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Cooperative Localization of Drones by using Interval Methods

Ide-Flore Kenmogne*, Vincent Drevelle* and Eric Marchand*

Abstract

In this article we address the problem of cooperative pose estimation in a group of unmanned aerial vehicles (UAVs) in a bounded-error context. The UAVs are equipped with cameras to track landmarks, and with a communication and ranging system to cooperate with their neighbors. Measurements are represented by intervals, and constraints are expressed on the robots poses (positions and orientations). Pose domains subpavings are obtained by using set inversion via interval analysis. Each robot of the group first computes a pose domain using only its sensors measurements. Then, through position boxes exchanges, the positions are cooperatively refined by constraint propagation in the group. Results with real robot data are presented, and show that the position accuracy is improved thanks to cooperation.

Keywords: cooperative localization, intervals, vision, constraint propagation

1 Introduction

Unmanned aerial vehicles (UAVs) have significantly attracted the attention and interest in several applications areas involving multi-robot tasks, such as search and coverage missions [18, 4], exploration [10], cooperative manipulation [20, 11], control [15, 25], etc. In each of these cases, one problem to be solved is the cooperative localization (CL) in a group of robots [23]. CL consists in improving the positioning capacity of each robot through information exchanges (e.g. sensors measurements) with other robots in the group.

Several methods exist for solving CL, such as the Extended Kalman Filter (EKF) for a centralized system [12, 22, 8] or, if the computation is decentralized and the communication is unreliable, other techniques like Covariance Intersection [27] or Interleaved Update [1]. Approaches that assume bounded errors using polytopes and linear programming algorithms have also been proposed in [26, 5].

In a bounded-error measurements context, interval set-membership methods [21] allow rigorous errors bounds propagation in non-linear estimation problems.

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Many applications of these methods are found in practical areas like mobile robots localization [7] or positioning integrity for autonomous cars [9], and as part of the cooperative localization of underwater robots with sonar [3] and vehicle networks with GNSS [17]. Interval methods also enable to derive efficient particle filter implementations for highly non-linear localization problems [19]. In [16], the authors have shown that interval methods are an effective tool for vision-based bounded-error positioning of a drone.

In this paper, we propose to use interval set-membership methods as a tool to solve the problem of cooperative localization of a fleet of drones. Each drone in the group is equipped with a camera able to track georeferenced landmarks, and a communication and ranging system providing each robot a way to exchange data and measure distances with its neighbors. Communication and ranging are also available with a base station of known position. The aim is to calculate a pose domain for each robot from constraint propagation and set inversion techniques. The proposed method computes, for each drone, a set that contains all its feasible poses. The solution sets take into account image measurements, distance measurements and the georeferenced landmarks positions; all being uncertain with bounded errors. The computed pose domain of each robot is guaranteed to contain the solution as long as the measurements error bounds are not violated. The paper is structured as follows: Section 2 presents the problem statement, then the proposed estimation method is presented in Section 3. Finally, experimental results are reported in Section 4.

2 Problem statement

Let us consider the global reference frame \mathcal{F}_w , in which evolves a fleet of n drones R_k ($k \in \{1 \dots n\}$). A reference frame \mathcal{F}_{r_k} (also known as *body frame*) is attached to the center of gravity of each robot. The pose of a drone R_k is given by $\mathbf{r}_k = (x_k, y_k, z_k, \phi_k, \theta_k, \psi_k)$ in the global reference frame.

In the sequel, we consider that the drones are identical in their architecture. They are equipped with calibrated onboard cameras (the intrinsic parameters are known), and the rigid transformation between the camera frame and the robot body frame is known by calibration and represented by the homogeneous rotation and translation matrix ${}^c\mathbf{T}_r$. We also suppose, as in [25], that each robot flies in *near-hovering* regime, thus allowing the precise measurement of roll and pitch angles. The neighborhood of a robot R_k , i.e. the set of robots it can communicate with, is denoted by $\mathcal{N}(R_k)$.

