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Machine learning into metaheuristics: A survey and taxonomy of data-driven metaheuristics

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During the last years, research in applying machine learning (ML) to design efficient, effective and robust metaheuristics became increasingly popular. Many of those data driven metaheuristics have generated high quality results and represent state-of-the-art optimization algorithms. Although various appproaches have been proposed, there is a lack of a comprehensive survey and taxonomy on this research topic. In this paper we will investigate different opportunities for using ML into metaheuristics. We define uniformly the various ways synergies which might be achieved. A detailed taxonomy is proposed according to the concerned search component: target optimization problem, low-level and high-level components of metaheuristics. Our goal is also to motivate researchers in optimization to include ideas from ML into metaheuristics. We identify some open research issues in this topic which needs further in-depth investigations.

CCS Concepts: • Computing methodologies → Search methodologies.

Additional Key Words and Phrases: Metaheuristics, Machine learning, Optimization, Data-driven metaheuristics

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1 INTRODUCTION

In the last decades, metaheuristics have shown their efficiency in solving various complex optimization problems in science and industry [195]. In general, metaheuristics do not use explicit knowledge discovered during the search using advanced machine learning (ML) models. Metaheuristics generate a lot of data in the search process. The data can be *static* when it concerns the target problem and instance features to solve. Moreover several *dynamic* data are generated during the iterative search process: solutions in the decision and the objective spaces, sequence of solutions or trajectories, successive populations of solutions, moves, recombinations, local optima, elite solutions, bad solutions, etc. Thus ML can be helpful in analyzing these data to extract useful knowledge. This knowledge will guide and enhance the search performance of metaheuristics and make them "smarter" and "well informed". Data-driven metaheuristics have been proven to be advantageous in both convergence speed, solution quality and robustness.

In this paper, a survey of data-driven metaheuristics to solve difficult optimization problems is presented. A taxonomy is also proposed in an attempt to provide a common terminology and classification mechanisms. The goal of the general taxonomy given here is to provide a framework to allow comparison of data-driven metaheuristics in a qualitative way. In addition, it is hoped

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that the categories and their relationships to each other have been chosen carefully enough to indicate areas requiring research efforts as well as to help classify future work. We distinguish three hierarchical ways to use ML in metaheuristics (Fig.1):

- **Problem-level data-driven metaheuristics:** ML can help in modeling the optimization problem to solve (e.g. objective function, constraints). It can also assist landscape analysis and the decomposition of the problem.
- Low-level data-driven metaheuristics: a metaheuristic is composed of different search components. ML can drive any search component such as the initialization of solution(s), and the search variation operators (e.g. neighborhoods in local search, mutation and crossover in evolutionary algorithms). It may also be used to tune the various parameters of a metaheuristic.
- High-level data-driven metaheuristics: this class of data-driven metaheuristics concerns
 the selection and generation of metaheuristics, and the design of hybrid and parallel cooperative metaheuristics.

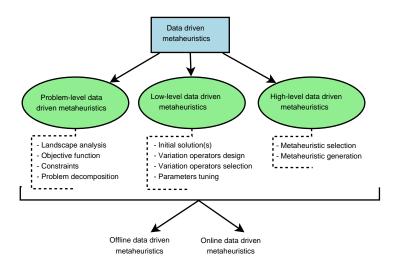


Fig. 1. A general taxonomy of data-driven metaheuristics.

Other flat criteria are used in the taxonomy such as the learning time. In *offline* data-driven metaheuristics, the ML process occurs a priori before starting to solve the problem. In *online* data driven-metaheuristics, ML gather knowledge during the search while solving the problem.

