Evaluating Multi-User Selection for Exploring Graph Topology on Wall-Displays

Arnaud Prouzeau, Anastasia Bezerianos, Olivier Chapuis

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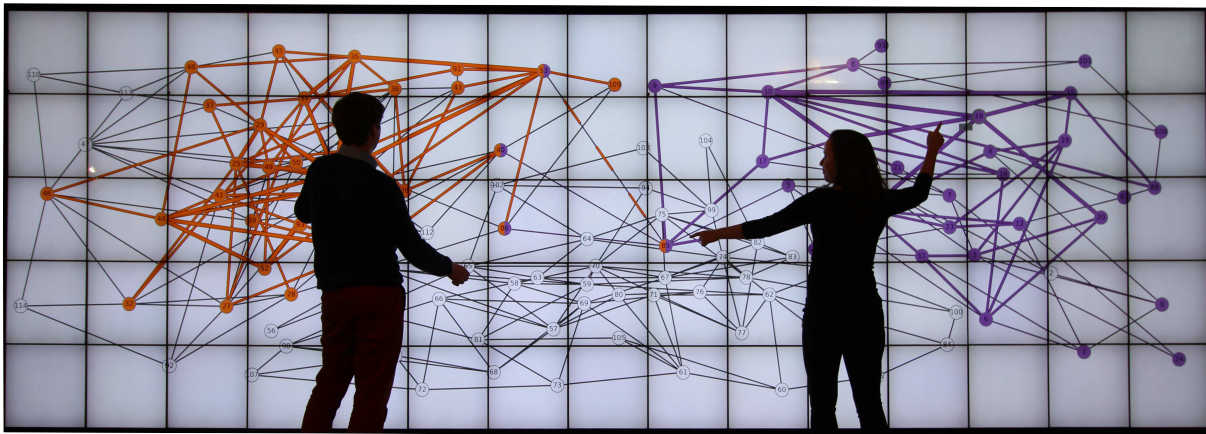Arnaud Prouzeau, Anastasia Bezerianos, Olivier Chapuis

Figure 1. A pair using the propagation technique to explore a graph. They discuss two communities, in orange and purple, selected using the propagation technique. The communities are linked by a specific node shown by the right user. The remaining 3 orange-purple nodes show how by propagating the purple community, it flows into the orange one through this node.

Abstract—Wall-displays allow multiple users to simultaneously view and analyze large amounts of information, such as the increasingly complex graphs present in domains like biology or social network analysis. We focus on how pairs explore graphs on a touch enabled wall-display using two techniques, both adapted for collaboration: a basic localized selection, and a propagation selection technique that uses the idea of diffusion/transmission from an origin node. We assess in a controlled experiment the impact of selection technique on a shortest path identification task. Pairs consistently divided space even if the task is not spatially divisible, and for the basic selection technique that has a localized visual effect, it led to parallel work that negatively impacted accuracy. The large visual footprint of the propagation technique led to close coordination, improving speed and accuracy for complex graphs only. We then observed the use of propagation on additional graph topology tasks, confirming pair strategies on spatial division and coordination.

Index Terms—Wall-Displays; Multi-user interaction; Graph visualization; Selection techniques; Co-located Collaboration

✦

1 INTRODUCTION

Graph structures, consisting of vertices and edges, exist in various application areas: in social networks they are used to represent people and their relationships, in molecular biology proteins and their interactions, in transport networks they can represent air-flight routes, etc. Graph data structures are frequently represented as node-link diagrams, but like many visual representations of large datasets today, they can be too wide to view comfortably on regular screen monitors [64].

High-resolution wall-sized displays [8, 54] are promising data analysis environments, as their size and high pixel density allow simultaneous viewing, comparison, and exploration of large amounts of data. Their size can also comfortably accommodate multiple viewers, supporting collaborative analysis [60]. Despite their promise as collaboration platforms, they have received little attention for graph exploration. We take a step in this direction.

We present a systematic study of how pairs use a wall-display to solve topology based tasks, that are common components of more complex graph analysis tasks [37]. We study how the choice of interaction technique supports or hinders pairs collaborating on these tasks. We focus on techniques for selection, a fundamental visualization task, as it is a pre-requisite to many interactions such as filtering, comparisons, details on demand, etc.

We adapt two general purpose graph selection techniques for use by multiple users on a touch-enabled wall-display. Our baseline is an extension of basic node/edge selection for multiple users. It is easy to master, and has a limited, and thus fairly localized, visual footprint on the wall display, that does not interfere with colleagues' work. The propagated selection extends for multiple users the idea of transmitting a selection to neighboring nodes/edges [21, 42]. It highlights the connectivity structure of the graph (Figure 1), but may have a large visual footprint that disturbs colleagues.

We first assess the impact of selection technique on pairs conducting a specific topology analysis task, namely identifying a shortest path. As there is no work on pairs working on such tasks on wall-displays, we tease out effects due to the technique or due to collaboration, by also studying single user selections. We

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then examine how propagation, the most promising technique, is used by pairs on other graph analysis tasks [37]. Our studies are conducted on a touch enabled wall-display, instead of interacting using mice and keyboards, as mobility allows viewers to perform implicit zooming [7] and correct for visual distortions [10].

We contribute: (i) The adaptation of two graph selection techniques for collaboration on wall-displays. (ii) The controlled study of how pairs use these techniques on a graph topology task (shortest path identification) on wall-displays. (iii) A discussion and observational study on how one technique, propagation, supports different topology tasks. And (iii) a set of design implications: as pairs divide the work spatially, even when tasks are not spatially divisible, the use of a localized selection technique may be detrimental to performance in complex graphs; while a technique with global reach leads to tighter collaboration and coordination, that is more effective and accurate for such graphs.

2   RELATED WORK

A wide range of topics surrounding large displays have been studied in HCI and Visualization. We focus on the most relevant, namely visual exploration and collaboration on wall-displays, in particular exploration of graphs, and the idea of transmission.

2.1   Walls in Visual Exploration

Wall-sized displays have been studied in the context of information visualization and analysis, as they can naturally display a large amount of visual information. Previous work comparing large displays to traditional desktops [40, 58] or to smaller displays [52] has shown performance improvements when moving to larger displays. Considering visual analysis in particular, Yost and North [68] tested several data visualizations for their scalability when moving from small to large displays. They found their visualizations to scale well for the tasks of finding detailed and overview information, and note that spatial encoding of information was particularly important on large displays. Jakobsen and Hornbæk [31] examined the interplay between display size, information space size and scaling, and found that all these factors need to be taken into account, and that increased display size did not improve navigation performance in tasks where targets are visible at all scales. Reda et al. [52] found that larger displays encourage longer visual analysis sessions, and result in deeper and more complex insights. Finally, Rajabiyazdi et al. [51] observed that they can lead to previously missed insights in multiple disciplines.

Beyond their benefits, researchers have studied specific issues related to visual perception of wall-displays due to their scale. Endert et al. [17] discuss how a viewer's distance from the wall influences the visual aggregation of displayed information. Bezerianos et al. [10] showed large discrepancies in the perception of basic visual encodings depending on viewing distances and angles, that nevertheless decrease if appropriate physical navigation is used. Ball et al. [6] compared the benefits of added peripheral vision vs. physical navigation, and found that physical navigation influenced task performance while peripheral vision did not. Isenberg et al. [28] blended two visualizations so that each is perceived at a different viewing distance from the wall. Collectively this work stresses the importance of physical navigation for visualization and visual perception tasks, even if it is not necessarily better than virtual navigation in classification tasks [33].

Despite the importance of physical navigation, a large body of this past work either assumes the use of mouse and keyboard, or simply does not study interaction. Nevertheless, recent work supports both interaction and physical navigation using handheld devices or direct touch. Handhelds are used as touch-pads to conduct classification tasks [40], or as a support for physical controllers [34] or for explicitly sketching interactive slider controllers [61] to conduct multi-dimensional data exploration. In a sensemaking task, Jakobsen and Hornbæk [32] allow users to move freely and use direct touch to interact with the wall. We similarly use touch to support pairs working on graph topology tasks.

2.2   Walls in Collaborative Analysis

When it comes to co-located collaborative work and visual analysis (see [22, 29] for reviews), work has focused mostly on tabletops, and "small" vertical displays (SDG and whiteboards). For example, researchers have explored how collaborators shift from tight to loose work coupling [59], how users divide space (territoriality) [62], how they analyze text documents [30], compare tree visualizations [26], etc.

There are few works on co-located collaborative work on large (ultra-high resolution) walls. Notable exceptions are recent work by Jakobsen and Hornbæk [32] that studies the behavior of a pair of users in a sense-making task, and Liu C. et al. [39] that studies the effect of different collaboration styles and interaction in a classification task. Both these works stress the importance of users' coordination (possibly at distance) in these environments. Our work is along the same lines, but focuses on graph analysis in particular, and the effect of different interaction techniques on it, a topic that so far has not been studied.

