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# Compositional Verification in Action

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## Abstract

Concurrent systems are intrinsically complex and their verification is hampered by the well-known “state-space explosion” issue. Compositional verification is a powerful approach, based on the divide-and-conquer paradigm, to address this issue. Despite impressive results, this approach is not used widely enough in practice, probably because it exists under multiple variants that make knowledge of the field hard to attain. In this article, we highlight the seminal results of Graf & Steffen and propose a survey of compositional verification techniques that exploit (or not) these results.

**Keywords:** Bisimulation, Compositional minimisation, Compositional reachability analysis, Compositional verification, Concurrency theory, Equivalence checking, Formal method, Labelled Transition System, Model checking, Process algebra, Process calculus, Validation, Verification

## 1 Introduction

The present article was written in honour of Susanne Graf and Bernhard Steffen at the occasion of their 60th birthdays.

Concurrent systems are commonly found in software programs, hardware circuits, and telecommunication networks, where many processes have to execute simultaneously, synchronise to properly access shared resources, and communicate together to achieve common tasks. Concurrent systems are notoriously hard to design correctly, as they are prone to subtle errors, such as deadlocks, livelocks, or synchronisation issues. To avoid or detect such errors, formal methods, supported by computer-aided verification tools, are established techniques for the design of concurrent systems [23].

Unfortunately, verification algorithms for concurrent systems are often hampered by the “state-space explosion” issue, which arises when the complexity of verification (which can be exponential in the number of concurrent processes)

exceeds the capabilities of the computer on which verification is performed. This makes it difficult, if not unfeasible, to analyse large systems with many processes, such as most industrial case studies. Various verification approaches have been proposed to fight state-space explosion, but there is no silver bullet, as each approach works under specific assumptions, for particular classes of problems.

The present article focuses on one of these approaches, *compositional verification*, which relies on “divide-and-conquer” strategies that decompose a global system into local concurrent processes and seek to exploit locality properties of these processes. There are many different branches of formal methods and, consequently, very diverse forms of compositional verification. The present article is centred around a series of papers published between 1990 and 1996 by Susanne Graf and Bernhard Steffen [36] [37] [38] [39] [40], the three latter ones being co-authored with Gerald Lüttgen. More precisely, the scope of the present article is defined as follows:

- We consider the established framework of *asynchronous concurrency*, in which concurrent processes execute without assumption about their respective speeds. These processes can synchronise and communicate using Hoare’s rendezvous<sup>1</sup> [44]. Communicating automata [1] and process calculi [7] naturally fit in this setting. Other communication schemes, such as shared memories or message queues, can be expressed, as particular cases, in terms of rendezvous.
- We do not consider compositional verification techniques designed for theorem proving or static analysis, but only those designed for *enumerative verification* (or *reachability analysis*) methods, which rely on state-space exploration and include both *model checking* (in which the properties to be verified are expressed in some temporal logic) and *equivalence checking* (in which the properties to be verified are expressed using bisimulations or behavioural preorders).
- We do not consider *state-based* models, such as Kripke structures (in which relevant information is attached to the states, usually in the form of *state variables*, so that the properties to be verified are expressed using predicates or invariants relating these variables); instead, we consider *action-based* models, such as labelled transition systems (in which relevant information is attached to the transitions, usually in the form of *transition labels*, so that the properties are expressed as sequences, trees, or graphs of actions).
- We consider both *explicit-state* methods (in which reachable states and transitions are analysed individually) and *symbolic* methods (in which sets of reachable states are analysed collectively). Actually, many papers discussed in this survey use explicit-state methods, but symbolic methods are also applicable. There is a common belief that symbolic methods systematically outperform explicit-state ones, which hardly exceed  $10^{12}$  states on current

<sup>1</sup> Some authors consider rendezvous as synchronous and message queues as asynchronous.

machines; this is a misconception and the situation is more contrasted. In particular, explicit-state methods handle dynamic data structures (e.g., lists, trees, etc.) more easily, and, even in the case of pure control structures (e.g., Petri nets), recent results [48] show that explicit-state methods, combined with appropriate reductions, compete well with symbolic methods.

The compositional verification approaches we consider here are traditionally referred to as *compositional minimisation* or *compositional reachability analysis*; they are *action-based* and rely on *equivalence-checking* concepts, especially behavioural equivalence and preorder relations between labelled transition systems. In the sequel, *compositional verification* is often used as a synonym for *compositional minimisation*, although the latter is clearly more specific.

There exist indeed alternative approaches, referred to as *compositional reasoning*, *assume-guarantee*, or *rely-guarantee*, which are often *state-based* and rely on *model-checking* concepts, including assertions, logic formulas and satisfaction relations. See, e.g., [66] and [34] for detailed presentations of these approaches.

The present article is organised as follows. Section 2 introduces compositional minimisation in its simplest forms. Section 3 recalls the main concepts, namely *interfaces* and *semi-composition*, put forward in the seminal papers of Graf, Steffen & Lüttgen. Section 4 discusses enhanced compositional approaches that use interfaces without semi-composition. Section 5 presents the most advanced approach, in which interfaces and semi-composition are both used. Practical applications of compositional verification to realistic case studies are reported whenever possible. Finally, Section 6 gives a few concluding remarks.

## 2 Compositional Minimisation without Interfaces

### 2.1 Principles

To perform compositional minimisation in an action-based setting, one needs six ingredients carefully designed to fit well together:

1. A *low-level model*  $M$ , which is a state-transition formalism<sup>2</sup> in which the behaviour of the system  $S$  under verification can be encoded. This model is usually very simple, with a low abstraction level, so that the properties to be verified for  $S$  can be easily checked on  $M$ . As a counterpart, the encoding of  $S$  in  $M$  can get large and verbose. Two famous examples of such models are: *labelled transition systems* [63], which are the underlying semantic model of most process calculi and play a central role in major functional verification tools, and *interactive Markov chains* [42], which are performance evaluation

<sup>2</sup> For conciseness, we use the same term “model” and the same letter  $M$  to refer both to the “meta-model” (i.e., the low-level formalism) and the “models” (i.e., all particular instances expressed in this formalism).

models that combine ordinary transitions and stochastic ones, the firing time of the latter being governed by exponential distributions.