The synergy between ML and optimization has received increasing attention. Most of the related works basically focus on the use of optimization algorithms in solving ML problems [24][192][126][42][51]. Indeed most of the ML problems can be formulated as optimization problems. In the last decade there was a considerable interest in the use of ML into optimization. Very few papers investigate the role of ML into exact optimization algorithms (e.g. branch and bound, dynamic programming), constraint programming, and mathematical programming [20]. To our knowledge there is no comprehensive survey which identifies in a unified way how ML can help the design of metaheuristics. In some outdated surveys [100][42][234], the authors enumerate some data-driven metaheuristics. In [33] the authors focus on dynamic combinatorial optimization problems. In [196], we have proposed a taxonomy of hybrid metaheuristics, in which the combination of metaheuristics with mathematical programming, constraint programming and ML has been addressed. In this

 paper a more complete and general taxonomy of data-driven metaheuristics is proposed. More than 125 references have been analyzed according to our taxonomy. The unified taxonomy is kept as small as possible by proceeding in a hierarchical way as long as possible; then a flat classification is presented according to other criteria.

The paper is structured as follows. In section 2, the main concepts of metaheuristics and ML are detailed in a general and unified way. Section 3 focuses on problem-level data-driven metaheuristics. In section 4, low-level data-driven metaheuristics are presented, while in section 5 we describe high-level data-driven metaheuristics. Finally, the last section presents the main conclusions and identifies some research perspectives.

2 MAIN CONCEPTS

This section presents in a unified way the main concepts used for metaheuristics and machine learning.

2.1 Metaheuristics

An optimization problem consists in searching the optimal solution(s) x^* from a set of solutions X which maximize (or minimize) an *objective function* f(x) while satisfying a set of *constraints*. Metaheuristics represent a class of general-purpose heuristic algorithms that can be applied to any optimization problem. Unlike exact methods, metaheuristics allow to tackle large scale problems by delivering satisfactory solutions in a reasonable time. There is no guarantee to find global optimal solutions or even bounded solutions. Metaheuristics have received more and more popularity in the past 30 years. Indeed, their use in many applications shows their efficiency and effectiveness to solve large and complex problems.

In the design of a metaheuristic, two contradictory criteria must be taken into account: *exploration* of the search space (*diversification*), and *exploitation* of the best solutions found (*intensification*). Promising regions are determined through the "good" solutions obtained. In intensification, the promising regions are explored more throughly with the hope to find better solutions. In diversification, non explored regions must be visited to be sure that all regions of the search space are evenly explored and that the search is not only confined to a reduced number of regions.

2.1.1 Single-solution based metaheuristics. Single-solution based metaheuristics (S-metaheuristics) improve a single solution. They could be seen as "walks" through neighborhoods or search trajectories through the search space of the target problem [195]. S-metaheuristics iteratively apply the generation and replacement procedures from the current solution. In the generation phase, a set of candidate solutions are generated from the current solution s. This set C(s) is generally obtained by local transformations of the solution. In the replacement phase¹, a selection is performed from the candidate solution set C(s) to replace the current solution, i.e. a solution $s' \in C(s)$ is selected to be the new solution. This process iterates until a defined stopping criteria. The generation and the replacement phases may be memoryless. In this case, the two procedures are based only on the current solution. Otherwise, some history of the search stored in a memory can be used in the generation of the candidate list of solutions and the selection of the new solution. Popular examples of such S-metaheuristics are local search, simulated annealing and tabu search. Algorithm1 illustrates the high-level template of this family of metaheuristics. Their common search concepts are the definition of the neighborhood structure and the generation of the initial solution.

¹Also named transition rule, pivoting rule and selection strategy.