2.1 Scenario description

The navigation environment consists of a base station B (see Figure 1) able to communicate with the drones, and m georeferenced landmarks (for which the positions are known). In order to accomplish its navigation task, each robot of the group must be located relative to \mathcal{F}_w . Each drone R_k is equipped with the following

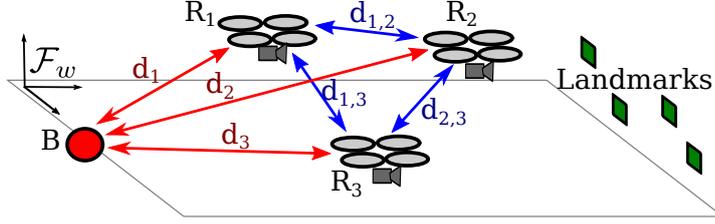


Figure 1: Cooperative localization with camera and range measurements

embedded sensors: camera, altimeter and inertial measurement unit (IMU) with a compass. This enables the following measurements:

- the altitude z_k ;
- the roll ϕ_k and pitch θ_k angles, with good precision;
- the yaw angle ψ_k (with rough precision due to magnetic disturbances);
- and the 2-D points $\bar{\mathbf{x}}_1^k, \dots, \bar{\mathbf{x}}_m^k$ in the image I_k , corresponding to the observable 3-D landmarks ${}^w\mathbf{X}_1^k, \dots, {}^w\mathbf{X}_m^k$ in the environment.

In addition to these on-board sensor measurements, each robot R_k is able to:

- measure its distance $d_{k,j}$ to a neighboring robot R_j ($R_j \in \mathcal{N}(R_k)$),
- measure its distance d_k to the base station B ($\mathbf{b} = (x_B, y_B, z_B)^\top$ in \mathcal{F}_w)
- communicate and exchange information with each robot in its neighborhood.

This can be done by using for instance an IEEE 802.15.4.a Ultrawide Band (UWB) communication system [24] which allows time-of-flight ranging.

Under the assumption of bounded-error measurements, we want to compute the domains of all the feasible 6-DOF poses for each drone in the global reference frame \mathcal{F}_w . The components of the pose are those of the position vector $\mathbf{p}_k = (x_k, y_k, z_k)$ and the attitude (roll, pitch and yaw) $\mathbf{q}_k = (\phi_k, \theta_k, \psi_k)$. Given that three of the six degrees of freedoms are measured with low uncertainty (z_k, ϕ_k, θ_k) , our attention will be focused on estimating the horizontal position (x_k, y_k) and the yaw angle ψ_k of each robot. The knowledge on the altitude, the roll and the pitch measured for each robot will be integrated into the problem in the form of constraints. The set of observation equations allows us to define, for each robot, a set of constraints described in the following section.

2.2 Set of constraints related to the measurements

To solve the problem described in the previous scenario, let us express it as a constraint satisfaction problem (CSP). We will then be able to use the SIVIA [13] branch-and-bound algorithm with contractors (see Section 2.3) to characterize the

domain of feasible poses for each robot. For this, each measurement is related to the state of the robot by a constraint in the CSP describing the problem.

2.2.1 2D image measurements constraints

The pinhole camera model describes the projection of a 3D point in the image plane. In homogeneous coordinates, a world point ${}^w\mathbf{X}_i = (X, Y, Z, 1)^\top$ is projected in the image at the pixel coordinates $\bar{\mathbf{x}}_i^k = (u, v, 1)^\top$ given by:

$$\bar{\mathbf{x}}_i^k = \mathbf{K} \mathbf{\Pi} {}^c\mathbf{T}_w(\mathbf{r}_k) {}^w\mathbf{X}_i, \quad (1)$$

where \mathbf{K} is the camera intrinsic parameters matrix (principal point coordinates u_0, v_0 and focal length to pixel size ratios p_x and p_y) and $\mathbf{\Pi}$ is the perspective projection matrix:

$$\mathbf{K} = \begin{pmatrix} p_x & 0 & u_0 \\ 0 & p_y & v_0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \mathbf{\Pi} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, \quad (2)$$

and ${}^c\mathbf{T}_w(\mathbf{r}_k)$ is the world to camera rigid transformation matrix, which depends on the robot pose \mathbf{r}_k and the known robot to camera transformation ${}^c\mathbf{T}_r$.

Let us denote by $({}^cX^k, {}^cY^k, {}^cZ^k, 1)^\top = {}^c\mathbf{T}_w(\mathbf{r}_k) {}^w\mathbf{X}_i$ the coordinates of a landmark in the coordinate frame attached to the camera of the robot R_k . We can now define the set of constraints related to measurements in the image:

- The perspective projection constraint of a point in the image C_{proj}^k :

$$C_{proj,i}^k : \left\{ \begin{array}{l} u = p_x x_i^k + u_0, \\ v = p_y y_i^k + v_0 \end{array} \right\}, \quad \text{with } x_i^k = \frac{{}^cX^k}{{}^cZ^k} \text{ and } y_i^k = \frac{{}^cY^k}{{}^cZ^k}. \quad (3)$$

- The front looking camera constraint C_{front}^k , ensuring that the landmark is in the front half-space of the camera:

$$C_{front,i}^k : \{ {}^cZ_i^k > 0 \}. \quad (4)$$

The pose of each drone R_k will have to verify the constraints $C_{proj,i}^k$ and $C_{front,i}^k$ for all i corresponding to the observed landmarks.

