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# Don't Interrupt Me When You Reconfigure my Service Function Chains

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**RESEARCH  
REPORT**

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## Don't Interrupt Me When You Reconfigure my Service Function Chains

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### Abstract:

Network Functions Virtualization (NFV) enables the complete decoupling of network functions from proprietary appliances and runs them as software applications on general-purpose servers. NFV allows network operators to dynamically deploy Virtual Network Functions (VNFs).

Software Defined Networking (SDN) introduces a logically centralized controller which maintains a global view of the network state. The centralized routing model of SDN jointly with the possibility of instantiating VNFs on-demand open the way for a more efficient operation and management of networks.

In this paper, we consider the problem of reconfiguring network connections with the goal of bringing the network from a sub-optimal to an optimal operational state. We propose optimization models based on the *make-before-break* mechanism, in which a new path is set up before the old one is torn down. Our method takes into consideration the chaining requirements of the flows and scales well with the number of nodes in the network. We show that, with our approach, the network operational cost defined in terms of both bandwidth and installed network function costs can be reduced and a higher acceptance rate can be achieved.

**Key-words:** Reconfiguration, Software Defined Networking, Service Function Chains, Network Function Virtualization

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## N'interrompez pas mes Chaines de Service Lorsque Je les Reconfigure

**Résumé :** La virtualisation des fonctions réseau (NFV) permet le découplage complet des fonctions réseau des appareils propriétaires et leur exécution en tant qu'applications logicielles. NFV permet aux opérateurs de réseaux de déployer dynamiquement des fonctions de réseau virtuel (VNF). Le Software Defined Networking (SDN) introduit un contrôleur centralisé qui maintient une vue globale de l'état du réseau. Le modèle de routage centralisé du SDN et la possibilité d'instancier les VNF à la demande ouvrent la voie à une exploitation et une gestion plus efficaces des réseaux.

Dans cet article, nous examinons le problème de la reconfiguration des connexions réseau dans le but de faire passer le réseau d'un état sous-optimal à un état opérationnel optimal. Nous proposons des modèles d'optimisation basés sur le mécanisme *make-before-break*, dans lequel un nouveau chemin est mis en place avant que l'ancien ne soit détruit. Ceci permet de ne pas avoir d'interruption du trafic. Notre méthode prend en compte les exigences de chaînage des flux et s'adapte bien au nombre de nœuds du réseau. Nous montrons qu'avec notre approche, le coût d'exploitation du réseau défini en termes de bande passante et de coûts des NFV installées peut être réduit tout en augmentant le taux d'acceptation des requêtes.

**Mots-clés :** Reconfiguration, SDN (réseaux logiciels), SFC (chaînes de service), NFV (fonctions réseaux virtuelles)

## 1 Introduction

The last decade has seen the development of new paradigms to pave the way for a more flexible, open, and economical networking. In this context, Software Defined Networking (SDN) and Network Function Virtualization (NFV) are two of the more promising technologies for the Next-Generation Network.

SDN aims at simplifying network management by decoupling the control plane from the data plane. Network intelligence is logically centralized in an SDN controller that maintains a global view of the network state. As a consequence, the network becomes programmable and can be coupled to users' business applications. Indeed, network devices do not need to be configured individually anymore as it becomes easier to manipulate them through a software program [1].

With the NFV paradigm, network functions (e.g., a firewall, a load balancer, and a content filtering) can be implemented in software and executed on generic-purpose servers located in small cloud nodes. Virtual Network Functions (VNFs) can be instantiated and scaled on-demand without the need of installing new equipment. The goal is to shift from specialized hardware appliances to commoditized hardware in order to deal with the major problems of today's enterprise middlebox infrastructure, such as cost, capacity rigidity, management complexity, and failures [2].

To meet customers' demands, VNFs are required to be interconnected to form complete end-to-end services. Besides, network flows are often required to be processed by an ordered sequence of network functions. For example, an Intrusion Detection System may need to inspect the packet before compression or encryption are performed. This notion is known as Service Function Chaining (SFC) [3].

Even though SDN and NFV are two different independent technologies, they are complementary. Each one can leverage off the other to improve networks and service delivery over them [4]. For instance, SDN has the potential to make the chaining of the network functions much easier.

In this context, a fundamental problem that arises is how to map these VNFs to nodes (servers) in the network to satisfy all demands, while routing them through the right sequence of functions and meeting service level agreements. In doing this, the capacity constraints on both nodes and links must be respected.

The network state changes continually due to the arrival and departure of flows. An optimal or near-optimal resource allocation may result after a lapse of time in over-provisioning or in an inefficient resource usage. Also, it may lead to a higher blocking probability even though there are enough resources to serve new demands. Indeed, as reported by [5], 99% of rejections were caused by bandwidth shortage even though there were enough resources to satisfy the request.

Therefore, operators must take it into consideration and adjust network configurations in response to changing network conditions to fully exploit the benefits of the SDN and NFV paradigms, and to avoid undue extra cost (e.g., software licenses, energy consumption, and Service Level Agreement (SLA) violation).

Thus, another problem is how to reroute traffic flows through the network and how to improve the mapping of network functions to nodes in the presence of dynamic traffic, with the goal being to bring the network closer to an optimal operating state, in terms of resource usage.

In this paper, we consider the problem of providing, for each demand, a path through the network in the case of dynamic traffic while respecting capacities on both links and nodes. Moreover, the problem also consists in provisioning VNFs in order to ensure that the traversal order of the network functions by each path is respected. Our goal is to minimize the network operational cost, defined as the sum of the bandwidth cost to route the demands and the cost for all the VNFs running in the network.

Since traffic is dynamic, the allocation of a demand is performed individually without having full knowledge of the incoming traffic. This may lead to a fragmented network which uses more resources than necessary. For instance, requests may be routed on long paths, and there may be more active network functions than needed. In order to overcome this issue and to minimize the network's operator cost, we also consider the problem of reconfiguring the demands, i.e., moving them from a *local optimal* allocation

to a *global optimal* one.

Reconfiguration can be performed at several moments in time. It can be done as soon as a new request arrives [6], when a request is rejected [7], when the physical network is modified [8], or it could also be done periodically when the network is not yet saturated.

Rerouting demands and migrating VNFs may take several time steps. If during this time, traffic is interrupted, it may have a non-negligible impact on the QoS experienced by the users. To tackle this issue, our strategy performs the reconfiguration by using a two-phase approach. First, a new route for the transmission is established while keeping the initial one enabled (i.e., two redundant data streams are both active in parallel), and after the network has been updated to the new state, the transmission moves on the new route and the resources used by the initial one are released. This strategy is often referred to as *make-before-break*.

Our contributions can be summarized as follows.

- We provide the first method, *Break-Free*, to reconfigure, with a *make-before-break mechanism*, a network routing a set of demands which have to go through service function chains. This mechanism allows to reach closer to optimal resource allocation while *not interrupting the demands* which have to be rerouted.
- We show that *Break-Free* allows to *lower the network cost* and *increase the acceptance rate*. It can achieve, in most considered cases, a gain close to the one of a reconfiguration algorithm that interrupts the requests (referred to as *Breaking-Bad* in the following), as proposed in the literature.
- We additionally exhibit that the percentage of demands which have to be rerouted to achieve a significant gain in terms of network cost or acceptance rate is very high. This shows the importance of considering mechanisms limiting the impact on the demands.
- Network reconfiguration has to be done frequently to achieve a significant gain, however this reconfiguration can be quickly computed and carried out, making it possible to be put into practice in real time.

The rest of this paper is organized as follows. In Section 2, we discuss related work. In Section 3, we formally state the problem addressed in this paper. Section 4 presents the optimization framework and develops the optimization models for solving the problem of routing a demand and reconfiguring the network. In Section 5, we validate our proposed optimization models by various numerical results on two real-world network topologies of different sizes. Finally, we draw our conclusion in Section 6.

