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► **To cite this version:**

Giles Fearon, Steven Herbette, Jennifer Veitch, Gildas Cambon, Andrew J Lucas, et al.. Enhanced vertical mixing in coastal upwelling systems driven by diurnal-inertial resonance: numerical experiments. *Journal of Geophysical Research. Oceans*, 2020, 125 (9), pp.e2020JC016208. 10.1029/2020JC016208 . hal-02544118v2

HAL Id: hal-02544118

<https://inria.hal.science/hal-02544118v2>

Submitted on 16 Apr 2020

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1 **Enhanced vertical mixing in coastal upwelling systems**
2 **driven by diurnal-inertial resonance: numerical**
3 **experiments**

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16 **Key Points:**

- 17 • Land-sea breeze driven vertical mixing is studied using a 1D model including the
18 land boundary effect
- 19 • The land boundary effect dampens vertical mixing, particularly when bottom fric-
20 tion is non-negligible
- 21 • The diurnal anticyclonic rotary component of the wind stress provides a diagnos-
22 tic for diapycnal mixing

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Abstract

The land-sea breeze is resonant with the inertial response of the ocean at the critical latitude of 30° N/S. 1D-vertical numerical experiments were undertaken to study the key drivers of enhanced diapycnal mixing in coastal upwelling systems driven by diurnal-inertial resonance near the critical latitude. The effect of the land boundary was implicitly included in the model through the ‘Craig approximation’ for first order cross-shore surface elevation gradient response. The model indicates that for shallow water depths ($< \sim 100$ m), bottom shear stresses must be accounted for in the formulation of the ‘Craig approximation’, as they serve to enhance the cross-shore surface elevation gradient response, while reducing shear and mixing at the thermocline. The model was able to predict the observed temperature and current features during an upwelling/mixing event in 60 m water depth in St Helena Bay ($\sim 32.5^\circ$ S, southern Benguela), indicating that the locally forced response to the land-sea breeze is a key driver of diapycnal mixing over the event. Alignment of the sub-inertial Ekman transport with the surface inertial oscillation produces ‘shear spikes’ at the diurnal-inertial frequency, however their impact on mixing is secondary when compared with the diurnal-inertial resonance phenomenon. The amplitude of the diurnal anticlockwise rotary component of the wind stress represents a good diagnostic for the prediction of diapycnal mixing due to diurnal-inertial resonance. The local enhancement of this quantity over St Helena Bay provides strong evidence for the importance of the land-sea breeze in contributing to primary production in this region through nutrient enrichment of the surface layer.

Plain Language Summary

Winds near the coast often have a daily cycle known as the land-sea breeze. Near latitudes of 30° N/S ubiquitous rotating ocean currents also have a daily frequency and therefore become enhanced by daily winds at these latitudes. The ocean currents result in vertical mixing of subsurface and surface water layers, bringing subsurface nutrients to the surface where they stimulate phytoplankton growth. In this study we use a simple model of the ocean (comprised of the vertical dimension only) to study the key drivers of vertical mixing due to the land-sea breeze. We show how vertical mixing is reduced in shallow water ($< \sim 100$ m) near the coast, where currents are slowed down by friction at the seabed. We find that vertical mixing can be predicted by a parameter computed from wind speed and direction over time. This parameter is shown to be enhanced over St Helena Bay on the west

55 coast of South Africa, where phytoplankton blooms are known to be particularly prevalent.
56 The results suggest that the land-sea breeze is likely to be an important contributor to
57 phytoplankton bloom development in this region. Similar processes are likely to be at play
58 in other coastal regions where phytoplankton productivity is enhanced.

59 **1 Introduction**

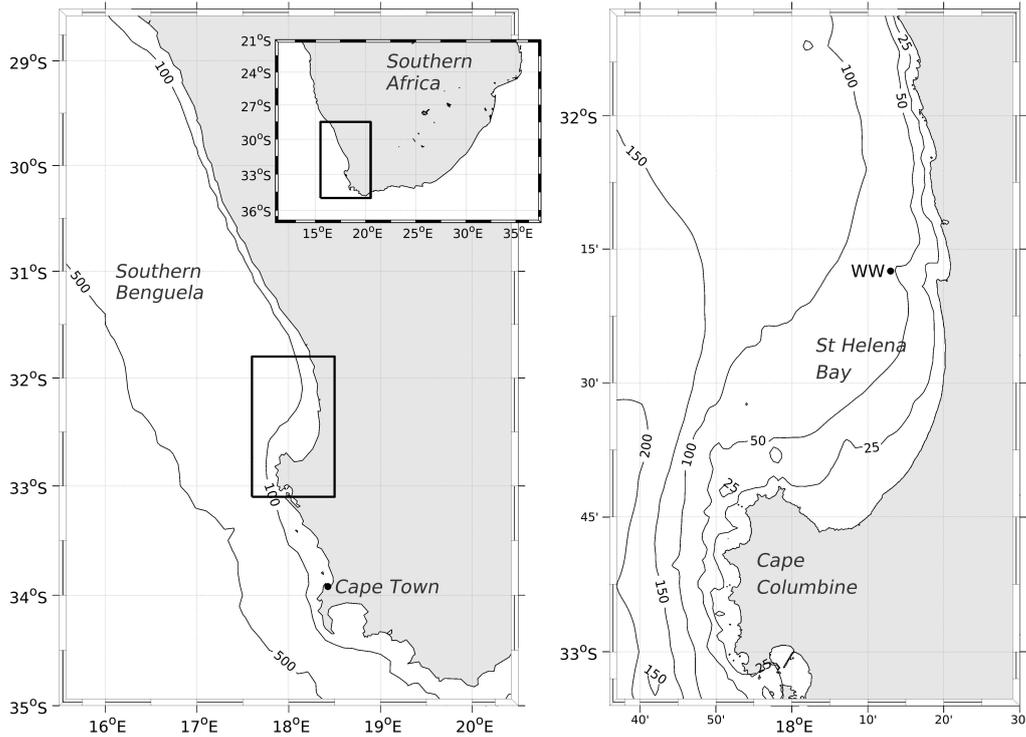
60 The four major Eastern Boundary Upwelling Systems (EBUS) are regions along the
61 eastern land boundaries of the Pacific and Atlantic Oceans where the upwelling of cold
62 nutrient-rich waters to the euphotic zone promotes phytoplankton growth. Although they
63 account for less than 1% of the ocean surface area, EBUS are responsible for about a
64 third of global primary productivity (Pauly & Christensen, 1995). Sustained alongshore
65 equatorward winds (driving Ekman transport) and wind stress curl corresponding to the
66 wind drop-off at the coast (driving Ekman suction) are the primary drivers of upwelling,
67 while retention mechanisms during wind relaxation are important for the accumulation of
68 high biomass coastal blooms (G. Pitcher et al., 2010). A feature common to all EBUS is the
69 land-sea breeze phenomenon, characterised by pronounced diurnal wind variability driven
70 by differential heating over the land and the ocean (Gille, 2003, 2005). As Ekman dynamics
71 responds to wind variability with a time scale in the order of days, diurnal wind variability
72 over EBUS is often assumed to be of low importance for understanding the physical and
73 biogeochemical processes of these systems relative to sub-inertial winds. The land-sea breeze
74 has however been identified as a mechanism for contributing to nutrient enrichment of the
75 surface layer through diapycnal mixing (Aguilar-González et al., 2011; Lucas et al., 2014).
76 This paper further explores the contribution of the land-sea breeze to driving vertical mixing
77 and consequent diapycnal nutrient flux in coastal upwelling systems.

78 The response of the ocean to a surface wind stress takes the form of both rotary and non-
79 rotary components (Ekman, 1905), with Ekman dynamics corresponding to the non-rotary
80 component. The rotary component refers to inertial oscillations, which can be described as
81 anticyclonic circular motions with a frequency equal to the Coriolis parameter $f = 2\Omega \sin \phi$,
82 where Ω is the angular rotation of the earth, and ϕ is the latitude. In the case of a uniform
83 wind stress, a forcing duration of half the inertial period (less than one day at all latitudes
84 by definition) is optimal for imparting energy into the inertial response (R. Pollard, 1970).
85 The most efficient way of imparting energy into surface mixed layer inertial currents is in
86 the form of an anticyclonically rotating wind stress with a frequency ω equal to the inertial

87 frequency f , as in this case the wind stress and surface current vectors are always aligned
88 (R. Pollard & Millard, 1970; D’Asaro, 1985; Alford, 2001). Near latitudes of 30° N/S
89 the inertial frequency is diurnal, leading to resonance between the land-sea breeze and the
90 inertial response; a phenomenon known as diurnal-inertial resonance (Craig, 1989; Simpson
91 et al., 2002). This implies that even low amplitude diurnal wind variability can give rise to
92 significant amplitude inertial oscillations at these latitudes.

93 In proximity to a land boundary, a two layer vertical current structure is commonly ob-
94 served, with a 180° phase shift between surface and subsurface layers (e.g. Millot & Crépon,
95 1981; Shearman, 2005; Simpson et al., 2002; Lucas et al., 2014). This phenomenon has
96 been explained using an analytical model for the first order coast-normal surface elevation
97 gradient response (termed the ‘Craig approximation’) imposed by the barotropic no-flow
98 condition perpendicular to the land boundary (Craig, 1989; Simpson et al., 2002). It should
99 however be highlighted that the two layer current structure produced in this way is not a
100 true first baroclinic mode, but rather the superposition of the forced surface mixed layer
101 response and the opposing barotropic pressure gradient, with a net effect of zero depth-
102 averaged coast-normal transport. The two layer current structure can even be produced in
103 a vertically homogeneous water column (Pettigrew, 1980; S. Chen et al., 2017). The pres-
104 ence of a land boundary does however introduce horizontal convergence and divergence of
105 the forced surface mixed layer response, leading to inertial pumping of the pycnocline and
106 the generation of propagating near-inertial internal waves (e.g. Alford et al., 2016; Kelly,
107 2019). The first baroclinic mode internal wave response can be difficult to separate from
108 the forced response due to their similar vertical current structures and frequencies.

109 An important consequence of the vertical structure of inertial currents is the enhance-
110 ment of shear at the pycnocline, leading to turbulence and diapycnal mixing. Observations
111 of wind-driven inertial oscillations in shallow stratified shelf seas have been shown to pro-
112 duce bursts of enhanced shear at the inertial frequency, termed ‘shear spikes’, which promote
113 vertical mixing and deepening of the thermocline (Burchard & Rippeth, 2009; Lincoln et
114 al., 2016). The analytical shear production theory of Burchard and Rippeth (2009) has been
115 shown to provide a good explanation for these observations. Such ‘shear spikes’ have been
116 further shown to contribute significantly to surface nutrient availability and consequently
117 primary productivity in shelf seas (Williams et al., 2013). The theory of Burchard and
118 Rippeth (2009) is however yet to be applied in the context of diurnal-inertial resonance.



131 **Figure 1.** Locality map for St Helena Bay and the Lucas et al. (2014) offshore mooring (labelled
 132 ‘WW’). Bathymetric contours were derived from digital navigational charts for the region provided
 133 by the Hydrographer of the SA Navy.

119 Perhaps the clearest demonstration of inertial oscillation-driven mixing and consequent
 120 enhancement of primary productivity in upwelling systems are the nearshore measurements
 121 of Lucas et al. (2014) in St Helena Bay, located in the Southern Benguela Upwelling System.
 122 Data from the mooring in ~ 60 m water depth (Figure 1) are revisited in this study. Analysis
 123 of land-based wind measurements indicate strong diurnal wind variability, and at a latitude
 124 of $\sim 32.5^\circ$ S (inertial period of ~ 22 hr), diurnal-inertial resonance leads to the ubiquitous
 125 presence of energetic inertial oscillations (surface amplitude > 0.5 m/s) within the bay
 126 (Fawcett et al., 2008; Lucas et al., 2014). St Helena Bay is also one of the most productive
 127 regions of the Benguela Upwelling System, as evidenced by a clear peak in coastal chlorophyll
 128 derived from satellite data (Demarcq et al., 2007). It is therefore an ideal location for
 129 studying inertial oscillation-driven diapycnal mixing and implications for phytoplankton
 130 phenomenology in coastal upwelling systems.