2.3   Graph Exploration on Large Surfaces

Collaborative analysis is one of the next challenges of the analysis of graphs [64]. Existing systems support mainly remote collaboration (e.g. [69]). Less work has targeted co-located analysis, like that by Isenberg et al. [27] that retrofitted an existing graph visualization application for use by multiple analysts with mice and keyboards. We are not aware of any work that studies analysis of graphs by multiple users moving freely in front of wall-displays.

Although work on graph exploration using wall-displays is limited, researchers have identified their potential early on. For example, Abello et al. [1] used a wall display to visualize communication network data. Later, Mueller et al. [47] designed an algorithm to interactively layout graphs optimized for tiled displays and distributed environments, while Marner et al. [41] let users interactively adapt the layout on the wall using a mouse and keyboard. Finally, Lehmann et al. [38] leverage physical navigation as an implicit interaction, using the viewer's distance from the wall to adjusted the level of detail of a graph, and Kister et al. [36] use it to move a lens with contextual information. This past work on wall displays does not study the use of explicit interactions (e.g., selections) during collaboration, as we do.

Finally, although not explicitly testing collaboration, researchers have introduced multi-touch techniques for manipulating graphs on interactive tabletops. For example, Henry Riche et al. [23] use multi-touch interactions to fan out links leaving a node, to bundle them, or use link magnets to attract certain types of links. Schmidt et al. [55] alter link trajectories, pin, or make them vibrate by plucking them. This work introduces multi-touch techniques on tabletops for different purposes. While we also use touch, we focus specifically on selection and study how pairs use it to perform graph topology tasks on wall-displays.

2.4 Graph Exploration using Transmission

Visual analysis of graphs is a long standing field, with numerous research questions (see [24, 64] for reviews). We focus on techniques related to our propagation selection (section 3.2), that use the idea of propagating/transmitting information to neighboring nodes or links that is central to graph analysis (e.g., [53]).

As graph structures can be very large, exploration is often localized on interesting nodes and their neighbors. For example, van Ham and Perer [63] designed a Degree-of-Interest function for graph exploration that first proposes interesting nodes, and lets the user indicate interesting nodes to expand to. Archambault et al. [4] use specifically the notion of distance to progressively reveal and render nodes proximal to a node of interest from within a larger graph hierarchy. Moscovich et al. [46] propose interaction techniques for panning within a graph, or bringing neighbors closer, based on the graph's connectivity. Finally, egocentric techniques (e.g., [67]) re-layout graphs by focusing around one node and laying out the rest based on their distance from it; or focus on two nodes [13] and highlight their common neighbors. This work can lead to a user-driven re-layout of the graph, that may disrupt the work of other viewers in a multi-user setting.

Other techniques related to propagation preserve the layout. Heer et al. [21, 20], allow users to highlight the contour of the 1st or 2nd degree neighbors, or the connected component of a node, by hovering over it or by using repeated mouse clicks. McGuffin and Jurisica [42] propose techniques to locally select and manipulate nodes, including a menu option that selects a node's neighbors of increasing distance progressively. Ware and Bobrow [65] evaluate different means of highlighting connections to neighbors of arbitrary degree specified by a text field, and found that motion representations are not better than static highlighting. We extend this notion of propagated selection to multiple origin nodes, providing appropriate input and visual design, to support such selections by multiple users.

3 INTERACTION TECHNIQUES

Our goal is to investigate how interaction techniques affect multiple users working on graphs. We focus on selection, as it is a required first step for many other visualization tasks, such as filtering, comparison, details on demand, etc. Two techniques were considered, a simple selection (*Basic*), and one based on the graph's connectivity structure (*Propagation*). These techniques were chosen due to their properties: they can benefit graph exploration differently but also face different challenges when adapted for multiple users on wall-displays. We describe next how we adapted the techniques for touch interaction on wall-displays, and for collaborative use. Each description finishes with a summary of the technique's properties, motivation for their use, and possible challenges when used in a multi-user context on wall displays.

3.1 Basic Selection

Basic is inspired by colored selections available in graph visualization software extended for multiple users. We chose it to investigate the limits of basic selections in collaborative settings.

3.1.1 Interaction and Visual Design

A node (or link) is selected by tapping on it once, and deselected if tapped again. Inspired by previous work [4, 21], we also highlight the links (or nodes) attached to it so as to demonstrate its connections, but do not re-layout the graph to avoid disrupting

collaborators. Given that we do not have keyboard modifiers, and wanted to keep the touch input vocabulary simple, we decided to allow users to modify this selection in the following way: if the user taps on a node adjacent to an existing selection (direct neighbor), then this node is added to the selection and it, and its links, are highlighted with the selection's color. If the node is adjacent to more than one existing selections it takes the color of the last edited selection. Tapping on a selected node removes it from the selection. This way users can edit their selections with simple taps, keeping the input vocabulary very simple. We chose to not use lasso-type selections that require dragging to select multiple items, as they are not well suited to large interactive surfaces, such as walls, where prolonged dragging is inaccurate, fatiguing [25], and often disrupted by bezels in tiled walls.

Our wall, similar to many touch enabled surfaces, does not differentiate between users. Nevertheless, it is important for colleagues to differentiate their work. Thus, if users tap on nodes that are not adjacent to existing selections, we assume a new selection is being made (potentially by a different user) and assign it a new color, chosen randomly from a set that is easily distinguishable.

3.1.2 Summary

Basic extends the simple selection available in graph visualization software to selection of multiple nodes/edges by multiple users. It is familiar, easy to understand, and our design ensures it relies on simple taps. It has a small visual footprint as it selects a single node and its edges at a time, and thus will likely not disrupt collaborators when used in a multi-user context on wall displays. Nevertheless, it may require extensive physical movement if users need to select multiple nodes that are far away on the wall.

3.2 Propagation Selection

As an alternative, we investigate *Propagation* selection, based on the idea of progressive transmission of a selection to neighboring nodes. Propagation allows local interaction on a node that can highlight its influence across a larger area on the graph (and wall), without requiring extensive physical movement that can be tiring. Nevertheless, it may have a large visual footprint if neighboring nodes are far away, potentially disrupting collaboration.

Variations of the propagation selection from past work (e.g. [21, 42]) allow a single user to either highlight neighboring nodes up-to a specific degree only [21], usually 2, or use a menu or text option to select a node and its neighbors of a certain degree [42]. We explain how we adapted the technique allowing multiple users to easily expand the selection to the *n*-th degree using simple touch interactions. We finally describe its properties and how it can be used to perform topology-based tasks [37] when analyzing graphs.

3.2.1 Interaction

Propagation allows users to select a node, which we will refer to as the *origin*, and then propagate the selection first to its neighbors, then to their neighbors, and so on. Propagation of a selection is done through a series of taps (clicks) on a node. The first tap selects the node itself (Figure 2-a), and the following taps propagate the selection progressively to the neighboring edges and nodes: the second tap adds to the selection outgoing links and first-degree neighbors of the origin (Figure 2-b), and so on for all following taps[1] (Figure 2-c). If users continue tapping,

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[1] Propagation starts either from a node or a link. To simplify the discussion we talk about node propagation, but we use a similar selection pattern for links: link selected first, adjacent nodes and their links next, and so on.
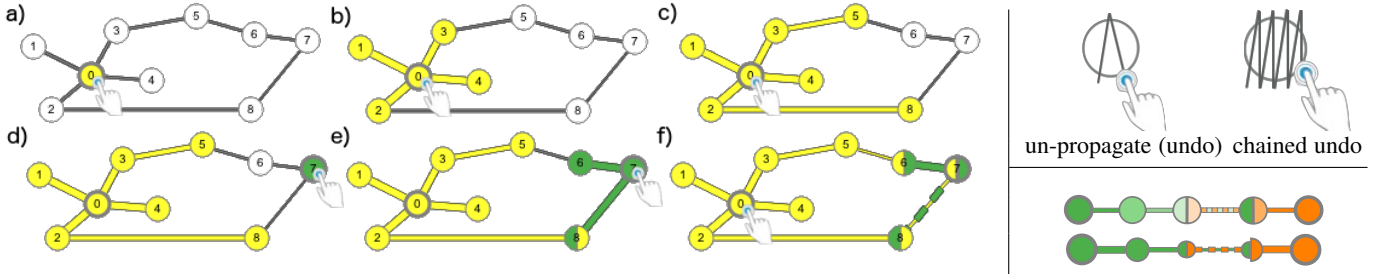
Figure 2. On the **left** multiple propagations: (a) a first tap on node 0 selects it; (b) a second tap propagates the selection to immediate neighbors; (c) and a third tap to 2nd degree neighbors (notice the difference in link width according to distance); (d) a tap on node 7 selects it with a new color; (e) a second tap selects its neighbors, one of which (node 8) is shared with the first propagation and has both colors; (f) a fourth tap on node 0 propagates the first selection a third time, resulting in nodes 6,7,8, and link 8-7 being shared between propagations, with the color and width on shared link 8-7 alternating. On the **top right** gesture to undo one propagation step on a node (left) and chained undo for backtracking multiple steps (right). On the **bottom right** design variations for displaying propagation distance using color intensity (top) and node-link size (bottom).

propagation continues until no more nodes can be reached from (are connected to) the origin node. Thus a propagated selection is a progressive query selection, that adds elements connected to the origin node at progressively increasing distances.