2. A *parallel composition operator*  $\parallel$  that takes  $n$  models  $M_1, \dots, M_n$  and returns a new model  $M' = M_1 \parallel \dots \parallel M_n$ . The notation  $\parallel$  is a crude simplification, as parallel composition operators usually carry extra information to determine which synchronisations have to be done (see, e.g., [30]). The resulting model  $M'$  is often referred to as a *composition*, while  $M_1, \dots, M_n$  are referred to as *components*<sup>3</sup>. More often than not, the complexity of  $M'$  (measured in number of states and transitions) is the product (rather than the sum) of the complexities of  $M_1, \dots, M_n$ : the state-space explosion problem precisely lies in such complexity growth.
3. An *equivalence relation*  $\approx$  defined over models. This relation (which differs from graph isomorphism noted  $=$ ) should be a congruence with respect to parallel composition, i.e., if  $M_i \approx M'_i$  for all  $i \in \{1, \dots, n\}$ , then  $M_1 \parallel \dots \parallel M_n \approx M'_1 \parallel \dots \parallel M'_n$ . Two examples of such equivalences are: strong bisimulation [60], which is a congruence for the parallel composition operators of most process calculi (see [88] for a discussion) and branching bisimulation [84]. Equivalence relations may incorporate *abstractions*: for instance, branching bisimulation can remove some  $\tau$ -transitions ( $\tau.M \approx M$ ), and Markov-chain lumpability can merge some stochastic transitions ( $\lambda.M + \mu.M \approx (\lambda + \mu).M$ ).
4. A *minimisation function*  $\min : M \rightarrow M$  that maps each model to a distinguished element of its equivalence class in the quotient set  $M / \approx$ ; this distinguished element is usually chosen to minimise some complexity criterion. For bisimulation relations, for example, one chooses a labelled transition system that has the least number of states. Minimising a model applies to this model the abstractions inherent to relation  $\approx$ . Because of the congruence property, one has  $M_1 \parallel \dots \parallel M_n \approx \min(M_1) \parallel \dots \parallel \min(M_n)$  and  $\min(M_1 \parallel \dots \parallel M_n) = \min(\min(M_1) \parallel \dots \parallel \min(M_n))$ .
5. A *high-level language*  $L$  in which the system  $S$  can be specified. Theoretical papers on compositional verification often use  $M$  in place of  $L$ , but this is not realistic, as complex systems are never described using low-level models only. The language  $L$  should be equipped with a concept of components and a parallel composition, also noted  $\parallel$ , for assembling these components. A composition  $C_1 \parallel \dots \parallel C_n$  is said to be *flat* if all components  $C_i$  are sequential, or *hierarchical* if some components  $C_i$  are themselves compositions.
6. A *translation function*  $\llbracket \cdot \rrbracket : L \rightarrow M$  that maps each system  $S$  written in  $L$  to a corresponding low-level model  $\llbracket S \rrbracket$ . This function should be able to translate components taken individually, and should be a morphism for parallel composition, meaning that, given  $n$  components  $C_1, \dots, C_n$ ,  $\llbracket C_1 \parallel \dots \parallel C_n \rrbracket \approx \llbracket C_1 \rrbracket \parallel \dots \parallel \llbracket C_n \rrbracket$ . The translation of an entire system may vary

<sup>3</sup> Also called *subsystems*, *agents*, or *processes* in the literature.

well fail due to state explosion<sup>4</sup>, but the translation of individual components is expected to succeed, at least for a majority of them.

Given a system  $S = C_1 || \dots || C_n$  such that  $\llbracket S \rrbracket$  is excessively large, compositional minimisation, in its simplest form, avoids to compute  $\llbracket S \rrbracket$  directly and computes  $\min \llbracket C_1 \rrbracket || \dots || \min \llbracket C_n \rrbracket$  instead. This idea was advocated in many papers, both in the functional verification setting [18] [54] [68] [88] [76] [75] [79] [80] [83] and in the performance evaluation setting [42] [24].

## 2.2 Strategies

In practice, compositional minimisation is more complex than the simple form exposed above. For systems with many components, there are multiple ways (called *strategies*) to perform compositional minimisation, and all strategies do not necessarily have the same efficiency, i.e., provide the same amount of state-space reduction. The efficiency of a strategy is inversely proportional to the size (e.g., number of states) of the largest intermediate model that is generated; a good strategy strives to keep this size as small as possible, in order to avoid state-space explosion during the compositional verification process. There are several causes leading to the existence of multiple strategies.

First, if the system has a hierarchical structure, e.g.,  $(C_1 || C_2) || (C_3 || C_4)$ , minimisation can be applied either to the leaf components only, i.e.,  $(\min \llbracket C_1 \rrbracket || \min \llbracket C_2 \rrbracket) || (\min \llbracket C_3 \rrbracket || \min \llbracket C_4 \rrbracket)$ , or to every intermediate level in the hierarchy, i.e.,  $\min(\min(\min \llbracket C_1 \rrbracket || \min \llbracket C_2 \rrbracket) || \min(\min \llbracket C_3 \rrbracket || \min \llbracket C_4 \rrbracket))$ , or any intermediate combination between these two extremes. Such strategies are called *static* as they are uniformly applied to all components.

Second, compositional minimisation is sometimes counterproductive. Replacing, in a parallel composition  $M_1 || \dots || M_n$ , some model  $M_i$  by its quotient  $\min(M_i)$  never increases the complexity, but computing  $(\min \llbracket C_1 \rrbracket || \dots || \min \llbracket C_n \rrbracket)$  rather than  $\llbracket C_1 || \dots || C_n \rrbracket$  may fail if the complexity of some  $\llbracket C_i \rrbracket$  is larger than that of  $\llbracket C_1 || \dots || C_n \rrbracket$ . This may very well occur when components are so tightly synchronised that the behaviour of a component  $C_i$  is strongly constrained by the other components; ignoring such components may lead to a huge, or even unbounded, state space for  $C_i$ . Shared memories, network links, and hardware buses are typical examples of components  $C_i$  whose models  $\llbracket C_i \rrbracket$  cannot be generated in isolation because they allow a potentially infinite number of read/write or send/receive operations, whereas the components that use these memories, links, or buses actually employ a much smaller set of operations. Thus, when performing compositional minimisation on a system  $S = C_1 || \dots || C_n$ , it is not necessarily optimal to minimise all components one by one; it might be more efficient to consider them two by two, three by three, etc., leading to a number of combinations that is an exponential of  $n$ .