134 As inertial oscillations have been observed to be tightly coupled to the local wind forc-
 135 ing, salient features of the observations have been reasonably reproduced by linearly damped

136 slab models of the surface layer (e.g. R. Pollard & Millard, 1970; R. T. Pollard, 1980; Alford,
137 2001; Jarosz et al., 2007). Such models however do not account for the deepening of the sur-
138 face layer due to diapycnal mixing and explicitly ignore subsurface effects. One-dimensional
139 (1D) models have been used to simulate inertial oscillation-driven vertical mixing in response
140 to local wind forcing, but are limited by the exclusion of propagating near-inertial internal
141 waves which can be an important source of turbulence and mixing (Xing et al., 2004; Zhang
142 et al., 2010). Hyder et al. (2011) showed that a 1D model forced with the ‘Craig approxima-
143 tion’ is able to qualitatively reproduce the 180° phase shift between surface and subsurface
144 layers off the Namibian coastline in 175 m water depth.

145 In this paper we carry out 1D-vertical numerical experiments with the aim of elucidating
146 diapycnal mixing dynamics of a coastal system characterised by two layers separated by
147 strong stratification and forced by a land-sea breeze near the critical latitude of 30° N/S.
148 Vertical mixing is parameterised in the model using the k - ε turbulent closure scheme (Umlauf
149 & Burchard, 2003, 2005). The use of a 1D model precludes the internal wave response,
150 allowing us to isolate the impact of the forced response. The no-flow condition perpendicular
151 to the land boundary is included in the model through the ‘Craig approximation’, although
152 the formulation presented in Simpson et al. (2002) has been extended here to include bottom
153 friction terms. The bulk shear production theory of Burchard and Rippeth (2009) has been
154 compared with both the model and observations, providing a useful lens through which to
155 interpret the event-scale mixing dynamics. Diapycnal mixing has been further diagnosed
156 through the initialisation of the model with a passive tracer below the surface layer, used
157 to represent a reservoir of subsurface nutrients. The model is used to undertake a series of
158 experiments to explore the physical processes and key drivers of enhanced vertical mixing in
159 coastal upwelling systems due to diurnal-inertial resonance. Comparison of the model with
160 the observations of Lucas et al. (2014) provides insight into the strengths and limitations of
161 the model. Implications of the model results for surface layer nutrient enhancement in St
162 Helena Bay and other EBUS is then inferred.

163 **2 Methods**

164 **2.1 In-situ observations**

165 This paper makes use of in-situ observations from Wirewalker wave-powered profil-
166 ers (Rainville & Pinkel, 2001; Pinkel et al., 2011) and bottom-mounted Acoustic Doppler

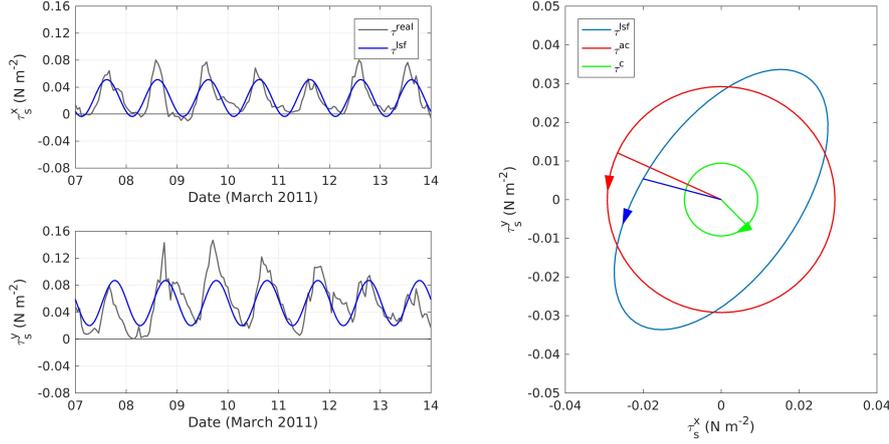
167 Current Profilers (ADCP), providing concurrent high-frequency nearshore measurements
 168 of velocity, temperature, salinity, dissolved oxygen and chlorophyll fluorescence within St
 169 Helena Bay. The full dataset is described in detail in Lucas et al. (2014), although only
 170 the velocity and temperature data from the offshore mooring (~ 60 m water depth) over
 171 the February-April 2011 deployment are revisited in this paper (see Figure 1). The vertical
 172 resolution of the ADCP velocity data is 1 m while temperature is available at 0.25 m inter-
 173 vals. All measurements presented in this paper were filtered in time to provide a two hour
 174 running mean at 30 min intervals, sufficient for analysing processes at the diurnal-inertial
 175 frequency of interest for this study. The observations are compared with the model over a
 176 7 day event in March 2011, having been identified in Lucas et al. (2014) as a period which
 177 clearly demonstrates the response of a highly stratified two layer system to the onset of
 178 upwelling favourable winds with an anticlockwise sense of rotation.

179 2.2 Atmospheric forcing

180 Atmospheric forcing data for this study have been obtained from a Weather Research
 181 and Forecasting (WRF) model configuration developed by the Climate Systems Analysis
 182 Group (CSAG) at the University of Cape Town (UCT). The atmospheric simulation forms
 183 part of the Wind Atlas for South Africa (WASA) project and has been validated against
 184 a number of land-based weather stations, including one deployed at the southern end of
 185 St Helena Bay over a three year period (Lennard et al., 2015). Model output is available
 186 on a ~ 3 km resolution horizontal grid at hourly intervals for the period November 2005 to
 187 October 2013 (8 years). Surface wind stresses used in this study have been derived from the
 188 CSAG 10 m wind speeds using the empirical drag formulation of Large and Pond (1981).

189 Rotary analyses have been carried out on the wind stress data to extract the diurnal
 190 anticyclonic (anticlockwise in the southern hemisphere) rotary component of the wind stress
 191 (τ^{ac}). Near latitudes of 30° N/S, τ^{ac} represents the component of the wind stress which
 192 rotates in the same direction and frequency as the inertial oscillation, and so energy flux
 193 from the wind is at all times positive (in the absence of background currents).

199 The complex function $\tau^{ac} = \tau^{ac0} e^{i(\omega t + \phi^{ac})}$ defines a wind stress vector rotating in an
 200 anticlockwise direction with a diurnal frequency ω , a constant amplitude τ^{ac0} , and a phase
 201 angle ϕ^{ac} . The purpose of the rotary analysis is to compute the parameters τ^{ac0} and ϕ^{ac}
 202 from the time-series of wind stress components. To do this, the wind ellipse parameters



194 **Figure 2.** Rotary analysis of wind stress over an example

195 7 day period used to carry out realistically forced 1D simulations. The blue time-series are the
 196 diurnal least squares fit curves to the wind stress components which sweep the blue ellipse (τ^{lsf}).
 197 The ellipse is decomposed into clockwise (τ^c) and anticlockwise (τ^{ac}) rotating components. The
 198 radial lines indicate the associated phase angles.

203 were firstly determined via a diurnal least squares fit (lsf) harmonic analysis on each of
 204 the wind stress components, from which the parameters τ^{ac0} and ϕ^{ac} were extracted using
 205 standard conversion techniques provided in the tidal_ellipse Matlab package (Xu, 2002). As
 206 the periodicity of the wind stress varies over time (unlike a tidal constituent whose phase and
 207 amplitude are constant), the result of the rotary analysis is particularly sensitive to the time
 208 window over which the analysis is carried out. Longer windows lead to smaller amplitude
 209 rotary components and a poorer fit to inter-diurnal variability. All rotary analyses presented
 210 in this paper have been carried out on 7 day windows, representative of the time-scale of
 211 individual upwelling events. The methodology described above is depicted in Figure 2 for
 212 the period used to compare observed event-scale mixing dynamics with the model. The
 213 WRF model output was extracted at the location of the observations (Figure 1), providing
 214 the wind stress and heat flux input for the ocean model.

215 **2.3 Ocean model**

216 The ocean model employed in this study is a standalone 1D version of the Coastal
 217 and Regional Ocean COmmunity model (CROCO) (<http://www.croco-ocean.org/>), an
 218 ocean modelling system built upon ROMS_AGRIF (Shchepetkin & McWilliams, 2005), in

219 which we retain the horizontal pressure gradient term normal to the coast. The 1D-vertical
 220 model solves the following equations for the horizontal velocity components (u, v) , active
 221 tracers temperature (T) and salinity (S) , and a passive tracer (C) used to represent the
 222 concentration of subsurface nutrients:

$$223 \quad \frac{\partial u}{\partial t} = fv + \frac{\partial}{\partial z} \left(K_m \frac{\partial u}{\partial z} \right) - g \frac{\partial \eta}{\partial x}, \quad (1a)$$

$$224 \quad \frac{\partial v}{\partial t} = -fu + \frac{\partial}{\partial z} \left(K_m \frac{\partial v}{\partial z} \right), \quad (1b)$$

$$225 \quad \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} \left(K_s \frac{\partial T}{\partial z} \right) + \frac{1}{\rho_0 C_p} \left(-\frac{\partial Q_s}{\partial z} \right), \quad (1c)$$

$$226 \quad \frac{\partial S}{\partial t} = \frac{\partial}{\partial z} \left(K_s \frac{\partial S}{\partial z} \right), \quad (1d)$$

$$227 \quad \frac{\partial C}{\partial t} = \frac{\partial}{\partial z} \left(K_s \frac{\partial C}{\partial z} \right), \quad (1e)$$

228 where K_m and K_s are the turbulent viscosity and diffusivity, respectively, η is the surface
 229 elevation, f is the Coriolis parameter, Q_s is a downward solar flux, ρ_0 is the reference density
 230 (1024 kg m^{-3}), and C_p is the specific heat coefficient ($3985 \text{ J kg}^{-1} \text{ K}^{-1}$). K_m and K_s are
 231 computed using a k - ε turbulent closure parameterisation within the Generic Length-Scale
 232 (GLS) formulation (Umlauf & Burchard, 2003, 2005, and Appendix A for a description of
 233 the implementation in CROCO). Minimum values for K_m and K_s are taken as $10^{-4} \text{ m}^2 \text{ s}^{-1}$
 234 and $10^{-5} \text{ m}^2 \text{ s}^{-1}$, respectively, representing background values for turbulence and mixing.
 235 The model is completed by the following top ($z = 0$) and bottom ($z = -H$) boundary
 236 conditions for velocity components:

$$237 \quad \rho_0 K_m \frac{\partial}{\partial z} \vec{u}(0, t) = \vec{\tau}_s, \quad (2a)$$

$$238 \quad K_m \frac{\partial}{\partial z} \vec{u}(-H, t) = \vec{\tau}_b = C_d |\vec{u}(-H, t)| \vec{u}(-H, t), \quad (2b)$$

239 where the surface stress $\vec{\tau}_s = (\tau_s^x, \tau_s^y)$ is specified analytically or through external data,
 240 while the bottom stress $\vec{\tau}_b = (\tau_b^x, \tau_b^y)$ is determined from the shown quadratic drag law with
 241 a drag coefficient (C_d) defined as:

$$242 \quad C_d = \left(\frac{\kappa}{\ln(z_b/z_0)} \right)^2, \quad (3)$$

243 where κ is the von Kármán constant (0.4), z_0 is the bottom roughness length parameter
 244 (taken as 0.1 m) and z_b is the thickness of the bottom layer of the model. Upper and lower
 245 limits for C_d were applied as 0.02 and 0.0025, respectively. The surface boundary conditions
 246 for the tracers are:

$$247 \quad \rho_0 C_p K_s \frac{\partial}{\partial z} T(0, t) = -(Q_0(t) - Q_s(0, t)), \quad (4a)$$

$$248 \quad K_s \frac{\partial}{\partial z} S(0, t) = 0, \quad (4b)$$

$$249 \quad K_s \frac{\partial}{\partial z} C(0, t) = 0, \quad (4c)$$

250 with $Q_0(t)$ the net heat flux and $Q_s(0, t)$ the surface downward solar radiation both extracted
 251 either from WRF model outputs or set analytically (see Section 2.5). The penetration of
 252 downward solar radiation in the vertical is parameterized using a standard Jerlov law. We
 253 assume zero water flux at the surface since temperature is the major driver for density
 254 in the region. The bottom boundary conditions for tracers are simply $K_s \frac{\partial}{\partial z} T(-H, t) =$
 255 $K_s \frac{\partial}{\partial z} S(-H, t) = K_s \frac{\partial}{\partial z} C(-H, t) = 0$. The model is discretised using an implicit Euler
 256 scheme in time and a standard second-order finite-volume approach in space consistent with
 257 the CROCO discretisation of vertical mixing terms. Because the Brunt-Väisälä frequency
 258 is required by the k - ε turbulent scheme an equation of state for seawater must be added to
 259 the system of equations (1). For the present study a nonlinear equation of state adapted
 260 from Jackett and McDougall (1995) is used.