## 2 Related Work

The problem of how to deploy and manage network services conceived as a chain of VNFs has received a significant interest in the research and industrial community. We refer to [9] and [10] for comprehensive surveys on the relevant state of the art.

Although a lot of effort has been made to develop efficient strategies to route demands and satisfy their chaining requirements, not enough has been made to improve resources usage during network operation. Recently, some research work has started to explore SDN capabilities for a more efficient usage of the network resources by dynamically adapting the routing configuration over time. For instance, Paris *et al.* [11] study the problem of online SDN controllers to decide when to perform flow reconfigurations for efficient network updating such that the flow reallocation cost is minimized. However, the network function requirements are not considered in their work. Indeed, the traffic of a request may need to be steered to traverse middleboxes implementing the required network functions.

Ayoubi *et al.* [12] propose an availability-aware resource allocation and reconfiguration framework for elastic services in failure-prone data center networks. Their work is limited to the case of Virtual Network scale-up requests such as resource demands increase, new network components arrival, and/or service

$G = (V, E)$	the network where $V$ represents the set of nodes and $E$ the set of links.
$C_{uv}$	capacity of a link $(u, v) \in E$ expressed as its total bandwidth available.
$C_u$	available resources <sup>1</sup> such as CPU, memory, and disk of a node $u \in V$ .
$\Delta_f$	number of units of bandwidth required by the function $f \in F$ .
$c_{u,f}$	installation cost of the function $f \in F$ which also depends on the node $u$ .
$(v_s, v_d, c_d, bw_d)$	each demand $d \in D$ is modeled by a quadruple with $v_s$ the source, $v_d$ the destination, $c_d$ the ordered sequence of network functions that need to be performed, and $bw_d$ the required units of bandwidth.

Table 1: Notation used throughout the paper

class upgrade. The goal is to provide the highest availability improvement minimizing the overall reconfiguration cost which reflects the amount of resources as well as any service disruption/downtime.

Ghaznavi *et al.* [13] propose a consolidation algorithm that optimizes the placement of the VNFs in response to on-demand workload. The algorithm decides the VNF Instances to be migrated on the basis of the reconfiguration costs implied by the migration. However, they assume only one type of VNF and do not consider chaining requirements.

In [14], Eramo *et al.* study the problem of migrating VNFs in the dynamic scenario. The considered objective is to minimize the network operation cost which is the sum of the energy consumption costs and the revenue loss due to the bit loss occurring during the downtime. However, their model does not consider the bandwidth resources.

The closest study to our work is from Liu *et al.* [15]. They consider the problem of optimizing VNFs deployment and readjustment to efficiently orchestrate dynamic demands. When a new request arrives, the service provider can serve it or change the provisioning schemes of the already deployed ones at time instances with a fixed interval in between. They consider the maximization of the service provider's profit which is the total profit from the served requests minus the total deployment cost as an optimization task. For this purpose, they formulate an Integer Linear Programming (ILP) model. Then, to reduce the time complexity, they design a column generation model. An important unaddressed issue concerns the revenue loss of an operator due to the QoS degradation occurring when demands are reconfigured [14]. Indeed, in their model, transmissions may need to be interrupted in order to be moved to the new computed state. Different from the above mentioned works, our aim is to provide efficient mechanisms to dynamically reallocate the demands *without the consequential QoS deterioration due to the traffic interruption, but instead using make-before-break strategy.*

### 3 Problem Statement and Notations

We model the network as a directed capacitated graph and the set of demands  $D$  as a set of quadruples as shown in Table 1, which defines the notation used throughout the paper.

We consider a setting with splittable flows as it is frequent to have load balancing in networks [16] and as it makes the model quicker to solve [17]. Following the model of [18], a demand can follow different paths and the network functions of its chain can be processed in different cloud nodes.

The optimization task consists in routing each demand while *minimizing the network operational cost* defined in terms of bandwidth and VNFs cost (licenses, energy consumption, etc). Also, as the dynamics related to the arrival and departure of demands may leave the network in a sub-optimal operational state, we want to reconfigure the network to improve resources usage and to be able to accommodate new incoming traffic. In doing this, we use the *make-before-break* mechanism to avoid network services disruption due to traffic rerouting resulting from the re-optimization process.

<sup>1</sup>A node  $u$  with a strictly positive number of cores (i.e.,  $C_u \in \mathbb{N}^+ = \{1, 2, \dots\}$ ) represents a cloud location with the capability to execute VNFs, while a node with  $C_u = 0$  is a node that serves only as an SDN router.

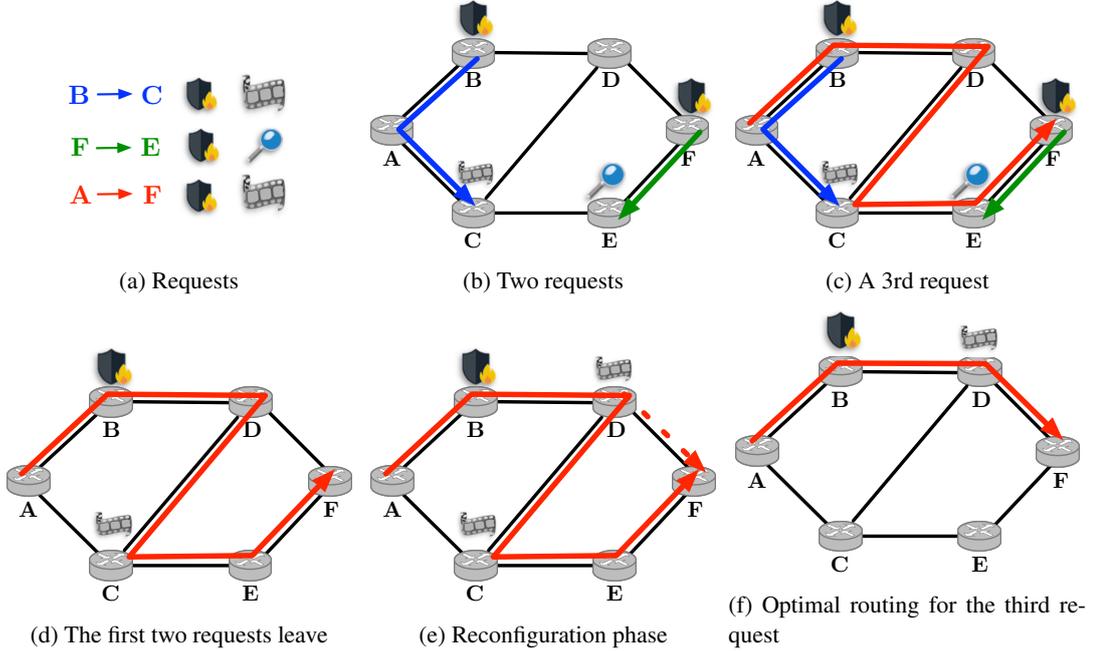


Figure 1: An example of the reconfiguration of a request using the *make-before-break* procedure.

*An Example.* Figure 1 illustrates an example for the reconfiguration of a request using a *make-before-break* process. When the request from A to F arrives, two requests have already been routed (step (b)). To avoid the cost of installing new VNFs, the route from A to F with minimum cost is a long 5-hops route (step (c)). When requests from B to C and from F to C leave, the request is routed on a non-optimal path (step (d)) which uses more resources than necessary. We compute one optimal 3-hops path and reroute the request to it (step (f)) with an intermediate *make-before-break* step (step (e)) in which both routes co-exist.

## 4 Modeling

In the considered setting, demands arrive and leave the network. To route them, we consider them one by one, and find the route which minimizes the *additional network operational cost* to be paid. Indeed, in an SDN network, even if multiple flows arrive simultaneously, they will be processed one by one by the SDN controller [19]. We then reconfigure the network to improve the network operational cost when one of the following conditions holds:

- Periodically, after a given period of time;
- When the set of requests has changed significantly (after a given number of SFC arrivals and departures);
- When a request arrives and cannot be accepted with the current provisioning and routing solution.