We note that the first step of propagation (selecting only the node) is not the same as *Basic* (selecting the node and its edges). We made this design choice as initial feedback indicated that the metaphor of transmission is better served if we consider that each tap opens the flow of transmission from the selected nodes to their neighborhood (both links and nodes).

To accommodate multiple users working in parallel, when users select a node that is not part of an existing propagated query, it becomes the origin of a new propagation selection (Figure 2-d). If they select a node already inside a propagation query (but not its origin), the query expands to also include propagations from this new origin. Thus one propagation query can have multiple origins.

As we designed the technique for touch surfaces, we chose a simple crossing zig-zag gesture to undo propagation steps. When performed on the origin, it backtracks the propagation by one step (Figure 2 left). The gesture can be chained to perform multiple backtracks without lifting a finger, undoing quickly several propagation steps in one interaction. When the selection is reduced to a single node (the origin), this gesture unselects the node.

A crossing gesture on an element (node or link) that is not the origin of a propagation, removes this node from the selection and blocks future propagation paths of this selection to go through it.

3.2.2 Visual design

Nodes and links in a propagated selection share a common color (as traditional color queries). Propagation origins stand out with a thicker border (Figure 2-a), and new propagations are assigned a different color, similar to *Basic* (Figure 2-d).

Due to the propagation of selections, a node can be selected by two or more colors. The node in question is divided visually into slices equal to the number of selections, and given the respective colors (Figure 2-e).

Links can similarly be part of several selections. Dividing them in segments equal to the number of selection colors (similar to nodes) could lead to few, but long, colored segments if links are long. Thus the multiple colors could be hard to see locally on a wall display. We decided instead to streak (dashing pattern) the links with the selection colors (Figure 2-f). We fixed the number of streaks to seven, as we observed that on our wall they were still visible locally, even on long links. Moreover, as the fixed number of streaks have different length depending on the total length of the link, they give locally an indication of its overall length.

We explored different design variations to emphasize the distance of elements (nodes and links) from the origin. This is of interest both within a single selection (to identify the farthest elements), but also for elements that are part of multiple selections to identify which origin is closest. As color is already used in selections, we considered other visual variables (Figure 2 right). Color intensity that drops with distance was considered, but rejected, as the perception of intensity may be affected by viewing distance and angle across the wall-display, and color intensity may vary across screens in tiled wall-displays [57]. We thus chose the size of elements, i.e., the thickness for the links and the radius for the node slices. While testing our prototype, we observed that as nodes have multiple incoming links, it is hard to identify which path and origin is responsible for the shortest distance that determines their size. Thus to avoid confusion and reduce clutter, we chose to only display distance information on the links.

As the thickness of selected links indicates their distance to the propagation origin node, the thicker the link the closer to the origin it is. We chose to display three visual levels of thickness: links with maximum thickness are linked to first-degree neighbors, ones of medium thickness link first and second-degree neighbors, and all remaining links selected through propagation have a similar minimum thickness. We found that more levels led to small variations in thickness that were hard to perceive in dense graphs. When a link is traversed multiple ways inside a selection (e.g., there are multiple origins in a selection, or the link belongs to multiple paths of different length), the link thickness is determined by the smallest distance to the closest origin in the selection.

3.2.3 Propagation Properties, Support for Graph Analysis

Multiple propagations allow multiple users to simultaneously explore different parts of the graph with their own color, examining connectivity relationships in different areas, as well as interactions between their selections made visible by the combined colors in nodes and links when propagations coincide. They also highlight relationships that may span large distances on wall displays, without the need for extensive physical movement.

Multiple propagations can also aid a single user to visually conduct basic set operations between selections. For example, the union of two or more propagation selections is the set of all the colored nodes. Their intersection are the nodes and edges colored by all respective colors simultaneously. And the difference of two selections (i.e. elements in one but not in the other), are all nodes and edges that colored by a single color.

Thus propagation from multiple nodes could be used to answer fairly complex topological questions, such as identifying all common neighbors of N-degree or less of multiple actors in a social network (union of N-level propagations), all the co-authors of one researcher that are not co-authors of her colleagues in a co-authorship network (difference of 1st level propagations), etc. We consider next topological tasks, such as the ones described by Lee et al. [37], that are well supported by propagation.

- Adjacency (direct connections): It is trivial to find and highlight the neighbors of a node by propagating one level. Nevertheless, there is no clear strategy for how to identify the node with most neighbors (highest degree) using the propagation technique.
- Accessibility (direct or indirect connections): This set of tasks are well supported by propagation. Nodes accessible from an origin are colored by the propagation. And the propagation level highlights nodes at distances less or equal to that level.
- Common Connections: To find the common neighbors of two or more nodes, we can propagate from each of these origin nodes and identify nodes that have both colors (i.e. belong to both propagation selections). And as before we control the distance of neighbors.
- Connected Components: To identify discrete connected components, i.e. subgraphs not connected to each other, we can choose a node and propagate until no more nodes are added, thus identifying a connected component. Repeating the process with uncolored nodes will identify the remaining connected components.
- Shortest distance between two nodes: The length of the shortest distance between two nodes can be found by propagating from one node and counting the number of propagation steps to reach the second. Nevertheless, determining the *actual shortest path* is more challenging: although the path is part of the propagated selection, it can be hard to identify it within all the selected elements, particularly in dense graphs.

This is a non exhaustive list of tasks well supported by propagation, and tested later on. More complex strategies could be devised for other tasks, to find for example articulation points or bridges (a node or link that is the only connection between two subgraphs).

3.2.4 Summary

Our adapted *Propagation* technique for interactive surfaces uses fast taps to expand, and a crossing gesture to backtrack. We support multiple propagations that can aid with several graph topology tasks. By design, propagation can select several nodes quickly, based on the connectivity structure of the graph, without requiring extensive moving around the wall-display. Nevertheless, it may cause visual disturbance in well connected graphs, as it will quickly span the entire graph, and it may disrupt the work of colleagues if links cross their work space.

4 EXPERIMENT 1: PROPAGATION VS. BASIC

It is unclear how *Propagation* and *Basic* selection will affect multiple users working on a wall-display. As there is little work on graph analysis on wall-displays in general, we also studied an individual user context, to tease out effects due to collaboration and ones due to the techniques.

As an instrument for this exploration we chose a well-defined topology task, the identification of the shortest path between two nodes, for several reasons. First, identifying the shortest path, or variations thereof, is a task used often in controlled graph evaluation studies (e.g. [59], [15]) and can be fairly involved in complex graphs. It requires an understanding of both the local context of nodes (identifying neighbors), as well as more global structure information, as a shortest path is not necessarily small in absolute distance. And as it is a well-defined, closed task, with an objective solution, it is well suited for controlled experiments. Second, the task is not clearly divisible, as a more global understanding of the graph structure is required. Thus it is unclear if multiple users working together would fare better than single users. As it can be performed individually, it gives us the opportunity to compare individual vs. multiple user work. Finally, and very importantly for our purposes, the task does not bias against *Basic* as it is not trivial to do with *Propagation*. As *Propagation* highlights a large number of possible paths (explained in section 3.2.3), this task could reveal issues with visual clutter caused by *Propagation*.

Based on the design and properties of the two techniques, we formulate the following general hypotheses:

H1 In both *Individual* and *Multi-user* contexts, performance (time & accuracy) will be better with *Propagation* than *Basic*.

H2 With both techniques, performance will be better in the *Multi-user* context than in the *Individual* context.

H3 *Propagation* will result in less participant movement, but will cause higher visual disturbance.

4.1 Experimental Design

4.1.1 Participants

We recruited 16 participants in pairs (6 females, 10 males), aged 23 to 39, with normal or corrected-to-normal vision. Pairs knew each other beforehand. Participants were HCI and visualization researchers or graduate students, with experience in reading graphs. Most (15/16) reported using at least once a day a device with touch interaction, and having already used a wall-display (13/16).

4.1.2 Apparatus

We used an interactive wall made of 75 LCD displays (21.6 inches, 3mm bezels each), composing a 5.9m × 1.96m wide wall, with a resolution of $14\,400 \times 4800$ pixels (Figure 1). The wall was driven by a rendering cluster of 10 computers. A PQ labs[2] multi-touch layer allowed for direct touch over the wall. Participants' positions were tracked by a VICON motion-capture system[3].

The experimental software ran on a master machine connected to the cluster through 1Gbit ethernet, and was implemented in Java using the ZVTM[4] Cluster toolkit [49]. The operator controlled the experiment progression using a smartphone running an android application implemented with the Smarties[5] toolkit [11].

4.1.3 Graph Types

We considered two different GRAPH types:

- *Planar*: These graphs can be drawn without edge crossings. Transport networks (e.g. subway or air-routing networks) are often planar. We generated them using an algorithm inspired by Mehadhebi [43] to design air route networks.
- *SmallWorld*: These illustrate the small-world phenomenon identified by Milgram [45] in social networks, where most actors are linked by short chains of acquaintances. Social networks, communication networks, and airline networks are often Small-world graphs. We generated them using Kleinberg's algorithm in the JUNG toolkit [48].