261 **2.4 ‘Craig approximation’**

262 The effect of the land boundary (assumed to be orientated along the y -axis for the
 263 purposes of this study) is implicitly included in the model through the surface elevation
 264 gradient term ($\frac{\partial \eta}{\partial x}$) in Equation 1a, being a user-specified input to the model. This term
 265 has been determined according to Craig (1989) and Simpson et al. (2002), however here we
 266 extend the formulation to include the effect of bottom friction. The governing equations for
 267 depth-averaged velocity components (U, V) can be written as:

$$268 \quad \frac{\partial U}{\partial t} = fV - g \frac{\partial \eta}{\partial x} + \frac{\tau_s^x}{\rho H} - \frac{\tau_b^x}{H}, \quad (5a)$$

$$269 \quad \frac{\partial V}{\partial t} = -fU - g \frac{\partial \eta}{\partial y} + \frac{\tau_s^y}{\rho H} - \frac{\tau_b^y}{H}, \quad (5b)$$

270 where H is the water depth. If U and V are taken to represent the cross-shore and alongshore
 271 depth-averaged velocity components, respectively, then the condition of zero depth-average
 272 flow perpendicular to the coast dictates that $U = 0$ and therefore $\frac{\partial U}{\partial t} = 0$. Assuming
 273 zero alongshore pressure gradients ($\frac{\partial \eta}{\partial y} = 0$) and a wave solution for the alongshore depth-
 274 averaged velocity ($\frac{\partial V}{\partial t} = -i\omega V$), then Equation 5b can be recast as $V = \frac{i}{\omega H} (\frac{\tau_s^y}{\rho} - \tau_b^y)$.
 275 Substitution of V into Equation 5a yields the surface elevation gradient response:

$$276 \quad \frac{\partial \eta}{\partial x} = \frac{\tau_s^x + i(f/\omega)\tau_s^y}{\rho g H} - \frac{\tau_b^x + i(f/\omega)\tau_b^y}{g H}. \quad (6)$$

277 The wind stress terms ($\frac{\tau_s^x + i(f/\omega)\tau_s^y}{\rho g H}$) correspond to the ‘Craig approximation’ as pre-
 278 sented in Simpson et al. (2002). As we aim to force the model with realistic wind stresses,
 279 and do not have an a priori analytical solution for bottom shear stresses, the complex terms
 280 in Equation 6 preclude an analytical solution for $\frac{\partial \eta}{\partial x}$. The assumption of diurnal variability
 281 as the dominant signal in both surface and bottom stress is however made, being valid in
 282 the case of land-sea breeze forcing near the critical latitude, as the periodicity in both the
 283 forcing and the ocean response can be assumed to be near-diurnal. In the case of periodi-
 284 cally oscillating wind and bottom stress, the complex terms in Equation 6 correspond to a
 285 $\frac{\pi}{2}$ phase shift in these variables. We therefore assign the terms $i\tau_s^y$ and $i\tau_b^y$ to be equal to
 286 the values of τ_s^y and τ_b^y at a time 6 hours prior to the given time-step, respectively.

287 2.5 Model configuration

288 The number of vertical layers was assigned to be equal to the water depth in metres,
 289 ensuring the same vertical grid resolution for all simulations. A time-step of 10 s was
 290 used to integrate the model solution over a period of 7 days from initialisation, typical of
 291 the time-scale of upwelling events. Model output at 30 min intervals was filtered in time
 292 to provide a two hour running mean at each time-step, consistent with the processing of
 293 observations. Both analytical and realistic model configurations were employed. Simulations
 294 were initialised from rest using a constant salinity of 35 and a temperature profile defined
 295 either analytically or from observations, as described below.

296 The purpose of the analytical model configurations was to explore the physical pro-
 297 cesses and key drivers of enhanced vertical mixing in a two layer coastal system due to
 298 diurnal-inertial resonance. The initial temperature profile for these experiments was speci-

299 fied according to a hyperbolic tangent function as follows:

$$300 \quad T(z) = 10 + \Delta T/2(1 - \tanh(((z - \text{MLD})/3))), \quad (7)$$

301 where ΔT is the difference between surface and subsurface temperatures and MLD the initial
 302 mixed layer depth, corresponding to the depth of maximum stratification. The resulting
 303 profile increases from 10° C in the subsurface to a specified surface layer temperature.
 304 Higher ΔT 's imply higher levels of stratification. Surface wind stress forcing took the form
 305 of constant amplitude rotating winds at a diurnal frequency (representative of the land-sea
 306 breeze), constant winds (representative of a mean alongshore wind), or a combination of the
 307 two. Surface heat fluxes were ignored in the analytical configurations.

308 A realistic model configuration was used to compare the model with the observations
 309 of Lucas et al. (2014) over the period 7-14 March 2011. The initial temperature profile
 310 was interpolated directly from the observations. Surface wind stress forcing took the form
 311 of both realistic wind stresses derived from the WRF model output as well as the diurnal
 312 anticlockwise rotary component of the wind stress (τ^{ac}), as shown in Figure 2. Surface heat
 313 flux forcing was estimated as the net heat flux derived from short and long wave radiation
 314 output from the WRF model, ignoring contributions of latent and sensible heat. This yielded
 315 daily peaks in positive heat flux of approximately 800 W/m² over the simulation period.

316 2.6 Diapycnal mixing diagnostics

317 As this paper focusses on diapycnal mixing at the interface of a two layer system, we
 318 use the bulk shear vector $\vec{S} = (S_u, S_v)$ as defined by Burchard and Rippeth (2009) as an
 319 indicator of shear between the surface and bottom layers:

$$320 \quad S_u = \frac{u_s - u_b}{1/2H}, \quad S_v = \frac{v_s - v_b}{1/2H}, \quad (8)$$

321 where $\vec{u}_s = (u_s, v_s)$ and $\vec{u}_b = (u_b, v_b)$ are the depth-averaged velocity vectors for the surface
 322 and bottom layers, respectively. Based on the one-dimensional momentum equations for a
 323 two layer system, Burchard and Rippeth (2009) derived the dynamical equation for bulk
 324 shear squared ($S^2 = S_u^2 + S_v^2$), used in this paper as a tool for interpreting event-scale mixing
 325 dynamics:

$$\frac{\partial S^2}{\partial t} = \frac{4}{H} \vec{S} \cdot \left(\frac{\vec{\tau}_s}{H_s} + \frac{\vec{\tau}_b}{H_b} \right) - c_i \frac{H^2}{H_s H_b} S^3, \quad (9)$$

where H_s and H_b are the depths of the surface and subsurface layers, respectively, $\vec{\tau}_s = (\tau_s^x, \tau_s^y)$ is the surface shear stress vector, $\vec{\tau}_b = (\tau_b^x, \tau_b^y)$ is the bottom shear stress vector and c_i is the interfacial drag coefficient. In this study H_s is computed from a defined isotherm (varying depending on the configuration), used as a proxy for the interface between the upper and lower layers. c_i may be roughly estimated as follows:

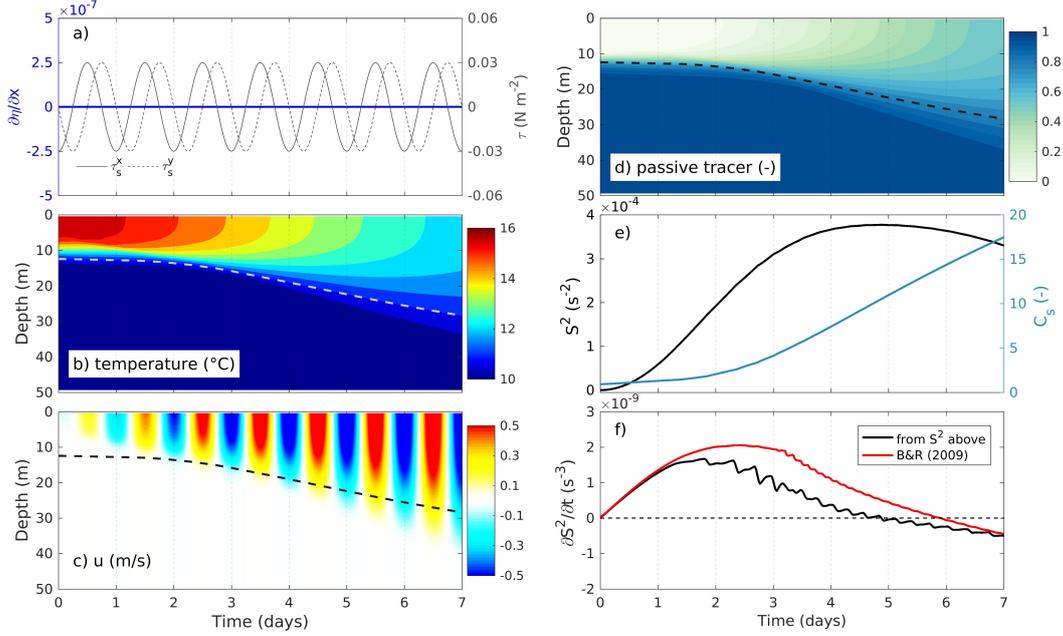
$$c_i = K_m \frac{4S_i}{H^2 S^2}, \quad (10)$$

where S_i is the interfacial shear estimated locally at the interface of the two layers (Burchard & Rippeth, 2009). Estimates of c_i from the model output were computed using the K_m returned from the k - ε turbulent closure scheme, while a constant value of $K_m = 1.5 \times 10^{-4} \text{ m}^2 \text{ s}^{-1}$ was adopted for processing of the observations. Equation 9 dictates that bulk shear is generated when the bulk shear vector is in alignment with the surface and/or bottom shear stress vectors. The last term on the right hand side of Equation 9 represents the loss of bulk shear due to interfacial mixing between the two layers. In this paper we compare the theoretical bulk shear production of Equation 9 with that computed directly from the model output and from the observations. $\frac{\partial S^2}{\partial t}$ from both the model output and observations is computed as the gradient of a least squares fit straight line for data within a 2 hour window of each 30 min time-step.

The quantification of diapycnal mixing over the simulations was further aided by initialising the model with a passive tracer (C) below the surface mixed layer, representing a reservoir of subsurface nutrients. The cumulative diapycnal mixing of the passive tracer to the surface layer has been computed by integrating the passive tracer concentration multiplied by the grid cell height (Δz) over the surface layer:

$$C_s = \sum_{z=-H_s}^{z=0} C \times \Delta z. \quad (11)$$

C_s provides an indicator of enhanced availability of surface layer nutrients for primary productivity.



355 **Figure 3.** Open Ocean Case. (a) Wind stress components (τ_s^x , τ_s^y) and cross-shore surface
 356 elevation gradient forcing ($\partial\eta/\partial x$); (b) Vertical profile of temperature (the dotted line denotes
 357 the 11° C isotherm used as a proxy for the interface between the upper and lower layers); (c)
 358 Vertical profile of the cross-shore component of velocity (u); (d) Vertical profile of passive tracer
 359 concentration; (e) Bulk shear (S^2) and passive tracer integrated over the surface layer (C_s); (f) Bulk
 360 shear production ($\frac{\partial S^2}{\partial t}$) computed from both the model output and from the theory of Burchard
 361 and Rippeth (2009) (Equation 9). Results are computed from a 7 day integration of the 1D-vertical
 362 model with input parameters $\tau^{ac0} = 0.03 \text{ N m}^{-2}$, $\frac{\partial\eta}{\partial x} = 0$ (excluding the land boundary effect),
 363 latitude = 30° S, initial MLD = 10 m, initial stratification = 6° C, water depth = 50 m.

