 **Qualitative and quantitative differences across ortho-surgical models**

284 *Xenograft Model: Breast metastasis*

285 Using the same growth model (Gomp-Exp) and parameters for both presurgical PT
286 and postsurgical MB, we were able to adequately fit the data, while ensuring
287 reasonable standard errors on the parameters estimates (Table 2). Although more
288 complex structures (e.g. models with one parameter differing between primary and
289 secondary growth) provided marginally better fits, robustness in estimating μ was

290 impaired (supplementary Figure 3). Quantitative inference of μ revealed small
291 metastatic potential (Table 2), which translated into late development of metastases
292 following xenograft and growth of the MB mostly dominated by proliferation (Figures
293 2B, 3A-C).

294 *Isograft Model: Kidney metastasis*

295 In contrast, the kidney model MB growth curves exhibited a different behavior, with
296 a marked change of regimen at the time of surgery. In the context of the model, this
297 means that most of the presurgical MB increase was driven by the dissemination
298 process, and not by proliferation of the metastases themselves. This was reflected by
299 a very large value of μ (Table 2), with nine orders of magnitude of difference
300 compared to the breast model. This feature was not directly visible, nor quantifiable,
301 by direct examination of the data, and reflects the large metastatic aggressiveness of
302 isograft spontaneous metastasis animal models, since overpassing the immune
303 surveillance is a major challenge in the metastatic process (4). When the PT was
304 removed, dissemination stopped and only proliferation remained for further growth of
305 the MB, which happened at a slower rate than at the primary site (Figures 2C and 3D-
306 F). In some cases, growth of the MB remained constant or even decreased after
307 surgery (see supplementary Figure 7). This result reflects the fact that the competent
308 immune status of the mice might have an important impact on the establishment of
309 durable, fast-growing metastatic colonies at the secondary sites (47).

310 Together, our data-based quantitative modeling analysis of presurgical PT and
311 postsurgical MB growth kinetics demonstrated the descriptive power of the models,
312 unraveled distinct growth patterns between the two animal models and emphasized
313 the critical role of the parameter μ for quantification of the inter-animal variability.

314 **Clinical data of metastatic relapse probability**

315 Clinical data reported in the literature generally do not provide detailed information
316 about the untreated growth of the metastatic burden, either because the residual

317 disease is invisible, or because the patients benefit from adjuvant therapy after
318 resection of their PT. Nevertheless, before the generalization of adjuvant therapy for
319 breast cancer, Koscielny et al. (26) reported data from a cohort of 2648 patients
320 followed for 20 years after surgery of the PT, without additional treatment. Their data
321 (reproduced in Table 1) demonstrated that, despite a clear association between PT
322 size at diagnosis and the probability of metastatic relapse, not all the patients having
323 a given PT size were relapsing. For instance, only 42% of patients with a PT diameter
324 at diagnosis between 2.5 and 3.5 centimeters developed metastasis. Based on this
325 observation, we used our model to describe inter-individual variability by means of a
326 limited number of parameters. We considered that the probability of developing a
327 metastasis in the next 20 years was equal to the probability of already having one at
328 the time of diagnosis (see Methods). Using a lognormal population distribution of
329 parameter μ we were able to obtain a significant fit to the data of metastatic relapse
330 for all size ranges (Table 1, $p = 0.023$). Interestingly, the median value of μ resulting
331 from these human data was close to the value from the preclinical breast data, in
332 comparison to the kidney model.

333 These results demonstrated that, within our semi-mechanistic modeling approach,
334 parameter μ was able to capture the inter-individual metastatic variability, not only in
335 animal models, but also for patient data.

336 **Assessing the impact of surgery on metastasis and survival: a** 337 **simulation study**

338 When diagnosis detects only a localized primary tumor, distant occult disease
339 might already be present. In our model, the extent of this invisible metastatic burden
340 depends on: 1) the PT size at diagnosis and 2) the patient's metastatic potential μ .
341 For instance, if the PT size (or μ) is small then the occult MB might be negligible and
342 surgery would substantially benefit to the patient in terms of metastatic reduction, by
343 stopping further spread of new foci. Conversely, if the PT size (or μ) is large, then the

344 occult MB might already be consequent and removing the PT might only have a
345 marginal impact.