Planar-Low (N: 100 and L: 288)

Planar-High (N: 200 and L: 582)

SmallWorld-Low (N: 36 and L: 103)

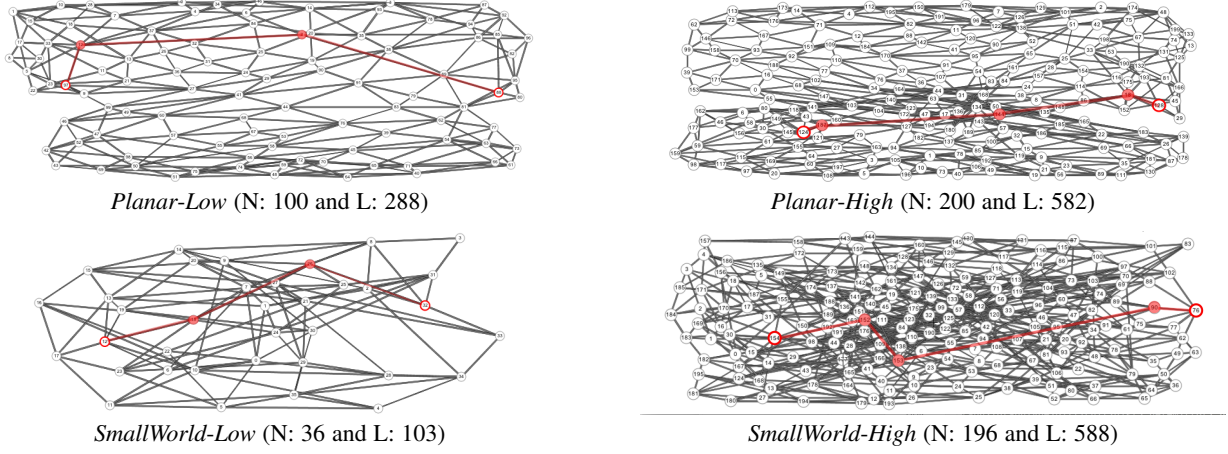
SmallWorld-High (N: 196 and L: 588)

Figure 3. Graph examples used in Experiment 1 with their number of nodes (N) and links (L). Colored paths are for illustration purposes only, and highlight the shortest path between the two target nodes. During the experiment participants were only shown the first and last node (target nodes).

In a pilot study (2 pairs) we tested three types of generated graphs: *Planar* and *SmallWorld* ones, as well as randomly generated ones inspired by Ware and Mitchell's [66] algorithm. Participants' performance with the random graphs was very similar (time, errors, subjective comments) to *SmallWorld* ones, and we thus removed them from the experiment.

4.1.4 Complexity
To explore graphs of different complexity, we created two variations for each graph type, *Low* and *High* COMPLEXITY. We generated them by varying structural characteristics, such as number of nodes and edges and mean shortest path, and visual aesthetic criteria that can affect readability, such as visual density and number of edge crossings [50]. Visual density is calculated as the ratio of pixels occupied by nodes and links, over the entire surface used to calculate the layout (discussed later).

GRAPH	COMPLEXITY	#Nodes	#Edges	Shortest Path	Visual Density	#Crossings
Planar	*Low*	100	288	4.27	0.06	179
	High	200	582	5.69	0.10	627
SmallWorld	*Low*	36	103	2.27	0.02	249
	High	196	588	3.55	0.12	4879

Table 1. Mean metrics of the graphs used in the experiments.

Table 1 reports mean values for the metrics of graphs used in the experiment. We note that our purpose was not to equate all metrics across graph types, but rather to create "difficult" and "easy" variations for each type (Figure 3). For high complexity graphs of all types (*Planar* and *SmallWorld*), we chose high complexity graphs with similar visual density, i.e. the amount of ink or clutter, and number of nodes and edges. For low complexity graphs we found in a pilot (1 pair) that tasks on *Planar* graphs with less than 100 nodes were trivial and did not require interaction. Thus for the low complexity variation of *Planar* we chose higher visual density than for *SmallWorld* ones.[6]

Density and crossings depend on the layout used to draw the graph. To ensure consistent drawing across graph types, we used for all graphs the ISOM layout [44]. We tested several layout algorithms, such as classic force directed ones [16, 18],

that position neighboring nodes close together and minimize edge crossings. Nevertheless, the tested force directed layouts [18] generated larger number of edge crossings compared to ISOM, a metric associated with readability [50], and did not uniformly fill our wall space. We thus moved to the ISOM layout that optimizes similar quantities to force directed layouts, while ensuring best coverage of our wall surface, and resulting into a smaller number of crossings. The ISOM layout is well adapted to planar graphs, but as other layout algorithms, it can lead to layout calculations that break somewhat the visual planarity of structurally planar graphs, as can be seen in Table 1. The same graphs and layouts were seen in both techniques (see Procedure), to keep this experimental factor consistent across techniques.

4.1.5 Task
Participants were asked to identify the shortest path between two target nodes. Target nodes were positioned in height at the middle 60% of the wall, thus not too high or too low to reach; and were spaced by a distance of at least 50% and 75% of the width of the wall to ensure paths were not too localized.

For each graph type and complexity we generated three variations to be used as "replications". In each of the three variations, we selected a path of LENGTH 3,4 and 5 respectively[7]. Paths of the given length were chosen automatically (using exhaustive search) to fulfill the following criteria: (i) the first and last node, that would become the "target nodes", met the above placement criteria; and (ii) all nodes in the path similarly fell into the middle 60% of the wall to ensure they were easily selectable.

4.1.6 Procedure and Design
The experiment was divided in two sessions, an *Individual* and a *Multi-user* one. To counterbalance these conditions, half of the participants did the *Individual* session first and half the *Multi-user* session first. In the *Multi-user* session, pairs saw both techniques (within-subject design), and the order of presentation was counterbalanced across groups. To end-up with an equal sample of group and individual sessions, in the *Individual* sessions each participant only saw one technique (between-subject design), chosen at random. *Individual* sessions lasted approximately 25 min, and *Multi-user* ones 40 min.

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[6] In our pilot we considered a no-interaction condition, but found that for our graphs (both *Low* and *High* complexities), tasks were respectively either very hard (double the time) or impossible to do without interaction to help trace one's process. Thus we did not test the "no interaction" condition further.

[7] The use of LENGTH as a replication factor was justified, as there was no interaction between LENGTH and TECH, CONTEXT, GRAPH (see Results).

Overall our mixed experiment design consisted of: 8 sessions (pairs or individuals) × 2 CONTEXTs (*Individual*, *Multi-user*) × 2 TECHs (*Basic*, *Propagation*) × 2 GRAPHs (*SmallWorld*, *Planar*) × 2 COMPLEXITIES (*Low*, *High*) × 3 LENGTHs (3, 4 and 5) = 384 measured trials.

For each TECH in both contexts, participants conducted 7 training trials before proceeding to the main experiment. Trials began with a screen indicating the position of the two target nodes, to ensure visual search was not required. Participants were then shown the actual graph with the target nodes highlighted. They then interacted with the wall display to find a shortest path, and when they had an answer they verbally indicated to the experimenter to stop the timer, and showed their solution. An experimenter followed the discussion to ensure they did not "cheat", i.e. report done before finding all nodes. No such cases were observed. If their answer was correct, they would proceed to the next trial. If their answer was wrong, the trial was marked as an error. Nevertheless, the task resumed and participants had to continue the trial until they found the correct answer. This ensured participants did not rush to give partially formed answers. At the end of the sessions participants filled a questionnaire on the perceived load and visual disturbance, and provided general preferences and subjective comments.

We chose a verbal indication of when pairs had reached a consensus, because in a third pilot (1 pair) we found that other procedures did not always ensure a consensus. We first provided each participant with a mobile device with a "done" button. We observed that choosing as a trial completion the first time one of the two participants pressed "done" was problematic, as they often did so while the other was still working. We also considered the time both participants had pressed "done", but found that some would occasionally forget to press their button while discussing with their partner. We next provided a single mobile device to only one participant. Although in most cases a very clear verbal agreement would take place before they pressed "done", occasionally the participant holding the mobile would forget getting verbal agreement and would press the button too soon. Thus we decided to enforce verbal agreement between participants, by asking them to instead tell the experimenter together when they were done, a process they practiced during training. When the two verbal indications were given the experimenter would log the time.

For each technique and context, participants were shown the *Low* complexity graphs first to ease them into the task, while the order of graph type and path length was randomized, but consistent, across participants. The same graphs were seen across techniques and collaboration contexts, but to avoid learning we used mirrored versions of the graphs on the x and/or y axis (resulting in 4 variations per graph).

Participants were instructed to be as fast as possible while avoiding errors. We recorded the time to the first given answer as our task completion time (*Time*), and the count of incorrect answers. We logged kinematic data of participants' movements using a motion tracking system, and video recorded the sessions.

4.2 Results

We report on the measures: (i) *Time* taken by participants to state for the first time that they completed the task, approximating expert behavior. When the first answer was wrong trials were marked as errors and the task would resume to discourage participants from rushing through trials (but the extra timing was not logged).