2.2.2 Base station distance constraint

Considering a measurement d_k of the distance to the base station B , the constraint C_{base}^k expresses the fact that the Euclidean distance between the robot R_k and B is equal to the measured distance. Recalling that the position part of the robot pose is $\mathbf{p}_k = (x_k, y_k, z_k)^\top$, we have :

$$C_{base}^k : \{ d_k = \|\mathbf{p}_k - \mathbf{b}\|_2 \}. \quad (5)$$

This constraint is used to reduce the robot's position domain. Indeed, as the position of the base station \mathbf{b} is known, the knowledge of d_k constrains the position \mathbf{r}_k of the drone to be located on a sphere $S^2(\mathbf{b}, d_k)$ as shown in Figure 2.

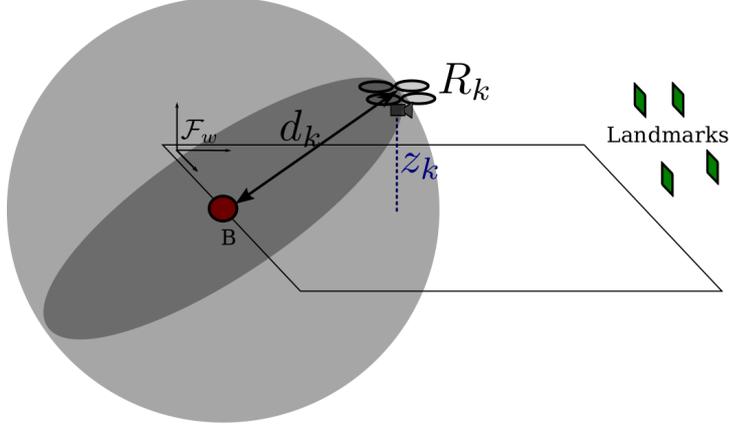


Figure 2: Distance constraint to the base station

2.2.3 Inter-distance measurements constraints

Assuming that the ranging system antenna coincides with the center of mass of the drone, distance measurements are independent of the robot attitude. The constraint related to inter-distance measurements between a drone R_k and its neighbor R_j with $R_j \in \mathcal{N}(R_k)$ is defined by:

$$d_{k,j} = \|\mathbf{p}_k - \mathbf{p}_j\|_2 \quad \text{with } (k, j) \text{ in } \{1 \dots n\}^2 \text{ and } k \neq j, \quad (6)$$

$$C_{r_k, r_j} : \{d_{k,j} = \|\mathbf{p}_k - \mathbf{p}_j\|_2\}. \quad (7)$$

The additional knowledge of $d_{k,j}$ by the robot R_k restricts the possible configurations. For a given candidate position of neighbor R_j , the eligible positions of R_k are limited to a circle (intersection of the two spheres $S^2(\mathbf{b}, d_k)$ and $S^2(\mathbf{p}_k, d_{k,j})$).

Measurements of distances d_k and $d_{k,j}$ provide constraints on the robot positions, but there are still 3 degrees of freedom (on 6DoF) corresponding to all rotations of the formation around the base station.

2.2.4 Altitude measurement constraint

Let us consider the altitude z_k^{meas} of each robot measured by the altimeter, we have the constraint $z_k = z_k^{\text{meas}}$ which places R_k on a plane.

It allows to constrain the sphere $S^2(\mathbf{b}, d_k)$ formed by the distance to the base station B and the robot R_k on a horizontal circle resulting from the intersection of $S^2(\mathbf{b}, d_k)$ and the plane.

It also allows to constrain the sphere $S^2(\mathbf{p}_k, d_{k,j})$ solution of the measurement of the inter-distances $d_{k,j}$. For a known position of R_j , R_k has only two possible positions corresponding to the intersection of the horizontal position circle of R_k with the sphere $S^2(\mathbf{p}_k, d_{k,j})$.

Using only distance and altitude measurements leads to an ambiguity on the position of the robot, dependent on the orientation and corresponding to the rotations around the vertical axis of the base station B . Adding the constraints from the image measurements will enable to remove the ambiguity.