<sup>4</sup> In theoretical papers that use  $M$  in place of  $L$ , there is a notational confusion between  $C_i$  and  $\llbracket C_i \rrbracket$ , which is particularly annoying when the latter cannot be computed.

Finding an optimal strategy is difficult, and computationally out of reach if the number of components is large. So, one can only rely on heuristics. Rather than using the aforementioned static strategies, which are probably suboptimal, it is more suitable to use *dynamic* strategies that decide, at each verification step, which subset of components is the best candidate for being generated and minimised.

Such a heuristic (called *smart reduction*) is proposed in [16], based on metrics that consider both the amount of synchronisations between components (trying to compose the most tightly synchronised components first, to avoid state-space explosion arising from the interleaving of loosely coupled components) and the proportion of transitions that can be hidden after composition (the more hidden transitions, the greater the gains during subsequent minimisation steps if a weak equivalence, e.g., branching bisimulation, is used).

### 2.3 Applications

Implementing compositional minimisation is a difficult challenge, because many software tools are required to implement  $M$ ,  $\parallel$ ,  $\approx$ ,  $\min$ ,  $L$ , and  $\llbracket \cdot \rrbracket$ . Moreover, if any of these tools is poorly implemented, the entire tool chain may become inefficient and useless for non-trivial applications.

A handful of tool prototypes have been developed in the 90s, but the best implementation of compositional minimisation available today is unquestionably the CADP toolbox [27], the development of which started in the late 80s and has been steadily pursued until now. Compositional verification, at large, is a particular strength of CADP [26]. Concerning compositional minimisation, CADP provides the following software tools and libraries:

- $M$  is implemented by BCG<sup>5</sup> (*Binary-Coded Graphs*), a compact format, with its associated software tools and libraries, that enable large transition systems (with billions of states and transitions) to be stored as computer files.
- $\parallel$  is implemented by EXP.OPEN<sup>6</sup>, a tool that, among other features, computes the parallel composition of transition systems executing concurrently and synchronised using the parallel operators of various process calculi.
- $\approx$  and  $\min$  are respectively implemented by BCG\_CMP<sup>7</sup> and BCG\_MIN<sup>8</sup>, two state-of-the-art tools (see [9] for an assessment) that compare and minimise transition systems modulo various equivalence and preorder relations.
- $L$  is implemented in multiple ways, as the CADP toolbox supports several high-level languages for describing value-passing concurrent systems. For many years, LOTOS (ISO/IEC international standard 8807) [46] has been the

<sup>5</sup> <http://cadp.inria.fr/man/bcg.html>

<sup>6</sup> <http://cadp.inria.fr/man/exp.open.html>

<sup>7</sup> [http://cadp.inria.fr/man/bcg\\_cmp.html](http://cadp.inria.fr/man/bcg_cmp.html)

<sup>8</sup> [http://cadp.inria.fr/man/bcg\\_min.html](http://cadp.inria.fr/man/bcg_min.html)

language of choice but, since 2010, it has been progressively replaced by LNT [28], a modern specification language combining features from process calculi, imperative languages, and functional languages.

- $[[\cdot]]$  is implemented by the two LOTOS compilers *CÆSAR*<sup>9</sup> and *CÆSAR.ADT*<sup>10</sup>, and by the *LNT2LOTOS*<sup>11</sup> translator, the combination of which delivers state-of-the-art user-friendliness and performance (see [57] [58] for an assessment).

Moreover, a unique feature of CADP is its scripting language SVL<sup>12</sup> [25], which can be seen as a process calculus extended with operations on labelled transition systems, e.g., comparison, minimisation, hiding and renaming of transition labels, detection of deadlocks and livelocks, etc. Designed with the goal of making compositional verification easily accessible to non-experts [51], SVL and its associated compiler<sup>13</sup> implement the aforementioned static and dynamic strategies, including smart reduction.

Compositional minimisation, as implemented in CADP, has been successfully used in many case studies. A dozen of small- or medium-size examples are available online, as part of the CADP demos<sup>14</sup>. In four of these examples (demos No. 05, 18, 25, and 35, which have between 5 and 20 components), compositional minimisation easily succeeds (generating intermediate models with  $2 \cdot 10^6$  states at most) where direct generation fails. In seven other examples (demos No. 01, 02, 08, 17, 27, 28, and 36, which have between 4 and 11 components), the largest intermediate model generated by compositional minimisation is between 1.7 and 24 times smaller than the model obtained using direct generation.

Here is a chronological list (since 1991) of case studies in which compositional minimisation, as implemented in CADP, has been used to achieve functional verification. For conciseness, we use the symbol  $\star$  to indicate those case studies in which the author's laboratories (INRIA Grenoble, LIG, and/or Verimag) have been involved:

- rel/REL reliable atomic multicast protocol<sup>15</sup> [3, 19], Hewlett-Packard (UK) $\star$ .
- Transit Node message router<sup>16</sup> [61] $\star$ .
- CoopScan framework for cooperative applications development<sup>17</sup> [47] $\star$ .
- Transmission Control Protocol (TCP)<sup>18</sup> [73], Berlin (DE).
- Distributed leader election for unidirectional ring networks<sup>19</sup> [29] $\star$ .

