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Numerical and experimental investigation of mucociliary clearance breakdown in cystic fibrosis

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Abstract

The human tracheobronchial tree surface is covered with mucus. A healthy mucus is an heterogeneous material flowing toward the esophagus and a major defense actor against local pathogen proliferation and pollutant deposition. An alteration of mucus or its environment such as in cystic fibrosis dramatically impacts the mucociliary clearance. In the present study, we investigate the mechanical organization and the physics of such mucus in human lungs by means of a joint experimental and numerical work. In particular, we focus on the influence of the shear-thinning mucus mobilized by a ciliated epithelium for mucociliary clearance. The proposed robust numerical method is able to manage variations of more than 5 orders of magnitude in the shear rate and viscosity. It leads to a cartography that allows to discuss major issues on defective mucociliary clearance in cystic fibrosis. Furthermore, the computational rheological analysis based on measurements shows that cystic fibrosis shear-thinning mucus tends to aggregate in regions of lower clearance. Yet, a rarefaction of periciliary fluid has a greater impact than the mucus shear-thinning effects.

Keywords: Computational biology, Cystic fibrosis, Mucociliary clearance, Modeling, Rheology, Partial differential equations, Hybrid grid-particle methods.

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1 1. Introduction

The human respiratory tract (nose, pharynx, larynx, trachea, bronchi, bronchioles, and alveoli) and its related cavities and conduits (sinuses and Eustachian tubes) has a wetted surface covered with mucus flowing toward the esophagus. Human conducting airways are lined with a pseudostratified, secretory, and ciliated epithelium (with ciliated, secretory, and basal cells) coating submucosal glands as well as cartilaginous structures in some segments of the respiratory tract such as partial or complete rings in the proximal part of the tracheo-bronchial tree.

An efficient mucociliary transport requires an appropriate mucus composition for optimal clearance, adequate production of periciliary fluid and number of functioning ciliated cells, and coordinated motion of cilia for mucus propulsion, as well as respiratory epithelium integrity over long distances. The mucociliary clearance protects the airway epithelium against inhaled pathogens and noxious entrapped micro- and nanoparticles. The mucociliary clearance also influences drug delivery to airways, drug absorption at a given station of the respiratory tract depending on the local rate of mucus transport.

The present study focuses on impaired mucociliary transport in cystic fibrosis. Cystic fibrosis (CF) is one of the most common life-shortening genetic diseases. It is observed on 1 in every 2500 infants in Europe and North America. It is most common among Caucasian population (1 in 22 individuals is a heterozygous carrier). The heterozygote frequency reaches 4% of the population of Western world. The prevalence of cystic fibrosis per 10000 inhabitants in the United States of America is 0.797 and is on average 0.737 in the 27 European Union countries (with a remarkable 2.98 in the Republic of Ireland) [23].

¹⁹ Defective mucus composition alters mucociliary transport. Impaired chloride transport in cystic fibrosis prevents ²⁰ normal hydration of mucus, leading to highly viscous accumulations. Cystic fibrosis airways are characterized by ²¹ airway surface liquid volume depletion and mucus accumulation, thereby hampering airway clearance of inhaled ²² pollutants and pathogens [17].

Our numerical and rheological investigations aim at providing an independent and self-consistent analysis of mucociliary clearance altered by cystic fibrosis allowing full reproducibility. Questions needed to be answered encompass the role on mucus viscosity of the disease itself, associated infection, and influence of the periciliary fluid (PCL). Current models assume two Newtonian layers of different viscosities or a single complex fluid [39], or two layers with a constant visco-elastic parameter superposed to a spatially varying diffusion [30]. In the present article, a rheological hydration/maturation law incorporates the mucin transfer through a Newtonian periciliary fluid and mucin meshwork formation in a non-Newtonian mucus layer (ML) with smooth and sharp transitions.

Many rheological laws have been used in the literature, from shear-thinning to viscoelastic models but non-shearthinning (Maxwell [40, 56], Oldroyd B model [44, 43, 30]), viscoplastic (Bingham [66], Carreau [41], and Herschel-Bulkley [37] constitutive laws). Mucus rheology depends on the context (mucus conservation, illness severity, treatment effect, mucus source, sampling mode, etc.). As mentioned by Besseris and Yeates [5]: "no constitutive law ever was proposed for this material because it was never clearly classified either as a chemically or physically linked gel".

The major issue of this study is to quantify the mucociliary clearance and to investigate the influence of the highly shear-thinning nature of mucus. To do that, a state-of-the-art solver is used to compute the variable-viscosity Stokes problem in a mobile domain due to beating cilia [8]. This model deals with noncartilaginous ciliated walls of the tracheobronchial tree, where the ciliated surface is assumed to be periodically flat.