352 3 Results

353 3.1 Diurnal-inertial resonance and mixing

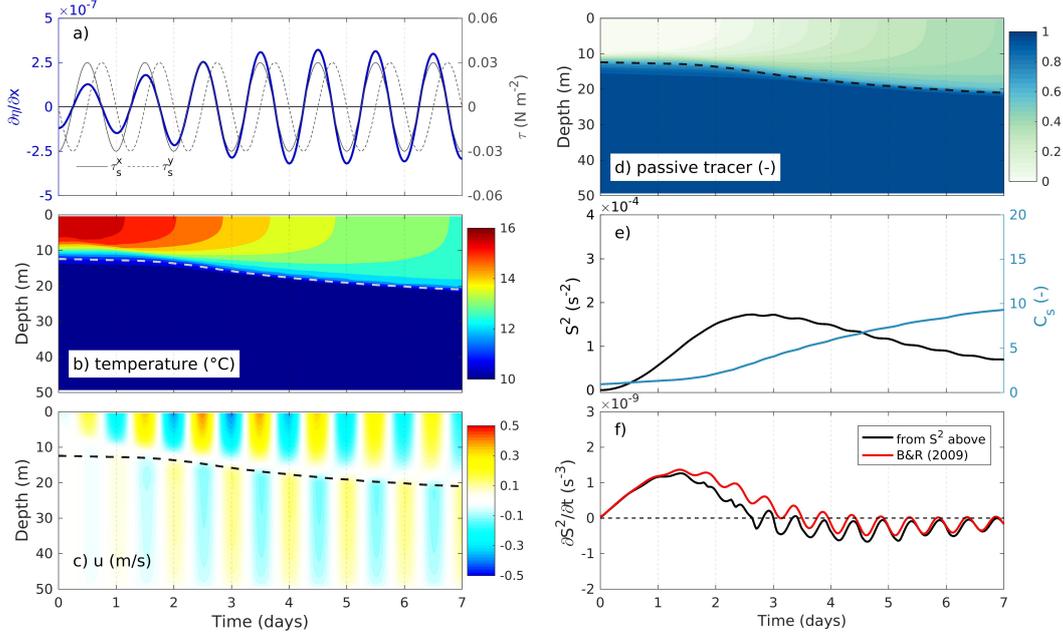
354 3.1.1 Open ocean case

364 We begin by considering a two layer system forced by a constant amplitude diurnal
 365 anticlockwise rotating wind stress at 30° S, in the absence of a land boundary ($\partial\eta/\partial x = 0$).
 366 The amplitude of the applied wind stress is 0.03 N m^{-2} , being typical of the amplitude of
 367 the diurnal anticlockwise rotary component of the wind stress (τ^{ac0}) over St Helena Bay
 368 (Figure 9). Figure 3 shows the input forcing time-series for the model, the evolution of the
 369 resulting temperature and cross-shore velocity profiles, and the diapycnal mixing diagnostics

370 described in Section 2.6. A diurnal anticlockwise rotating wind stress at 30° S represents the
 371 pure case of diurnal-inertial resonance, as the wind stress is always aligned with the surface
 372 inertial oscillation and so the energy flux from the wind to the ocean ($\vec{\tau}_s \cdot \vec{u}_s$) is maximised.
 373 Stratification between the surface and subsurface layers restricts the generation of wind-
 374 driven currents to within the surface mixed layer. In the absence of the land boundary effect
 375 subsurface currents are not generated. The impact of water depth is therefore negligible in
 376 this experiment. The enhancement of the surface inertial oscillation is accompanied by the
 377 deepening of the thermocline and the cooling of the surface waters due to the entrainment of
 378 sub-thermocline waters. The simulation indicates a steady enrichment of the surface layer
 379 with the subsurface tracer, as evidenced by the increase in C_s over the simulation. The
 380 enhanced diapycnal mixing is driven by elevated bulk shear, which is shown to increase
 381 rapidly over the first few days of the simulation, peaking at day ~ 5 , before decreasing
 382 thereafter.

383 Although the bulk shear production computed directly from the model is consistently
 384 higher than that predicted by the analytical theory of Burchard and Rippeth (2009) (Fig-
 385 ure 3f), the results suggest that Equation 9 provides a useful lens through which to interpret
 386 the results. The initial increase in bulk shear is explained by the perfect alignment of the
 387 surface wind stress ($\vec{\tau}_s$) with the surface current (\vec{u}_s) and therefore the bulk shear vector
 388 (\vec{S}). The enhanced bulk shear drives an increase in interfacial mixing (represented by the
 389 last term in Equation 9) as well as an increased depth of the surface layer (H_s), both of
 390 which serve to reduce shear production. The bottom shear stress term is negligible in this
 391 simulation due to the absence of a subsurface oscillation. Shear production lowers to zero
 392 when the interfacial mixing term balances the wind stress input term. In this way interfa-
 393 cial mixing represents a mechanism which limits the amplitude of the surface layer inertial
 394 oscillation.

395 It should be noted that simulations forced with a diurnal clockwise rotating wind stress
 396 at 30° S yield negligible current response as the winds continually dampen the rotating
 397 surface inertial oscillation, which by definition has an anticlockwise sense of rotation in the
 398 southern hemisphere. Figure S1 provides an example of such a case, and serves as a reference
 399 experiment for background levels of mixing in the absence of any notable current forcing.



401 **Figure 4.** Effect of land boundary. Same as Figure 3 but with the 1D-vertical model now
 402 integrated including the ‘Craig approximation’ for coast-normal surface elevation gradient response
 403 (Equation 6).

400 3.1.2 The land boundary effect

404 Figure 4 builds on the model presented in Figure 3 by including the effect of the land
 405 boundary through the ‘Craig approximation’ for coast-normal surface elevation gradient
 406 response (Equation 6). For the considered case of pure diurnal-inertial resonance, $\frac{\partial\eta}{\partial x}$ is
 407 in phase with the cross-shore component of the wind stress (τ_s^x), generating a barotropic
 408 current response in the opposite direction to the surface inertial oscillation. The result is
 409 a significantly weakened surface inertial oscillation when compared to Figure 3, and the
 410 generation of a subsurface oscillation with a 180° phase shift to the surface layer. At the
 411 start of the simulation, bottom friction is negligible and $\frac{\partial\eta}{\partial x}$ is determined from the wind
 412 stress terms of Equation 6 alone. As the subsurface oscillation increases in amplitude, so do
 413 bottom friction losses, serving to further enhance $\frac{\partial\eta}{\partial x}$ (as dictated by Equation 6), thereby
 414 dampening the surface oscillation. For the shown example, the bottom friction terms of
 415 Equation 6 approximately double the amplitude of $\frac{\partial\eta}{\partial x}$ before the solution stabilises.

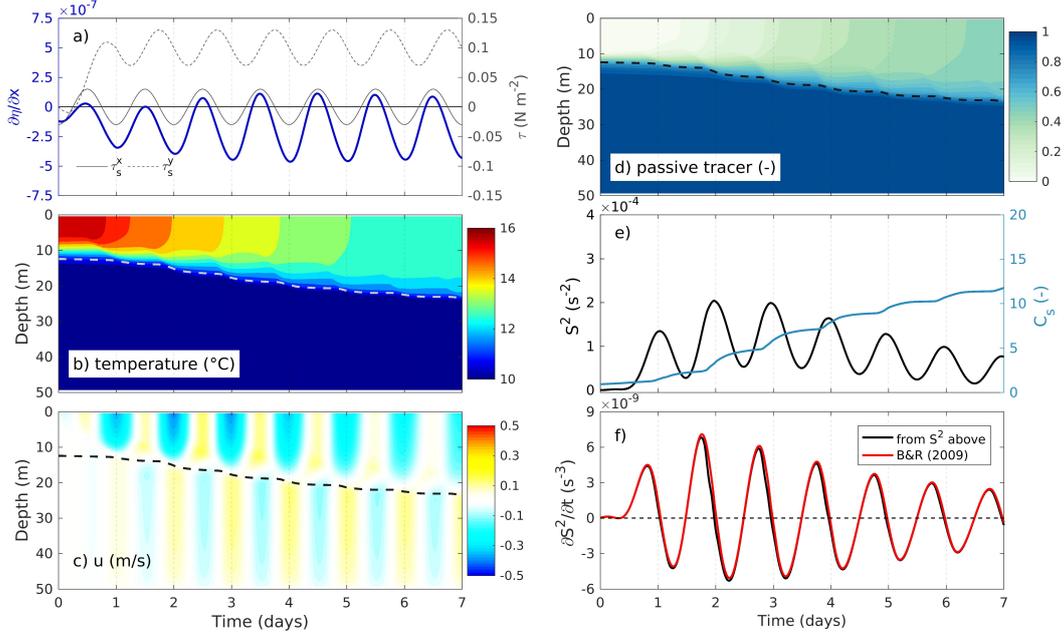
416 A comparison of the mixing diagnostics from Figures 3 and 4 shows that forcing the
 417 model with the ‘Craig approximation’ serves to significantly reduce bulk shear and therefore

418 diapycnal mixing. For the shown example, C_s at 7 days is approximately halved through the
 419 inclusion of the land boundary effect. The evolution of bulk shear can again be interpreted
 420 using the bulk shear production theory of Burchard and Rippeth (2009). In addition to
 421 the processes already described for Figure 3, the subsurface oscillation generated by the
 422 ‘Craig approximation’ introduces a non-negligible bottom shear stress ($\overline{\tau}_b^x$) which is at all
 423 times directly opposed to the surface shear stress ($\overline{\tau}_s^x$). Equation 9 dictates that bulk
 424 shear production, and therefore diapycnal mixing, will be reduced as the cross-shore surface
 425 elevation gradient is enhanced.

426 It is important to note that the model solution results in near-zero depth averaged
 427 cross-shore transport, in line with the assumptions made in the formulation of the analytical
 428 theory for $\frac{\partial \eta}{\partial x}$ (Section 2.4). The bottom friction terms in Equation 6 are instrumental in
 429 this regard, as they account for bottom friction losses in the subsurface layer by amplifying
 430 $\frac{\partial \eta}{\partial x}$. In the absence of bottom friction terms in Equation 6, surface layer current velocities
 431 are over-estimated leading to a violation of the assumption of zero cross-shore transport, and
 432 the over-prediction of diapycnal mixing (Figure S2). Sensitivity tests indicate that bottom
 433 friction terms become negligible for maintaining near-zero cross-shore transport for water
 434 depths greater than ~ 200 m (Figure S3).

435 **3.1.3 Effect of Ekman transport**

438 The results thus far have considered only a diurnally rotating wind stress of constant
 439 amplitude, representative of the land-sea breeze. Upwelling systems are however also defined
 440 by sustained alongshore wind stresses. Figure 5 builds on the model presented in Figure 4
 441 by including the effect of a mean alongshore wind stress ($\overline{\tau}_s^y$) of 0.1 N m^{-2} , representative of
 442 a relatively strong alongshore wind stress over St Helena Bay (Figure 9). The classic case
 443 of Ekman transport in response to a constant τ_s^y of 0.1 N m^{-2} is provided in Figure S4. The
 444 inclusion of a mean alongshore wind stress is shown to introduce a mean surface transport
 445 in the offshore direction, consistent with Ekman theory, with the surface inertial oscillation
 446 superimposed onto the offshore transport (Figure 5c). The bulk shear time-series (Figure 5e)
 447 is characterised by a pronounced diurnal signal, or ‘shear spikes’ at the inertial frequency
 448 to use the terminology of Burchard and Rippeth (2009). The diurnal variability in bulk
 449 shear is superimposed onto a sub-inertial signal similar to that shown in Figure 4, namely
 450 that of an initial increase in shear followed by a subsequent decrease from day ~ 3 onwards.
 451 The sub-inertial variability in shear has been explained above, while the diurnal variability



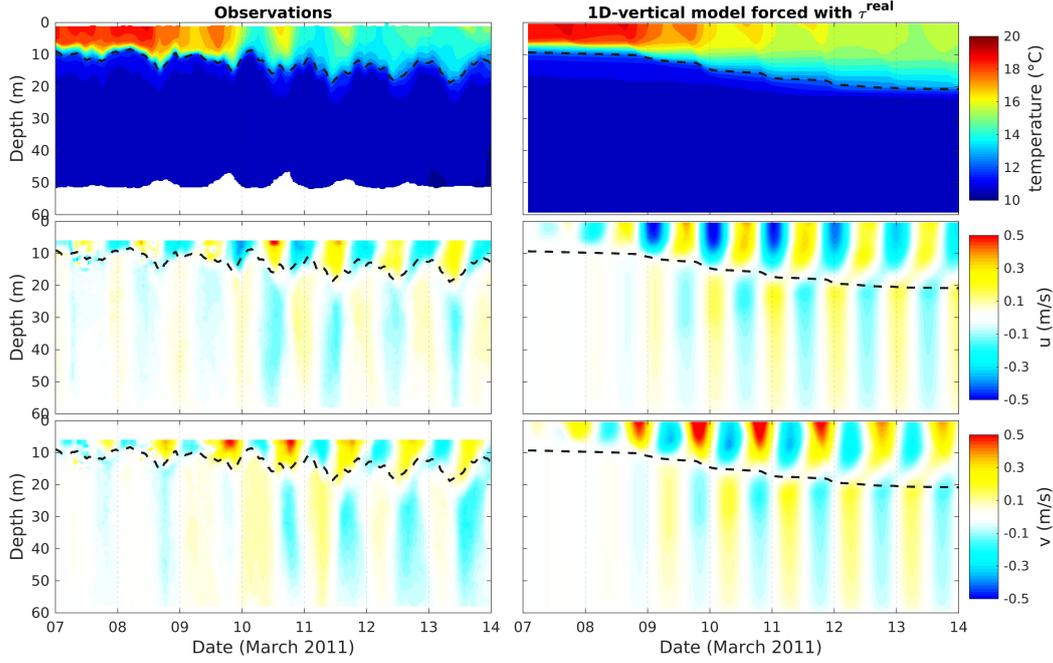
436 **Figure 5.** Effect of Ekman transport. Same as Figure 4, but with the 1D-vertical model now
 437 integrated including a mean alongshore wind stress ($\overline{\tau}_s^y$) of 0.1 N m^{-2} .