<sup>9</sup> <http://cadp.inria.fr/man/caesar.html>

<sup>10</sup> <http://cadp.inria.fr/man/caesar.adt.html>

<sup>11</sup> <http://cadp.inria.fr/man/lnt2lotos.html>

<sup>12</sup> <http://cadp.inria.fr/man/svl-lang.html>

<sup>13</sup> <http://cadp.inria.fr/man/svl.html>

<sup>14</sup> <http://cadp.inria.fr/demos>

<sup>15</sup> <http://cadp.inria.fr/case-studies/91-c-relrel.html>

<sup>16</sup> <http://cadp.inria.fr/case-studies/94-a-transitnode.html>

<sup>17</sup> <http://cadp.inria.fr/case-studies/95-c-groupware.html>

<sup>18</sup> <http://cadp.inria.fr/case-studies/96-d-tcp.html>

<sup>19</sup> <http://cadp.inria.fr/case-studies/96-f-leADERelection.html>



- Bus arbitration of the Powerscale architecture<sup>20</sup> [11], Bull, Les Clayes (FR)\*.
- Eurocontrol’s Departure Clearance Protocol<sup>21</sup> [17], Brussels (BE).
- OM/RR protocol for traffic control<sup>22</sup> [86, 85], Eindhoven (NL).
- INRES protocol<sup>23</sup> [53], Nokia Research Center (FI).
- Bull’s CFS distributed file system for AIX<sup>24</sup> [64]\*.
- Philips’ HAVi leader election protocol<sup>25</sup> [67], Amsterdam (NL).
- Single pulser and bus arbitration hardware designs<sup>26</sup> [41], Stirling (UK).
- Sync-stop & Chandi-Lamport checkpoint algorithms<sup>27</sup> [35], Bucharest (RO)\*.
- Chilean electronic invoices system<sup>28</sup> [2, 6], Sophia Antipolis (FR).
- FRACTAL software components<sup>29</sup> [4, 5], Sophia Antipolis (FR), London (UK).
- FAUST asynchronous network-on-chip<sup>30</sup> [71, 72], CEA/Leti, Grenoble (FR)\*.
- Diagrams for choreographies<sup>31</sup> [70], Málaga (ES) and Santa Barbara (US).
- Trivial File Transfer Protocol (TFTP)<sup>32</sup> [31], Airbus, Toulouse (FR)\*.
- CRESS diagrams for Web and grid services<sup>33</sup> [77], Stirling (UK).
- Logical regulatory modules<sup>34</sup> [59], Oeiras (PT), Evry-Paris-Marseille (FR)\*.
- Fault-tolerant routing algorithm for a network-on-chip<sup>35</sup> [89], Utah (US)\*.
- Graphical user interfaces<sup>36</sup> [62], Atos, Grenoble (FR)\*.

Compositional minimisation has also been used for performance evaluation:

- Performance analysis of a Plain Old Telephone System<sup>37</sup> [43], Erlangen (DE).
- SCSI-2 bus arbitration protocol<sup>38</sup> [24], Twente (NL)\*.
- European Train Control System<sup>39</sup> [8], Saarbrücken (DE), Freiburg (DE).

<sup>20</sup> <http://cadp.inria.fr/case-studies/96-h-powerscale.html>

<sup>21</sup> <http://cadp.inria.fr/case-studies/97-c-dcl.html>

<sup>22</sup> <http://cadp.inria.fr/case-studies/98-d-omrr.html>

<sup>23</sup> <http://cadp.inria.fr/case-studies/98-g-inres.html>

<sup>24</sup> <http://cadp.inria.fr/case-studies/98-i-cfs.html>

<sup>25</sup> <http://cadp.inria.fr/case-studies/99-a-havi.html>

<sup>26</sup> <http://cadp.inria.fr/case-studies/99-b-dill.html>

<sup>27</sup> <http://cadp.inria.fr/case-studies/01-d-checkpointing.html>

<sup>28</sup> <http://cadp.inria.fr/case-studies/04-a-electronic-invoices.html>

<sup>29</sup> <http://cadp.inria.fr/case-studies/05-c-components.html>

<sup>30</sup> <http://cadp.inria.fr/case-studies/07-a-faust.html>

<sup>31</sup> <http://cadp.inria.fr/case-studies/09-a-collab-diag.html>

<sup>32</sup> <http://cadp.inria.fr/case-studies/09-h-tftp.html>

<sup>33</sup> <http://cadp.inria.fr/case-studies/09-p-web-and-grid.html>

<sup>34</sup> <http://cadp.inria.fr/case-studies/13-c-regulatory-modules.html>

<sup>35</sup> <http://cadp.inria.fr/case-studies/13-f-utahnoc.html>

<sup>36</sup> <http://cadp.inria.fr/case-studies/14-d-hmi.html>

<sup>37</sup> <http://cadp.inria.fr/case-studies/98-b-markov-pots.html>

<sup>38</sup> <http://cadp.inria.fr/case-studies/02-f-scsi-2.html>

<sup>39</sup> <http://cadp.inria.fr/case-studies/06-e-etcs.html>

### 3 The Seminal Papers of Graf, Steffen, and Lüttgen

In spite of these achievements, compositional minimisation still faces practical limitations when some components (such as the aforementioned shared memories, network links, and hardware buses) cannot be analysed separately from their neighbour components. This problem was addressed, as early as 1990, by Graf & Steffen in a series of five scientific papers:

- [36]: the original paper, published at the first CAV workshop in 1990, which contains all the fundamental contributions;
- [37]: a technical report from RWTH Aachen, published in 1991, which gives the proofs for the theorems of [36];
- [38]: a technical report from Universität Passau, with Gerald Lüttgen as third author, published in 1995, which extends the theoretical developments of the former papers and includes a running example that illustrates the key steps of the approach;
- [39]: a 10-page extended abstract published in the paper version of the *Journal on Formal Aspects of Computing*; due to constraints on the number of pages, this paper does not contain more material than the initial paper [36];
- [40]: a 28-page journal article, which is based on [38] and can be considered as the most complete version; this article is available online from the electronic repository of the *Journal on Formal Aspects of Computing*<sup>40</sup>.