The solution we propose, called *Break-Free* (for *Break-Free Reconfiguration* algorithm), implements a *make-before-break* mechanism to avoid the interruption of the flows. In our experiments, we compare its results with a reconfiguration algorithm which does not implement such a mechanism, called *Breaking-Bad* (for *Breaking-Bad Reconfiguration* algorithm). This algorithm breaks the flows before

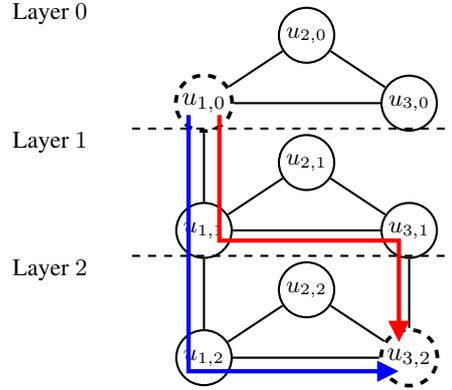


Figure 2: The layered network  $G^L(d)$  associated with a demand  $d$  such that  $v_s = u_1$ ,  $v_d = u_3$ , and  $c_d = f_1, f_2$ , within a triangle network.  $f_1$  is allowed to be installed on  $u_1$  and  $f_2$  on  $u_1$  and  $u_3$ . Source and destination nodes of  $G^L(d)$  are  $u_{1,0}$  and  $u_{3,2}$ . Two possible SFCs that satisfy  $d$  are drawn in red ( $f_1$  is in  $u_1$ ,  $f_2$  in  $u_3$ ) and blue ( $f_1$  and  $f_2$  is in  $u_1$ ).

rerouting them, and then packet loss occurred and QoS is degraded for these flows. When a reconfiguration has to be carried out, `Breaking-Bad` considers basically a static setting with the requests present in the network and finds an optimal Routing & Provisioning solution (R&P) without considering the current setting.

We present here three optimization models: (i) to solve the static problem (Section 4.2) used by `Breaking-Bad`, (ii) to route one demand when it arrives (Section 4.3), and (iii) to reconfigure the network with the make-before-break mechanism of `Break-Free` (Section 4.4).

Our models are based on the concept of a layered graph explained in a preliminary section (Section 4.1).

## 4.1 Layered graph

Similarly as in [20], in order to model the chaining constraint of a demand, we associate to each demand  $d$  a layered graph  $G^L(d)$ . We denote by  $u_{i,l}$  the copy of node  $u_i$  in layer  $l$ . The path for demand  $d$  starts from node  $v_{s,0}$  in layer 0 and ends at node  $v_{d,|c_d|}$  in layer  $|c_d|$  where  $|c_d|$  denotes the number of VNFs in the chain of the demand.

Given a link  $(u_i, v_j)$ , each layer  $l$  has a link  $(u_{i,l}, v_{j,l})$  defined. This property does not hold for links of the kind  $(u_{i,l}, u_{i,l+1})$ . Indeed, a node may be enabled to run only a subset of the virtual functions. To model this constraint, given a demand  $d$  we add a link  $(u_{i,l}, u_{i,l+1})$  only if Node  $u$  is enabled to run the  $(l+1)$ -th function of the chain of  $d$ . The  $l$ -th function of the chain of  $d$  will be denoted by  $f_l^{c_d}$ .

A path on the layered graph corresponds to an assignment to a demand of both a path and the locations where functions are being run. Using a link  $(u_{i,l}, v_{j,l})$  on  $G^L$ , implies using link  $(u, v)$  on  $G$ . On the other hand, using link  $(u_{i,l}, u_{i,l+1})$  implies using the  $(l+1)$ -th function of the chain at node  $u$ . Capacities of both nodes and links are shared among layers.

## 4.2 Static R&P: `Breaking-Bad`

To solve the static R&P problem, we use an ILP given below. The ILP routes the demands by finding a path on the layered graph for each of them. In doing this, both node and link capacities must be respected

as they are shared among all the demands. The ILP has the minimization of the network operational cost (i.e., bandwidth cost and network function activation cost) as an objective. As network functions can be shared, the ILP will try to activate a small number of network functions. The parameter  $\beta \geq 0$  specified by the network administrator accounts for different scales over which the functions' activation cost is put in relationship with the network bandwidth cost.  $\beta$  can be defined as the ratio between the cost of sending 1 TB of traffic on a link and the cost of installing a function which can handle 1 TB of data.

*Model.* The ILP takes as an input the set of demands  $D$ . The output corresponds to the *minimum cost SFC-R&P*.

Variables:

- $\varphi_{uv,i}^d \geq 0$  is the amount of flow on Link  $(u, v)$  in Layer  $i$  for Demand  $d$ .
- $\alpha_{u,i}^d \geq 0$  is the fraction of flow of Demand  $d$  using Node  $u$  in Layer  $i$ .
- $z_{u,f} \in \{0, 1\}$ , where  $z_{u,f} = 1$  if function  $f$  is activated on Node  $u$ .

Objective: minimize the amount of network resources consumed.

$$\min \sum_{d \in D} \sum_{(u,v) \in E} \sum_{i=0}^{|c_d|} bw_d \cdot \varphi_{uv,i}^d + \beta \cdot \sum_{u \in V} \sum_{f \in F} c_{u,f} \cdot z_{u,f}$$

*Flow conservation constraints.* For each Demand  $d \in D$ , Node  $u \in V$ .

$$\sum_{(u,v) \in \omega^+(u)} \varphi_{uv,0}^d - \sum_{(v,u) \in \omega^-(u)} \varphi_{vu,0}^d + \alpha_{u,0}^d = \begin{cases} 1 & \text{if } u = v_s \\ 0 & \text{else} \end{cases} \quad (1)$$

$$\sum_{(u,v) \in \omega^+(v)} \varphi_{uv,|c_d|}^d - \sum_{(v,u) \in \omega^-(v)} \varphi_{vu,|c_d|}^d - \alpha_{u,|c_d|-1}^d = \begin{cases} -1 & \text{if } v = v_d \\ 0 & \text{else} \end{cases} \quad (2)$$

$$\sum_{(u,v) \in \omega^+(u)} \varphi_{uv,i}^d - \sum_{(v,u) \in \omega^-(u)} \varphi_{vu,i}^d + \alpha_{u,i-1}^d - \alpha_{u,i}^d = 0, (0 < i < |c_d|) \quad (3)$$

*Node capacity constraints.* The capacity of a node  $u$  in  $V$  is shared between each layer and cannot exceed  $C_u$ . For each Node  $u \in V$ .

$$\sum_{d \in D} bw_d \sum_{i=0}^{|c_d|-1} \Delta_{f_i}^{c_d} \cdot \alpha_{u,i}^d \leq C_u. \quad (4)$$

*Link capacity constraints.* The capacity of a link  $(u, v) \in E$  is shared between each layer and cannot exceed  $C_{uv}$ . For each Link  $(u, v) \in E$ .

$$\sum_{d \in D} bw_d \sum_{i=0}^{|c_d|} \varphi_{uv,i}^d \leq C_{uv}. \quad (5)$$

*Functions activation.* To know which functions are activated on which nodes. For each Node  $u \in V$ , Function  $f \in F$ , Demand  $d \in D$ , Layer  $i \in \{0, \dots, |c_d| - 1\}$ .

$$\alpha_{u,i}^d \leq z_{u,f_i^{c_d}} \quad (6)$$

*Location constraints.* A node may be enabled to run only a subset of the virtual network functions. For each Demand  $d \in D$ , Node  $u \in V$ , layer  $i \in \{0, \dots, |c_d| - 1\}$ , if the  $(i + 1)$ -th function of  $c_d$  cannot be installed on Node  $u$ , we add the following constraint.

$$\alpha_{u,i}^d = 0 \quad (7)$$

### 4.3 R&P for a single demand

Note first, that even routing a single demand is NP-hard as it is equivalent to find a shortest Weight-Constrained Path [21] in the layered graph as link and node capacities are shared between layers [20]. A solution is to use the ILP for static R&P in which all the demands routed in the past are fixed. The ILP routes the demand (if possible) with the goal of minimizing the additional needed cost without exceeding the available network resources. To deal with the already installed network function, the *current cost*  $\tilde{c}_{u,f}$  of installing a network function  $f$  on a Node  $u$  is defined as follows. Let  $\mathcal{I}$  be the set with the already installed network function, then  $\tilde{c}_{u,f} = 0$  if  $(u, f) \in \mathcal{I}$ , and  $c_{u,f}$  otherwise.