2.3 Set inversion via interval analysis with contractors

The set inversion via interval analysis (SIVIA) algorithm [13] is a branch-and-bound method, which enables to compute an outer approximation of the solution of a CSP. The algorithm starts from an arbitrarily big box $[\mathbf{x}_0]$ that must contain the solution set. The solution is then enclosed in an outer *subpaving* $\bar{\mathbb{S}}$, i.e. a set of non-overlapping boxes, which covers the solution. A parameter ϵ controls the precision of the obtained solution approximation. SIVIA can be implemented with box reduction operators called *contractors* [6]. A contractor for a CSP takes an input box, and returns a smaller included box without losing any solution. Assuming a *contractor* \mathcal{C} is available for the CSP, using for instance interval constraint propagation techniques [2], a very straightforward implementation of SIVIA is given by the following algorithm (see the book [14] for more detailed algorithms):

Algorithm 1 Outer SIVIA with contractor.

Input: $[\mathbf{x}_0]$: initial box, \mathcal{C} : contractor, ϵ : subpaving box width

Result: $\bar{\mathbb{S}}$: outer solution subpaving

```

1:  $\bar{\mathbb{S}} \leftarrow \emptyset$ 
2:  $\mathcal{L} \leftarrow [\mathbf{x}_0]$  Stack of working boxes initialized with  $[\mathbf{x}_0]$ .
3: while  $\mathcal{L}$  is not empty do
4:    $[\mathbf{x}] \leftarrow \text{pop}(\mathcal{L})$  Get the next working box from the stack.
5:    $[\mathbf{x}] \leftarrow \mathcal{C}([\mathbf{x}])$  Contract the working box.
6:   if  $\text{width}([\mathbf{x}]) > \epsilon$  then If the contracted box is larger than  $\epsilon$ ,
7:      $([\mathbf{x}_1], [\mathbf{x}_2]) \leftarrow \text{bisect}([\mathbf{x}])$  bisect it,
8:     push  $[\mathbf{x}_1]$  into  $\mathcal{L}$ ; push  $[\mathbf{x}_2]$  into  $\mathcal{L}$  and add the subboxes to the stack.
9:   else
10:     $\bar{\mathbb{S}} \leftarrow \bar{\mathbb{S}} \cup [\mathbf{x}]$  Otherwise, add the box to the solution set.
11:   end if
12: end while

```

3 Cooperative localization via position domain exchange

From the set of constraints related to the measurements defined in Section 2.2, it is possible to define a CSP which will allow the effective computation of the robot poses domains by propagating the uncertainties on the measurements. We propose a distributed approach that consists in performing a data fusion based on position domains sharing.

Each robot computes its own pose domain only. In this way, whatever the number n of robots, the number of bisections dimensions in SIVIA remains unchanged (equal to 3).

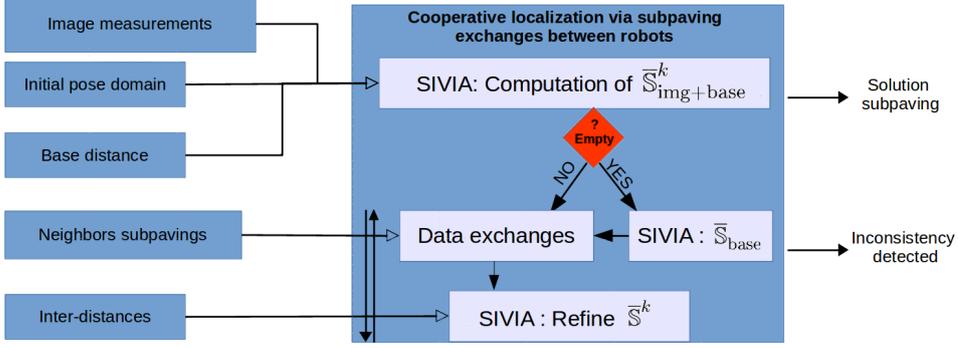


Figure 3: Distributed set-membership pose estimation method.

Position estimation is done in two steps (Figure 3). Firstly, each drone R_k (k in $1 \dots n$) estimates its pose domain by using image measurements and distance to the base station (measurements that depends on robot R_k only). Secondly, each drone exchanges its resulting position domain with all its neighbors and, by using inter-distance measurements, refines its position thanks to the constraints of distances between each robot R_k and its neighbors $R_j, j \in \mathcal{N}(k)$.

To solve the two steps, we define two CSPs for which we characterize a solution set using SIVIA with the HC4 contractor [2].