452 can again be interpreted using the bulk shear production theory of Burchard and Rippeth
 453 (2009). Bulk shear production (Figure 5f) is shown to be maximised when the y component
 454 of the wind stress (τ_s^y) is highest, as at these times $\overline{\tau}_s^y \cdot \overline{S}$ is maximised. Shear production
 455 becomes negative at times when the surface current and wind stress are opposed. Bulk
 456 shear is maximised at a phase $\frac{\pi}{2}$ (6 hours) after the peak in bulk shear production, as this is
 457 when the surface inertial oscillation is aligned with the sub-inertial Ekman transport. The
 458 diurnal peaks in bulk shear are coincident with bursts of diapycnal mixing that inject the
 459 subsurface tracer into the surface layer. Although the impact on bulk shear and diapycnal
 460 mixing is significant at the diurnal time-scale, the net tracer injection into the surface layer
 461 (C_s) is very similar to the simulation excluding the alongshore wind stress (Figure 4).

462 3.2 Case study of St Helena Bay

463 3.2.1 Comparison with observations

464 We now turn to the nearshore observations in St Helena Bay and assess the extent to
 465 which the simple 1D-vertical model dynamics described above can explain the observations.
 466 Figure 6 presents the evolution of observed and modelled temperature and velocity through



474 **Figure 6.** Observed (left) and modelled (right) temperature and velocity components over an
 475 upwelling event accompanied by diapycnal mixing in ~ 60 m water depth in St Helena Bay (‘WW’
 476 in Figure 1). The dotted line denotes the 12.5° C isotherm used as a proxy for the interface between
 477 the upper and lower layers.

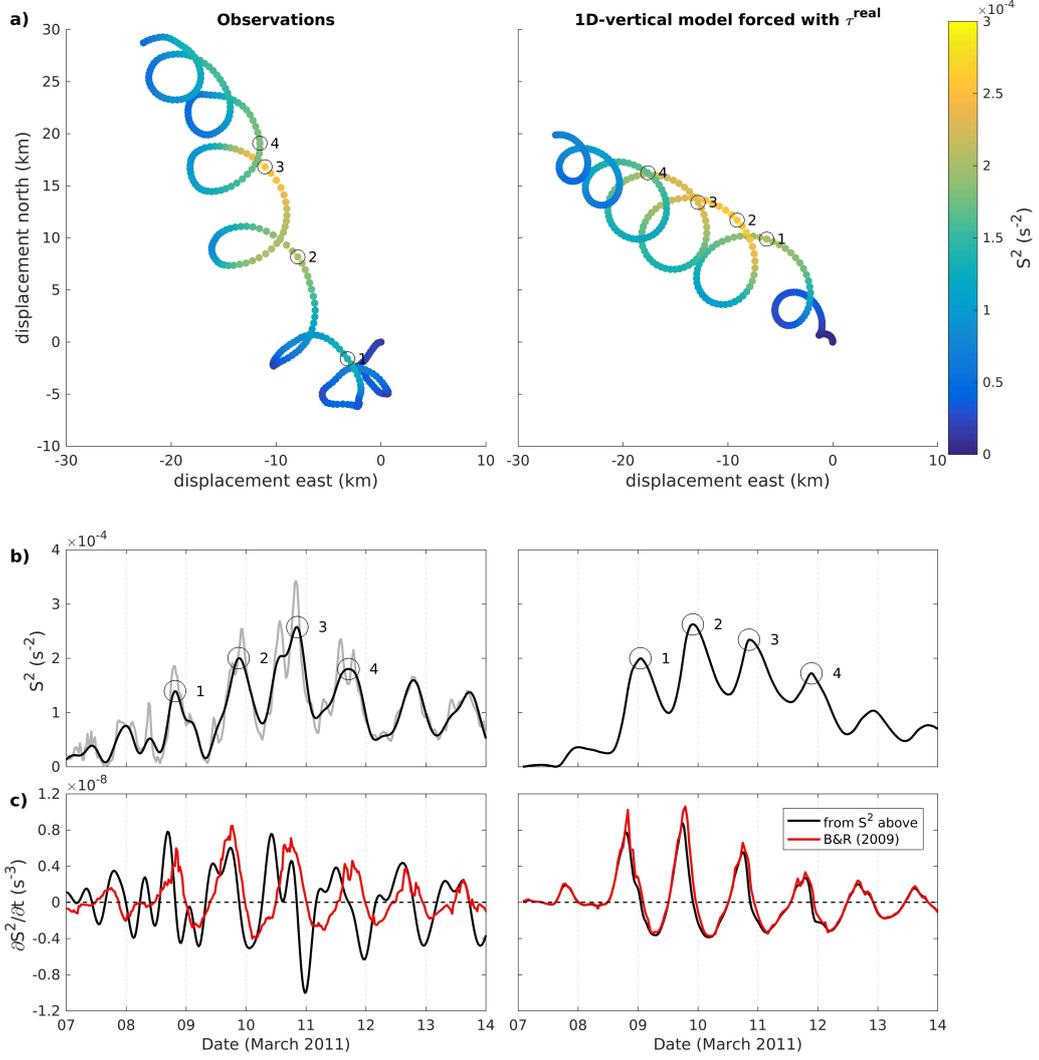
467 the water column over the considered upwelling/mixing event. It is again noted that this
 468 event was specifically identified as a period where the observations clearly demonstrate
 469 the response of a highly stratified two layer system to the onset of upwelling favourable
 470 winds with an anticlockwise sense of rotation (Lucas et al., 2014). The temperature initial
 471 condition for the model was interpolated directly from the observations, while hourly wind
 472 stress and heat flux forcing for the model were derived from the CSAG WRF simulation at
 473 the location of the observations (τ^{real} in Figure 2).

478 The model reproduces the observed two layer system comprised of anticlockwise oscil-
 479 lations at the diurnal-inertial frequency in both surface and subsurface layers with a 180°
 480 phase shift between the two. The contamination of the surface ADCP data complicates a
 481 direct comparison of modelled and measured surface currents, however the amplitudes and
 482 phases are shown to be in surprisingly good agreement, considering the simplified physics
 483 of the model. The reasonable representation of subsurface velocities through the ‘Craig
 484 approximation’ provides some confidence in the methodology as applied in this paper. The

485 good agreement may be surprising given that the 2D model experiments of Hyder et al.
 486 (2011) suggested that the ‘Craig approximation’ is not valid near the coast (< 140 km)
 487 where non-linear terms cannot be ignored. Given that the observations are ~ 12 km from
 488 the coast, significant deviations in surface elevation gradient from linear theory are expected
 489 at this location, however our results suggest that the net subsurface current response is pre-
 490 dominantly driven by the linear physics of the theory. It is noted that the inclusion of the
 491 bottom friction terms in Equation 6 significantly improved the realism of the model, given
 492 the ~ 60 m water depth of the observations.

493 Both the observations and the model indicate a rapid increase in surface current am-
 494 plitude until ~ 11 March, followed by a subsequent decrease. The onset of enhanced surface
 495 currents is accompanied by a deepening of the thermocline and a lowering of surface layer
 496 temperatures, consistent with the effects of diapycnal mixing. The model over-estimates
 497 the deepening of the thermocline, however the net cooling of the surface layer is somewhat
 498 contradictorily under-estimated. The observations reveal strong diurnal-inertial variability
 499 in surface temperature, particularly over the period 09-12 March, which is not reproduced
 500 in the model. The model does include a diurnal signal of surface layer warming due to the
 501 heat flux input, however the combination of mixing and heating alone cannot explain the
 502 observed diurnal variability. These discrepancies point to the presence of vertical and hori-
 503 zontal advection driven variability in the observations which is not included in the physics
 504 of the model. A further important difference between the model and the observations is
 505 that the observations include significant vertical displacements of the thermocline (~ 5 m
 506 amplitude) with a diurnal frequency which are absent in the model. This indicates the
 507 presence of near-inertial internal waves, likely generated by the convergence and divergence
 508 of the forced response near the land boundary, which are by definition not included in the
 509 physics of the model.

516 Figure 7 presents the evolution of bulk shear (S^2) as derived from the data shown in
 517 Figure 6. The computation of \vec{u}_s from the ADCP data required the filling of contami-
 518 nated surface layers with data from the uppermost bin considered to contain good data.
 519 This is likely to result in an under-estimation of surface layer velocities (and therefore bulk
 520 shear) computed from the observations. The bulk shear vector computed from the measure-
 521 ments was low-pass filtered to remove frequencies higher than 12 hours. The progressive
 522 displacement plots show the surface layer currents to be comprised of inertial oscillations
 523 superimposed onto a background mean flow. The modelled mean flow is perpendicular to

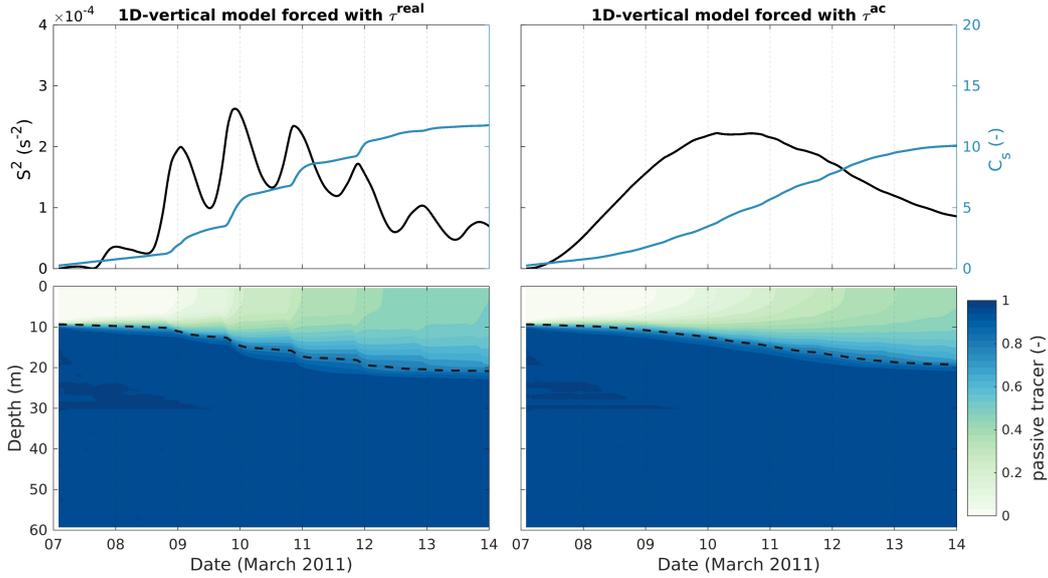


510 **Figure 7.** Observations (left) versus 1D-vertical model (right) during the event shown in Fig-
 511 ure 6. (a) Progressive displacement plots derived from surface layer velocities (\vec{u}_s). (b) Time-series
 512 of bulk shear (S^2). The grey line shows the unfiltered bulk shear derived from the observations
 513 while the black line shows the low-pass filtered data. (c) Time-series of bulk shear production
 514 ($\frac{\partial S^2}{\partial t}$) computed from the observations (left), model output (right), and the theory of Burchard and
 515 Rippeth (2009).