*Model.* The ILP takes as an input a demand  $d = (v_s, v_d, c_d, bw_d)$  and the network. We denote by  $R_u$  the residual capacity of a Node  $u$ , and finally by  $R_{uv}$  the residual capacity of a link  $(u, v)$ .

Variables:

- $\varphi_{uv,i} \geq 0$  is the amount of flow on Link  $(u, v)$  in Layer  $i$ .
- $\alpha_{u,i} \geq 0$  is the fraction of flow of the demand using Node  $u$  in Layer  $i$  at time step  $t$ .

Objective: minimize the additional increase in terms of network operational cost.

$$\min \sum_{(u,v) \in E} \sum_{i=0}^{|c_d|} bw_d \cdot \varphi_{uv,i} + \beta \cdot \sum_{u \in V} \sum_{i=0}^{|c_d|-1} \tilde{c}_{u,f_i^{c_d}} \cdot \alpha_{u,i}$$

*Flow conservation constraints.* For each Node  $u \in V$ .

$$\sum_{(u,v) \in \omega^+(u)} \varphi_{uv,0} - \sum_{(v,u) \in \omega^-(u)} \varphi_{vu,0} + \alpha_{u,0} = \begin{cases} 1 & \text{if } u = v_s \\ 0 & \text{else} \end{cases} \quad (8)$$

$$\sum_{(u,v) \in \omega^+(v)} \varphi_{uv,|c_d|} - \sum_{(v,u) \in \omega^-(v)} \varphi_{vu,|c_d|} - \alpha_{u,|c_d|-1} = \begin{cases} -1 & \text{if } v = v_d \\ 0 & \text{else} \end{cases} \quad (9)$$

$$\sum_{(u,v) \in \omega^+(u)} \varphi_{uv,i} - \sum_{(v,u) \in \omega^-(u)} \varphi_{vu,i} + \alpha_{u,i-1} - \alpha_{u,i} = 0. \quad (10)$$

$0 < i < |c_d|$

*Node capacity constraints.* The capacity of a node  $u$  in  $V$  is shared between each layer and cannot exceed the residual capacity  $R_u$ . For each Node  $u \in V$ .

$$bw_d \sum_{i=0}^{|c_d|-1} \Delta_{f_i^{c_d}} \cdot \alpha_{u,i} \leq R_u. \quad (11)$$

*Link capacity constraints.* The capacity of a link  $(u, v) \in E$  is shared between each layer and cannot exceed the residual capacity  $R_{uv}$ . For each Link  $(u, v) \in E$ .

$$bw_d \sum_{i=0}^{|c_d|} \varphi_{uv,i} \leq R_{uv}. \quad (12)$$

Another possibility is to adapt the pseudo-polynomial algorithms proposed for the shortest Weight-Constrained Path problem such as the Label-setting algorithm based on dynamic programming [22].

#### 4.4 Break-Free Reconfiguration (Make-before-break)

A first way to perform the reconfiguration at a given time  $t$  is to try to *reconfigure to optimal*. This is done in two phases. In the first one, we compute a minimum cost routing for the set of demands present at time  $t$ . This can be done by using the model for static R&P. In the second one, we compute the transitions from the current routing to the optimal routing for each demand, taking into account the intermediate make-before-break steps during which two paths co-exist for a demand which is changing its route. This can be done using the ILP presented in this section, taking as inputs the current and the minimum cost solutions.

However, the transitions to an optimal solution may be long to compute or even impossible to carry out. Indeed, in complex scenarios (which occur when the network is saturated), the transition to the new routes cannot be performed directly. This is mainly due to two reasons.

First, in an intermediate step of the reconfiguration, two routes are provided, leading to an increased use of the network resources. Second, a request may have to be moved in an intermediate routing before being able to be moved to its final one in order to make place for the new routing of the first request. This needs to be done during distinct reconfigurations steps. Because of this, several intermediate steps of reconfigurations may be necessary, and each additional step of reconfiguration significantly increases the number of variables and constraints of the problem, and thus the time needed to obtain an optimal solution. Therefore, we propose a *best effort reconfiguration*.

**Best Effort Reconfiguration.** The idea here consists in improving the R&P as much as possible instead of setting a final R&P as a target. To this end, we set a number of intermediate reconfiguration steps,  $T$ , (how to set  $T$  is discussed below) and the goal of the optimization is to find a routing with minimal cost which can be reached from the current routing using  $T$  reconfiguration steps. Note that the best effort reconfiguration has several advantages compared to the reconfiguration to optimal. It will give a solution as good as the reconfiguration to optimal when such a reconfiguration is possible. Indeed, several optimal solutions may exist, and only part of them could be reached using reconfiguration. Reconfiguration to optimal is focusing on only one, when Best Effort reconfiguration could reach any of those. Second, when reconfiguration to optimal is not possible, Best Effort reconfiguration may still be able to find a solution better than the current one. This is why we used Best Effort reconfiguration in our experiments.

Best Effort reconfiguration can be modeled using the ILP presented in the following. At time 0, the R&P is set to the current one. Then, at each step of reconfiguration, a set of demands can be rerouted as long as there are enough link and node capacities to satisfy the intermediate make-before-break reconfiguration steps. This can be modeled linearly by defining a variable which is equal to 1 if a resource is used by a request either at time  $t - 1$  or at time  $t$ . As a single step of reconfiguration may not be enough, the ILP has several intermediate reconfiguration steps, each corresponding to a solution of the R&P problem. The objective function is to minimize the cost of the R&P of the final state.

Note that reconfiguration to optimal can be modeled using the same ILP with a few changes. We just have to set the variables corresponding to the final state to the minimum cost R&P computed previously.

**Choosing  $T$ , the number of reconfiguration steps.** The value of  $T$  is an important parameter. Indeed, a value too small may lead to models with no solution, while a value too large to models with prohibitive execution times. This is why we tested different values in our experiments. We observe that when the network is not congested, corresponding to the low-traffic scenarios of Section 5.2, a single reconfiguration step is enough to provide optimal (or close to optimal) solutions while it leads to solutions almost as bad as without reconfiguration in the high-traffic scenarios of Section 5.3. In the later scenarios, at least 2 reconfiguration steps are necessary. A good way to find the right value is to start with  $T = 1$ , which is the fastest model, and then to increase progressively the value of  $T$  until either the solution does not improve any more or the model solving time is too long. Note that, when a maximum solving time is set, the largest possible value of  $T$  leading to a lower solving time can also be found by dichotomy.

*Model.* The ILP takes as an input both the current configuration (i.e., paths and function locations for all the demands) and the number of time steps  $T$  to be used in the reconfiguration process. The output corresponds to both the final SFC-R&P at time  $T$  after the reconfiguration process and the intermediate SFC-R&P to be used to reach the final state. Between two consecutive time steps  $t_0 < \dots < t_i < t_{i+1} < \dots < T$ , a subset of the demands may be moved to a new route. In doing this, resources of both nodes and links must not be exceeded in order to not interrupt connections (*make-before-break*).