3.1 CSP related to vision and distance to the base station

At each time step, R_k first computes an outer approximation $\bar{S}_{\text{img+base}}^k$ of the solution set of the CSP $\mathcal{H}_{\text{img+base}}$ defined from the constraints of Section 2.2 and given by:

$$\mathcal{H}_{\text{img+base}} : \left(\begin{array}{c} \mathbf{r}_k \in [\mathbf{r}_k], \\ \bar{\mathbf{x}}_i^k \in [\bar{\mathbf{x}}_i^k], \\ w \mathbf{X}_i^k \in [w \mathbf{X}_i^k], \\ d_k \in [d_k], \\ \{C_{proj,i}^k, C_{front,i}^k, C_{base}^k\}, i \in 1 \dots m \end{array} \right). \quad (8)$$

Adding the distance measurement to the base station makes it possible to refine the position of the robot. We can observe this tightening of the bounds through the result of Figure 4 where a drone observes five landmarks and has a measurement of its distance to the base station. Figure 4a shows the subpaving result for the image measurements only. Figure 4b shows the result with measurement in the image and distance to the base station.

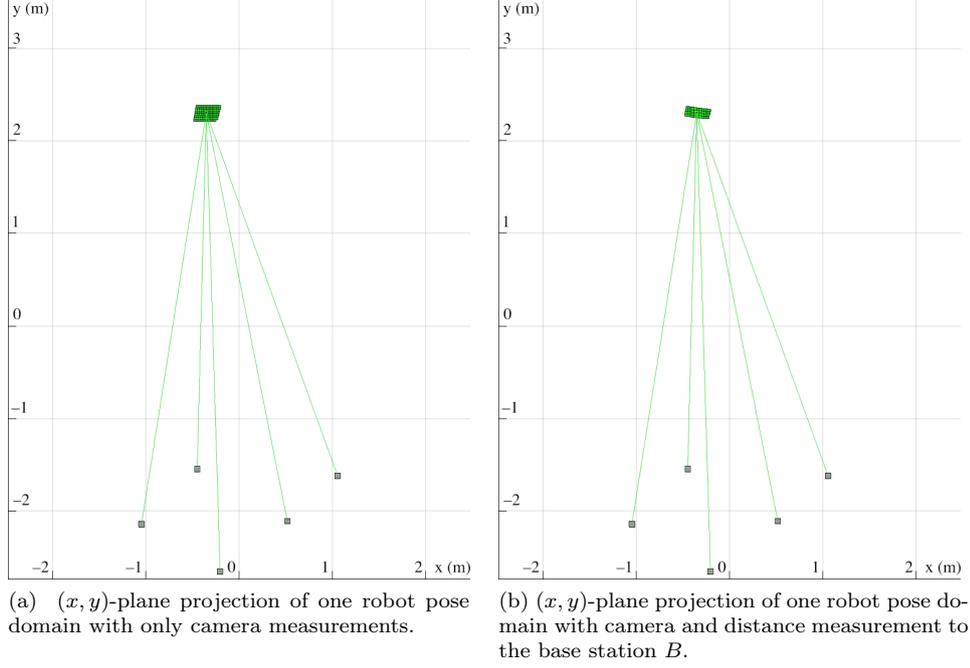


Figure 4: Single drone pose domain computation (horizontal projection).

3.2 CSP related to inter-distance measurements for cooperation

After computing the set $\bar{\mathbb{S}}_{\text{img} + \text{base}}^k$ of poses that are compatible with the distance to the base station and the image, R_k computes the bounding box $[\mathbf{p}_k]$ of its position domain:

$$[\mathbf{p}_k] = \square \text{proj}_{\mathbf{p}}(\bar{\mathbb{S}}_{\text{img} + \text{base}}^k)$$

where \square is the bounding box operator and $\text{proj}_{\mathbf{p}}$ the projection of the pose domain on the position space:

$$\begin{aligned} \text{proj}_{\mathbf{p}} : SE(3) &\rightarrow \mathbb{R}^3 \\ (x, y, z, \phi, \theta, \psi)^\top &\mapsto (x, y, z)^\top. \end{aligned}$$

The domain $[\mathbf{p}_k]$ is then shared to all the neighbors $R_j, j \in \mathcal{N}(k)$ of the robot R_k , and the distances $d_{k,j}$ between R_k and R_j are simultaneously measured.

3.2.1 Pose domain contraction

After receiving information from its neighbors (position boxes $[\mathbf{p}_j]$ and distance measurements $[d_{k,j}]$), each drone R_k tries to refine the current bounds ($\bar{\mathbb{S}}_{\text{img} + \text{base}}^k$)

of its pose domain. It propagates the information on new inter-distance measurements by locally contracting the CSP $\mathcal{H}_{\text{inter}}$ defined as follows:

$$\mathcal{H}_{\text{inter}} : \left(\begin{array}{l} \mathbf{r}_k \in \overline{\mathbb{S}}_{\text{img}+\text{base}}^k \\ \mathbf{p}_k = \text{proj}_{\mathbf{p}}(\mathbf{r}_k), \\ \mathbf{p}_j \in [\mathbf{p}_j], j \in \mathcal{N}(k) \\ d_{k,j} \in [d_{k,j}], j \in \mathcal{N}(k) \\ d_{k,j} = \|\mathbf{p}_k - \mathbf{p}_j\|_2, j \in \mathcal{N}(k) \end{array} \right) \quad (9)$$

where $\mathbf{p}_k = (x_k, y_k, z_k)^\top$ is the position of R_k . The pose domain $\overline{\mathbb{S}}_{\text{img}+\text{base}}^k$ is thus reduced by using interval constraint propagation to contract $\mathcal{H}_{\text{inter}}$ and provide the final solution set $\overline{\mathbb{S}}^k$.