(ii) *ErrorRate*, i.e. the percent of trials where participants provided incorrect answers. (iii) *TraveledDistance* by participants in front of the wall. (iv) Subjective *rating* of visual disruption.

Statistical Method – Following recommendations from the APA [3], our analysis and discussion on continuous measures (*Time*, *TraveledDistance*) are based on estimation, i.e., effect sizes with 95% confidence intervals (CI). Our confidence intervals were computed using BCa bootstrapping. Error bars in our images reporting means, are computed using all data for a given condition.

When comparing means, we average the data by participants/groups (random variable) and compare the two conditions globally using a $(-1, 1)$ contrast (between-subject case), or by computing the CI of the set of differences by participants/groups (within-subject case). In our images we display the computed CI of the differences, and report the corresponding Cohen's d effect size, that roughly expresses the difference in standard deviation units. Finally, for completeness, we also report p values. These are computed as an approximation of the smallest $p \geq 0.001$ such that the $100.(1 - p)\%$ CI interval does not contain 0 (i.e., we compute the "largest" I-levels that lead to a "significant" result)[8].

To compare errors and Likert results we use non-parametric tests (Wilcoxon rank sum), which are more adapted to bi-valued and ordinal measures.

As mentioned, LENGTH was used as a replication factor, and as such is not considered as part of the analysis. Nevertheless, we conducted a-posteriori tests and verified that although there was a difference between the 3 length variations in time and errors, there were *no interaction* effects between length and interaction technique, context, or graph type. We also did not find any learning effects due to technique presentation order.

4.2.1 Time

Individual: When working individually, participants were faster with *Propagation* (29.3 s) than *Basic* (54.1 s). To better understand the nature of this difference, we looked separately at each COMPLEXITY and GRAPH. Our analysis (Figure 4) shows *Propagation* consistently outperforming *Basic*, with the effect being stronger in *SmallWorld-High* (most complex graphs).

Multi-user: Similarly, *Propagation* (22 s) was measurably faster than *Basic* (30 s) for pairs, even though the difference was not as pronounced. Looking at conditions in detail (Figure 5), the effect mainly exists in the *High* complexity graphs.

Individual vs. Multi-user: Individuals were slower with *Basic* (almost double the time) than with *Propagation*. This tendency was also visible in the *Multi-user* condition, although mainly for the larger graph sizes. This indicates that *Propagation* is more efficient, in particular for larger and complex graphs.

When we compare the *Individual* and *Multi-user* condition, mean times for both *Basic* and *Propagation* were better for pairs, but this difference was not measurable (Figure 6-left). However, examining the different complexities, we found a measurable time improvement for *Basic* when collaborating on *Low* complexity graphs, and a measurable improvement for *Propagation* when collaborating on *High* complexity graphs (Figure 6-right). This indicates that collaboration does not compensate for the weakness of *Basic* for complex graphs (in particular the *SmallWorld-High* ones). While with *Propagation*, one user is as effective as pairs for simple graphs, but that the collaboration benefit is seen in more complex graphs.

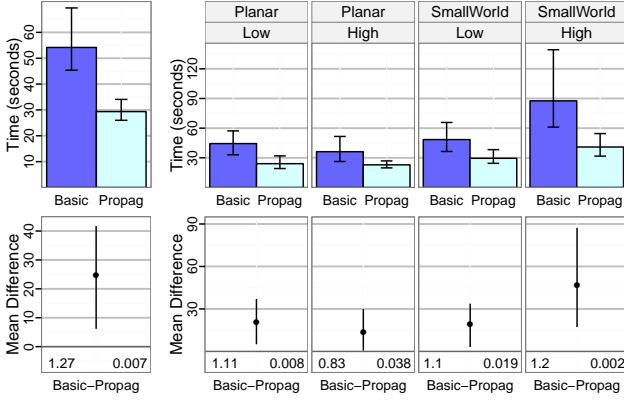[8] A CI of a difference that does not cross 0, can be read as "significant".

Figure 4. (Top) Average time to complet the task per TECH in the individual user case, aggregated on the left, and by GRAPH × COMPLEXITY conditions on the right. (Bottom) Corresponding 95% CIs for the mean differences *Basic − Propagation* used in analysis: bottom left numbers show the Cohen's *d* effect size and the right ones the *p* values. This convention is followed in all images.
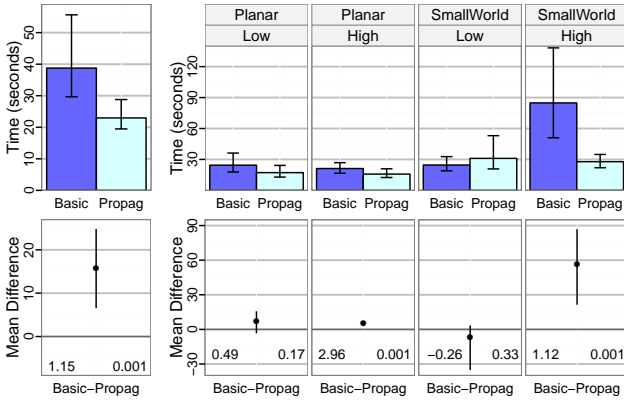

Figure 5. (Top) Average time to complet the task per TECH in the multi-user case, aggregated on the left, and by GRAPH × COMPLEXITY conditions on the right. (Bottom) Corresponding 95% CIs for the mean differences *Propagation − Basic*.
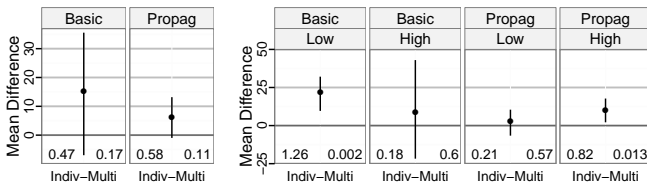

Figure 6. 95% CIs for mean time differences *Individual − Multi-user*, by TECH and by TECH × COMPLEXITY.
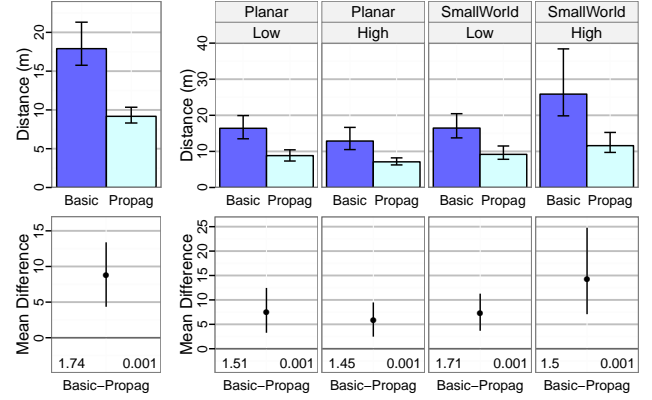

Figure 7. (Top) Average distance traveled by participant per TECH in the individual user case, aggregated on the left, and for each GRAPH × COMPLEXITY conditions on the right. (Bottom) Difference CIs for the analysis.
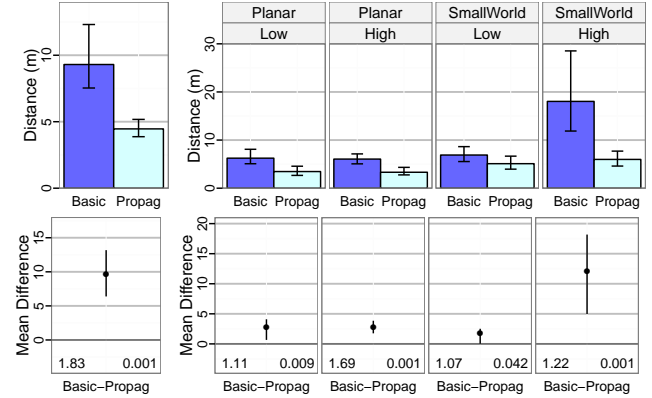

Figure 8. (Top) Average distance traveled by each participant per TECH in the multi-user case, aggregated on the left, and for each GRAPH × COMPLEXITY conditions on the right. (Bottom) Difference CI for the analysis.

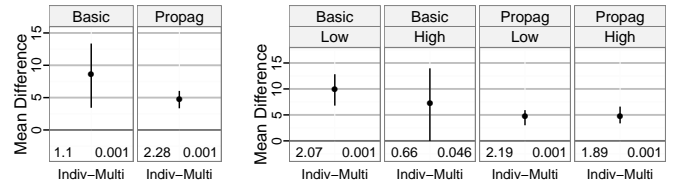Figure 9. 95% CIs for mean differences of the traveled distance *Individual − Multi-user*, by TECH and TECH × COMPLEXITY.

4.2.2 Error Rate

Individual: We observed no measurable difference in *ErrorRate* between *Propagation* (9%) and *Basic* (13%), even if mean error rate was lower for *Propagation*. Table 2 shows the error rate for the different conditions. We can observe that almost all errors (95%) occurred with *SmallWorld* graphs irrespective of TECH.

Multi-user: On the contrary, we measured a difference in *ErrorRate* between *Propagation* (3.1%) and *Basic* (16.7%) in the

collaborative case (*p*'s < .01). We observed that *Propagation* led to less errors in all conditions (*p*'s < .05), except in the *SmallWorld-Low*. Table 2 gives a break down for the different conditions.