This article is structured as follows. Firstly, the experimental method is described from samples collection to measurement validation. Secondly, we introduce the mathematical model for flow and maturation which enables the transition from the Newtonian PCL to non-Newtonian ML. The numerical method solving efficiently this heterogeneous fluid dynamics around beating cilia is then described. It involves only standard elliptic problems and avoid matrix assembly, thereby leading to a low storage method [9]. This is then applied to a wide range of rheological parameters, which gives a cartography of mucociliary efficiency. This allows comparison of our data with literature data.

In addition to the agreement between experimental observations and numerical parametric studies, the situation of healthy and pathological mucus is achieved on a map. A collection of these maps is finally provided in order to quantify the impact of PCL reduction on mucociliary clearance.

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2. Rheology measurements and experimental setup

The main and mandatory property for numerical simulations of shear-thinning fluids is the viscosity function $\eta(\dot{\gamma})$ with respect to the shear-rate $\dot{\gamma}$, the full contraction of the symmetric part of the gradient of the fluid velocity *u*:

$$\dot{\gamma} = (2D(u):D(u))^{1/2}$$

where $D(u) = (\nabla u + \nabla u^T)/2$. Two types of equipments are used to assess this parameter: classical rheometers with a cone and plate or parallel plates geometry [42, 54, 58, 61], and magnetic microrheometers which only allow small amplitude oscillatory motions [34, 49, 67].

Experiments were carried out on a Mars III rheometer (Thermo Sc.) equipped with a cone and plate geometry (angle 1°, diameter 35 mm) which requires a small volume of fluid (0.2 ml). Measurements were conducted at the body temperature ($37^{\circ}C$). The lower plate Peltier system for temperature regulation was completed by a home-made sample hood with a specific temperature regulation and wet sponges to saturate the measuring chamber and to prevent samples evaporation.

The rheological characterization consists of dynamic measurements (small amplitude oscillations) with determination of the linear domain followed by measurement of the storage G' and loss modulus G'' as functions of the oscillation frequency ω . $G'(\omega)$ and $G''(\omega)$ are respectively the elastic (in-phase) and viscous (out-of-phase) components of the complex modulus $G^* = G' + iG''$ which is the ratio between shear stress and strain during oscillation measurements. The viscosity $\eta(\dot{\gamma})$ was then determined by a steady shear flow test for shear rates ranging from $10^{-3} s^{-1}$ to $10^3 s^{-1}$. A special attention was paid to reach a steady state regime for low shear rate values.

15 2.1. Methodology validation

¹⁶ Mucus was sampled during consultation (in stabilized CF patients as well as in a patient with bronchiectasis ¹⁷ without CF) or hospitalization (both decompensated or stabilized post-therapeutic states). Samples were frozen before ¹⁸ transport and processing. Comparison between fresh and frozen mucus (freezing duration 21 and 30 days) were ¹⁹ carried out on three samples and confirmed that the freezing does not alter the rheological propoerties as it was ²⁰ already observed by Sanders et al. [50] and Rubin et al. [49].

Thixotropy is sometimes mentioned in mucus studies and related measurements [46]. For a given patient, when the mucus sample volume was sufficient, shear viscosity was successively measured on the same and on different samples. The dispersion observed using these two series of measures was similar, that is, thixotropy was comparable to the natural dispersion arising from heterogeneity of the sample. The weak thixotropy was already observed in viscosity measurements for increasing and decreasing shear rate [65]. In addition, no phase separation was observed during defrosting and during measurement.

²⁷ Fifteen mucus samples were analyzed and among them two were rejected. They were visually too heterogeneous

and gave rise to a large dispersion in viscosity and modulus values.

2.2. Rheological results

A shear-thinning behavior is observed in the entire shear rate range. The storage modulus $G'(\omega)$ and the viscous modulus $G''(\omega)$ clearly display the viscoelastic character of mucus. These curves cross each other at a frequency ω_c . The characteristic time defined from ω_c is of the order $10^2 s$.

A power law model $\eta = K\dot{\gamma}^{N-1}$ was fitted on the shear rate range $[0.01 - 100 \, s^{-1}]$, which is representative of shear rate involved in the studied flow. Values for the power-law index *N* and the consistency *K* are obtained by mean-square log-fitting of measures (see Fig. 1 and Table 1). Three examples of steady-state shear viscosity curves for different mucus from two to three measurements, each on different mucus samples are displayed in Fig. 1. These curves illustrate both the usual intra- and inter-subject variability of any biological material.