3.2.2 Propagation of the position domain improvement

The constraint network formed by the group of robots can contain cycles covering several robots. The contraction of the local CSPs $\mathcal{H}_{\text{inter}}$ must be propagated again across the network to improve the reduction of the feasible pose domain of each robot.

If, after solving $\mathcal{H}_{\text{inter}}$ the bounding box of the robot's position domain $[\mathbf{p}_k]$ is reduced, R_k therefore re-transmits the update of $[\mathbf{p}_k]$ to its neighborhood. This process is iterated until a fixed point is reached, i.e. when there is no significant improvement on the position domains.

The proposed method has been implemented and tested using real data and results are presented in the following section.

4 Experimental results

The proposed method has been tested for a fleet of $n = 4$ drones, with data acquired on a Parrot AR-Drone2 UAV. The environment contains $m = 5$ landmarks, which are boxes on which are placed AprilTag markers [28]. A Vicon motion capture system has been employed to determine the landmarks coordinates, and to provide the ground truth position and orientation of the drone. Figure 5 illustrates the views of the onboard cameras for each drone at time $t = 8$ s. Error bounds in the image are equal to ± 0.5 px and the distance measurement error is assumed to be less than ± 5 cm.

4.1 Influence of cooperation on the size of the pose domain

The acquired dataset enables to test our method for a different number of drones. Figure 6 shows in green the position subpaving obtained for the drone R_1 at time $t = 6.3$ s in the different cases, from $n = 1$ (R_1 alone, no cooperation) to $n = 4$ (the full fleet cooperates).

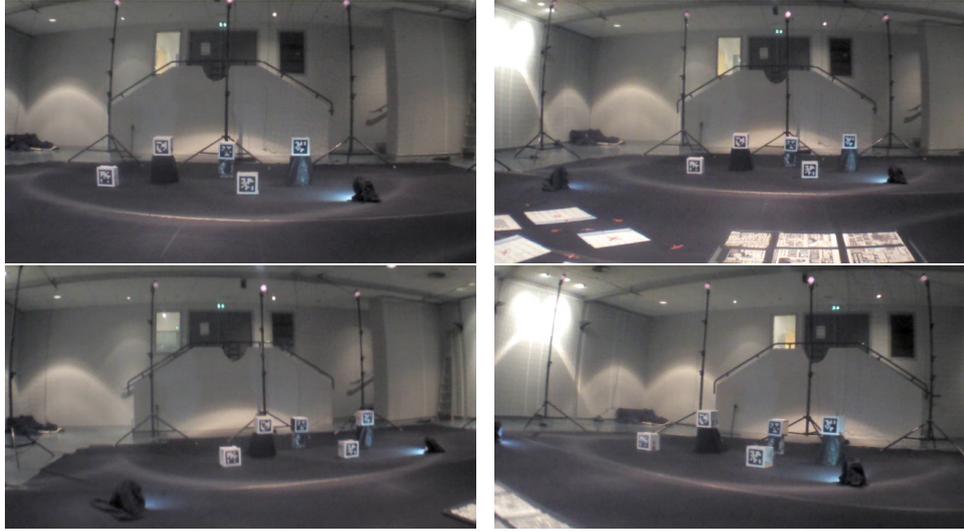


Figure 5: Onboard cameras views at $t = 8$ s. Landmarks are boxes with AprilTag printed pattern.

At the measurement epoch of Figure 6, the tracking of the landmarks in the image has completely failed for R_1 , which leads to the violation of the image measurements error bounds. Therefore, in step 1 of the computation, the solution $\bar{\mathbb{S}}_{\text{img} + \text{base}}^1$ is the empty set.

An inconsistency management test has been integrated to the process so that, if $\bar{\mathbb{S}}_{\text{img} + \text{base}}^k = \emptyset$, a domain $\bar{\mathbb{S}}_{\text{base}}^k$ related to the base station distance only is computed. Hence the domain of R_1 in Figure 6a is $\bar{\mathbb{S}}_{\text{base}}^1$, a thick green arc centered on the position of the base station.