346 *Virtual simulation of two breast cancer patients*

347 We simulated the quantitative impact of PT surgery in two virtual breast cancer
348 patients having a PT diagnosed at 4.32 cm and two values of μ (median and 90th
349 percentile within a population distributed according to our previous estimate). Results
350 are reported in Figure 4 and supplementary movies 1 and 2. A discrete and stochastic
351 version of the metastatic dissemination was employed here for the simulations (see
352 supplementary methods for details). Interestingly, our simulation revealed that at the
353 time of diagnosis, no metastasis was detectable (i.e. below the imaging detection
354 limit, taken here to 10^8 cells), in both cases (Figure 4A-B). In clinical terms, this
355 means that both patients would have been diagnosed with a localized disease.
356 However, the two size distributions were very different, with a much larger residual
357 burden in the “large μ ” case, illustrative of the increased metastatic potential.

358 For the “median μ ” case, our model predicted the presence of two small
359 metastases, with respective sizes 6 and 278 cells. Not surprisingly, when no surgery
360 was simulated, this number continued to increase, reaching 160 secondary lesions
361 after 15 years (Figure 4C). However, most of the metastatic burden (126 tumors, i.e.
362 78.8% of the total burden) was composed of lesions smaller than 10^9 cells (≈ 1 g).
363 Panels E and G of Figure 4 demonstrate that a substantial relative benefit (larger than
364 10%) in MB reduction was eventually obtained, but only after 7.8 years. Nevertheless,
365 at the end of the simulation (15 years after surgery), the predicted two occult
366 metastases at diagnosis had reached substantial sizes (1.41×10^{11} and 1.89×10^{11}
367 cells). Therefore, for this patient with median metastatic potential, the model indicates
368 an important benefit in using adjuvant therapy.

369 For a patient with higher metastatic potential (at the level of the 90th percentile,
370 see Figure 4 panels B, D, F and H, and supplementary movie 2), even with a PT

371 diagnosed at the same size, the predicted metastatic burden at diagnosis was
372 considerably more important, with 76 lesions and the largest comprising 6.23×10^6
373 cells. This consequent occult burden translated into poor outcome and the metastatic
374 mass would have reached a lethal burden of 10^{12} cells 9.3 years after the initial
375 diagnosis if no therapy would have been administered.

376 These results illustrate the potential of the model as a diagnosis and prognosis
377 numerical tool for assessment of the occult metastatic burden and post-surgery
378 growth. In this, it could help to determine the extent of adjuvant therapy necessary to
379 achieve a long-term control of the disease.

380 *Impact of tumor size on postsurgical survival*

381 To further examine the relationship between the PT size at surgery and survival,
382 we performed simulations for 1) an individual with fixed value of μ (the population
383 median, see Figure 5A) or 2) an entire population (simulated survival curves in Figure
384 5B), for three PT sizes. Numerical survival was defined by the time to reach a lethal
385 burden of 1 kg ($\approx 10^{12}$ cells) (2) from the time of cancer inception. Interestingly, we
386 observed a highly nonlinear relationship between the PT size and the survival, which
387 suggested three size ranges delimited by two thresholds (Figure 5A). The lower
388 threshold — termed ‘recurrence’ threshold (4 cm in Figure 5A) — was defined as the
389 maximal limit whereupon no metastasis was present at surgery (number of
390 metastases lower than 1). The upper size threshold — termed ‘benefit’ threshold
391 (5.2 cm in Figure 5A) — was defined as the size above which surgery had a negligible
392 (< 10%) impact on survival time. Above and below these ‘recurrence’ and ‘benefit’
393 thresholds, PT size had no important correlative value. Conversely, within the PT size
394 range delimited by these two bounds, the relationship between presurgical PT and
395 postsurgical MB/survival was highly correlative, with a large derivative and a sharp
396 transition between the two extremes. The same qualitative PT size/survival

397 relationship was obtained for any value of μ sampled within the population distribution
398 (see supplementary Figure 9).