Few literature data on human airway mucus are available for steady state viscosity, whereas numerous data exist for complex viscosity $\eta^* = G^*/\omega$, giving

$$|\eta^*| = |G^*|/\omega = \sqrt{G'(\omega)^2 + G''(\omega)^2 / \omega}$$
(1)

2

The $|\eta^*|$ modulus is considered as an admissible estimation of viscosity when shear viscosity is not obtainable (Cox-13 Merz rule [6]), and this was largely used. Nevertheless, all authors recognize a strong shear-thinning behavior. This is 14 illustrated by the power law parameters extracted from literature data on G' and G'' and displayed on Table 1, which 15 constitutes a comparison basis for the shear viscosity measured in this study. Whereas some authors [42, 15, 58] 16 observed a small Newtonian plateau at low shear rates $(0.1 - 1.0 s^{-1})$, others [65, 46, 47] did not monitor any trend to 17 a plateau although exploring shear rate from $0.01 \, s^{-1}$. Our own experience does not reveal any plateau even for shear 18 rate values of $10^{-3} s^{-1}$. This behavior is generally linked to viscoplasticity, but the $\tau(\dot{\gamma})$ curves obtained on the tested 19 samples do not display any tendency to a yield stress. So, from our measurements, it appears that, if a yield stress 20 exists, it is likely very low (typically < 0.01 Pa). 21

The power-law index *N* values reported in Table 1, which derive from rheograms $\eta(\dot{\gamma})$ ranges from 0.2 to 0.4; they are similar to literature data [47, 58]. Values of consistency *K* and viscosity are also similar. All viscosity curves are limited by two envelope curves defined by ($K_{min} = 0.45$, $N_{min} = 0.39$) and ($K_{max} = 5.8$, $N_{max} = 0.20$). The large shear rate range explored in this study gives an appropriate description of viscosity for the mucus film displacement.

1 3. Modeling of mucus maturation

This section first presents the airway surface liquid structure, composed of mucus and periciliary fluid surrounding the lung epithelial cells. The two next subsections present how the fluid velocity u and the fluid viscosity η_G are linked, and finally how the viscosity η_G is modeled for such a mixture, by a Carreau law with spatially varying coefficients.

5 3.1. Airway surface liquid

The airway surface liquid (ASL) covering bronchial walls is a stratified medium composed of a mucus layer (ML)
overlying a periciliary fluid layer (PCL), which behaves as a Newtonian fluid with a viscosity close to that of water.
Both PCL and ML are chiefly composed of water (>98%). Several works in the literature [25, 12, 55, 33, 39] (an
exhaustive reference list is given in [56]) have considered two layers of fluid with constant fluid properties.

The periciliary fluid wetting the bronchial wall has a height generally estimated to be at least 2/3 of the total ASL thickness. Once they are released by goblet cells, polymerized mucins are further hydrated, expand, and travel freely in the PCL away from the wetted surface [13, 14, 20, 4].

The innermost mucus layer results from progressive maturation and structuration of mucins in the core of the fluid. Yet, the transition between the PCL and ML layers is supposed to be continuous, assuming a progressive mucin maturation between the epithelial surface and mucus, characterized by a progressive meshwork loop size [7].

The present model considers this continuous heterogeneity. The ASL rheological parameters depends on the mucin maturation parameter α , defined as the volumic fraction of matured mucins at a given ASL height, that is, on the cross-linking magnitude of mucin polymers [26, 48, 64]. The maturation α varies from 0 at the PCL–epithelium interface to 1 in the ML with a sigmoid or tan⁻¹ profile.

20 3.2. Flow modeling and domain geometry

The computational domain Ω contains a full ciliated cell (a segment of the respiratory epithelium, cf. Fig. 2). The ciliated cell is the time-dependent domain $\mathcal{B}(t)$ and the ASL domain $\mathcal{F}(t) = \Omega \setminus \overline{\mathcal{B}(t)}$. The rectangular domain is bounded by the mucus-air interface at its top and the wetted epithelial surface at its bottom, with periodical conditions in the streamwise direction.

The Reynolds, Womersley, and Froude numbers are sufficiently small to suppose a mucus regime following the stationary 3D Stokes equations in a time-dependent fluid domain $\mathcal{F}(t)$, that is to say the flow is always at its quasiequilibrium [19]:

$$-\operatorname{div}(2\eta_G D(u)) + \nabla p = f \text{ in } \mathcal{F}(t), \tag{2}$$

where *u* is the velocity field satisfying divu = 0 in $\mathcal{F}(t)$, *p* the pressure, $D(u) = (\nabla u + \nabla u^T)/2$ the strain rate tensor, η_G the dynamic viscosity, and $u = \bar{u}$ on boundary $\partial \mathcal{F}(t)$. The penalty method [2] is then used to take into account the influence of the beating cilia on the fluid. It is a robust fictitious domain method compatible with any spatial discretization, in particular regular grids which permits to use fast solvers, as detailed below.