Variables:

- $\varphi_{uv,i}^{d,t} \geq 0$  is the amount of flow on Link  $(u, v)$  in Layer  $i$  at time step  $t$  for Demand  $d$ .
- $\alpha_{u,i}^{d,t} \geq 0$  is the fraction of flow of Demand  $d$  using Node  $u$  in Layer  $i$  at time step  $t$ .
- $x_{uv,i}^{d,t} \geq 0$  is the maximum amount of flow on Link  $(u, v)$  in Layer  $i$  at time steps  $t$  and  $t-1$  for Demand  $d$ .
- $y_{u,i}^{d,t} \geq 0$  is the maximum fraction of flow of demand  $d$  using Node  $u$  in Layer  $i$  at time steps  $t$  or  $t-1$ .
- $z_{u,f}^T \in \{0, 1\}$ , where  $z_{u,f}^T = 1$  if function  $f$  is activated on Node  $u$  at time step  $T$  in the final routing.

The optimization model starts with the initial configuration as an input. Thus, for each demand  $d \in D$  the variables  $\varphi_{uv,i}^{d,0}$  (for each node  $u \in V$ , layer  $i \in \{0, \dots, |c_d|\}$ ) and  $\alpha_{u,i}^{d,0}$  (for each link  $(u, v) \in E$ , layer  $i \in \{0, \dots, |c_d|\}$ ) are known. The ILP is based on the layered graph described in Section 4.1 and it is written as follows.

Objective: minimize the amount of network resources consumed during the last reconfiguration time step  $T$ .

$$\min \sum_{d \in D} \sum_{(u,v) \in E} \sum_{i=0}^{|c_d|} bw_d \cdot \varphi_{uv,i}^{d,T} + \beta \cdot \sum_{u \in V} \sum_{f \in F} c_{u,f} \cdot z_{u,f}^T$$

*Flow conservation constraints.* For each Demand  $d \in D$ , Node  $u \in V$ , time step  $t \in \{1, \dots, T\}$ .

$$\sum_{(u,v) \in \omega^+(u)} \varphi_{uv,0}^{d,t} - \sum_{(v,u) \in \omega^-(u)} \varphi_{vu,0}^{d,t} + \alpha_{u,0}^{d,t} = \begin{cases} 1 & \text{if } u = v_s \\ 0 & \text{else} \end{cases} \quad (13)$$

$$\sum_{(u,v) \in \omega^+(v)} \varphi_{uv,|c_d|}^{d,t} - \sum_{(v,u) \in \omega^-(v)} \varphi_{vu,|c_d|}^{d,t} - \alpha_{u,|c_d|-1}^{d,t} = \begin{cases} -1 & \text{if } v = v_d \\ 0 & \text{else} \end{cases} \quad (14)$$

$$\sum_{(u,v) \in \omega^+(u)} \varphi_{uv,i}^{d,t} - \sum_{(v,u) \in \omega^-(u)} \varphi_{vu,i}^{d,t} + \alpha_{u,i-1}^{d,t} - \alpha_{u,i-1}^{d,t} = 0. \quad (15)$$

$0 < i < |c_d|$

*Node usage over two consecutive time periods.* For each Demand  $d \in D$ , Node  $u \in V$ , Layer  $i \in \{0, \dots, |c_d| - 1\}$  time step  $t \in \{1, \dots, T\}$ .

$$\alpha_{u,i}^{d,t} \leq y_{u,i}^{d,t} \text{ and } \alpha_{u,i}^{d,t-1} \leq y_{u,i}^{d,t}$$

$$\alpha_{u,i}^{d,t} + \alpha_{u,i}^{d,t-1} \geq y_{u,i}^{d,t}$$

*Link usage over two consecutive time periods.* For each Demand  $d \in D$ , Link  $(u, v) \in E$ , Layer

$i \in \{0, \dots, |c_d|\}$  time step  $t \in \{1, \dots, T\}$ .

$$\begin{aligned} \varphi_{uv,i}^{d,t} &\leq x_{uv,i}^{d,t} \text{ and } \varphi_{uv,i}^{d,t-1} \leq x_{uv,i}^{d,t} \\ \varphi_{uv,i}^{d,t} + \varphi_{uv,i}^{d,t-1} &\geq x_{uv,i}^{d,t} \end{aligned}$$

*Make Before Break - Node capacity constraints.* The capacity of a node  $u$  in  $V$  is shared between each layer and cannot exceed  $C_u$  considering the resources used over two consecutive time periods. For each Node  $u \in V$ , time step  $t \in \{1, \dots, T\}$ .

$$\sum_{d \in D} bw_d \sum_{i=0}^{|c_d|-1} \Delta_{f_i^{c_d}} \cdot y_{u,i}^{d,t} \leq C_u. \quad (16)$$

*Make Before Break - Link capacity constraints.* The capacity of a link  $(u, v) \in E$  is shared between each layer and cannot exceed  $C_{uv}$  considering the resources used over two consecutive time periods. For each Link  $(u, v) \in E$ , time step  $t \in \{1, \dots, T\}$ .

$$\sum_{d \in D} bw_d \sum_{i=0}^{|c_d|} x_{uv,i}^{d,t} \leq C_{uv}. \quad (17)$$

*Location constraints.* A node may be enabled to run only a subset of the virtual network functions. For each Demand  $d \in D$ , Node  $u \in V$ , layer  $i \in \{0, \dots, |c_d| - 1\}$ , if the  $(i + 1)$ -th function of  $c_d$  cannot be installed on Node  $u$ , we add the following constraint for each time step  $t \in \{1, \dots, T\}$ .

$$\alpha_{u,i}^{d,t} = 0 \quad (18)$$

*Functions activation.* To know which functions are activated on which nodes in the final routing. For each Node  $u \in V$ , Function  $f \in F$ , Demand  $d \in D$ , and Layer  $i \in \{0, \dots, |c_d| - 1\}$ ,

$$\alpha_{u,i}^{d,T} \leq z_{u,f_i^{c_d}}^T. \quad (19)$$

Note that we do not consider the cost of potential activations of VNFs during the reconfiguration process. Indeed, our goal is to minimize the network operational cost over time and the reconfiguration duration is very small in comparison in an SDN network [23].

## 5 Numerical Results

In this section, we evaluate the performance of our proposed solution, *Break-Free*. We study the impact of the reconfiguration on different metrics such as cost savings, acceptance rate, and resource usage. We first present the data sets we use for the experiments. Then, we compare the results with the ones of *Breaking-Bad*, which computes an optimal R&P for the whole set of requests (ILP of Section 4.2) for each SFC arrival and with *No-Reconf* which computes the R&P problem for a single demand, the newly arrived SFC (Section 4.3).

We consider two scenarios, one with low traffic in which basically all demands can be accepted and one with high traffic in which some have to be rejected. In the low traffic scenario, we can fairly compare resource usage using the different algorithms *Break-Free*, *Breaking-Bad*, and *No-Reconf*, as they are accepting the same demands. In the high traffic scenarios, we can compare them in terms of acceptance rate of demands.

We show in particular that *Break-Free* allows to lower the network cost and increase the acceptance rate almost as much as *Breaking-Bad*. For both algorithms, a large number of demands have to be rerouted, showing that it is crucial to implement a mechanism to avoid an impact on them. Network reconfiguration has to be done often to attain a significant gain, however, this reconfiguration can be quickly computed. This makes reconfiguration feasible to be put into practice.

## 5.1 Data sets

We conduct experiments on two real-world topologies from SNDlib [24] of different sizes: `pdh` (11 nodes, 34 links), and `tal` (24 nodes, 55 links). We generate our problem instances as follows. We considered 250 demands for each network. The source and destination of each demand are chosen uniformly at random among the nodes. Following [25], the lifetime of a demand is exponentially distributed with mean  $\mu = 25$ . We then round this lifetime to an integral number of time steps. The volume of the demands is chosen randomly and is on average 2 times higher in the high-traffic scenario than in the low-traffic one. Also, each demand is associated with an ordered sequence of 2 to 3 functions uniformly chosen at random from a set of 5 different functions. Experiments have been conducted on an Intel Xeon E5520 with 24GB of RAM.