399 In Figure 5C, we present quantitative estimates of the recurrence and benefit
400 thresholds for various percentiles of μ within the population distribution (see also
401 supplementary Figure 9). Our simulations predicted that for the first half of the
402 population, surgery was almost always leading to negligible metastatic recurrence
403 risk, with large values of the recurrence threshold (larger than the usual detection
404 levels). On the other hand, the patients with large metastatic potential were predicted
405 not to substantially benefit from the surgery, as far as reduction of future MB was
406 concerned. For instance, a patient with μ at the level of the 90th percentile and a PT
407 diagnosed at 4 cm would have an increase in absolute survival time of only 1.9%
408 following surgery (Figure 5C).

409 **Discussion**

410 Using a formalism based on simple laws of metastatic development (including
411 dissemination and proliferation), we derived mathematical models able to connect
412 presurgical PT growth to postsurgical development of the MB in two ortho-surgical
413 animal models (with two immune states) as well as one clinical data set. These
414 quantitative models allowed identification of different metastatic growth patterns and
415 characterization of the metastatic potential (and associated inter-animal/individual
416 variability) as a critical parameter, μ . Our results also revealed a nonlinear quantitative
417 relationship between the PT size at diagnosis and post-surgical survival improvement.

418 Previous studies have utilized experimental data derived from mouse metastasis
419 models to inform mathematical analysis. For instance, Hartung and colleagues used
420 human MDA-MB-231 breast cancer cells implanted orthotopically in mice in order to
421 validate a mathematical model for longitudinal data of metastatic burden growth (21).
422 This animal model was non-surgical and utilized severe immunocompromised Nod
423 SCID γ mice to improve the low metastatic potential observed in the MDA-MB-231, a
424 phenomena recently reported elsewhere (47). In our studies, we utilized a variant of
425 the MDA-MB-231 previously selected for increased metastatic potential by repeated
426 orthotopic implantation and metastatic resection in SCID mice (36). Since the
427 selection of cells and immune state could influence analysis, we also included an
428 immunocompetent mouse kidney model to confirm (and compare) findings. While
429 these and other modifications to the metastatic systems could significantly influence
430 mathematical modeling (i.e., different mouse strain and cell line, different
431 bioluminescence technique, etc...), the impact of surgery appears to be the most

432 significant factor. In this regard, several technical discrepancies likely impair a
433 relevant comparison between surgical and non-surgical models presented by
434 Hartung, et al. (21) and the current study. For instance, in surgical models we found it
435 unnecessary to assume different growth between the primary and secondary lesions
436 in surgical models. Additionally, we considered a less complex dissemination rate
437 (expression $d(V_p) = \mu V_p^\gamma$ and $\gamma = \frac{2}{3}$ was used in (21)). Notably, we could fit our data
438 equally well with various values of γ and thus concluded that it cannot be identified
439 from combined PT growth and MB dynamics data alone (supplementary Figure 10).
440 Future studies would require more data, especially on the number and size
441 distribution of the secondary lesions, to precisely determine the shape of the
442 dissemination coefficient. When using the dissemination and growth terms from (21)
443 and fitting the resulting model to our surgical data, we found a much larger metastatic
444 potential μ and a significantly faster metastatic growth kinetics parameter than
445 computed in the non-surgical model (21) (see supplementary text). While the former
446 probably illustrates higher metastatic propensity due to a more permissive immune
447 state, the latter possibly suggests post-surgery metastatic acceleration (48-50).

448 In this regard, this raises another critical consideration of the impact of surgery on
449 metastatic potential in mathematical modeling. Preclinical and clinical works have
450 suggested that removal of the PT might provoke acceleration of metastatic growth
451 (50,52). There are various biological rationales that could explain this, including
452 inhibition of secondary growth by the presence of a primary neoplasm as a result of
453 nutrient availability, concomitant immunity, or even systemic inhibition of angiogenesis
454 (53). Such a theory could conceivably be assessed within the context of our model by
455 defining different pre- and post-surgical metastatic growth rates $g(v)$ and comparing