The cilia velocity \bar{u} is computed from the beating model presented in [8], based on damped Young modulus propagation, and compatible with the cilia beating cycle [24, 27, 51, 40]. Since the cilia velocities are prescribed, this is a one-way fluid-structure interaction. This assumption is valid only for early stage of the sickness or for stabilized patients, that is to say for moderate deviation from the healthy case, and does not concern critical care. In particular, the modification and adaptation of the beating patterns and frequency with respect to the modification of the mucus behavior (viscosity and non-Newtonian effect) is not taken into account in this numerical model. This had been investigated experimentally [31], and the development of a coherent numerical model remains, to our knowledge, an open problem.

The set of cilia is beating, involving a sufficiently large number of cilia, conforming *in-vivo* [51] and *in-vitro* [32] ¹⁴ cilia behavior, leading to the flow displayed on Fig. 2. The cell we consider involves 25 cilia, yielding to a sufficiently ¹⁵ dense cilia array to get a velocity no longer depending on the number of cilia. Their configuration and simulation parameters are displayed on Table 2. Cilia beat in a coordinated manner and the resulting beating exhibits an antipleptic ¹⁷ wave. This parameter remains constant in all the computations, its influence on the mucuciliary clearance was already ¹⁸ investigated in the literature [32, 40, 56, 29, 18].

3.3. Rheology and maturation modeling

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As mentioned in introduction and in section 2.2, the mucus layer exhibits both shear-thinning, visco-elastic and/or visco-plastic features. While several studies have focused on the visco-elastic aspects [30, 29, 18, 55, 56, 53], studies focusing on visco-plastic effects are less numerous [41]. The present study focus on the shear-thinning behavior, and bring a new light on this kind of non-Newtonian feature. In order to take in account the transition between the Newtonian PCL and the shear-thinning mucus, an exponential growth is considered between the two fluids of viscosities η_{PCL} and $\eta_{ML}(\dot{\gamma}) = K_{ML}\dot{\gamma}^{N_{ML}-1}$. The parameters of the power-law model depend on α :

$$K(\alpha) = \eta_{PCL} \left(\frac{K_{ML}}{\eta_{PCL}}\right)^{\alpha} \text{ and } N(\alpha) = \alpha \cdot N_{ML} + (1 - \alpha)$$
(3)

² where $\eta_{PCL} = 10^{-3} Pa \cdot s$ is the Newtonian solvent viscosity assumed to the water viscosity.

The power-law model needs to be regularized in the vicinity of zero as viscosity tends to infinity. Otherwise, the effective viscosity has a lower bound at high shear rates, the solvent viscosity η_{PCL} . The Carreau model matches these two features:

$$\eta_G(\alpha, u) = \eta_{PCL} + (\eta_0(\alpha) - \eta_{PCL}) \left[1 + (\beta \dot{\gamma})^2 \right]^{\frac{N(\alpha) - 1}{2}}$$
(4)

where the regularization parameter β is the inverse of the cut-shear rate (low shear rates; $\beta = 4 \times 10^3 s$). The parameter $\eta_0(\alpha)$ is the cut-viscosity and is determined by the choice of the power-law coefficients and cut-shear rate. This leads to: $(K_{res})^{\alpha}$

$$\eta_0(\alpha) = \eta_{PCL} \left(\frac{K_{ML}}{\eta_{PCL}}\right)^{\alpha} \beta^{\alpha(1-N_{ML})}$$
(5)

⁹ This class of functions is able to generate variable concentration features [57, 16].

Equation 4 corresponds to a Newtonian fluid $\eta_G(\dot{\gamma}, \alpha) \equiv \eta_{PCL}$ when $\alpha = 0$ and evolves to the Carreau law when α increase to 1 in the ML:

$$\eta_{ML}(\dot{\gamma}) = \eta_{PCL} + \left(\eta_{ML} - \eta_{PCL}\right) \left[1 + (\beta \dot{\gamma})^2\right]^{\frac{mL}{2}}$$
(6)