Individual vs. Multi-user: Overall, the effect of *ErrorRate* was different for each technique across the individual and multi-user case. For *Propagation* there are marginally less errors when working in pairs (3.1%) compared to individuals (9.4%) (*p* = 0.066), with a very marked drop in error rate in the hardest graph *SmallWorld-High*, where pairs had an error rate of 8% compared to the 25% error rate for individuals.

We do not have such an effect for *Basic*, where error rate increased when pairs worked together (16.7%) compared to individuals (13.5%). When looking at different conditions, the trend was measurable for the *Planar* graphs (*p* = 0.023), but mean error rates were indeed higher for all conditions apart from *SmallWorld-Low*. We come back to this result in our discussion section.

| | aggregated | | Planar | | | | SmallWorld | | | |
| | | | Low | | High | | Low | | High | |
	Basic	Prop	Basic	Prop	Basic	Prop	Basic	Prop	Basic	Prop
Indiv.	13.5%	9.4%	0%	4.2%	0%	0%	16.7%	8.3%	37.5%	25.0%
Collab.	16.7%	3.1%	8.3%	0%	12.5%	0%	4.2%	4.2%	41.7%	8.3%

Table 2. Error rate per TECH, aggregated and by GRAPH × COMPLEXITY conditions, in the individual user case and in the multi-user case.
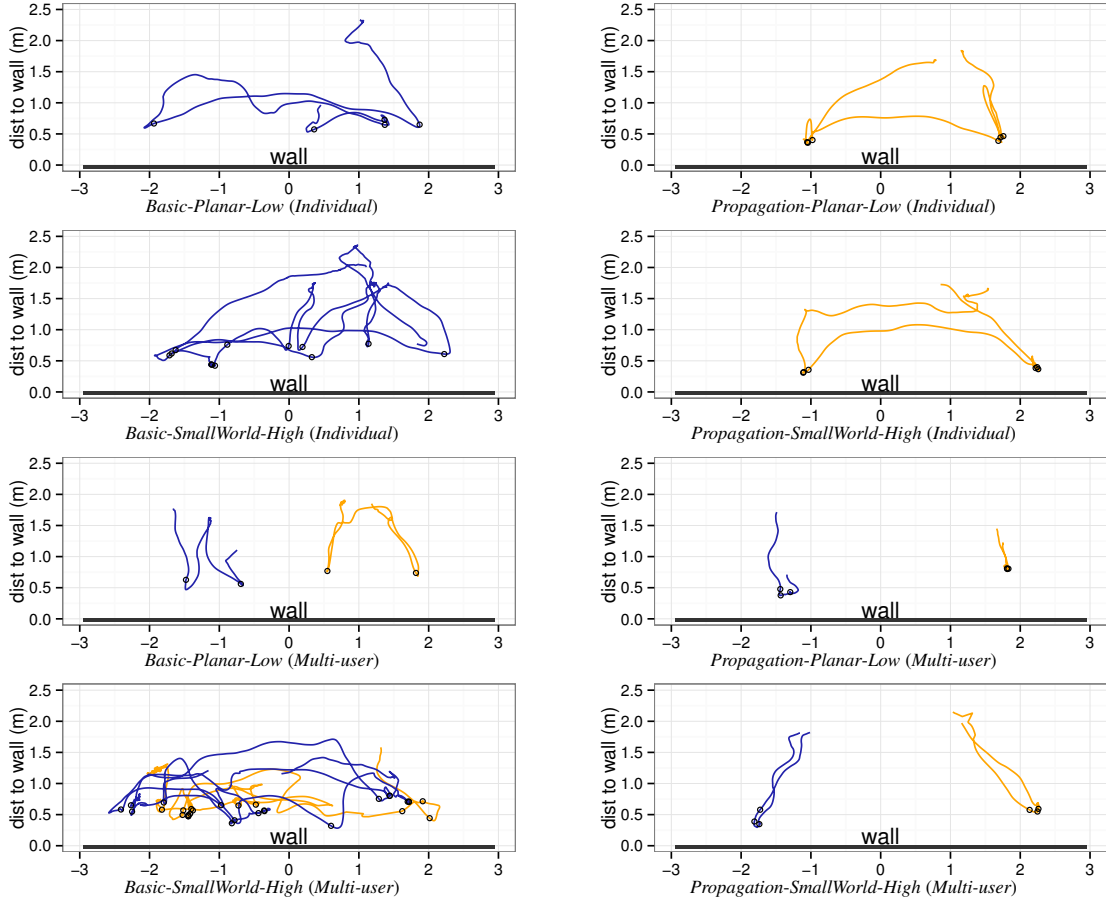
Figure 10. Bird's eye views of the movement of participants in trials for individual (2 top lines) and pairs (2 bottom lines), under the condition *Planar-Low* (easiest) and *SmallWorld-High* (hardest). *Basic* is seen in the left column, and *Propagation* in the right column. The wall is at the bottom of each graph, the unit is the meter, and the black little circles (○) indicate a touch interaction.

4.2.3 Distance Traveled

Individual: The amount of movement in the individual case was higher for *Basic* (17.9m) than for *Propagation* (9.2m), almost twice as much (three times in complex graphs), and the effect exists for all GRAPH × COMPLEXITY conditions (Figure 7).

Multi-user: Similarly, the distance covered by each participant when working in pairs was less with *Propagation* (4.6m) than *Basic* (9.3m), in all conditions (Figure 8).

Individual vs. Multi-user: As expected the distance traveled by participants in individual sessions is about twice that traveled by each participant in *Multi-user* sessions for both techniques (Figure 9-left). However, as shown in Figure 9-right, this effect is strong for *Propagation* for both *Low* and *High* complexity graphs, but only for *Low* complexity ones for *Basic*. This reinforces that the gain of working in pairs is less with *Basic* in complex graphs.

Figure 10 illustrates these results with examples of participant trajectories in front of the wall. Pairs tend to divide their work spatially, with the exception of using *Basic* in *SmallWorld-High*. Nevertheless, video recording indicates that even here participants start the task by dividing the space, but as they cannot reach a solution, they start moving more around the space to verify their work, stepping back likely to get an overview. Thus, these patterns are not just due to the need to reach nodes to interact with, but also due to the nature of collaboration using *Basic* in complex graphs.

4.2.4 Observed Strategies

Individual: Instead of propagating from a single node, all individuals using *Propagation* selected one node, propagated typ-

ically one time (sometimes two), and then moved to the second to propagate, alternating between the two until they saw an intersection (two-color node). This strategy reduced the number of selected nodes and visual clutter (less propagation steps), helping them identify the shortest path as intersection points are inside it.

The strategy used for *Basic* was different. Participants consistently selected a subset of neighbors that seem to be between the two nodes, trying to reconstruct short paths moving from one node to the other. This was successful for the smaller and less complex graphs, but did not work well for the hardest condition *SmallWorld-High*, where participants had to consider a large number of nodes, as seen by the high error rate in this condition.

Multi-user: When performing the task in pairs, participants were again consistent in their strategy. With *Propagation* it was similar to the individual sessions, but now each participant took charge of one of the two nodes, and propagated alternatively (but not concurrently) until they found intersecting nodes. They coordinated this asynchronous double-propagation using verbal communication. Then, both participants reconstructed together a shorter path candidate, each taking responsibility of their own end of the propagation. In more complex graphs, they occasionally checked each other's work (6 groups).

For *Basic*, participants again took charge of one node each, and tried to define paths using selections towards their partner, until they reached each other's work area. They worked more or less independently, and in parallel, until they started finding intersection nodes. After that, for the more complex *SmallWorld*

graphs, they tried checking together candidate paths before making their choice (e.g. Figure 10 bottom-left graph, notice movement overlap). But, pairs did not double check each other's work in the easier *Planar* graphs (e.g. in Figure 10, 3rd row on the left, we see no movement overlap), which may explain the increased error rate. There was one notable strategy exception, one group decided to propagate systematically, simulating on their own the *Propagation* technique (which they had seen first).

4.2.5 Subjective Comments

Individual Users: Answers to the quantitative questions of the questionnaire (physical demand, visual disturbance, enjoyment) was very similar between the two TECH (p's = 1). This is not very surprising given that we used a between-subject design for TECH.

Multi-Users: After the collaborative session participants were able to directly compare the two techniques. All 16 preferred *Propagation*. On a 7-point Likert scale participants found that *Propagation* was less physically demanding (Avg=2.5, SD=1.2) than *Basic* (Avg=4, SD=1.6) since they were required to walk less (p's < 0.05). They also found *Propagation* more enjoyable (Avg=5.3, SD=1.1) than *Basic* (Avg=4.1, SD=1.2).

Surprisingly, they also found *Propagation* to be *less* visually disturbing (Avg=2.9, SD=1.6) than *Basic* (Avg=4.8, SD=1.8) (p's < 0.05), contrary to our hypothesis. When asked to explain why they found *Propagation* less visually disturbing, they explained that *Propagation* helped highlight paths of interest *"helps to see how many possible shortest paths there are, which is very convenient"*. Although four mentioned explicitly in their comments the existence of visual disturbance in *Propagation*, they commented that the visual footprint was desirable for tracking their work *"it gets visually disturbing very quickly after a few propagations, but it is good to be able to see the changes when we can go back and forth with the propagation easily."*.