## 5.2 Low-traffic scenario - Resource usage

In Figure 5, we show the network cost for our *low-traffic scenario*. The results are given for `No-Reconf` and `Breaking-Bad` as a measure of comparison, and for several variants of `Break-Free` with different numbers of reconfiguration steps from 1 to 4.

We first see that `Break-Free` has similar performances to `Breaking-Bad`, which interrupts the requests when moving them to an optimal state in terms of network operational cost. This means that our solution is as efficient as possible as `Breaking-Bad` provides a lower bound of the best our algorithm can achieve. Moreover, `Break-Free` achieves this performance for any number of time steps (even 1). This leads to a very fast algorithm as discussed below. This is due to the fact that when the network is not congested, there is enough capacity to host both the old and new routes.

Reconfiguration leads to a better resource utilization and reduces the network operational cost compared to `No-Reconf`, and this given a same volume of traffic (note that no demand is rejected in this scenario). Indeed, reconfiguring the network regularly permits a reduction of 19% of network operational cost while using 22.5% fewer VNFs and 18.5% less link bandwidth compared to the no-reconfiguration case. Results for bandwidth and VNF usages are given in Fig. 3, Fig. 4. Recall that the network cost is the result of the addition of the bandwidth and VNF costs.

## 5.3 High-Traffic scenario - Acceptance Rate

In our *high-traffic scenario*, the network is congested as there are not enough resources to satisfy all the demands. As a consequence, some requests cannot be accepted. We show, in Figure 6, the profit achieved by `Break-Free`, `Breaking-Bad`, and `No-Reconf`. We define the profit associated with an accepted demand as the asked volume of bandwidth multiplied by its duration.

The global profit is defined as the sum of all the accepted requests' profits. We show the profit as a percentage in terms of maximum achievable profit. It can be seen that `No-Reconf` and `Break-Free` (with 1-step) lead to equivalent profit, around 70% for `pdh` (and between 78 and 81% for `tal`), while `Break-Free` (with 2, 3, and 4 steps) and `Breaking-Bad` have similar performances (around 80% for `pdh` and 90% for `tal`). For this congested scenario, one step of reconfiguration is not enough as there is not enough place to move the requests. Therefore, some requests are rejected. Allowing to use more steps in our *make-before-break* reconfiguration process, without interrupting the requests, we can reach the same performances as `Breaking-Bad`.

In Figure 7, we show the network operational cost for `Break-Free`, `Breaking-Bad`, and `No-Reconf` as a function of the number of demands arrived. The first observation is that `Break-Free` (with 2, 3, 4 steps) leads to a smaller network operational cost than `No-Reconf`. It accepts more, with less cost. The second observation is that even if `Break-Free` (with 1-step) has a similar profit to `No-Reconf`, it has substantially less network operational cost than all the other algorithms.

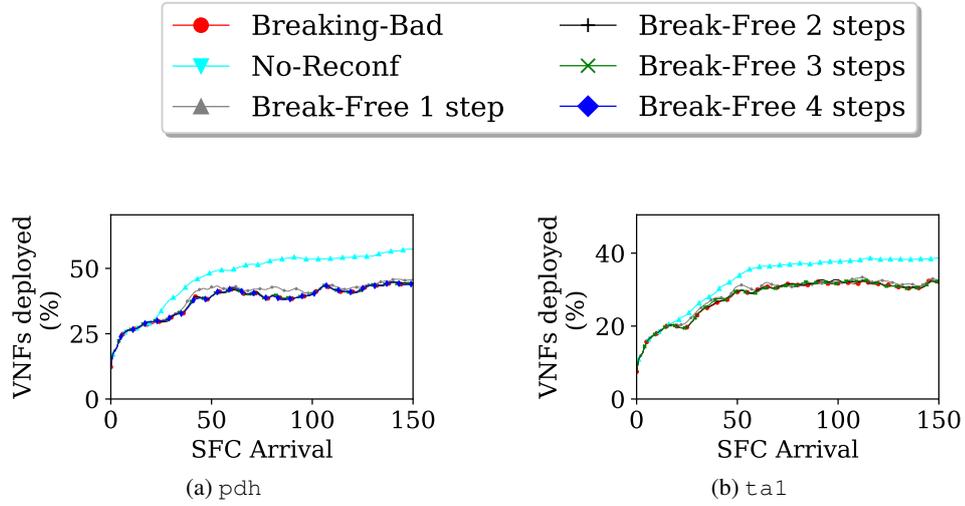


Figure 3: Low-Traffic scenario - Number of VNFs deployed across time.

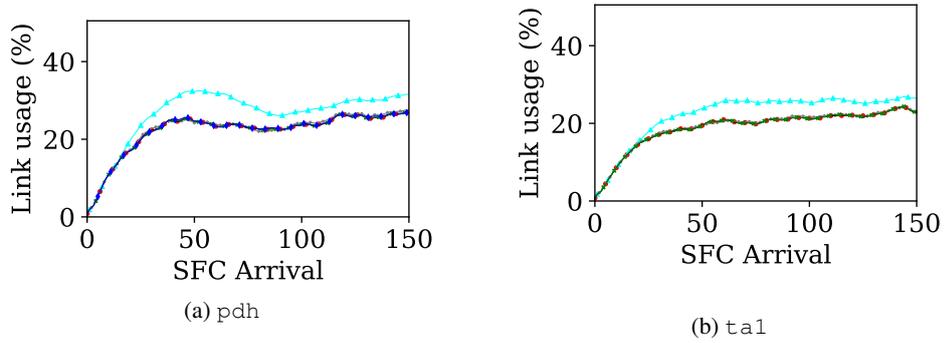


Figure 4: Low-Traffic scenario - Bandwidth usage across time.

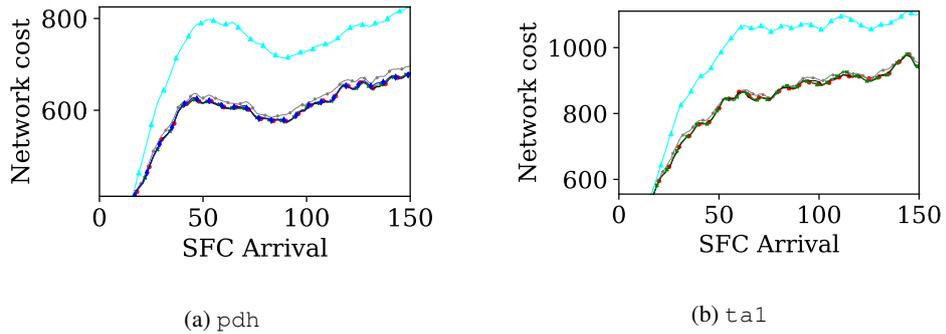


Figure 5: Low-Traffic scenario - Network cost.