524 the left of the major axis of the wind variability (Figure 2), consistent with Ekman trans-
525 port. There is a difference in the orientation of the mean flow between the observations
526 and the model, likely reflecting an error in the mean wind direction of the WRF model
527 with respect to the actual winds over this event. Both the observations and the model show
528 strong diurnal variability in bulk shear. The amplitude and timing of the ‘shear spikes’ in
529 the model and the observations are in reasonable agreement. Four ‘shear spikes’ have been
530 identified (labelled 1-4) and are indicated on the progressive displacement plots. In both
531 the observations and the model, the ‘shear spikes’ are shown to occur when the oscillation
532 and the mean flow are aligned leading to enhanced surface layer velocities and therefore
533 bulk shear, consistent with the analytical configurations described in Section 3.1.3. The
534 diurnal variability in bulk shear is superimposed onto a sub-inertial signal which indicates
535 an increase in bulk shear until 10-11 March followed by a subsequent decrease, which is
536 again consistent with the physics described for the analytical configurations. Comparison of
537 the bulk shear production computed from the observations and the theory of Burchard and
538 Rippeth (2009) (Figure 7c) reveals that the timing of the diurnal peaks is not always con-
539 sistent. This could again be largely explained by errors in the WRF model wind direction
540 over this event, as the theoretical bulk shear production is computed from the dot product
541 of the WRF model wind stress and the observed bulk shear vector (Equation 9). The bulk
542 shear production computed from the model is however in good agreement with the theory.

543 **3.2.2 τ^{ac0} as a diagnostic for diapycnal mixing**

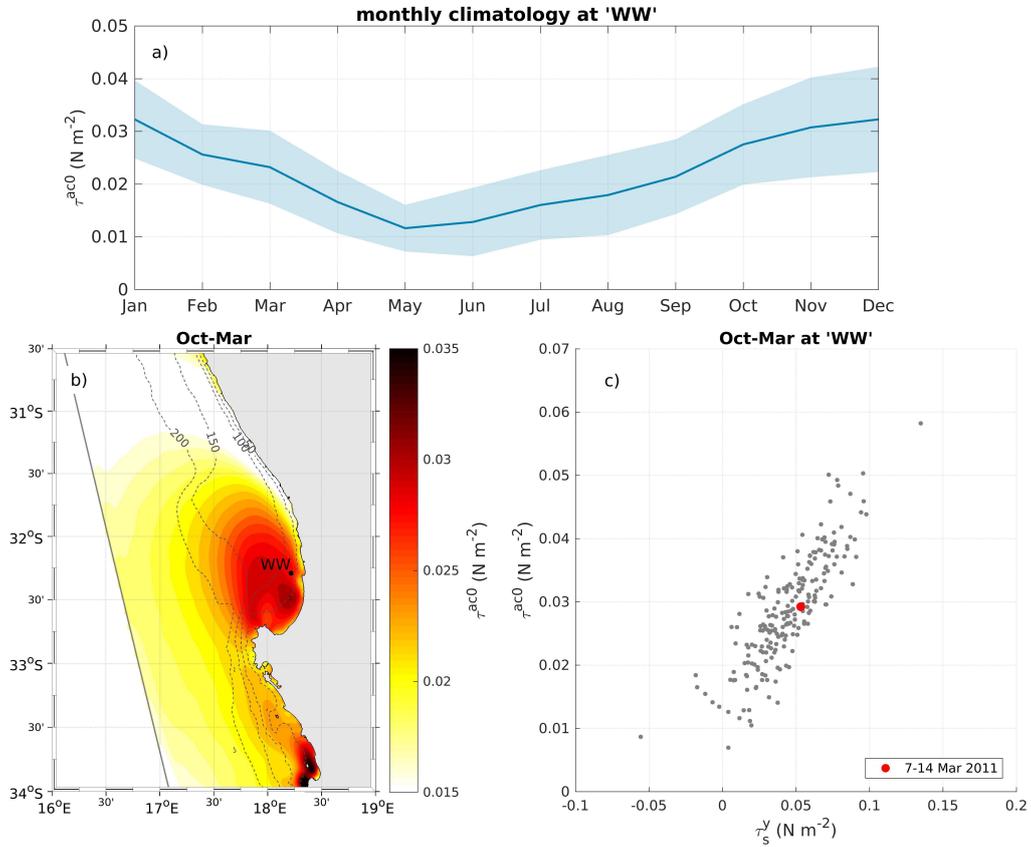
547 The comparison of the realistic model configuration with the observations shown above
548 was carried out using realistic wind stresses (τ^{real}), while the analytical model configura-
549 tions presented in Section 3.1 were carried out using a constant amplitude anticlockwise
550 rotating wind stress (τ^{ac}). Figure 8 presents bulk shear and mixing results for simulations
551 forced with both τ^{real} and τ^{ac} , to ascertain the extent to which τ^{ac} alone contributes to
552 diapycnal mixing over the event. τ^{ac} for this simulation was computed from the 7 day period
553 of 7-14 March 2011, as depicted by the red circle in Figure 2. Further detailed output from
554 these simulations are provided in Figures S5 and S6. The notable difference between the
555 simulations is the absence of diurnal ‘shear spikes’ in the simulation forced with τ^{ac} alone.
556 In the absence of Ekman transport (τ^{ac} has a mean wind stress of zero), the mechanism for
557 the generation of diurnal ‘shear spikes’ through the superposition of the mean flow and the
558 inertial oscillations is no longer present. The sub-inertial evolution of bulk shear is however



544 **Figure 8.** Bulk shear evolution and diapycnal mixing during the event shown in Figure 7 for
 545 simulations forced with realistic wind stresses τ^{real} (left) and its diurnal anticlockwise rotary com-
 546 ponent τ^{ac} (right). The wind stress forcing for these simulations is shown in Figure 2.

559 quite similar between the two simulations. Despite the large differences in the magnitude of
 560 the applied surface wind stresses (τ^{real} attains a maximum value of $\sim 0.15 \text{ N m}^{-2}$ while τ^{ac}
 561 has a constant amplitude of 0.03 N m^{-2}), the cumulative diapycnal mixing response, as re-
 562 vealed by C_s , is comparable between the two simulations. The results therefore suggest that
 563 the amplitude of τ^{ac} (τ^{ac0}) can be used as a reasonable diagnostic for event-scale diapycnal
 564 mixing in response to the land-sea breeze. ‘Shear spikes’ introduced by the interaction of
 565 the surface inertial oscillation with the Ekman transport are shown to play a secondary role.

574 As τ^{ac0} represents a diagnostic for diapycnal mixing, the spatial and seasonal variability
 575 of this parameter over St Helena Bay has been assessed, as shown in Figure 9. The monthly
 576 climatology of τ^{ac0} computed at the location of the Lucas et al. (2014) observations (Fig-
 577 ure 9a) reveals a distinct seasonality in the land-sea breeze, with a peak coinciding with the
 578 austral summer (November - January). This seasonality corresponds to that of the upwelling
 579 favourable winds in the region. Figure 9c reveals that τ^{ac0} and τ_s^y are strongly correlated,
 580 indicating that periods of enhanced inertial oscillations are coincident with enhanced up-
 581 welling. The period coinciding with the historical mixing/upwelling event considered in this
 582 study (7-14 March 2011) is highlighted and shown to be typical in terms of both upwelling
 583 and land-sea breeze forcing. The spatial variability in τ^{ac0} (Figure 9b) indicates a strong



566 **Figure 9.** Spatial and seasonal variability in the amplitude of the diurnal anticlockwise rotary
 567 component of wind stress (τ^{ac0}) over St Helena Bay. τ^{ac0} has been estimated from consecutive 7 day
 568 windows over the 8 year duration of the 3 km resolution WRF simulation described in Section 2.2.
 569 (a) Monthly climatology of $\tau^{ac0} \pm 1\sigma$ at the location of the Lucas et al. (2014) observations. (b)
 570 Spatial variability in the six month climatology of τ^{ac0} over the upwelling favourable months of
 571 October to March. Overlain are the bathymetric contours. (c) Scatter plot of τ^{ac0} vs the 7 day
 572 mean alongshore wind stress (τ_s^y) at the location of the Lucas et al. (2014) observations over the
 573 upwelling favourable months of October to March.

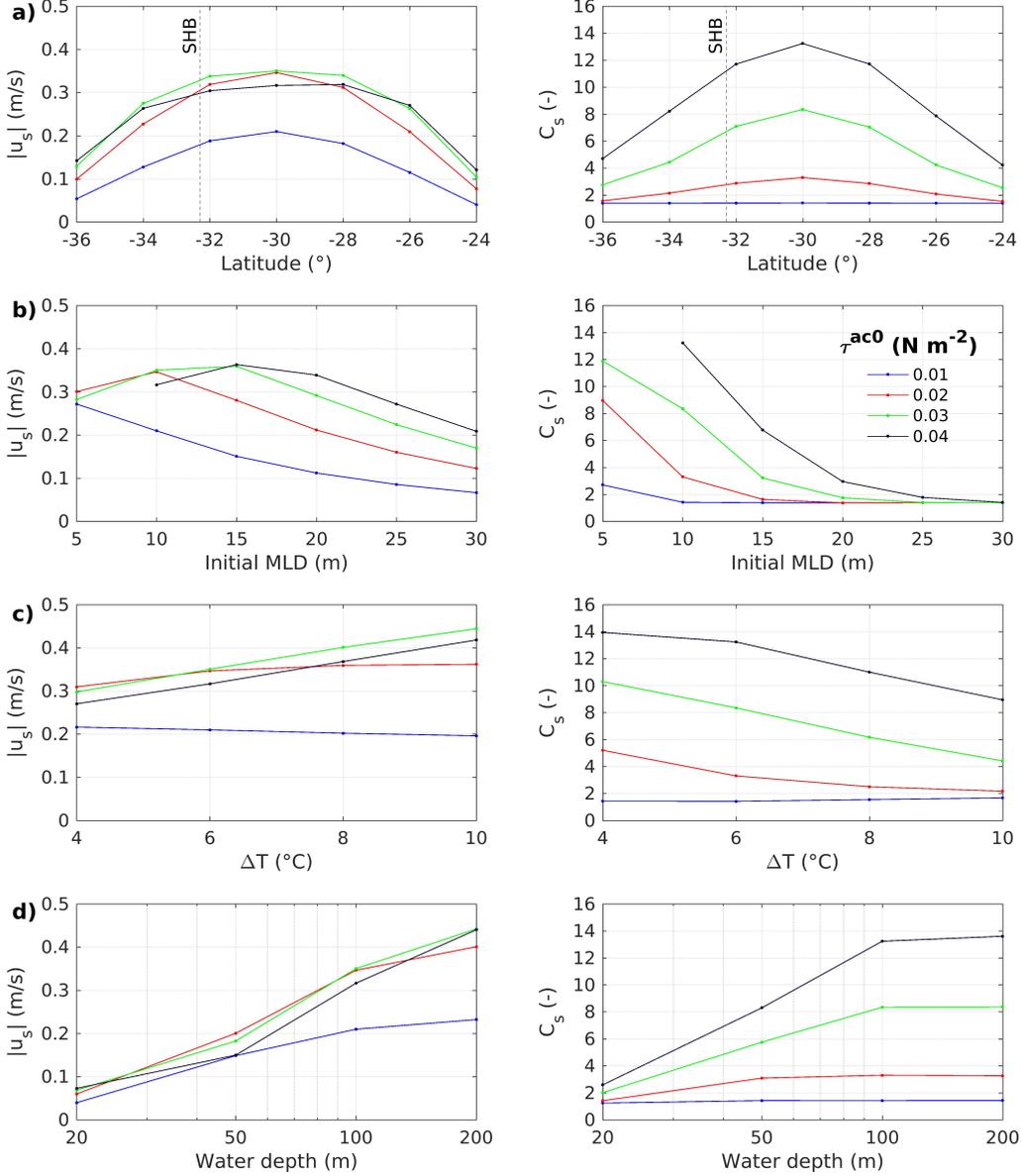
584 amplification of the land-sea breeze over St Helena Bay. The orographic effects of Cape
 585 Columbine and high spatial variability in coastal sea surface temperatures in this region
 586 have been shown to significantly influence the spatial variability of low level winds (Burls
 587 & Reason, 2008), and are likely to be responsible for the shown amplification.

588 3.3 Sensitivity experiments

589 Various sensitivity experiments have been carried out with the analytical model con-
 590 figuration in an attempt to generalise the results of the model (the ‘Craig approximation’
 591 for the cross-shore free surface elevation gradient is included in these experiments). The
 592 baseline configuration employs the input parameters: latitude = 30° S, initial MLD = 10 m,
 593 $\Delta T = 6^\circ$ C and water depth = 100 m. Figure 10 presents the sensitivity of the model to
 594 varying each of these parameters, as quantified through the amplitude of the surface layer
 595 velocity ($|\vec{u}_s|$) and the passive tracer integrated over the surface layer (C_s), both averaged
 596 over the fifth day of each simulation. Results are presented for a range of amplitudes of
 597 diurnal anticlockwise rotating wind stress (τ^{ac0}), being typical of those experienced over St
 598 Helena Bay (Figure 9).