When asked if they preferred conducting the task individually or collaborating with a partner, participants had mixed opinions. Six out of the eight that run the individual session with *Propagation* preferred to run the experiment in pairs with *Propagation*, instead of alone. As one explained *"having a partner is easier because there's someone to help check whether the answer is correct or not and I don't have to move around. However I'm not sure if doing it together is faster because sometimes communicating takes time"*. Five out of eight participants that run the individual session with *Basic* preferred to do the task in pairs with *Basic*. But, as one participant explained *"it happens that the other was exploring different solutions than me* [parallel work]*, so he was disturbing me"*. Thus, overall the multi-user context was been only slightly preferred than the individual context.

4.2.6 Discussion

Propagation was faster than *Basic* selection when identifying shortest paths, particularly in the more complex small-world graphs (confirming *H1* on time). This can be explained by participants moving more with *Basic*, twice as much overall and three times for complex graphs (confirming *H3* on movement). This is backed by subjective comments reporting less fatigue and higher preference for *Propagation*.

When moving from individuals to pairs, the mean time of both *Propagation* and *Basic* was faster, although this difference was not measurable overall. But there is a clear speed-up for complex graphs with *Propagation*, and for easy graphs with *Basic* (partially confirming *H2* on time). These differences are likely due

to participant strategies. Individuals were fast with *Propagation* to begin with, and since pairs spent time coordinating and taking turns propagating, speedup due to collaboration is not visible. But as we move to more complex tasks, the cost of coordination drops compared to that of the task. On the other hand, individuals were slow with *Basic*, and as pairs worked in parallel first and combined their results later, this accelerated the work with simple graphs. But in more complex graphs this strategy was not effective, and collaboration did not compensate for the weakness of *Basic* when dealing with complex graphs.

Collaboration had an effect on accuracy. It increased when passing from individuals to pairs in *Propagation* (partially confirming *H2* on accuracy), particularly in the most complex graphs. Participants chose to closely coordinate their actions taking turns to avoid visual interference (supporting *H3* on visual disturbance). Thus it is possible they had increased workspace awareness [14], a fact supported by the ease with which they double checked each other's work. The colored propagation queries provided a filter to the interesting areas of the graph, that also helped participants focus more effectively on both their partner's and their own work, leading to the unexpected subjective feeling that propagation was less visually disturbing (subjective feel contrary to *H3* on visual disturbance). Surprisingly, accuracy decreased for *Basic* when moving to the collaborative setting. This can be explained by the adopted strategy of conducting part of the task independently, thus lacking a "big picture", that participants were forced to adopt in the individual case. This big picture is crucial for tasks such as shortest path identification, where dividing the task into spatial subtasks is not straightforward[9].

4.2.7 Summary

The two techniques, *Propagation* and *Basic*, support collaboration and wall display interaction differently:

● *Propagation* is promising for individual work for the shortest path finding task, requiring little physical movement. In group work it leads to increased accuracy, but no measurable increase in speed as there is an overhead related to coordination due to its visual footprint. Thus tight coordination, combined with the technique's highlighting of areas of interest, helped maintain an understanding of partners' work and increased accuracy.

● The *Basic* technique is as accurate when dealing with simple graphs for individuals, but considerably slower. And its performance degrades with more complex graphs. More importantly, when pairs divide tasks spatially, it can lead to loss of awareness of partners' work, resulting in loss of accuracy in collaborative work (compared to individual) when task division is not straightforward.

5 EXPERIMENT 2: OBSERVATIONAL STUDY

In the previous study we focused on a single controlled task that is not clearly divisible and parallelizable in its nature. Although pairs naturally took responsibility of one node, an overview of a larger area of the graph is required to correctly address the task. This is true for most low level graph analysis tasks suggested in the literature [37]. Nevertheless, studying them gives us insight as to how users can appropriate existing techniques in a collaborative manner. For example, *Propagation*, which quickly affected a large part of the graph, required explicit coordination. We examine, now, if this is true for other low level tasks.

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9 For example, when choosing among shortest path candidates, considering only the left half of paths is not enough to identify good candidates.

More specifically, we are interested in assessing *Propagation*, that proved more promising, as a general graph exploration technique, observing if pairs can "discover" on their own how to perform new tasks without task specific training. And in whether they adopt similar coordination strategies as in Exp 1. Thus we are less interested in recording time, and more in observing if and how pairs collaborated.

5.1 Experimental Design

5.1.1 Participants & Apparatus

We recruited 8 volunteers (4 females, 4 males) in pairs, aged 23 to 39, with normal or corrected-to-normal vision. Pairs knew each other and had taken part in Exp 1. Sessions lasted 30min, using the same apparatus as in the first experiment.

5.1.2 Tasks

Groups performed the following topology tasks [37]:

T1 Find the shortest *distance* between two nodes (as opposed to the shortest path as in Exp 1).
T2 Find the common neighbors of degree 2 between two nodes.
T3 Find all connected components.
T4 Find an articulation point between connected components.
T5 Open exploration, reporting interesting observations.

5.1.3 Graph Types

In *T1* and *T2* we used high complexity small-world graphs similar to Exp 1. In *T1* the shortest distance was 6 and the two target nodes were separated by a physical distance of about 75% of the wall width. In *T2* the two target nodes were closer (about 50% of the wall width) and had 5 common neighbors.

In *T3* and *T4*, we combined unconnected small-world graphs (20 nodes each) of high complexity: three in *T3* (60 nodes in total) and two fin *T4* (40 nodes). To complicate the tasks, we tweaked the layout to get overlap between subgraphs. And in *T4* we hid the articulation point connecting the subgraphs inside one of them.

The graph used in the open task *T5* (similar to Figure 1) consisted of three subgraphs of different densities, and two unconnected nodes. Two subgraphs where connected through an articulation point, hidden within the third subgraph. These were the insights we wanted our participants to identify. The layout was tweaked so that subgraphs were not easy to separate visually.

5.1.4 Procedure

Participants were first reminded of the propagation technique, but no task specific training was given. Then the experimenter introduced the task without giving instructions on how to solve it, and participants performed the five tasks in order. Participants indicated they were done verbally, in a way similar to Experiment 1. If participants succeeded on their first trial within a timeout limit of 3000sec (5min), they moved on to the next task. If they failed, a strategy to solve the task was explained to them, and they were presented with another trial for that task. If they failed again, they were given a final trial, and then moved to the next task.

The experiment was recorded, and one experimenter took notes. A second experimenter gave instructions and logged the time (as in Exp 1). At the end, we asked participants if they had any suggestions for improving the technique, their thoughts on collaboration, and how confident they were in their answers.

Tasks	Discovered	Avg.Time (SD)	Correct
shortest distance	✓ (4/4)	63.5s (SD=21.9)	✓ (4/4)
2nd degree neighbors	✓ (4/4)	77.6s (SD=90.3)	✓ (4/4)
connected components	✓ (4/4)	47.6s (SD=22.4)	✓ (4/4)
articulation point	X (0/4)	timeout (3000s)	2nd try (3/4)
			3rd try (1/4)

Table 3. Summary of findings for specific Tasks T1-4, indicating whether our pairs were able to discover how to perform a task, and the time it took them to do so (mean and SD). If they did not discover a strategy on their own within the timeout period, column Correct indicates on what try they succeeded.

5.2 Results

We report next participants' success in discovering a correct strategy and time averages logged during the experiment, as well as the strategies they adopted based on video log analysis and notes taken in the experiment.

5.2.1 Discovering

All pairs discovered without any training correct strategies for identifying the shortest distance between two points, the common neighbors of degree two, and the connected components (*T1-3*). No pair was able to develop a correct strategy for finding an articulation point (*T4*), but three pairs understood how to identify possible candidates. After instruction, three pairs were able to perform a new *T4* trial, and one pair on their third attempt.

All pairs conducted *T1-T3* within the time limit, with connected component completed faster 47.6s (SD=22.4), followed by shortest distance 63.5s (SD=21.9) and 2nd degree neighbors 77.6s (SD=90.3). The larger mean time and standard deviation of 2nd degree neighbors is due to one pair that did an extensive verification of their answer (described next in strategies). We note that the times reported here include both the discussion of strategy and the actual interaction to find the solution. Table 3 summarizes the discoverability of strategies and the time taken by our pairs.

In the open task, three pairs found four out of five possible insights, and one pair found all insights within the time limit. All pairs found two connected subgraphs and identified an articulation point between them. They also verified that the third subgraph was disconnected, and identified the extra disconnected nodes. One pair noticed the differences in the density of the subgraphs by calculating shortest paths.

5.2.2 Observed Strategies

We describe next the strategies adopted by participants, focusing on how they coordinated, and report their subjective comments.