12 **4. Numerical method**

Solving numerically the equation (2) in a mobile and complex geometry, could have been done using various 13 approaches, such as accelerated kernel methods [63], immersed boundary methods designed for heterogeneous flows 14 (See [22, 45] for its time-dependent formulation), or improved penalization techniques [2, 8, 9]. Among the different 15 numerical methods applied to a fluid bathing a set of cilia, one can find Stokeslets methods [29, 24], finite element 16 methods [41, 55, 56] or immersed boundary coupled to lattice Boltzmann methods [33, 39], this being not exhaustive. 17 In this study, we have used the equation (2) penalized by $\varepsilon^{-1}(u-\bar{u})$ over the cilia domain $\mathcal{B}(t)$, in order to satisfy 18 the continuity between the cilia and the fluid. This is a nonlinear Stokes problem, analyzed mathematically in [10], 19 which is robust and well-fitted to deformable geometry: 20

$$-\operatorname{div}(2\eta_G(\alpha, u)D(u)) + \frac{\chi(t)}{\varepsilon}(u - \bar{u}) = f \text{ in } \Omega,$$
(7)

in the whole computational domain Ω , $\overline{u}(t)$ is the cilium velocity deduced from the beating model, $\chi(t)$ the characteristic function of $\mathcal{B}(t)$, and $\varepsilon \ll 1$ the penalization parameter.

In [8], an iterative projection algorithm was developed to compute separately the pressure and the velocity field of a Newtonian variable viscosity Stokes problem. This numerical method efficiently computes the velocity field close to the boundaries (an inherent problem of classical projection methods [28]). This original methodology allows (in the same iteration) the explicit integration of the nonlinearity of the power law so that the generalized algorithm becomes a multi-criterion fixed point.

First, we introduce a projection on divergence-free fields denoted $\Pi(u^*) = u^* - \nabla \zeta$ where ζ is the solution to the following linear elliptic partial differential equation:

$$-\Delta \zeta = -\operatorname{div} u^* \text{ in the domain } \Omega$$

$$\frac{\partial \zeta}{\partial n} = u^* \cdot n \text{ on the boundary } \partial \Omega$$
(8)

where *n* is the outer unit vector normal to $\partial \Omega$. This numerical algorithm relies on fast solvers [59], based on FFT decompositions, guaranteeing a quasi linear computational cost with respect to the number of grid points, which suits very well to large 3D computations.

A globally second order numerical solution of Eq. 7 is the limit of the sequence $u_k = \Pi(u_k^*)$ where u_k^* is defined by:

$$-\eta_G(\alpha, u_k)\Delta u_{k+1}^* + \frac{\chi(t)}{\varepsilon}(u_{k+1}^* + \Pi(u_k^*) - u_k^* - \bar{u})$$

= $f + \left[2D(u_k) + (\operatorname{div} u_k^*)\operatorname{Id}\right]\nabla\eta_G(\alpha, u_k)$ in Ω (9)
 $u_{k+1}^* = g - \Pi(u_k^*) + u_k^*$ on $\partial\Omega$

The solution obtained by this method satisfies the boundary conditions u = g, which is usually not the case when such a Dirichlet conditions is set together with projection methods [28]. The equation (9) can be written

$$-\Delta u_{k+1}^* + \chi(t) \left[\varepsilon \,\eta_G \right]^{-1} u_{k+1}^* = RHS(u_k^*, \bar{u}) \tag{10}$$

where

$$RHS(u_k^*, \bar{u}) = \eta_G^{-1} f + \chi(t) [\varepsilon \eta_G]^{-1} (\bar{u} + u_k^* - \Pi(u_k^*))$$
(11)

+
$$\left[2D(u_k) + (\operatorname{div} u_k^*)\operatorname{Id}\right] \nabla \log \eta_G(\alpha, u_k)$$

The successive iterations of equation (10) have been firstly solved by a multigrid efficient solver [1, 8]. However, ¹⁸ this had been improved by the use of matrix perturbation theory [9]: Indeed, the penalization operator $\chi(t) [\varepsilon \eta_G]^{-1}$ Id ¹⁹

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in (10) exhibits large jumps, but localized, and can be seen as a large perturbation of the $-\Delta$ operator. By means of the Sherman-Morrison-Woodbury formula, this elliptic PDE is reduced to a linear system whose size is the number of grid point in the cilia body $\mathcal{B}(t)$, and whose any evaluation requires a call to a FFT solver (see [9] for more details).

4 The mucin maturation parameter α can be only a function of distance from the airway wall (called *static mixing*),

⁵ such as the following sigmoid expression:

$$\alpha(x, y, z) = \frac{\tan^{-1} (\lambda(z/H - \delta)) - \tan^{-1}(-\lambda\delta)}{\tan^{-1} (\lambda(1 - \delta)) - \tan^{-1}(-\lambda\delta)}$$
(12)

⁶ where is the ASL height is *H*, PCL height is δH , and the dimensionless transition coefficient is λ . It can also satisfy a ⁷ transport equation (called *convected mixing*):

$$\partial_t \alpha + u \nabla \alpha - \sigma \Delta \alpha = 0 \tag{13}$$

⁸ where Eq. (12) then stands for the initial condition, where σ is a numerical smoothing diffusion chosen as small as ⁹ possible in order to avoid spurious jumps occurring in pure transport $(10^{-11}m^2.s^{-1}$ for instance). When the convected ¹⁰ mixing is used, convection is dominant and a Lagrangian method is used to integrate in time this partial differential ¹¹ equation [8]. Once it is coupled with the Eulerian 3D Stokes solver, it yields to a robust numerical tool, allowing ¹² large time steps without significant loss on accuracy, up to 34-fold the time step satisfying the usual transport stability ¹³ condition $u_{max}\Delta t < \Delta x$.