599 Figure 10a indicates a strong dependence of both $|\vec{u}_s|$ and C_s on latitude with the peak
 600 response at the critical latitude of 30° S. The inertial response is shown to drop off within 6°
 601 latitude either side of the critical latitude. The approximate latitude of St Helena Bay (SHB)
 602 is shown for reference, indicating that this site experiences near-peak response to diurnal
 603 forcing. For $\tau^{ac0} = 0.01$ N m⁻² the shear generated by the surface inertial oscillation is not
 604 high enough to trigger diapycnal mixing above background levels. Increasing τ^{ac0} leads to
 605 an increase in $|\vec{u}_s|$ and C_s , however the amplitude of the surface oscillation is limited by
 606 enhanced diapycnal mixing, as dictated by bulk shear production theory used to interpret
 607 the results shown in Section 2.6.

608 The sensitivity of the model to initial MLD and stratification (Figure 10b and 10c) can
 609 be largely understood in terms of the gradient Richardson number, $Ri = N^2/S^2$ which quan-
 610 tifies the balance of stabilising forces due to stratification (N^2) and the destabilising forces
 611 due to vertically sheared flow (S^2). Shallower surface mixed layers lead to higher amplitude
 612 surface currents and therefore enhanced shear. A given stratification can only sustain a
 613 defined shear before Ri is reduced sufficiently to trigger diapycnal mixing. Exaggerated
 614 mixing serves to dampen the amplitude of the surface oscillation as already described in
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589 **Figure 10.** Sensitivity of the analytical model configuration, as quantified through the amplitude
 590 of the surface layer velocity ($|\vec{u}_s|$) and the passive tracer integrated over the surface layer (C_s), both
 591 averaged over the fifth day of each simulation. (a) Sensitivity to latitude. (b) Sensitivity to initial
 592 mixed layer depth (MLD). (c) Sensitivity to stratification (ΔT represents the temperature difference
 593 between surface and subsurface layers). (d) Sensitivity to water depth. The different colour lines
 594 correspond to different wind stress amplitudes.

621 Section 3.1.1. Diapycnal mixing is therefore particularly sensitive to initial MLD, while the
 622 surface current amplitude is modulated and even reduced in cases of exaggerated mixing.
 623 Note that the result for $\tau^{ac0} = 0.04 \text{ N m}^{-2}$ and initial MLD = 5 m is not plotted as excessive
 624 mixing effectively eroded the two layer system to form a homogeneous water column with
 625 temperatures of between 10 and 11° C. The results indicate that event-scale diapycnal mix-
 626 ing reduces to background levels for MLD's greater than ~ 30 m. Elevated stratification has
 627 a dampening effect on diapycnal mixing, while allowing for higher amplitude currents to be
 628 sustained in the surface layer. Surface current amplitude is however insensitive to stratifi-
 629 cation for low wind stress amplitudes which do not drive exaggerated mixing, as the depth
 630 of the surface layer remains largely unchanged over these simulations. The initial MLD
 631 therefore has a primary role in governing the diapycnal mixing response to diurnal-inertial
 632 resonance, while stratification plays a secondary modulating role.

633 Figure 10d shows that shallower water depths lead to significantly reduced surface
 634 current amplitudes and mixing. The formulation for the ‘Craig approximation’ (Equation 6)
 635 dictates that shallower water depths have an amplifying effect on $\frac{\partial \eta}{\partial x}$. As already described in
 636 Section 3.1, this has a dampening effect on both the amplitude of the surface layer oscillation
 637 as well as diapycnal mixing. Simulations run at 20 m water depth are shown to result in
 638 very low amplitude oscillations ($|\vec{u}_s| < 0.1 \text{ m/s}$ for all tested wind stress amplitudes), and
 639 a complete dampening of diapycnal mixing to near-background levels. The C_s results from
 640 Figure 10d at 100 m are very similar to those at 200 m, indicating that the impact of the
 641 land boundary on diapycnal mixing from the locally generated inertial response becomes
 642 negligible for water depth for depths greater than ~ 100 m.

643 4 Discussion and conclusions

644 4.1 Diapycnal mixing dynamics

645 Despite the simplicity of the 1D-vertical model introduced in this paper, the results
 646 of the realistic configuration are in good agreement with nearshore observations over an
 647 upwelling event accompanied by diapycnal mixing in ~ 60 m water depth in the Benguela
 648 system. One of the main limitations of applying 1D models to study diurnal-inertial reso-
 649 nance near a land boundary is the difficulty in reproducing the first baroclinic mode vertical
 650 structure of the currents (Zhang et al., 2010). Here we address this limitation through the
 651 implementation of the ‘Craig approximation’ for first order surface elevation gradient re-

652 sponse, extending the formulation of Simpson et al. (2002) through the inclusion of bottom
653 friction terms. The results of the model have been interpreted using the bulk shear produc-
654 tion theory of Burchard and Rippeth (2009). This work represents the first application of
655 this theory in the context of diurnal-inertial resonance near the critical latitude of 30° N/S.
656 The theory dictates that bulk shear will be produced (and mixing enhanced) when the bulk
657 shear vector is aligned with the surface and bottom shear stresses, weighted by the depth of
658 the two layers, and moderated by interfacial mixing. Near latitudes of 30° N/S, the diurnal
659 anticyclonic rotary component of the wind is always in alignment with the bulk shear vector
660 induced by the presence of inertial oscillations, which provides a constant source of bulk
661 shear production. The effect of the land boundary is to generate a subsurface oscillation
662 with a 180° phase shift with the surface layer, thereby introducing bottom shear stresses
663 in the opposite direction to the surface stresses. The latter has a dampening effect on
664 shear production (Figure 4), which in turn reduces diapycnal mixing. The land boundary
665 effect becomes increasingly important for shallow water depths ($< \sim 100$ m), where bottom
666 friction losses serve to amplify the response of the cross-shore surface elevation gradient,
667 which in turn further dampens the amplitude of the surface inertial oscillations. For depths
668 $< \sim 200$ m, the introduction of bottom friction terms in the formulation of the ‘Craig ap-
669 proximation’ is crucial for achieving realistic currents and mixing in the model through the
670 maintenance of near-zero depth averaged cross-shore transport. Diapycnal mixing is reduced
671 to near-background levels in water depths of ~ 20 m (Figure 10d). In this way, the first order
672 response of the cross-shore surface elevation gradient offers a mechanism for contributing to
673 the well known decrease in near-inertial energy towards the coast (Shearman, 2005; C. Chen
674 & Xie, 1997; Xing et al., 2004).

675 Many previous studies cite the 180° phase shift between surface and subsurface layers,
676 introduced by the land boundary, as a source of shear and mixing. This is seemingly in
677 contrast with our results which suggest that the land boundary has a dampening effect on
678 diapycnal mixing associated with the forced response to the land-sea breeze. It is however
679 important to emphasise that the 1D-vertical model excludes propagating near-inertial first
680 baroclinic mode internal waves. These waves are known to be generated by the inertial
681 pumping of the thermocline due to convergence and divergence of the forced response at
682 the land boundary (Millot & Crépon, 1981; Tintoré et al., 1995; S. Chen et al., 2017; Kelly,
683 2019). The large vertical displacements of the thermocline as seen in the observations (Fig-
684 ure 6) provide evidence for the propagating near-inertial internal wave component in the

685 observations. First baroclinic mode internal waves also introduce a 180° phase shift between
686 surface and subsurface layers, which is an important contributor to diapycnal mixing (Xing
687 et al., 2004; Zhang et al., 2010). Separating the contribution of the internal wave compo-
688 nent from the locally forced response described in this paper is complicated by the similar
689 vertical current structures and frequencies of these processes. The good agreement between
690 observations and the 1D-vertical model however suggests that diapycnal mixing over the
691 considered event was dominated by resonance between the local diurnal wind variability
692 and the locally generated inertial oscillation, while the propagating near-inertial internal
693 wave component was of lower importance. 2D numerical experiments designed to ascertain
694 the diapycnal mixing contribution of near-inertial internal waves set up by diurnal-inertial
695 resonance at a land boundary is a topic of ongoing investigation.

696 The introduction of a non-zero mean alongshore wind stress serves to introduce ‘shear
697 spikes’ at the diurnal-inertial frequency, coinciding with times where the surface inertial
698 oscillation and Ekman transport are aligned. While ‘shear spikes’ have been found to be
699 important for driving diapycnal mixing and bloom enhancement in shallow stratified seas
700 (Burchard & Rippeth, 2009; Lincoln et al., 2016; Williams et al., 2013), our results suggest
701 that this process plays a secondary role in the integrated nutrient enrichment of the surface
702 layer, when compared with the diurnal-inertial resonance phenomenon (Figure 8). It should
703 however be noted that the timing of the diurnal ‘shear spikes’ in relation to sunlight avail-
704 ability would have consequences for the diurnal variability in phytoplankton growth. Both
705 observations and model results indicate night time nutrient enrichment of the surface layer
706 over the considered event (Figure 7), which would benefit phytoplankton growth during the
707 following day.

708 **4.2 Implications for St Helena Bay and EBUS generally**

709 St Helena Bay is exposed to a pronounced enhancement of the diurnal anticlockwise
710 rotary component of the wind stress (Figure 9), which has been shown to be a reasonable
711 diagnostic for event-scale diapycnal mixing (Figure 8). Sensitivity tests to latitude (Fig-
712 ure 10a) indicate that St Helena Bay ($\sim 32.5^\circ$ S), experiences near-peak inertial response to
713 diurnal forcing. These results alone provide strong evidence for the forcing mechanism of the
714 energetic diurnal-inertial current variability which has been observed in the bay (Fawcett et
715 al., 2008; Lucas et al., 2014).

716 Productivity within St Helena Bay is largely understood in terms of the retentive prop-
717 erties of the bay which allow for the utilisation of upwelled nutrients during wind relax-
718 ation/reversal (G. Pitcher et al., 2010). As such, productivity tends to be highest in late
719 summer when extended relaxation events following active upwelling allow for the forma-
720 tion of shallow stratified surface mixed layers, considered favourable for development of
721 high biomass dinoflagellate blooms (Fawcett et al., 2007; G. C. Pitcher & Weeks, 2006;
722 G. Pitcher et al., 2010). Shallow surface mixed layers have also been shown to be a key
723 determinant for enhanced diapycnal mixing, as moderated by the level of stratification be-
724 tween surface and subsurface layers (Figure 10b and 10c). Although relaxation events are
725 generally associated with a lower amplitude land-sea breeze (Figure 9), even low amplitude
726 diurnal wind variability would serve to moderate the formation of shallow mixed layers
727 through the entrainment of subsurface waters and nutrients. Furthermore, successive events
728 of enhanced diurnal wind variability would act on the inertial currents set up by the previous
729 event, serving to further enhance the ocean response. The results presented in this paper
730 therefore provide further evidence that the land-sea breeze plays a major role in determining
731 the evolution of primary productivity within St Helena Bay through surface layer nutrient
732 enrichment.

733 Given the significant impact of diurnal wind variability on the vertical water column
734 structure, our results indicate that diapycnal mixing may have further implications for the
735 nearshore sub-inertial upwelling/relaxation dynamics of St Helena Bay. Deeper surface
736 mixed layers induced by nearshore mixing would reduce offshore surface Ekman velocities,
737 thereby acting as a retention mechanism within the studied bay, and more generally in the
738 EBUS regions. The modulation of cross-shore pressure gradients due to diapycnal mixing
739 would also affect alongshore geostrophic currents and therefore bay-scale circulation. Ob-
740 servations in the Coastal Southern California Bight indicate that diurnal-inertial resonance
741 can lead to steeper cross-shore isotherms and intensified alongshore flows (Nam & Send,
742 2013). These processes are currently being investigated with a high resolution 3D model of
743 St Helena Bay.

744 Although this work has used St Helena Bay as a case study, the results and impli-
745 cations are transferable to other regions, as all four major EBUS include land-sea breeze
746 forcing near the critical latitude. A dedicated analyses of the diurnal anticlockwise rotary
747 component of the wind stress could highlight other regions where the local inertial response
748 and diapycnal mixing could be enhanced. A general consideration for future studies is the

749 requirement for atmospheric products of sufficient spatial and temporal resolution to cap-
 750 ture the nearshore spatial variability in the land-sea breeze. This can be considerable where
 751 local orographic features and sea surface temperatures may significantly impact nearshore
 752 diurnal wind variability, as highlighted by Figure 9. The inability to resolve the nearshore
 753 features of the land-sea breeze may be a significant shortcoming in large scale models which
 754 aim at simulating productivity in coastal upwelling systems. This study suggests that the
 755 mostly affected regions would be those where the development of shallow surface mixed
 756 layers through retention coincide with the local amplification of the land-sea breeze.