Shortest Distance: In all pairs, each participant propagated from one of the two target nodes, until one or more nodes were selected by both their colors. They took turns propagating and observed each other's work so as not to loose count of the total propagation steps performed. One pair also used the thickness of edges to confirm that bi-selected nodes were at a distance of 3 from each target node.

Common Neighbors of degree 2: All pairs propagated two levels from both target nodes and then counted the number of nodes selected in both colors. Two pairs worked independently first (propagated in parallel) and checked later the bi-colored nodes together. Of these pairs, one backtracked their propagation to verify all bi-colored nodes were neighbors of degree two exactly, rather than neighbors of degree two or less for one of the nodes. The other two took turns propagating and looking at their partner's work, ensuring they considered neighbors of exactly degree two.

Connected Components: All pairs discovered that the best strategy was to start propagating from nodes that seem distant, and if one propagation no longer had an effect (no more nodes added) they had identified and fully selected a connected component. Two pairs worked in parallel, propagating in different areas simultaneously. While the other two took turns propagating and observing. One such pair had a discussion at the end of the task, noting they could have interacted in parallel to be more efficient.

Articulation Point: This task was more complex, even if the concept of articulation was easy to understand by all participants. No pair managed to find a correct strategy on their own. Nevertheless, three identified several possible candidates using propagation (including the actual one), although they were unsure how to proceed with proving it. The strategy of all pairs consisted of propagating from nodes in different areas in the graph and consider bi-colored nodes. But they did not verify that all following propagation steps between subgraphs passed through their candidates. After this strategy was explained, three pairs succeeded in their next try, while the last pair ran out of time and succeeded in its third attempt.

Open Exploration Task: Being inspired by the previous tasks, all pairs began by propagating from far away nodes and found the subgraphs connected by an articulation point, and the third disconnected subgraph. Pairs mixed their strategies, propagating in parallel at the very beginning of the exploration, and then coming together to discuss hypothesis and taking turns propagating and observing.

5.2.3   Subjective comments

All participants felt confident in their answers and strategies, especially for the first three tasks. Six commented that collaboration increased their confidence in their solutions. When prompted about their coordination strategy, four explained that taking turns helped them be more aware of each other's work, while two mentioned that sometimes they still lacked awareness of each other's work when working at distant locations. Three participants also commented on the visual footprint of propagation: occasionally the colored query of their partner would enter their work area, causing some visual disturbance, while rarely they also missed the effects of their own propagation when it was far away from their location. Nevertheless, these participants also mentioned that these colors helped them verify their partner's work.

They all felt the articulation point task was difficult, and three users independently suggested extending the propagation selection to better support this task, for example by being able to "block" a node and prevent propagation from going through it, or removing nodes temporarily. Four participants commented that it was sometimes hard to tell how many propagation steps they had performed, and suggested adding it as a small number close to the propagation origin. These last two features were implemented. Two participants requested the possibility to collapse and bookmark propagation queries for later use, and another two suggested the option to propagate using a different color within an existing propagation.

5.2.4   Summary

Participants were able to devise correct strategies for the majority of tested tasks, and in the articulation point task identify good candidates, demonstrating that the extended *Propagation* is an interesting general purpose technique for graph exploration. As

in Exp1, participants divided the space and mostly took turns propagating (with few exceptions). We got several comments indicating that the reason for this turn taking was to coordinate and keep awareness of others' work, but also to avoid visual disruption due to the global footprint of the technique. Nevertheless, this global footprint also helped them check each other's work quickly.

6   DISCUSSION AND DESIGN IMPLICATIONS

We examined how pairs and individuals work on wall-displays to solve low-level graph topology tasks. Our findings indicate that:

Exploring complex graphs individually requires interaction that highlights the structure of the graph, while basic interaction is enough for simple graphs. Wall-displays can comfortably display large graphs, nevertheless it is still challenging for individuals to explore complex graphs such as large small-world ones. Here we observed a significant benefit in using advanced interaction techniques, such as *Propagation* selection. For individuals, *Basic* selection did not scale well for complex graphs, nevertheless it performed reasonably well for simpler planar graphs.

Collaboration improves accuracy only *if techniques allow verification of partners' work.* Pairs were more confident in their responses than individuals with both techniques. Nevertheless, their actual accuracy improved only for *Propagation*. On the contrary, pairs using *Basic* were more error prone than individuals. Our observations and participants' comments indicate that this is because with basic selection it is difficult to acquire an overview of all choices considered by one's partner, and thus maintain a global view of the work and identify possible errors. On the contrary, with propagation selection it was easier to verify at a glance the work of one's partner and check for errors. In collaborative graph exploration, lack of workspace awareness [14, 19] can decrease accuracy, compared to individual work.

Even when tasks are not clearly divisible, pairs divide the wall spatially. For many topology tasks identified in the literature, and used in our experiments, there is no clear strategy to divide them in space, as they may require a global understanding of subgraphs that extend across the display. Nevertheless, irrespective of task and technique, pairs divided the wall spatially. Even when not optimal, they each took responsibility of one part of the wall and then combined their work, with mixed results. This division was observed in tasks that are clearly spatially divisible [32, 39, 62], but not in tasks that are not clearly spatially divisible, such as route planning tasks [59]. Designers should anticipate this division of space and encourage tighter collaboration (discussed next) when tasks are not spatially divisible.

If a technique has a global footprint, tight coordination is adopted. Although pairs occasionally worked in parallel with *Propagation*, they mostly took turns, working on different sections of the wall. They commented that this tight coordination was needed because the technique had a visual footprint that could reach all areas of the wall, risking disturbing the partner's work. Theoretical work on automated graph exploration using a variation of propagation [12] has shown that automated agents with full knowledge of others' exploration (i.e. high awareness) tend to explore the graph fully more quickly. Given our findings on propagation accuracy and the theoretical result on efficiency, designers could use techniques with large visual footprints to *encourage* close collaboration that can increase accuracy and efficiency. This is complementary to findings that when collaborating loosely, participants *chose* techniques with local visual footprints [59].

Consider awareness vs. disruption tradeoff in techniques. Participants' comments indicate there is a clear tradeoff between awareness and visual disruption. *Propagation* can be visually disrupting and affect the partner's work, but it also provides higher degree of workspace awareness [14, 19]. While *Basic* has a small visual footprint and is less disturbing, but pairs can loose track of their partner's work due to the wall size and graph complexity. Both types of techniques should be supported, and collaborators should be able to transition between them depending on how tight their work coupling is [59], and how divisible their task is.

Provide techniques that do not require extensive walking. Free walking is beneficial in wall displays [6, 10]. Nevertheless, techniques that require users to repeatedly walk to interact with different areas of visualizations (such as *Basic*) are fatiguing. Designers should provide interaction alternatives that can be activated locally but act globally, such as *Propagation* or ones proposed in the HCI literature for remote reaching [9, 56] and data manipulation [39]. Alternatively, designers could provide a combination of touch and distant interaction (e.g. using mobile devices) to ensure users can perform large scale or remote interactions across distances.

7 CONCLUSION AND FUTURE WORK

In this work, we study two selection techniques for graph exploration on wall-displays, used by individuals and multiple users. We adapted two existing techniques for use by multiple users on a touch enabled display, a basic selection, and a propagation selection using the idea of transmission. We performed a user study that showed *Propagation* to be faster in both individual and multi-user contexts, to be more accurate for multiple users, and to require less movement than *Basic* in a shortest path identification task. It is also versatile enough to be used in a series of topology tasks, observed in a second study.

Nevertheless, as *Propagation* has a large visual footprint, it requires higher coordination when used by multiple users. When working in pairs, propagation selection increases accuracy overall, but due to a coordination cost it improves time only for complex graphs. When using basic selection, that has a small visual footprint, accuracy dropped for pairs, most noticeably in complex graphs. Indeed, we observed that using basic selections, participants tended to work independently and lose awareness of each other's work, which proved detrimental for the task we consider, that is not clearly divisible. We conclude with design implications, stressing the tradeoffs of techniques with global vs. local visual footprints, and the need to allow users to switch between such techniques depending on whether the task is spatially divisible, and on the nature of collaboration (loose or tight).

A possible future direction includes improving the propagation technique. As other multicolor query selections, it prevents the use of color for encoding other information on the graph. We plan to explore other visual encodings, such as motion [65], that nevertheless need to be considered carefully when applied to techniques that feature a large visual footprint in multi-user settings. More generally, we plan to investigate design variations for propagation that reduce this global footprint, for example re-layout the graph to move selected nodes closer together. Nevertheless, as we are dealing with multi-user settings, care must be taken to limit colleague disturbance. Finally, we plan to explore visualization techniques to better emphasize grouping of nodes belonging to one [35] or multiple selection groups.

As this is the first work to examine how multiple users that move freely to explore graphs on walls displays, we focused on fairly controlled topology tasks. We next plan to investigate more open ended exploration tasks, where we suspect task division will be different. Moreover, we plan to explore different types of input, for example combinations of touch and distant pointing, to better support user mobility.

Although the idea of multiple propagations was used in the context of a collaborative vertical surface, we believe it has potential in horizontal tabletops, but also in desktop settings, and should be further studied. It can also be adapted to serve other graph representations such as directed graphs and matrices, and for dynamic graphs [5, 2].

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