Figure 6b shows the position subpaving of the drones R_1 and R_2 , when $n = 2$. We notice the significant reduction of the position domain of R_1 following the cooperation with R_2 , although R_2 is not very well located (able to observe only two landmarks). More domain reduction occurs in the cases where $n = 3$ and $n = 4$. This can be observed in Figure 6c and Figure 6d.

These different figures show that cooperation allows a better localization of each robot, even in the case of full landmark visibility loss (case of the robot R_1). This can be confirmed by the statistics of domain widths and horizontal position errors of the 4 robots for groups of different sizes, computed over the whole dataset and presented in Table 1. The average width of the position domain of the drone R_1 is 1.29 m when the latter is located without cooperation. Thanks to the cooperation, the width of its domain can be reduced and reach a value of 33 cm (in the case of a group of 4 drones), which is a 74% decrease. The average horizontal position error for R_1 , using the center of the subpaving bounding box as a point estimate, improves from 22.6 cm to less than 5 cm (first column of Table 1b).

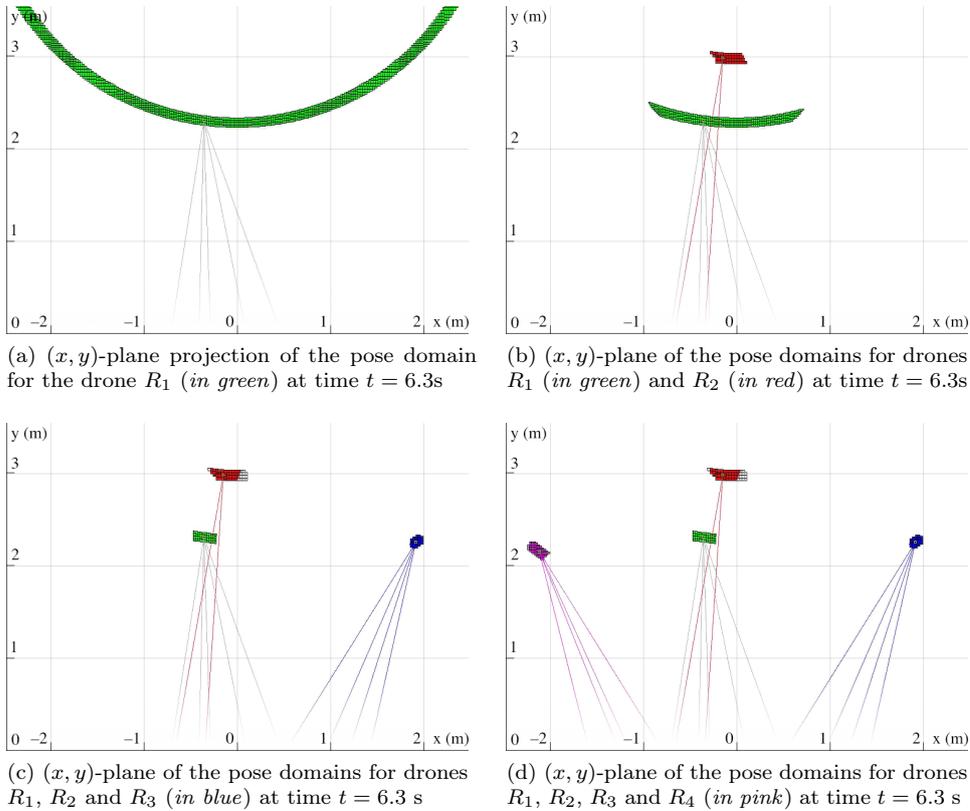


Figure 6: Horizontal projection of the pose domains computed for an increasing number of robots in the group, at time $t = 6.3s$.

With 4 UAVs, the mean horizontal position error of the fleet is about 13 cm.

4.2 Influence of cooperation in case of reduced visibility

At certain timestamps of the experiment, the tracking of landmarks in the image fails, thus leading to violations of the error bounds.

Figure 7 presents the subpaving results of our cooperative approach for each of the four drones. The first sub-figure (top-left) presents the case of complete visibility, where each of the drones is able to track the 5 landmarks. The other three sub-figures correspond to cases of reduced visibility where some of the 4 robots were not able to track any point in the image. Black outlines represent the subpavings obtained before cooperation. In case of inconsistency in the image measurements, they are discarded and only the distance to the base station is used to compute the black subpavings. The colored subpavings represent the results

	R_1	R_2	R_3	R_4
1 UAV	1.29			
2 UAVs	0.86	0.56		
3 UAVs	0.80	0.52	2.98	
4 UAVs	0.33	0.37	0.78	0.61

(a) Mean width of the horizontal position domain bounding box (in meters)

	R_1	R_2	R_3	R_4
1 UAV	0.23			
2 UAVs	0.16	0.09		
3 UAVs	0.14	0.07	1.22	
4 UAVs	0.04	0.05	0.25	0.19

(b) Mean horizontal position error, considering the center of the bounding box (in meters)

Table 1: Horizontal position results statistics, for groups of 1 to 4 drones. The reported figures are mean values over the whole experiment.