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Algorithm 1: High-level template of single-solution based metaheuristics

```
s = s_0; /* Generation of the initial solution */
t = 0;

Repeat
    /* Generate candidate solutions from s_t */
    Generate(C(s_t));
    /* Select a solution from C(s_t) to replace the current solution s_t */
    s_{t+1} = \text{Select}(C(s_t));
    t = t+1;

Until Stopping criteria satisfied

Output: Best solution found.
```

2.1.2 Population based metaheuristics. Population based metaheuristics (P-metaheuristics) could be viewed as an iterative improvement of a population of solutions. P-metaheuristics start from an initial population of solutions². Then, they iteratively apply the generation of a new population and the replacement of the current population. In the generation phase, a new population of solutions is created. In the replacement phase, a selection is carried out from the current and the new populations. This process iterates until a given stopping criteria. Popular examples of P-metaheuristics are evolutionary algorithms, ant colony optimization, scatter search, differential evolution, particle swarm optimization, bee colony and artificial immune systems. Algorithm 2 illustrates the high-level template of P-metaheuristics.

Algorithm 2: High-level template of P-metaheuristics

```
P = P_0; /* Generation of the initial population */
t = 0;

Repeat

Generate(P_t'); /* Generation a new population */
P_{t+1} = \text{Replace-Population}(P_t \cup P_t'); /* Select new population */
t = t+1;

Until Stopping criteria satisfied

Output: Best solution(s) found.
```

P-metaheuristics may be classified into two main categories:

- Evolutionary-based: in this category of P-metaheuristics, the solutions composing the population are selected and reproduced using variation operators (e.g. mutation, recombination³) acting *directly* on their representations. A new solution is constructed from the different attributes of solutions belonging to the current population. Evolutionary algorithms (EAs) and scatter search (SS) represent well-known examples of this class of P-metaheuristics.
- **Blackboard-based**⁴: It is based on the idea that the solutions of the population participate in the construction of a shared memory. This shared memory will be the main input in generating the new population of solutions. Ant colonies and estimation of distribution algorithms (EDA) belong to this class of P-metaheuristics. For the former, the shared memory

²Some P-metaheuristics such as ant colony optimization start from partial or empty solutions.

³Also called crossover and merge.

⁴A blackboard system is an artificial intelligence application based on the blackboard architectural model, where a shared knowledge, the "blackboard", is iteratively updated by a diverse group of agents [61].

is represented by the pheromone matrix while, in the latter strategy, it is represented by a probabilistic learning model. For instance, in ant colonies, the generated solutions by past ants will affect the generation of future ants via the pheromones. Then, the generated solutions participate in updating the pheromones.

2.2 Machine learning

ML is one of the most salient research domain in artificial intelligence. ML has experienced an important development in the last decade and has become a powerful analysis tool in a wide range of applications related to big data. ML is the science of extracting useful and hidden patterns from a training dataset considered composed of multiple examples. Various ML tasks can be used depending on the desired outcome of the model. Usually a distinction is made between supervised, semi-supervised and unsupervised learning. The most common ML tasks used in this paper are (Fig. 2):

- Regression and classification: this is a supervised ML task in which we predict a predefined category or class from a given set of attributes (continuous variables for regression and discrete variables for classification) [8]. The following ML techniques are generally used for solving this family of problems: Gaussian process, linear regression, K-nearest neighbors, artificial neural networks (ANN), support vector machine (SVM), random forests, decision trees, logistic regression, naive Bayes and deep learning.
- Clustering: this unsupervised ML task partitions the input data set into subsets (clusters), so that data in each subset share common aspects [64]. The partitioning is often indicated by a similarity measure defined by a distance. The main used techniques for clustering are: hierarchical clustering, partitioning methods (e.g K-means, K-medoids, Mean-Shift), grid based clustering (e.g. CLIQUE, Sting, Wave Cluster), model based clustering (e.g. EM, COBWEB) and density based methods (e.g. DBSCAN, Optics, Denclue).
- Association rules: association rule mining is a procedure which is meant to find frequent
 patterns, correlations, associations or causal structures from datasets found in various kinds
 of databases [67]. One of the most efficient used methods are Apriori, FP-growth and Eclat.
 Many measures of interestingness for rules have been proposed such as support, confidence,
 conviction, leverage, and lift (i.e. interest).
- Feature selection: the *feature selection* task consists in reducing the number of attributes (i.e. dimensionality of the dataset) [37]. It is an important task because selecting significant features would help to build simpler models of better accuracy and can reduce overfitting. The traditional techniques used for feature selection are: filter methods (e.g. Pearson's correlation, linear discriminant analysis (LDA), analysis of variance ANOVA, chi-square tests), wrapper methods (e.g. forward selection, backward selection, recursive feature elimination), and embedded methods (e.g. mRMR, Greedy).
- Reinforcement learning: reinforcement learning (RL) aims to learn optimal actions from a finite set of available actions through continuously interacting with an unknown environment [194]. The main components are: states, set of actions and rewards. From the current state, a RL agent takes an action, changes to a new state and receives a reward. The reward determines the quality of the carried action. RL is also referred to as approximate dynamic programming [155]. The goal of the agent is to maximize the accumulation of rewards over time. The main approaches for RL can be classified as follows:
 - Model-free: the optimal control policy is learned without first learning an explicit model.
 Such schemes include: policy search (e.g. metaheuristics, policy gradient) and value-function based, related to dynamic programming principles (e.g. temporal fifference (TD) learning,