These papers are a breakthrough in compositional verification, as they target the difficult case where some component  $C_i$  of a system  $S = C_1 || \dots || C_n$  cannot be minimised in isolation from its *environment*, i.e., from the other components  $C_1 || \dots || C_{i-1} || C_{i+1} || \dots || C_n$ . Precisely, this is the case where the behaviour of  $C_i$  is potentially huge, so that state-space explosion occurs when computing  $\llbracket C_i \rrbracket$ , but only a fraction of this behaviour is actually permitted by the environment of  $C_i$ . To address such situations, Graf & Steffen propose the following approach, which we reformulate here in a didactic manner:

- The constraints<sup>41</sup> exerted on  $C_i$  by its neighbour components must be expressed as an *interface*<sup>42</sup> noted  $I$ , which is intended to be a set of traces containing all the sequences of actions allowed by the environment. Concretely, the interface is represented as a labelled transition system, and the traces are the words of the language recognised by this automaton. In practice,  $I$  is usually specified in the same high-level language  $L$  as the components  $C_1, \dots, C_n$  and later translated to the low-level formalism  $M$ . It is assumed that  $I$  is small enough that state-space explosion never occurs when computing  $\llbracket I \rrbracket$ .

<sup>40</sup> Online manuscript at <http://www-verimag.imag.fr/~graf/PAPERS/GLS96.pdf>.

<sup>41</sup> Also called *context constraints* or *environment constraints* in the literature.

<sup>42</sup> Also called *behavioural interface*, *interface specifications*, or *process interface*.

- Graf & Steffen assume that the interface  $I$  is provided by the user, based on his/her own intuition of how the environment behaves. Thus, the interface is not necessarily *exact* because of human errors or approximations:
  - If the interface is too *restrictive*, i.e., if it contains less traces than allowed by the environment, this is a severe problem, as the model computed for  $C_i$  will be truncated, so that subsequent verification steps will be done under false assumptions. In such case, the interface is said to be *incorrect*.
  - If the interface is too *permissive*, i.e., if it contains more traces than allowed by the environment, there is no correction problem, but there might be a performance problem, as the model computed for  $C_i$  will be larger than actually needed. The most permissive interface is the “chaos” automaton that accepts all actions of  $C_i$  in any order, which is equivalent to having no interface for  $C_i$ .

So, a correct interface should be a superset of the traces allowed by the environment. Said differently, a correct interface should express some of, but not necessarily all, the constraints exerted by the neighbour components.

- Graf & Steffen define a *semi-composition*<sup>43</sup> operator  $\Pi_I(C_i) = \pi_1(\llbracket C_i \parallel I \rrbracket)$ , where  $\parallel$  denotes the parallel composition operator of CSP [45] that forces  $C_i$  and  $I$  to synchronise on their common actions, while letting  $C_i$  (resp.  $I$ ) interleave on its actions that are absent from  $I$  (resp.  $C_i$ ), and where  $\pi_1$  is a function that projects the product labelled transition system  $\llbracket C_i \parallel I \rrbracket$  onto the states of  $\llbracket C_i \rrbracket$ , meaning that each product state  $(x, y)$  is mapped to  $x$  and each product transition  $(x, y) \xrightarrow{a} (x', y')$  is either mapped to  $x \xrightarrow{a} x'$  if  $a$  is an action of  $C_i$ , or ignored otherwise.
- The semi-composition operator enjoys nice properties: (i)  $\Pi_I(C_i)$  is behaviourally included in  $\llbracket C_i \rrbracket$ , in the sense that both models have the same initial state and that any transition  $x \xrightarrow{a} x'$  of  $\Pi_I(C_i)$  is also a transition of  $\llbracket C_i \rrbracket$ ; (ii) the number of states in  $\Pi_I(C_i)$  is thus less or equal to the number of states in  $\llbracket C_i \rrbracket$  (the more restrictive the interface, the smaller this number); (iii) if  $I$  is the chaos automaton allowing all the actions of  $C_i$ , then  $\Pi_I(C_i) = \llbracket C_i \rrbracket$ ; (iv) interfaces can be safely minimised using language equivalence or any stronger equivalence.
- But the most important property is the following one: if interface  $I$  is correct, then  $\llbracket C_1 \parallel \dots \parallel C_n \rrbracket = \llbracket C_1 \rrbracket \parallel \dots \parallel \llbracket C_{i-1} \rrbracket \parallel \Pi_I(C_i) \parallel \llbracket C_{i+1} \rrbracket \parallel \dots \parallel \llbracket C_n \rrbracket$ , meaning that  $\llbracket C_i \rrbracket$  can be safely replaced with  $\Pi_I(C_i)$ , which is presumably less complex<sup>44</sup>, or even with  $\min(\Pi_I(C_i))$ , because  $\llbracket C_1 \parallel \dots \parallel C_n \rrbracket \approx \llbracket C_1 \rrbracket \parallel \dots \parallel \llbracket C_{i-1} \rrbracket \parallel \min(\Pi_I(C_i)) \parallel \llbracket C_{i+1} \rrbracket \parallel \dots \parallel \llbracket C_n \rrbracket$  since  $\approx$  is a congruence.

<sup>43</sup> This operator was actually named *reduction* in [36], but we prefer the term *semi-composition* later introduced by Krimm & Mounier [50], because the former term often denotes a minimisation operation that is incompletely done, yielding a smaller yet not necessarily minimal result: partial-order reduction, symmetry reduction, tau-confluence reduction, etc.

<sup>44</sup> In some cases [36, Sect. 6], interfaces reduce complexity from exponential to linear.

- Graf & Steffen also address the case of incorrect interfaces by extending  $\Pi_I(C_i)$  with *undefinedness predicates* that indicate, for each state, which actions of  $C_i$  have been cut off by  $I$ . Later, when recombining  $\Pi_I(C_i)$  with its environment, the parallel composition operator discharges those predicates corresponding to transitions of  $C_i$  that the environment is never ready to synchronise with, and would indeed never fire. If some predicates remain undischarged when the parallel composition is done, then  $I$  is incorrect; the user should analyse these predicates to understand why/where  $I$  is too restrictive, and restart compositional verification with a modified interface<sup>45</sup>.