757 Appendix A GLS implementation in CROCO

758 The objective of this section is to describe the current implementation of a Generic
 759 Length Scale (GLS) turbulence scheme in CROCO to determine K_m and K_s in (1). First of
 760 all, as usually done in most implementations, the assumption of a horizontally homogeneous
 761 flow is made and vertical advection is neglected. Following Umlauf and Burchard (2003),
 762 the equations satisfied by the two prognostic variables e (the kinetic energy) and ψ (the
 763 generic length scale) are:

$$764 \quad \frac{\partial e}{\partial t} = \frac{\partial}{\partial z} \left(K_e \frac{\partial e}{\partial z} \right) + P + B - \varepsilon, \quad K_e = K_m / Sc_e, \quad (\text{A1})$$

$$765 \quad \frac{\partial \psi}{\partial t} = \frac{\partial}{\partial z} \left(K_\psi \frac{\partial \psi}{\partial z} \right) + \psi e^{-1} (\beta_1 P + \beta_3^\pm B - \beta_2 \varepsilon), \quad K_\psi = K_m / Sc_\psi, \quad (\text{A2})$$

766 where the β_j ($j=1,3$) are constants to be defined, P represents the turbulent kinetic energy
 767 (TKE) production by vertical shear $P = K_m [(\frac{\partial u}{\partial z})^2 + (\frac{\partial v}{\partial z})^2]$ and B the TKE destruction
 768 by stratification $B = -K_s N^2$ (with N^2 the local Brunt-Väisälä frequency). The dissipation
 769 rate ε is related to the generic length scale ψ following:

$$770 \quad \varepsilon = (c_\mu^0)^{3+p/n} e^{3/2+m/n} \psi^{-1/n}, \quad \psi = (c_\mu^0)^p e^m l^n, \quad l = (c_\mu^0)^3 e^{3/2} \varepsilon^{-1}, \quad (\text{A3})$$

771 with l a mixing length and c_μ^0 a constant (whose value is between 0.526 and 0.555) to
 772 be defined. Depending on the parameter values for the triplet (m, n, p) the GLS scheme
 773 will either correspond to a k - ε , a k - ω or the so-called generic (Umlauf & Burchard, 2003)
 774 turbulence scheme (the so-called k - kl scheme is not implemented in CROCO to simplify the
 775 code and because this scheme does not generally outperform other schemes).

776 Once the quantities e and ψ (hence ε) are known, the turbulent viscosity/diffusivity
 777 are given by:

$$778 \quad K_m = c_\mu \left(\frac{e^2}{\varepsilon} \right) = \frac{c_\mu}{(c_\mu^0)^3} (l\sqrt{e}), \quad K_s = c'_\mu \left(\frac{e^2}{\varepsilon} \right) = \frac{c'_\mu}{(c_\mu^0)^3} (l\sqrt{e}), \quad (\text{A4})$$

788

Table A1. Parameter values corresponding to each particular GLS model.

GLS model	m	n	p	β_1	β_2	β_3^-	β_3^+	Sc_e	Sc_ψ
$k-\omega$	0.5	-1	-1	0.555	0.833	-0.6	1	0.5	0.5
$k-\varepsilon$	1.5	-1	3	1.44	1.92	-0.4	1	1	0.7692
Gen	1	-0.67	2	1	1.22	0.05	1	1.25	0.9345

779

where c_μ and c'_μ are determined through so-called stability functions (see below).

780

Choice of parameter values and stability functions

781

A particular GLS occurrence is defined by the following parameters :

782

- The exponents (m, n, p) in the definition of ε

783

- The Schmidt numbers Sc_e and Sc_ψ

784

- The coefficients β_j ($j=1,3$)

785

- The constant c_μ^0

786

- The stability functions which are generally function of:

787

$$\alpha_M = \left(\frac{e}{\varepsilon}\right)^2 \left[\left(\frac{\partial u}{\partial z}\right)^2 + \left(\frac{\partial v}{\partial z}\right)^2 \right], \quad \alpha_N = \left(\frac{e}{\varepsilon}\right)^2 N^2, \quad (\text{A5})$$

789

where (m, n, p) , Sc_e , Sc_ψ , β_j ($j = 1, 3$) are tied to a particular choice of GLS scheme

790

(see Table A1) while c_μ^0 , c_μ and c'_μ are tied to a particular choice of stability function. The

791

formulation of numerous stability functions can be reconciled when written using the generic

792

form:

793

$$c_\mu = \frac{n_0 + n_1\alpha_N + n_2\alpha_M}{d_0 + d_1\alpha_N + d_2\alpha_M + d_3\alpha_N\alpha_M + d_4\alpha_N^2 + d_5\alpha_M^2}, \quad (\text{A6})$$

794

$$c'_\mu = \frac{n'_0 + n'_1\alpha_N + n'_2\alpha_M}{d_0 + d_1\alpha_N + d_2\alpha_M + d_3\alpha_N\alpha_M + d_4\alpha_N^2 + d_5\alpha_M^2}, \quad (\text{A7})$$

795

where a given choice of stability function will define the parameter values for n_i , d_j , and

796

n'_k . For the present study the so-called CANUTO-A stability function is used.

797

The quantities α_N and α_M in the formulation of c_μ and c'_μ must satisfy some constraints

798

to guarantee the regularity of numerical solutions. In CROCO, the following steps are done:

- 799 1. Apply the Galperin (1988) limitation i.e. $l \leq l_{\text{lim}} = \beta_{\text{galp}} \sqrt{2e/N^2}$ on ψ with $\beta_{\text{galp}} =$
800 0.53. The first step is to use this mixing length l_{lim} to compute $\psi_{\text{min}} = (c_\mu^0)^p e^m (l_{\text{lim}})^n$
801 and to correct ψ to satisfy the constraint $\psi = \max(\psi, \psi_{\text{min}})$ here the max function is
802 used since the exponent n is negative whatever the GLS scheme.
- 803 2. Compute the dissipation rate $\varepsilon = (c_\mu^0)^{3+p/n} e^{3/2+m/n} \psi^{-1/n}$ and correct it $\varepsilon = \max(\varepsilon, \varepsilon_{\text{min}})$
- 804 3. Compute α_N and α_M using (A5), and apply "stability and realisability" constraints
805 following Umlauf and Burchard (2003) (Sec. 4). A first constraint applies on α_N to
806 ensure that $-\partial_{\alpha_N}(c'_\mu/\alpha_N) > 0$ to prevent the occurrence of oscillations in c'_μ . This
807 translates into the following limiter:

$$\alpha_N^{\text{min}} = \frac{-(d_1 + n'_0) + \sqrt{(d_1 + n'_0)^2 - 4d_0(d_4 + n'_1)}}{2(d_4 + n'_1)}, \quad \alpha_N = \min(\max(0.73\alpha_N^{\text{min}}, 10^{10}), 10^{10}),$$

(A8)

809 where the coefficient 0.73 is used to ensure the so-called realisability and has been
810 empirically computed thanks to Table 3 in Umlauf and Burchard (2003) in order to
811 satisfy their constraint (48). Then an upper limit is applied on α_M to ensure that
812 $\partial_{\alpha_M}(c_\mu \sqrt{\alpha_M}) \geq 0$ which is also a prerequisite for stability reasons:

$$\alpha_M^{\text{max}} = \frac{d_0 n_0 + (d_0 n_1 + d_1 n_0) \alpha_N + (d_1 n_1 + d_4 n_0) \alpha_N^2 + d_4 n_1 \alpha_N^3}{d_2 n_0 + (d_2 n_1 + d_3 n_0) \alpha_N + (d_3 n_1) \alpha_N^2}, \quad \alpha_M = \min(\alpha_M, \alpha_M^{\text{max}}).$$

(A9)

814 Once those quantities are computed, stability functions are evaluated as well as the turbulent
815 viscosity/diffusivity.

816 Surface and bottom boundary conditions

817 In the current version of CROCO, both e and ψ are formulated with Neumann boundary
818 conditions at the top and at the bottom. However the nature of those boundary conditions
819 also requires the determination of bottom and surface values for e and ψ .

- 820 • For turbulent kinetic energy, the "diagnostic" surface and bottom values are given
821 by:

$$e_{\text{sfc}} = (u_\star^s/c_\mu^0)^2, \quad e_{\text{bot}} = (u_\star^b/c_\mu^0)^2,$$

(A10)

823 and simple homogeneous Neumann boundary conditions are applied:

$$K_e \frac{\partial}{\partial z} e|_{\text{sfc}} = 0, \quad K_e \frac{\partial}{\partial z} e|_{\text{bot}} = 0.$$

(A11)

825 In practice, due to the placement of e and ψ on the computational grid, the Neumann
826 boundary condition is not applied strictly at the surface (resp. at the bottom) but at

827 $z = z_N$ (resp. $z = z_1$) whereas the surface (resp. bottom) is located at $z = z_{N+1/2}$
 828 (resp. $z = z_{1/2}$) with N the number of vertical levels (i.e. the number of cells in the
 829 vertical).

830

831

832 • For the generic length scale, a roughness is defined as:

$$833 \quad z_{0,s} = \max \left\{ 10^{-2} \text{ m}, \frac{C_{\text{ch}}}{g} (u_{\text{x}}^s)^2 \right\}, \quad C_{\text{ch}} = 1400, \quad (\text{A12})$$

834 at the surface and:

$$835 \quad z_{0,b} = \max \{ 10^{-4} \text{ m}, \text{Zob} \}, \quad (\text{A13})$$

836 at the bottom with Zob a user defined roughness length. Again, the boundary con-
 837 ditions are applied at the center of the shallowest and deepest grid cells and not at
 838 their interfaces which means that the relevant length scales are:

$$839 \quad L_{\text{sfc}} = \kappa \left(\frac{\Delta z_N}{2} + z_{0,s} \right), \quad L_{\text{bot}} = \kappa \left(\frac{\Delta z_1}{2} + z_{0,b} \right), \quad (\text{A14})$$

840 with κ the von Kármán constant. Moreover TKE values are interpolated at $z = z_N$
 841 and $z = z_1$:

$$842 \quad \tilde{e}_{\text{sfc}} = \frac{1}{2} (e_{\text{sfc}} + e_{N-1/2}), \quad \tilde{e}_{\text{bot}} = \frac{1}{2} (e_{\text{bot}} + e_{3/2}), \quad (\text{A15})$$

843 where e_{sfc} and e_{bot} are the diagnostic values given above. The "diagnostic" surface
 844 and bottom values for ψ are thus given by:

$$845 \quad \psi_{\text{sfc}} = (c_{\mu}^0)^p (L_{\text{sfc}})^n (\tilde{e}_{\text{sfc}})^m, \quad \psi_{\text{bot}} = (c_{\mu}^0)^p (L_{\text{bot}})^n (\tilde{e}_{\text{bot}})^m. \quad (\text{A16})$$

846 The surface and bottom fluxes are then defined as:

$$847 \quad \mathcal{F}_{\psi}^{\text{sfc}} = K_{\psi} \partial_z \psi|_{\text{sfc}} = -n (c_{\mu}^0)^{p+1} \frac{\kappa}{\text{Sc}_{\psi}} (\tilde{e}_{\text{sfc}})^{m+1/2} (L_{\text{sfc}})^n, \quad (\text{A17})$$

$$848 \quad \mathcal{F}_{\psi}^{\text{bot}} = K_{\psi} \partial_z \psi|_{\text{bot}} = -n (c_{\mu}^0)^{p+1} \frac{\kappa}{\text{Sc}_{\psi}} (\tilde{e}_{\text{bot}})^{m+1/2} (L_{\text{bot}})^n, \quad (\text{A18})$$

849 which correspond to the Neumann boundary conditions applied in the code.

850 **Acknowledgments**

851 The financial assistance of the South African Environmental Observation Network (SAEON)
 852 towards this research is acknowledged. Opinions expressed and conclusions arrived at are
 853 those of the author(s) and are not necessarily to be attributed to SAEON. Giles Fearon
 854 further acknowledges grants from LabexMER and the French Embassy in South Africa

855 which greatly facilitated this research. We thank the Climate Systems Analysis Group
856 (CSAG) for the provision of their WRF atmospheric model output and the South African
857 Navy Hydrographic Office (SANHO) for the provision of bathymetric data. The study
858 benefitted from computational facilities provided by the University of Cape Town's ICTS
859 High Performance Computing team: hpc.uct.ac.za.

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