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Q-learning [216], SARSA (State-Action-Reward-State-Action), DQN (Deep Q Network), DDPG (Deep Deterministic Policy Gradient, MCTS (Monte Carlo Tree Search)).

- Model-based: conversely model-based algorithm uses a reduced number of interactions with the real environment during the learning phase. Its aim is to construct a model based on these interactions, and then use this model to simulate further episodes, not in the real environment but by applying them to the constructed model and get the results from it.

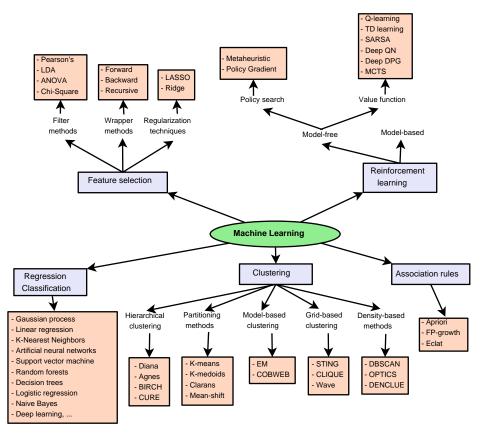


Fig. 2. Main machine learning tasks and associated methods.

3 PROBLEM-LEVEL DATA-DRIVEN METAHEURISTICS

In this class of data-driven metaheuristics, ML techniques are carried out on the optimization problem at hand. Knowledge is obtained by the analysis of the landscape of the problem using selected features. Moreover, the problem model can be reformulated (e.g. objective function, constraints) or decomposed for a more efficient and effective solving.

3.1 Landscape analysis

Exploratory landscape analysis represent a number of techniques used to extract knowledge on the characteristics of a given optimization problem. The main questions for this scientific challenge are:

- Which features? high-level features specified by human experts such as the level of multimodality or separability have been introduced to reflect the problem characteristics [16]. Other properties based on expert knowledge can be used such as: global basin structure, variable scaling, search space homogeneity, basin size homogeneity, global to local optima contrast, and size of plateaus. Low-level features are automatically and numerically computed to characterize the landscape of a given problem. The features can be grouped into five classes related to: the characteristics of the distribution of the objective function values (y-Distribution), the relative position of each objective value compared to the median of all values (Levelset), meta-modeling of the initial data set (Meta-Model), the estimated degree of convexity of the function (Convexity) as well as the assessment of multimodality by local searches starting from the initial design points (Local Search) [127].
- Which goal? those features are important for the design of efficient metaheuristics and understanding the behavior of the algorithms. This knowledge can be used for the selection of the best suited metaheuristic to solve a given problem by predicting the characteristics of the input instance [221][23]. It can also be used to tune the parameters of an algorithm [14], predict its runtime for solving a given benchmark instance [90], and generating hard benchmark instances [116].
- Which ML methods? many ML methods have been investigated to extract those features such as: Bayesian networks [151], support vector regression [23], random forest [90], Gaussian process [90], neural networks [189], regression trees [14], and ridge regression [221].