In the present cases, choosing static or convected mixing, whose resulting α -isovalues are displayed on Fig. 2, leads only to a 3% difference in the mucus mean velocity. Furthermore, the case of Newtonian fluids had been investigated in [11], with linear Stokes equation. The present study focuses specifically on non-Newtonian effects on the mucociliary clearance, involving a non-linear Stokes model. The resulting non-Newtonian effects and their impact on mucociliary clearance are discussed thereafter.

19 5. Phase cartography

Measurements on mucus samples and numerical simulations enable to plot phase cartography. Resulting maps yield positions of healthy and CF mucus from the present study and literature. The effect of PCL height, which markedly impairs the mucociliary clearance, can be investigated.

The balance between PCL and ML quantified by the scalar field α following Eq. (12), with a PCL height is chosen as δH where $\delta = 0.6$, for a total ASL height $H = 12 \,\mu m$, representing the proximal compartment of the tracheobronchial tree, and a transition coefficient $\lambda = 5$. In the second part of this study, the PCL height varies, δ_{1} ranging from 0.3 to 0.7.

Moreover, in order to quantify the efficiency of the mucociliary clearance, the velocity is averaged both in space, over the full ML, and in time, over 5 beating cycles:

$$\overline{U} = \frac{1}{5T \operatorname{meas}(\Omega)} \int_0^{5T} \iiint_\Omega u_x(x, y, z, t) \,\mathrm{d}V \,\mathrm{d}t \tag{14}$$

where x denotes the streamwise direction given by the cilia beating.

5.1. Cystic fibrotic mucus positioning in phase cartography

Because the cilium beating is asymmetrical, this velocity is positive and a net displacement of the ML is observed in the direction of the esophagus. A snapshot of a simulation is presented on Fig. 2. The mean mucus velocity is computed for different values of the $\{N, K\}$ couple. Simulations were carried out for 169 $\{N, K\}$ couples to obtain the phase cartography of Fig. 3.

Viscosity values are not fully meaningful for shear-thinning fluids. The consistency index *K* takes generally lower values than that in healthy subject samples. The power index varies with a greater extent in CF samples compared to values observed in healthy subject samples (except for HL9).

As depicted in Fig. 3, the mucus transport velocity does not evolve monotonously with neither N nor K, a moderate 14 decrease in the K index leading to a lower mucus transport with a loss of velocity in the range 6-14% for our mucus 15 samples (Table 1). An isolated drop of 6% in mucus mean velocity may suffice to be pathological. Although the 16 HL9 datum [54] is very different from others [34, 67] (but this might be linked to a nebulization realized prior to 17 the sampling), the mucus velocity magnitude varies less than 5% in these healthy mucus cases. The shear-thinning 18 behavior has a strong effect, as the mucus transport velocity decays to a large extent when N decreases to 0.2. This 19 result is quite counterintuitive, but might result from a larger backflow of the mucus layer when viscosity decreases. 20 This phenomenon depends highly on the respective ML and PCL height that affect the cilium impingement on mucus 21 (strength and duration). 22

Clinically, two classes of CF mucus can be considered: stabilized and decompensated. An acute secondary infection exacerbates chronic infection with ciliated cell death, further disrupting the mucus propulsion machinery. The expectoration rheology of the CFM3 patient was measured both in stabilized and decompensated states: posttreatment sputum, after 17 days of treatment [CFM3b, stabilized] and 2 days after hospitalization [CFM3a, acute]

1

displayed on Fig. 3 and Table 1. According to measures and computations, the mucociliary clearance improves, as
 expected using a combined antibiotic and steroid treatment.

3 5.2. Impact of PCL thickness

⁴ Altered mucus velocity is shown in {*K*, *N*} diagrams (Fig. 4) for several heights of periciliary fluid (i.e., several δ
⁵ values), representing the effect of variable CFTR deficiency [62, 20]. This alteration is given in percent of the mean
⁶ healthy data (i.e., HL6 and HL8 in Table 1 [34, 67]).