Figure 1 illustrates the semi-composition of a component  $C_i$  with an interface  $I$ , both having 0 as their initial state. All transitions of  $C_i$  labelled by actions  $a_0$ ,  $a_2$ ,  $b_0$ ,  $b_2$ ,  $c_0$ , and  $c_2$  are cut off, because they never synchronise in the parallel composition with  $I$ . The action sets attached to the states 0, 2, and 5 of  $\Pi_I(C_i)$  represent the undefinedness predicates; for instance, the set attached to state 0 indicates that transitions labelled by  $a_0$  and  $a_2$  have been cut off in this state.

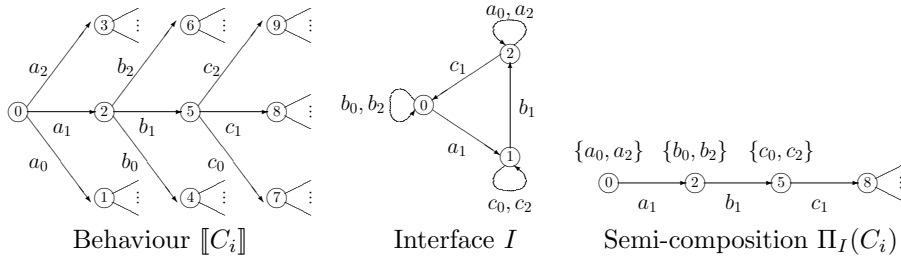


Figure 1: Reduction achieved using semi-composition with an interface

## 4 Compositional Minimisation with Interfaces but without Semi-Composition

We now examine two approaches that, given a set of asynchronous components  $S = C_1 || \dots || C_n$  synchronised by rendezvous, reuse the idea of interfaces to avoid state-space explosion when generating certain components. These approaches do not borrow the semi-composition operator concept, and thus technically differ from the work of Graf & Steffen.

The first approach was proposed by Cheung & Kramer [12] [13] [14] and implemented in the TRACTA tool [33]:

- In this approach, a component  $C_i$  having an interface  $I$  is replaced by  $\llbracket C_i || I \rrbracket$  instead of being replaced by the semi-composition  $\Pi_I(C_i) = \pi_1(\llbracket C_i || I \rrbracket)$ .

<sup>45</sup> Such an iterative approach based upon incremental refinement was very much the CEGAR idea published ten years later [15].

- To ensure that  $\llbracket C_1 \rrbracket \parallel \dots \parallel \llbracket C_{i-1} \rrbracket \parallel \llbracket C_i \parallel I \rrbracket \parallel \llbracket C_{i+1} \rrbracket \parallel \dots \parallel \llbracket C_n \rrbracket$  is strongly bisimilar to  $\llbracket C_1 \rrbracket \parallel \dots \parallel \llbracket C_n \rrbracket$ , the interface  $I$  must not only be correct in the sense of Graf & Steffen, but also deterministic and free of internal actions<sup>46</sup>.
- The initial paper [12] assumes that interfaces are correct without checking for correctness. In [13] [14], the approach is refined as follows to deal with incorrect interfaces. An *output-completion* operation is applied to transform the user-given interface  $I$  into an extended interface  $I'$ : this is done by adding an *undefined* state  $\pi$  and by creating, for each state  $y$  of  $I$  and each action  $a$  not enabled in  $y$ , an additional transition  $y \xrightarrow{a} \pi$ . When computing  $S' = \llbracket C_1 \rrbracket \parallel \dots \parallel \llbracket C_{i-1} \rrbracket \parallel \llbracket C_i \parallel I' \rrbracket \parallel \llbracket C_{i+1} \rrbracket \parallel \dots \parallel \llbracket C_n \rrbracket$ , each transition  $(x, y) \xrightarrow{a} (x', \pi)$  of  $\llbracket C_i \parallel I' \rrbracket$  should normally disappear (i.e., be blocked) unless it can synchronise with another action  $a$  present in the environment of  $C_i$ , i.e.,  $\llbracket C_1 \rrbracket \parallel \dots \parallel \llbracket C_{i-1} \rrbracket \parallel \llbracket C_{i+1} \rrbracket \parallel \dots \parallel \llbracket C_n \rrbracket$ , thus signalling that  $I$  is too restrictive. Hence, interface  $I$  is correct iff  $S'$  contains no reachable state whose  $i^{\text{th}}$  element has the form  $(x', \pi)$ .

The second approach was proposed by Valmari [81] and implemented in the ARA tool [82]. This approach is similar to the one of Cheung & Kramer, with two differences: interfaces are allowed to be nondeterministic, and the user must explicitly introduce the undefined state<sup>47</sup>  $\pi$  in the interface, i.e., provide an interface  $I'$  rather than  $I$ .

At first sight, these two approaches may look simpler and more elegant than the one of Graf & Steffen, because they do not require a semi-composition operator, but they are actually inferior (although they were published later than [36]), for at least three reasons:

1. Semi-composition is a reduction, meaning that  $\Pi_I(C_i)$  is smaller than  $\llbracket C_i \rrbracket$ , but parallel composition is not. Indeed,  $\llbracket C_i \parallel I \rrbracket$  can be (much) larger than  $\llbracket C_i \rrbracket$ . Figure 2 shows a simple example in which  $\llbracket C_i \parallel I \rrbracket$  has three times more states than  $\llbracket C_i \rrbracket$ . Thus, using interfaces without semi-composition can be counter-productive, keeping in mind that  $\llbracket C_i \rrbracket$  is expected to be huge.

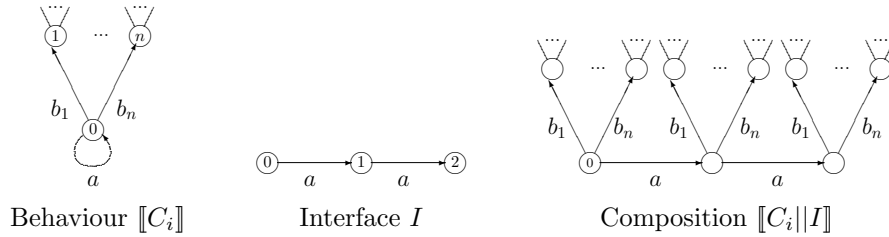


Figure 2: Example where  $\llbracket C_i \parallel I \rrbracket$  is larger than  $\llbracket C_i \rrbracket$

<sup>46</sup> Internal actions are usually noted  $\tau$  in most process calculi.