3.2 Data-driven objective function

Two different goals govern the use of ML in the objective function (Fig. 3):

- **Improving the convergence**: ML can help to transform the objective functions in order to better guide the metaheuristic through the search space. Those learnable objective functions include some knowledge extracted from the problem.
- Reducing the computational cost: it consists in approximating the objective function. The
 approximation is evaluated much faster than the original function for expensive optimization
 problems.
- 3.2.1 Learnable objective function. The main issue in this family of methods is to generate automatically improved objective functions from exploiting some knowledge of the target optimization problem and features extracted from states visited during the search process. Those learnable objective functions can help guiding the search to improve solutions. For instance, this is an important issue for problems characterized by multimodality and neutrality. A representative of such an approach is Guided Local Search (GLS) which modifies the objective function when trapped on a local optima. The augmented objective function of the problem include a set of penalty terms [210]. Whenever the S-metaheuristic gets caught in a local optima, the penalties are modified and search is iterated to minimize the transformed objective function. The penalty gives the degree up to which the solution features is constrained.

Some approaches to construct learnable objective functions using reinforcement learning have been proposed. In [25], some features characterizing good solutions are defined for the given problem. The objective function is predicted by analyzing search trajectories of local search methods. A $TD(\lambda)$ family of temporal-difference reinforcement learning algorithms is used. The learned evaluation function is then used to bias future search trajectories toward better solutions on the same problem. Transfer learning has also been used to transfer previously learned evaluation functions to new, similar optimization problems [66]. In [101], an inverse reinforcement learning

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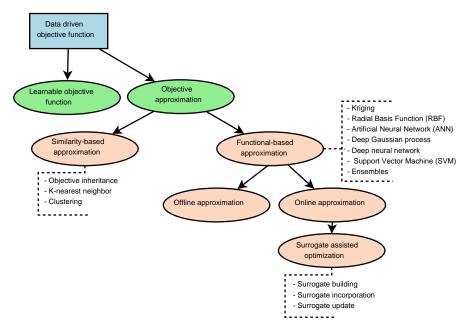


Fig. 3. Data-driven objective function.

(IRL) approach is proposed to learn the objective function in robotic problems. The main idea is to predict a suitable objective function given observations of optimal behavior. In many robotics problems, it is significantly easier to provide demonstrations of optimal behavior than it is to design an objective function that defines the required behavior. IRL is used to learn the observed behavior using features of solutions selected by L_1 regularization.

3.2.2 Objective approximation. Many optimization problems (e.g. engineering design) are concerned by extremely expensive objective functions. Those problems are generally characterized by black-box objective functions whose algebraic definitions are unknown (e.g. simulation based optimization). However, metaheuristics need to carry out a huge number of function evaluation in order to find good solutions. For such expensive optimization problems, the approximation of the objective function is an interesting alternative for designing efficient data-driven metaheuristics.

ML approaches can be used to build approximate models of the objective function [94]. In this context, previously evaluated solutions are learned by a ML approach to approximate the objective function of new generated solutions. The main issue here is to obtain a "good" approximation in terms of maximizing its quality and minimizing its computing time. Many questions arise in the design of this scheme such as: which proportion of the visited solutions are evaluated using the approximation, and at what time or in which component of the search algorithm the approximation is used. Objective approximation methods can be classified into two families (Fig.3):

• **Similarity-based approximation**: can be seen as Lazy learners or memory based learners. The most popular similarity-based approximation are objective inheritance, K-nearest neighbor, and clustering techniques. Objective inheritance methods⁵ are popular in P-metaheuristics.

⁵This scheme is also called fitness imitation or fitness inheritance.