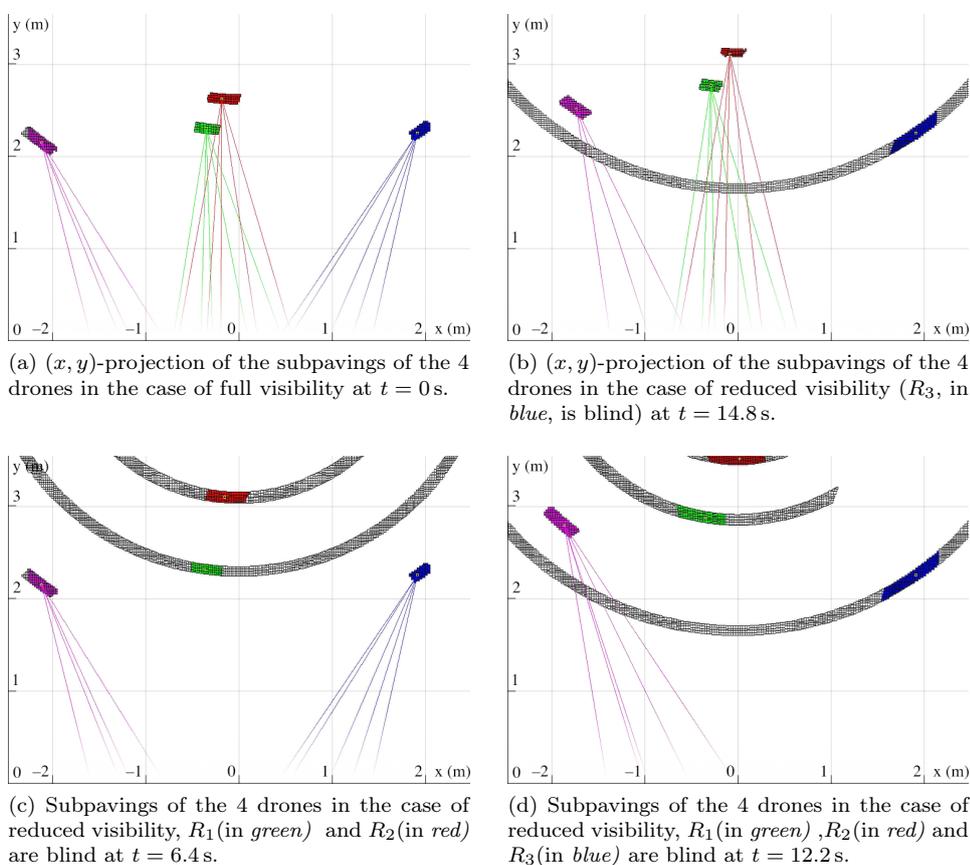


Figure 7: Position domains of the 4 drones. *Black outlines*: subpavings before robot cooperation. *Colored domains*: subpavings obtained after cooperative localization.

obtained for each robot after a fixed point has been reached at the cooperation stage.

These results show that if one of the drones is well located, the cooperation step allows to find an acceptable position domain for all its neighbors.

5 Conclusion

In this article, an interval analysis based approach to solve the problem of cooperative localization for a group of unmanned aerial vehicles has been proposed. The fleet of drones use cameras to track visual landmarks, and a communication and ranging system for cooperation. The approach is distributed and based on position domains exchanges between robots. We have shown that using cooperation and domain exchanges makes the approach extensible with respect to the number of robots in the group without a significant computational cost in the estimation process.

Experimental results with real image data have been presented for a group of 4 robots, with an average computation time for each of the drones equal to 350 ms without having implemented code optimization. Additionally, the results show that cooperation between robots is an asset for group operation when many robots have reduced visibility or are completely blind.

The proposed method can deal with *detectable* erroneous measurements in the images, i.e. outliers leading to an empty-set solution. It then only relies on distances measurements and data exchange with other robots for position determination. This basic fault detection scheme however does not prevent the propagation of *non-detectable* image measurements faults to the whole fleet, nor the mitigation of faulty distance measurements. Future work will aim towards the development of adding more fault-tolerance and robustness to interval-based distributed cooperative localization systems.

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