## 5.4 Impact of Parameter $\beta$

In Figures 8 and 9, we study the impact of the  $\beta$  parameter on the resources required in the network in terms of bandwidth and number of deployed VNFs, respectively. We focus on the low-traffic scenario as

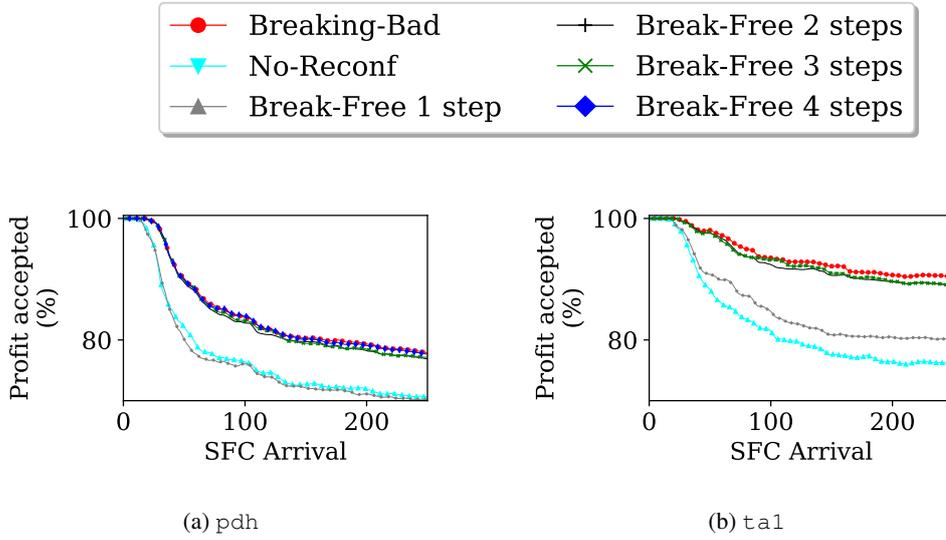


Figure 6: High-Traffic scenario - Percentage of accepted profit across time.

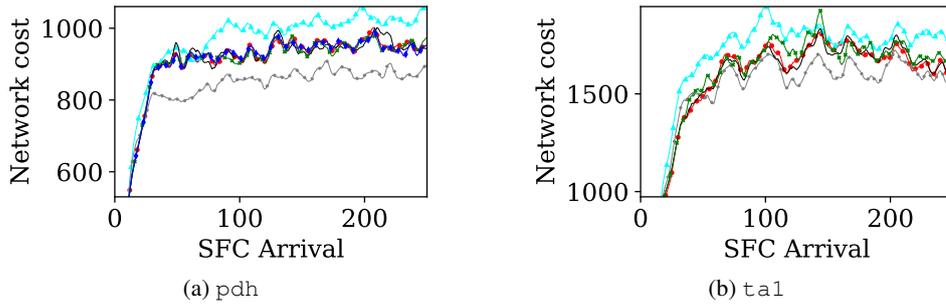


Figure 7: High-Traffic scenario - Cost gain across time.

the compared algorithms accept the same requests and therefore, we can compare the utilisation of the network resources in terms of link bandwidth and number of VNFs deployed for the same global volume of traffic.

As  $\beta$  increases, the impact of the VNF cost on the total cost is greater. As a consequence, the number of deployed VNFs decreases, leading to longer routes and thus, to an increased amount of bandwidth necessary in the network to route the demands in order to satisfy their chaining constraints.

Note also that, for all values of  $\beta$ , reconfiguration using `Break-Free` (for any number of steps) leads to similar gains to reconfiguration using `Breaking-Bad`. This shows that the conclusion discussed in Section 5.2 for a specific value of  $\beta = 25$  (our default value) is valid in more general settings for a wide range of  $\beta$ .

Another important observation is that the gain of reconfiguration is higher for larger values of  $\beta$ . The reason is that, when  $\beta$  is large, the requests tend to use longer routes as the cost of bandwidth is less important compared to the one of VNFs. This leads to requests routed in a very suboptimal way when other requests using the same VNFs leave (as shown in the example of Figure 1). On the contrary, when  $\beta$  is small, the routes try to always use close to shortest path solutions, leading to lower gains. There is still a gain as a shortest path is not always available (due to nodes and link capacities).

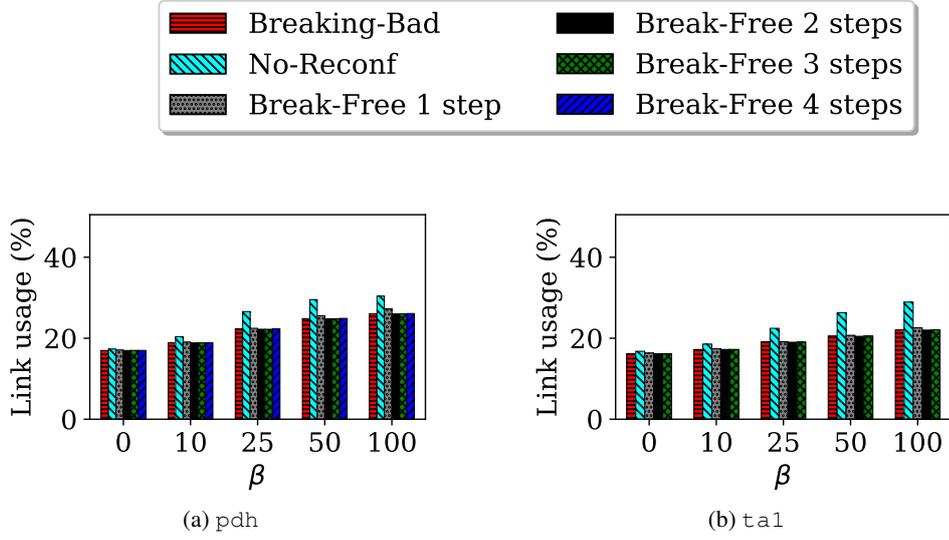


Figure 8: Low-Traffic scenario - Impact of parameter  $\beta$  - Bandwidth usage as a function of  $\beta$ .

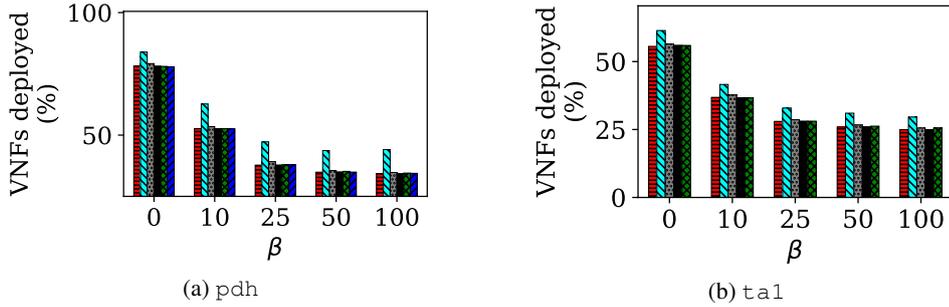


Figure 9: Low-Traffic scenario - Impact of parameter  $\beta$  - VNFs deployed as a function of  $\beta$ .

## 5.5 Time limits for the reconfiguration

Figure 10 shows the gains of network cost (compared to No-Reconf) in percentage for Break-Free (1 to 4 steps) and Breaking-Bad when limiting the time spent for the reconfiguration. Break-Free with 1 step needs only 1 second to reach its best solution. This variant of the algorithm is almost as fast as Breaking-Bad (which does not compute an intermediate make-before-break step). 10 seconds are needed to reach a close to optimal solution for the 2-step variant, and a good solution for the 3-step variant. The best solution is attained after 1 minute. We remind the reader that in the low-traffic scenario, the 1-step variant is enough to achieve solutions close to optimal, while in the high-traffic scenario, this is the case of the 2 step variant. It is thus possible to reconfigure a network with significant gain in a few seconds.

## 5.6 Reconfiguration Rate

In this experiment, we test different reconfiguration rates. Note that during the previous simulations, we reconfigured the network considering the three conditions defined in the beginning of Section 4. Here, the only condition to reconfigure is the first one, i.e., periodically, after a given number of time steps, defined as the reconfiguration rate.

