



mSAT:An OCaml SAT Solver

Guillaume Bury

► **To cite this version:**

Guillaume Bury. mSAT:An OCaml SAT Solver. OCaml Users and Developers Workshop, Sep 2017, Oxford, United Kingdom. <hal-01670765>

HAL Id: hal-01670765

<https://hal.inria.fr/hal-01670765>

Submitted on 21 Dec 2017

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Introduction

mSAT : a SAT solving library in OCaml. It solves the **satisfiability** of propositional clauses. It is **Modular** : the user provides the theory. And it **produces formal proofs**.

Conflict Driven Clause Learning

Propagation If there exists a clause $C = C' \vee a$, where C' is false in the partial model, then add $a \mapsto \top$ to the partial model, and record C as the reason for a .

Decision Take an atom a that is not yet in the partial model, and add $a \mapsto \top$ to the model.

Conflict A conflict is a clause C that is false in the current partial model.

Analyze Perform resolution between the analyzed clause and the reason behind the propagation of its most recently assigned literal, until the analyzed clause is suitable for backjumping.

Backjump A clause is suitable for backjumping if its most recently assigned literal a is a decision. We can then backtrack to before the decision, and add the analyzed clause to the solver, which will then enable to propagate $a \mapsto \perp$.

SMT Formulas using first-order theories can be handled using a theory. Each formula propagated or decided is sent to the theory, which then has the duty to check whether the conjunction of all formulas seen so far is satisfiable, if not, it should return a theory tautology (as a clause), that is not satisfied in the current partial model.

Implementation

- Imperative design
 - ✓ 2-watch literal
 - ✓ Backtrackable theories (less demanding than immutable theories)
- Features
 - ✓ Functorized design, using generative functors
 - ✓ Local assumptions
 - ✓ Model output and proof output (Coq, dot)

Solver Interface

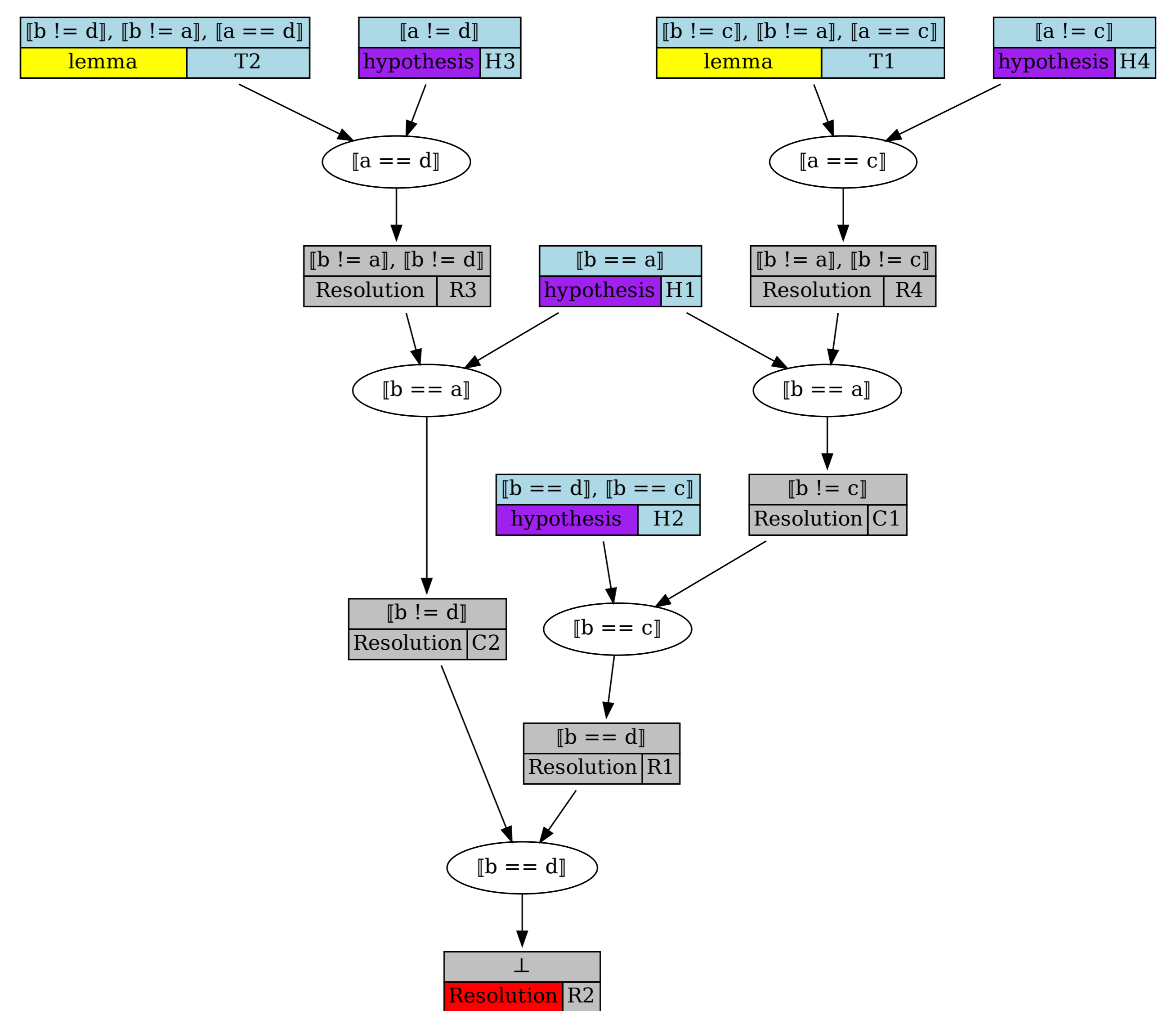
```
module Make(Th: Theory_intf.S)() : sig
  type 'f sat_state = { eval : 'f -> bool; ... }
  type ('c, 'p) unsat_state =
    { conflict: unit -> 'c; proof : unit -> 'p }
  type res = Sat of formula sat_state
    | Unsat of (clause, proof) unsat_state
  val assume : ?tag:int -> atom list list -> unit
  val solve : ?assumptions:atom list -> unit -> res
end
```