456 goodness of fit. However, this would add at least one degree of freedom (thus
457 deteriorating the reliability of the estimation) and invalidate the convolution formula
458 used for computation of the metastatic burden in a model with non-autonomous
459 $g(t, v)$ (instead of $g(v)$), and therefore was not considered here. Importantly,
460 theoretical integration of higher order phenomena for the biological dynamics of
461 metastatic development has been considered elsewhere (14,16,18,54) and recent
462 findings in the organism-scale dynamics of metastases (such as the self-seeding
463 phenomenon (5,6) or the influence of the (pre-) metastatic niche (55)) could be
464 embedded within the general formalism developed in our model. This could lead to
465 complex models, however, and given the amount of information contained in our
466 present data, reliable identification of such dynamics was not realistic. Instead, we
467 only considered metastatic dynamics as reduced to its most essential features:
468 dissemination and proliferation. Future studies should examine the potential of
469 metastases to metastasize, as has been extensively debated in the past (56-58),
470 particularly with the recent demonstration that some metastases are able to re-seed
471 the primary tumor (5,6). Although not included in this study, preliminary tests using
472 our model suggest negligible differences in the simulations and no impact on our
473 results, however a more extensive analysis is required.

474 Our modeling philosophy elaborates on Fisher's theory (59) of cancer as a
475 systemic disease and relates also to the parallel progression model (2). The
476 dissemination rate d , characterized by parameter μ , quantifies the metastatic potential
477 and allows for a *continuum* of possibilities between early and late dissemination. Our
478 results seem to parallel clinical evidence of the impact (and importance) of early
479 surgery – particularly in the case of breast cancer. For example, in a retrospective
480 study of 2838 breast cancer patients, the post-surgical residual recurrence-free

481 survival rate at 5 years for Stage I disease was 7% (60). Consistently, our quantitative
482 analysis demonstrates that in this case, for most patients, metastases that could have
483 been shed before diagnosis would not develop into overt clinical disease during the
484 remaining life history of the patient. For Stage IV breast cancer (that would
485 correspond, in our formalism, to a large value of μ), our analysis predicts only
486 negligible benefit of the surgery (if only considering reduction of metastatic shedding),
487 in accordance with preliminary results of a recent clinical trial (61). In order to use our
488 model as a practical diagnosis and prognosis tool that could help to refine and
489 individualize adjuvant therapy, the critical next step is to find a way to estimate the
490 parameter μ , in a patient-specific manner. One of the main challenges will be to do so
491 using data derived from the primary tumor only, since metastases are often
492 undetectable at the time of diagnosis. While the value of μ might very likely depend on
493 the combination of several phenomena (including some genetic alterations or the
494 immune status of the patient which could be linked to different biomarkers (62)),
495 recent successes of genetic signatures as prognosis factors for metastasis might
496 allow for patient-specific estimation of μ (63).

497 Any mathematical modeling attempt is limited by the intrinsic measurement error of
498 the experimental technique. For monitoring the dynamics of total metastatic burden,
499 bioluminescence imaging represents one of the best methods so far (51). However,
500 measurement variability is hard to assess due to inherent issues, such as the long
501 half-life of luciferin that prevents immediate replication of the measurements.
502 Comparison of bioluminescence with caliper measurements showed large variance
503 (supplementary Figure 1B), which increased with tumor size. This justified our
504 assumption of a proportional measurement error model. Standard deviation of the
505 relative error could in turn be estimated from the fit procedure and yielded a value of

506 0.72. This high degree of uncertainty should be taken into account as an inevitable
507 limitation for quantitative modeling studies of bioluminescence data. We therefore put
508 a strong emphasis on using a minimal number of parameters and assessed the
509 robustness of our results on various assumptions, such as the shape of d and the
510 value of V_0 (supplementary Figures 10 and 11).

511 Together, our mathematical methodology provides a quantitative *in silico*
512 framework that could be of valuable help for preclinical and clinical aims. Indeed,
513 validation of our modeling methodology allows us to address in future works the
514 differential effects of systemic therapies on primary tumor growth and metastases
515 (39,40). Clinically, our methodology could be used to refine/optimize therapeutic
516 strategies for patients diagnosed with a localized cancer and inform on the timing of
517 surgery, extent of occult metastatic disease and probability of recurrence. In turn, this
518 may impact decisions on duration and intensity of presurgical neoadjuvant or
519 postsurgical adjuvant treatments (64).

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528

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