In [188], the objective value of a new solution is computed as a linear weighted combination of the parents, in which the weights depend on similarity with the parents. In [29], a resampling technique is combined with an average combination to solve noisy problems. Other objective inheritance methods based on conditional probabilities tables and decision trees are proposed in [149]. In the k-nearest neighbors method, the objective value of a given solution is computed according to the k-nearest neighbors with known exact values [233]. Similarity-based approximation can also be carried out by clustering algorithms. A clustering algorithm is applied on a population of solutions to be evaluated. Each cluster will have a representative solution. Only the solution that represents the cluster is evaluated [162][106][97][226]. Then, the objective function of other solutions of the cluster is estimated with respect to its associated representative. Different clustering techniques may be used such as K-means and fuzzy C-means.

• Functional-based approximation: it consists in a new model of the objective function being built. The model construction strategy is based on previous data obtained from the original objective functions. Many ML algorithms have been investigated [94][13]: Polynomial models (i.e. Response Surface) [74], Radial Basis Functions (RBF), Kriging (i.e. Gaussian process) [28][107], Support Vector Machines (SVM) [186], Artificial Neural Networks (ANNs) [86][193][70][83]. A recent approach consists to use an ensemble of surrogates in order to improve the performance of the approximation [73]. Multiple criteria have to be used to compare the various models: number of samples provided to build the model, number of parameters of the model, quality of the approximation, cost of the model building, and cost of the model inference. In offline approximation, the model is built before the search starts, whereas in online approximation (i.e. surrogate assisted), the model is constructed and improved during the search.

Some hybrid approaches combining similarity-based and functional-based approximations have been proposed. An example of such a hybrid approache is a clustering approach applied in EAs in which we split the population into several clusters and then construct an approximate model for each cluster. Multiple approximate models are expected to use more local information about the search space and fit the original objective function better than a single global model [36][150][221].

3.2.3 Surrogate-assisted metaheuristics. Surrogate-assisted optimization⁶ is a popular approach to deal with the optimization of expensive problems [198]. These algorithms are iterative sampling procedures relying on surrogate models (i.e. metamodels) of the considered objective and constraint functions which are generally characterized by a negligible computational cost, in order to iteratively determine and explore the most promising locations of the design space, thus simultaneously refining the surrogate model and converging towards the problem optimum [95].

The main questions in designing surrogate-based metaheuristics are:

- Surrogate building: which ML approach is used to build the surrogate? Different approaches are used in the literature: Random Forest, Polynomial models, Gaussian Process [237], Neural Networks [211], radial basis functions [165], deep Gaussian processes [81], deep neural networks. A recent trend is to use multiple surrogates (i.e. ensembles of metamodels) to improve the accuracy of the surrogates [65].
- **Surrogate incorporation**: which solutions should be selected to be evaluated using the real objective function or the surrogate? *Evolution Control* uses jointly surrogates and original objective functions in a metaheuristic. The original objective functions are used to evaluate

⁶Also known as Bayesian Optimization

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some/all solutions in some/all iterations, in a fixed or adaptive way [39]. In *direct approximation*, the approximated objective function replaces the original one in the whole search process [188][177]. In the *indirect approximation*, the metaheuristic use the approximation in some search operators (e.g. neighborhood, population initialization, crossover, mutation) [161][92].

• Surrogate update: When and how the surrogate is updated? the surrogate can be updated in a fixed (e.g. each iteration, given number of iterations) or an adaptive way (e.g. improvement of solutions). Different *infill criteria* have been used for updating the surrogate: lower confidence bound (LCB), upper confidence bound (UCB), probability of improvement, expected improvement (EI) [230]. They are based on a tradeoff between exploration, by searching where predicted variance is high and exploitation by searching where expected value is minimized.