The PCL/ML thickness ratio impacts markedly the mucus transport. The mucus velocity is reduced from -14% to -21% when the PCL thickness decreases (δ falls from 0.6 to 0.3). Hence, for a mucus with a given set of values of the parameter couple {*N*, *K*}, a weak decrease in δ significantly reduces the mucus velocity. A limitation of this work is linked to the absence of interference between the mucus rheology and motion amplitude and frequency of respiratory cilia for a given state of ciliated cells. However, pathophysiological data are missing to handle this interaction, which can yet be explored using the present model.

13 6. Conclusion

The present work had two major objectives. Firstly, it was aimed at using an efficient solver that enables the anal-14 ysis of all influent shear-thinning parameters which control the mucus motion in the respiratory tract, using a mucus 15 maturation model closer to the biological process than a double-deck fluid domain with sharp PCF-ML transition. 16 This mucus baths beating cilia, through which travel immersed mucin polymers that hydrate and cross-link. Sec-17 ondly, it was aimed at providing a set of experimental parameters both in order to confront the numerical results (by 18 means of healthy/pathologic classification) and to provide input rheological parameters to the numerical simulations. 19 Despite the complexity and richness of our model, many data that are mandatory to perfectly handle the process are 20 still missing (effect of CF on the respective thickness of the PCL and ML layers, effect of mucus viscosity on cilium 21 beating, etc.). Nevertheless, we have shown that shear-thinning effects can of the same order as the visco-elastic 22 effects in such environments [53]. 23

The highly shear-thinning character of the mucus leads to very high ratio of the dynamic viscosity in the flow, around 10⁵ when the shear rate $\dot{\gamma}$ evolves in the range [10⁻²-10³]. Therefore the numerical method based on projective iteration [8, 9] extended herein to nonlinear viscosity proves to be extremely robust.

Cartographies show a strong influence of the power law index N that must be properly incorporated in numerical	1
simulations. In stabilized cystic fibrosis, the mucus viscosity observed for a given shear rate does not significantly	2
differ from values observed in healthy people. Nevertheless, as the mucus velocity does not evolve monotonously with	3
the rheological indices N and K , mucus transport in CF patients can be less efficient. A vicious circle is then created,	4
as a drop in mucuciliary clearance allow local pathogen proliferation and further deterioration of the respiratory	5
epithelium function.	6

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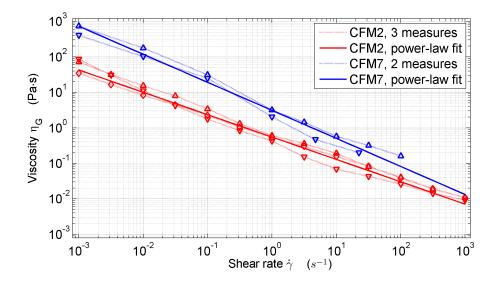


Figure 1: Curves from CFM2 and CFM7 measurements from Table 1 with their best-fitting power-law on $\dot{\gamma} \in [10^{-2}, 10^2]$.

Alias	N	K	Source
CFL1	0.408	0.544	[54]
CFL2	0.182	1.397	[61]
CFL3	0.166	2.245	[61]
CFL4	0.163	2.423	[61]
CFL5	0.17	7.34	[15]
HL6	0.19	14.1	[34]
HL7	0.195	15.49	[34]
HL8	0.215	13.18	[67]
HL9	0.482	0.355	[54]
CFM1	0.20	5.80	
CFM2	0.39	0.45	
CFM3	0.32	1.24	
CFM4	0.39	1.60	
CFM5	0.30	2.37	~
CFM6	0.23	4.22	resent study
CFM7	0.21	3.10	Presen
CFM8	0.23	3.53	
CFM9	0.37	0.51	
CFM10	0.36	2.17	
CFM11	0.22	4.75	
BM12	0.40	1.43	

Table 1: Rheological parameters (K, N) from collected samples (CFM1–CFM11 standing for Cystic Fibrosis, andBM12 standing for Bronchiectasis) and the literature (CFL1–CFL5 and HL6–HL9 from the complex modulus G*).Aliases CFL and HL stand for "Cystic Fibrosis from Literature" and "Healthy cases from Literature".

	I.
Name	Value
Cilia length	8 µm
Cilia diameter	0.3 µm
Number of Cilia	25
PCL viscosity (η_{PCL})	0.001 Pa.s
Viscosity transition stiffness (λ)	5
Transition length (δ)	0.6
ASL height (H)	12 µm
Beating frequency	10 <i>Hz</i>
Inverse low-frequency cut-off (β)	410^3s
Distance between adjacent cilia	1.5 µm
Metachronal wavelength	87.5 μm

 Table 2: Parameters used for the numerical simulations, gathered from [51, 56, 21, 60] or from our own measures.