Other Solvers

name	theory	bindings	features
regstab	SAT	binary only	only pure SAT
minisat			
sattools	SAT	C bindings	only pure SAT
ocaml-sat-solvers			
Alt-ergo	SMT	binary only	Fixed theory
Alt-ergo-zero	SMT	OCaml lib	Fixed theory
ocamlyices			
yices2	SMT	C bindings	Fixed theory

Problem Example

Are the following hypotheses satisfiable? $H1: a = b$ $H2: b = c \vee b = d$
 $H3: a \neq d$ $H4: a \neq c$



Theory Interface

```
type ('f, 'p) res = Sat | Unsat of 'f list * 'p
type 'f slice = { start:int; length:int; get:int -> 'f }
module type S = sig
  val backtrack : level -> unit
  val current_level : unit -> level
  val assume : formula slice -> (formula, proof) res
end
```

Proof Generation

- ✓ Each clause records its "history" which is the clauses used during analyzing
- ✓ Minimal impact on proof search (already done to compute unsat-core)
- ✓ Sufficient to rebuild the whole resolution tree
- ✓ A proof is a clause and proof nodes are expanded on demand
→ no memory issue
- ✓ Enables various proof outputs :
 - Dot/Graphviz (see example above)
 - Coq (and soon Dedukti) formal proofs

Performances

solver (package)	Alt-ergo-zero (aez)	mSAT (msat)	minisat (minisat/sattools)	cryptominisat (sattools)
uuf100 (1000 pbs)	0.125	0.012	0.004	0.006
uuf125 (100 pbs)	2.217	0.030	0.006	0.013
uuf150 (100 pbs)	67.563	0.087	0.017	0.045
pigeon/hole6	0.120	0.018	0.006	0.006
pigeon/hole7	4.257	0.213	0.015	0.073
pigeon/hole8	31.450	0.941	0.096	2.488
pigeon/hole9	timeout (600)	8.886	0.634	4.075
pigeon/hole10	timeout (600)	161.478	9.579 (minisat) 160.376 (sattools)	72.050