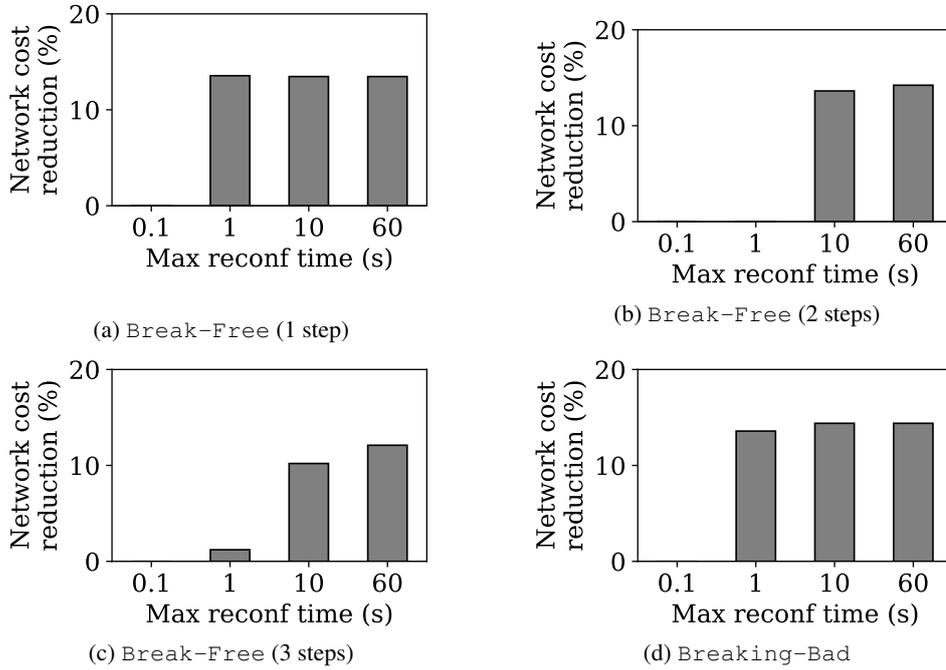


Figure 10: Low-Traffic scenario - Gains of network operational costs for different time limits for the optimization process.

The faster rate is to reconfigure every time step, while the slowest one in our setting would be to reconfigure every 100 time steps (only 1 or 2 reconfigurations are performed during the whole test). We thus present the results for reconfiguration rates of every 1, 5, 10, 15, 50, and 100 time steps. In Figure 11, we provide the network cost in the low-traffic scenario. The minimum cost is as expected achieved when reconfiguring at each time step. However, in this setting similar gain can be obtained when reconfiguring every 10 and 15 time steps for  $pdh$  and  $tal$ .

Results for the high-traffic scenarios can be seen in Figure 12, in which we report the profit generated by the accepted demands. In this setting, the network is congested. This means that very frequently the demand arriving at a time step cannot be routed directly. For  $pdh$ , not reconfiguring at every time step leads to poor performance, whatever the value of the reconfiguration rate. For  $tal$ , this effect is not as stringent. Different reconfiguration rates lead to different values of profit. However, only a reconfiguration every time step leads to an optimal performance.

Thus, the reconfiguration should be well chosen by network operators, depending on their network usage. The higher the congestion, the higher the rate should be.

## 5.7 Percentage of rerouted requests

To see the importance of implementing a make-before-break process, we study the percentage of rerouted requests during the reconfiguration process. We report in Figure 13 (left) the percentage of reconfigured SFCs for *Break-Free* (1 to 4 steps) and *Breaking-Bad* for the high-traffic scenario. Firstly, *Breaking-Bad* has to interrupt, on average, 78% of the requests (between 45% and 100%) to maintain an optimal solution. This is thus of *crucial importance to avoid impacting this large number of requests when reconfiguring*.

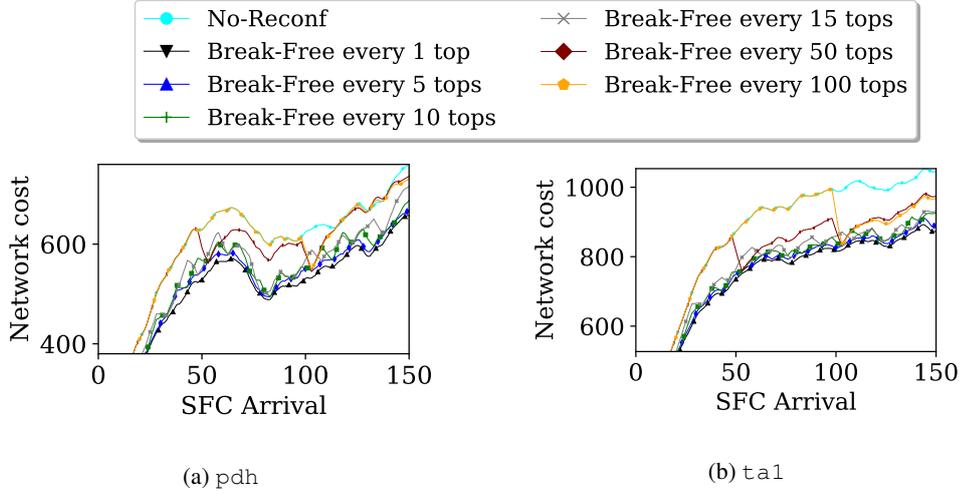


Figure 11: Low-Traffic scenario - impact of the reconfiguration rate on the network cost.

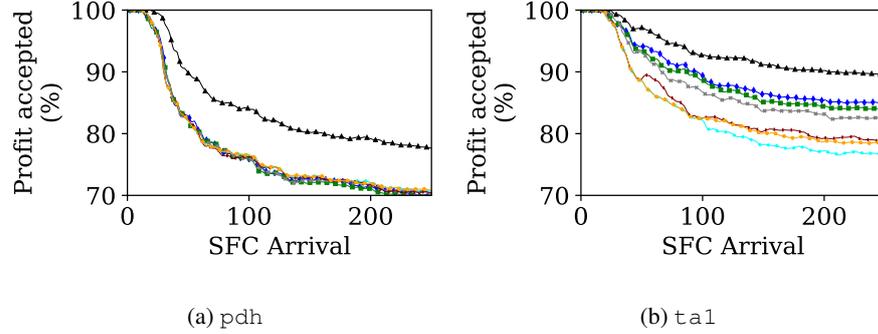


Figure 12: High-Traffic scenario - impact of the reconfiguration rate on the percentage of profit accepted.

*Break-Free* changes the routing of approximately the same number of requests but without any interruption of traffic. For the 1-step case, the reconfiguration is not always possible as the network is almost saturated. Therefore, when reconfiguration is achieved, it impacts slightly less requests: 65% on average for *pdh* and 70% for *ta1*.

Note that the number of reconfigured requests depends on the frequency of the reconfiguration, as shown in Figure 13 (right).

## 6 Conclusion

In this work, we provide a solution, *Break-Free*, to reconfigure a set of requests which have to go through service function chains. The requests are routed greedily when they arrive, leading to a sub-optimal use of network resources, bandwidth, and virtual network functions. *Break-Free* reroutes the requests to an optimal or close to optimal solution while providing a make-before-break mechanism to avoid impacting the rerouted requests.

Our algorithm is fast and provides a close to optimal reconfiguration in a few seconds. However, as a future work, we plan to propose algorithms to handle larger instances.

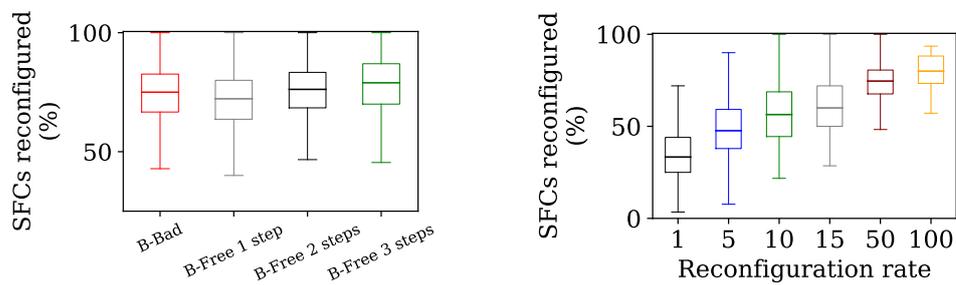


Figure 13: Percentage of rerouted requests for  $\tau_{a1}$ , considering (left) different intermediate reconfiguration steps and (right) different reconfiguration rates.

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