<sup>47</sup> This state is called *cut state* in [81].

2. The approach of Cheung & Kramer requires nondeterministic interfaces to be determinised [12, Sect. 5.1]. In the worst case, this may cause an exponential blowup in the number of states of the interface (e.g., a small interface with 40 states may get larger than one trillion states), thus compromising the compositional verification approach.
3. The approach of Valmari requires the introduction of the state  $\pi$  and its associated transitions into (possibly nondeterministic) interfaces. No algorithm is provided for such an operation, which might be trivial only for deterministic interfaces — unless determinisation (at the risk of exponential blowup) is first applied to nondeterministic interfaces. Figure 3 shows indeed that the aforementioned output-completion operation works for a deterministic interface  $I_1$ , but not for a nondeterministic interface  $I_2$  language-equivalent to  $I_1$ : the output-complete interfaces  $I'_1$  and  $I'_2$  are not language-equivalent (e.g.,  $I'_2$  accepts a trace  $a.b$  ending in  $\pi$ , whereas  $I'_1$  does not).

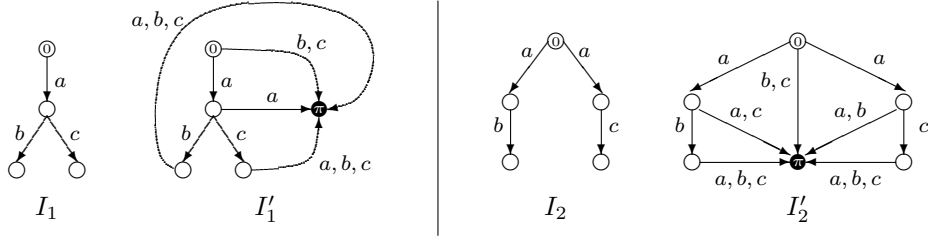


Figure 3: Example where language equivalence is not preserved by output completion

For the sake of completeness, one can mention a third approach [87] that, strictly speaking, does not use interfaces, but simulates their effect by introducing additional synchronisation actions *sleep* and *wake*. From a practical perspective, this approach is not suitable, as it requires to modify the code of components to insert these actions, and also changes the well-established semantic rules for the parallel composition operator, so as to perform look-ahead of *sleep* actions.

## 5 Compositional Minimisation with Interfaces and Semi-Composition

### 5.1 Principles

The first (and, to the best of our knowledge, the only) complete implementation of the ideas of Graf & Steffen has been done by Krimm & Mounier [49] [50], who adapted the approach to the case of LOTOS [46]. Such adaptation faces various changes in the base assumptions:

- Graf & Steffen (but also Cheung & Kramer and Valmari) consider the parallel composition operator  $\parallel$  of CSP [45], which forces synchronisation on all common actions. On the contrary, the parallel composition operator  $\parallel[g_1, \dots, g_n]$  forces synchronisation only on actions whose gate<sup>48</sup> belongs to the (possibly empty) list  $g_1, \dots, g_n$ , whereas all other actions do not synchronise (i.e., interleave).
- The LOTOS operator enables components to have common, yet non-synchronised actions, e.g., between two components  $C_1$  and  $C_2$  executing in full interleaving (i.e.,  $C_1 \parallel C_2$ ) and proposing the same actions.
- The LOTOS operator also enables nondeterministic synchronisations, e.g., between three components  $C_1$ ,  $C_2$ , and  $C_3$  connected using  $(C_1 \parallel C_2) \parallel[g] C_3$ : any action having gate  $g$  proposed by  $C_3$  may synchronise either with  $C_1$  or  $C_2$ . This is a most useful pattern to describe pools of clients and servers.
- The parallel operator of CSP is associative whereas, in LOTOS,  $(C_1 \parallel[g] C_2) \parallel[g'] C_3$  may be different from  $C_1 \parallel[g] (C_2 \parallel[g'] C_3)$  when  $g \neq g'$ .
- The LOTOS operator for action hiding, which was not considered by Graf & Steffen, needs to be taken into account.

In a nutshell, the solution proposed by Krimm & Mounier works as follows:

- Interfaces are labelled transition systems, which can be nondeterministic and contain internal actions (same as in the approach of Graf & Steffen).
- The semi-composition operator  $\Pi_I(C_i)$  is generalised to a new operator with four arguments: (i) a component  $C_i$ ; (ii) an interface  $I$ ; (iii) a list of gates  $g_1, \dots, g_n$  on which  $C_i$  and  $I$  must synchronise; (iv) a Boolean stating whether  $I$  is surely correct or possibly incorrect, the former case avoiding correctness checks. The useful properties of  $\Pi_I(C_i)$  also hold for this new operator.
- The undefinedness predicates of [36], which are a state-based concept incompatible with labelled transition systems, are encoded by means of *fail-transitions*. In the labelled transition system computed by the semi-composition operator for a possibly incorrect interface  $I$ , state  $s$  has a self-loop transition  $s \xrightarrow{\text{fail}(a)} s$  iff the interface has cut off action  $a$  in that state. The parallel composition operator of LOTOS is also slightly modified to handle these fail-transitions.

The prototype tools developed by Krimm & Mounier have been rewritten and integrated in CADP, which has become the reference framework for compositional minimisation techniques [26]. The DES2AUT tool has been subsumed by SVL<sup>49</sup>.

<sup>48</sup> A LOTOS action can be seen as a value tuple, the first element of which is the gate.

<sup>49</sup> <http://cadp.inria.fr/man/svl-lang.html> (see “abstraction”)

The PROJECTOR tool<sup>50</sup> implements the semi-composition operator; it is built upon the OPEN/CÆSAR application programming interface [22], which enables  $\Pi_I(C_i)$  to be computed on the fly, without computing  $\llbracket C_i \rrbracket$  first (this could cause state-space explosion), and also enables  $C_i$  to be expressed in any specification language connected to OPEN/CÆSAR, including LOTOS, LNT, EXP, etc.