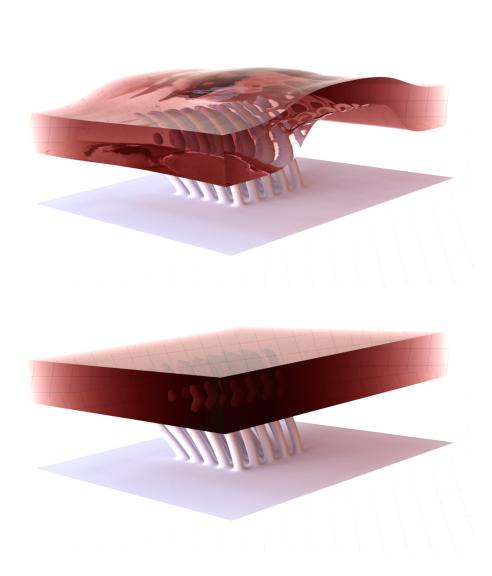


Figure 2: Evolution of isovalues of mucin maturation $\alpha \in [0.4, 0.9]$ (in red). Top picture: solution of transport equation (13) coupled to the 3D Stokes equation (7). Bottom picture: static mixing given by Eq. (12).

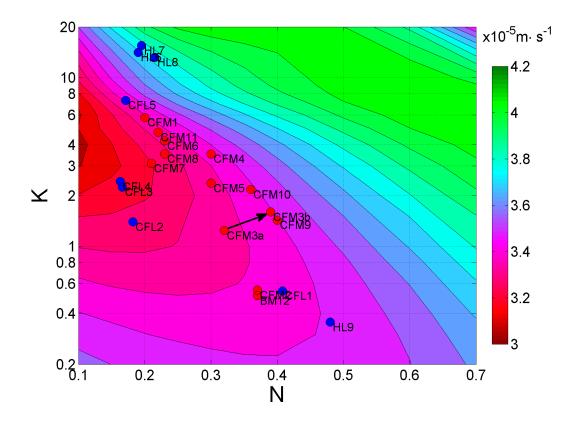


Figure 3: Phase cartography of the mucus transport velocity, with respect to rheological parameters $\{N, K\}$. Collected samples are displayed in red, while the results collected from literature are displayed in blue (Table 1).

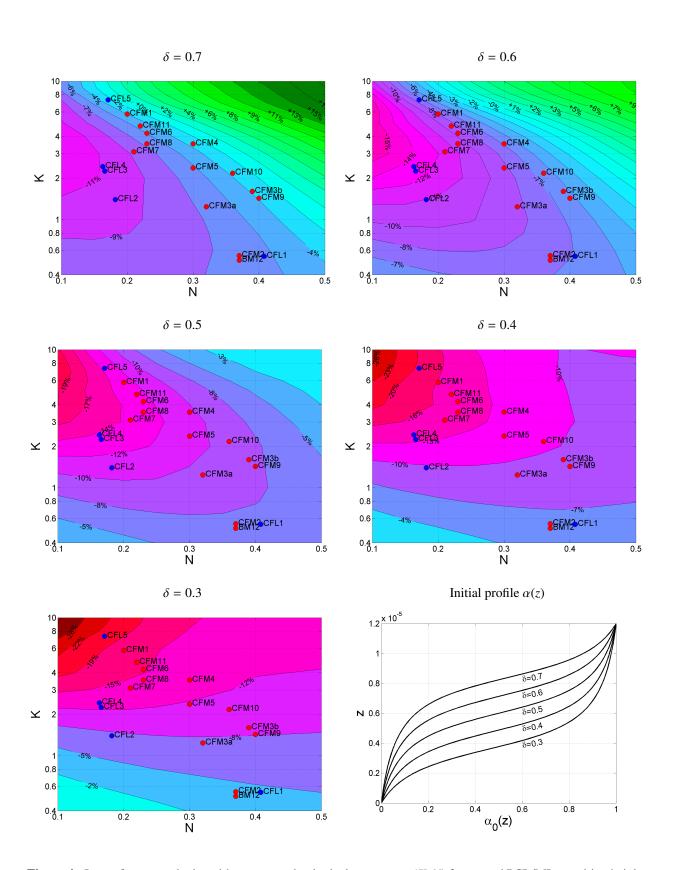


Figure 4: Loss of mucus velocity with respect to rheological parameters (*K*, *N*) for several PCL/ML transition heights δ , given in the bottom right plots. The reference velocity (0%) is the healthy cases from [34, 67], also displayed in Fig. 3 and 1 and Table 1.