## 5.2 Interface Synthesis

Assume a system  $S = C_1 || \dots || C_n$ , some components of which are too large to be generated separately from their neighbour components and thus require interfaces. Is it possible to generate automatically and correctly these interfaces, rather than asking the user to provide them, at the risk of human mistakes? This question has been studied in two papers.

The first paper [50] considers a process-algebraic setting in which components are combined inside expressions by means of the LOTOS operators for action hiding and parallel composition. An algorithm is given [50, Sect. 3, operator  $\Psi$ ] to automatically compute an interface for a given component, seen as a sub-expression contained in a larger expression describing the entire system or a part of it. This algorithm works recursively by structural induction on the syntax of LOTOS expressions and calculates the set of actions on which the component and its environment have to synchronise.

The second paper [52] considers a more expressive setting, communicating-automata networks, the components of which are combined using synchronisation vectors [1] that can encode action hiding, action renaming, and the parallel composition operators of most process calculi (including CCS, CSP,  $\mu$ CRL, LNT, LOTOS, etc.) as particular cases. An algorithm is given, which explores the synchronisation graph to compute a correct interface for a given component. This algorithm, which has been implemented in SVL<sup>51</sup>, improves over the one of [50] in several respects:

- It is applicable to other process calculi than LOTOS.
- It can compute an interface for a component, the environment of which can be arbitrarily chosen to be any subset of components, without requiring these components to be adjacent or closely connected in a process-algebraic expression (this is useful in presence of parallel composition operators that are not associative because they synchronise on different action sets).
- It handles the possible existence of common, yet non-synchronised actions between the component and its environment.
- It handles the possible existence of common, nondeterministically synchronised actions between the component and its environment (i.e., the environment can synchronise on a given action either with the component or

<sup>50</sup> <http://cadp.inria.fr/man/projector.html>

<sup>51</sup> <http://cadp.inria.fr/man/svl-lang.html> (see “refined abstraction”)



with another component, and vice versa). Such actions are ignored in [50], leading to over-permissive interfaces.

- It can generate, in the case of LOTOS, less permissive interfaces than [50], possibly leading to better reductions [52, Examples 2–3 and Figure 1].

### 5.3 Applications

Four examples of compositional verification with interfaces and semi-composition are available online, as part of the CADP demos<sup>52</sup>. For these examples (demos No. 20, 33, 37, and 38, which have between 3 and 60 components), both direct generation and compositional minimisation without interfaces fail, but compositional minimisation with interfaces and semi-composition succeeds, the largest intermediate model generated having less than 700,000 states.

Compositional verification with interfaces and semi-composition, as implemented in CADP, has been used with success in various (mostly industrial) case-studies:

- rel/REL reliable atomic multicast protocol<sup>53</sup> [50], Hewlett-Packard (UK)\*.
- Distributed leader election for unidirectional ring networks<sup>54</sup> [50]\*.
- ATC (Air Traffic Control) system<sup>55</sup> [69], Glasgow (UK).
- PolyKid CC-NUMA multiprocessor architecture<sup>56</sup> [32], Bull, Pregnana (IT)\*.
- ScalAgent’s deployment protocol for software components<sup>57</sup> [78]\*.
- Mutual exclusion protocols for CC-NUMA architectures<sup>58</sup> [55, 56]\*.
- Asynchronous circuit for the DES (Data Encryption Standard)<sup>59</sup> [74]\*.
- Asynchronous Memory Protection Unit<sup>60</sup> [10], Tiempo, Grenoble (FR)\*.

## 6 Conclusion

Although compositional verification is now thirty years old, and despite its true potential in overcoming state-space explosion (as demonstrated in many convincing case studies), it is not yet a widespread verification technique, and its use for practical problems remains rather an exception than the rule.

A major breakthrough was made in 1990 with a series of papers by Graf, Steffen & Lüttgen [36] [37] [38] [39] [40]. Unfortunately, the merits of these papers are

<sup>52</sup> <http://cadp.inria.fr/demos>

<sup>53</sup> <http://cadp.inria.fr/case-studies/91-c-relrel.html>

<sup>54</sup> <http://cadp.inria.fr/case-studies/96-f-leaderelection.html>

<sup>55</sup> <http://cadp.inria.fr/case-studies/99-e-atc.html>

<sup>56</sup> <http://cadp.inria.fr/case-studies/00-c-polykid.html>

<sup>57</sup> <http://cadp.inria.fr/case-studies/03-e-parfums.html>

<sup>58</sup> <http://cadp.inria.fr/case-studies/10-f-mutex.html>

<sup>59</sup> <http://cadp.inria.fr/case-studies/15-f-des.html>

<sup>60</sup> <http://cadp.inria.fr/case-studies/18-1-mpu.html>

not sufficiently understood. Either these papers are not mentioned in surveys [65] [20] [21] or they are merely cited without any further comment on the significance of their contributions [34]. These are injustices the present article tries to remedy.

The approach of [36] relies upon two key concepts: *interfaces* and *semi-composition*. Using these concepts is not mandatory, as it is possible to perform compositional minimisation without interfaces (Sect. 2) or with interfaces but without semi-composition (Sect. 4). We have shown, however, that the best results are obtained when both concepts are taken advantage of (Sect. 5).

The approach of [36] has been generalised to the case of LOTOS and its descendent languages, and fully implemented in the CADP verification toolbox [26] and successfully applied to numerous case studies, the most recent of which [10] shows impressive results, as an asynchronous hardware block containing not less than 660 concurrent processes was fully verified in a few hours by an industry engineer without prior training in formal methods. This is a clear indication that compositional minimisation techniques have reached a maturity level sufficient to enable their use in industry.

Concerning future research, we envision enhanced approaches for interface synthesis so as to generate interfaces automatically in complex cases that, today, must be dealt with manually, as well as applications of the ideas of Graf & Steffen to quantitative verification, including probabilistic, timed, and hybrid systems.

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