One of the most popular Bayesian Optimization algorithms is the "Efficient Global Optimization" (EGO) algorithm [98]. It is based on Gaussian Process (GP) regression (also called Kriging). First, a set of solutions are generated using Design of Experiments (DoE). Then, it consists in sampling iteratively, using the prediction and uncertainty by the Gaussian model, the most promising solution based on an *infill sampling criterion*. This point is evaluated using the real objective function and the surrogate is updated using the new training set, and a new solution is sampled, and so on, until a given stopping criterion is satisfied (Fig.4).

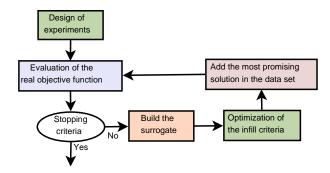


Fig. 4. The EGO Bayesian optimization algorithm.

3.3 Constraint handling

For a given problem, there are usually domain specific constraints that can be exploited to construct efficient metaheuristics. The most popular constraint handling procedures in metaheuristics are the penalization and the repairing procedures. Different data-driven constraint handling approaches exist (Fig.5):

• Constraint approximation: the approximation strategies detailed in the previous section for the objective functions may also applied to constraints. Surrogates for constraints have been applied to problems with expensive black-box constraints [164][132]. Various ML models have been investigated such as: ANN [96], Kriging [206], RBF [166], and SVM [120]. Different infill sampling criteria are used to deal with constrained global optimization problems (e.g. expected improvement with Probability of Feasibility (PoF) [217], Expected Violation (EV), Mean Constraint (MC)) [156]. The infill criteria aims to balance between exploitation and exploration of the objective and all the constraint approximations [145].

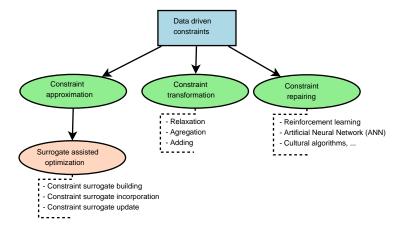


Fig. 5. Data-driven constraints.

- Constraint transformation: in penalization strategies, adaptive strategies have been used for switching from lower complexity surrogates to higher complexity models (e.g. SVM [184]). For problems with many constraints, the search process will be very sensitive to accuracy of the surrogates which are built on the agregation of objective function and constraints. Hence, techniques that aggregate constraint's surrogates to one or a few have been proposed [235]. Dealing with constraints for many real-world problems requires incorporating domain knowledge into optimization algorithms. In the ART (Adaptive Reasoning Technique), a search memory is used to learn the behavior of a greedy algorithm [146]. Some constraints are added to the problem. Those constraints are generated from the non interesting visited solutions according to the values associated to their decision variables. Similar to the tabu list strategy in tabu search, those constraints are deleted after a given number of iterations. In [136], the authors use constraints to incorporate domain knowledge into Bayesian networks. They have formally proved that adding constraints reduces variance and improves generalization for machine learning problems.
- Constraint repairing: some ML approaches have been used to design repairing procedures for constraint handling. In [236], *Reinforcement Learning TD*(Λ) method and *artificial neural networks* are applied to design efficient repairing procedures for scheduling problems. In *cultural algorithms*, adaptive knowledge represented by belief cells (i.e. intervals) is used to avoid infeasible regions and for promoting the exploration of feasible regions [93]. Different constraint handling techniques can be effective during different steps of the search process. ML could also be applied to the online selection of the best constraint handling technique.

3.4 Problem decomposition

ML approaches can be used in breaking large scale optimization problems into smaller subproblems. Those subproblems are then solved more efficiently by metaheuristics. Problem decomposition approaches can be carried out in both hierarchical and flat ways. *Hierarchical decomposition* is used when the problem can be successively refined. *Flat decomposition* generates separate subproblems that can be solve in a parallel way. Three types of decomposition strategies may be carried out:

• Data space decomposition: partitioning of data input space can be applied to decompose the input space into subspaces. Metaheuristics are then used to solve simpler subproblems associated each partition. Then, a global solution is built using partial final solutions. For

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instance, in geographical problems such as vehicle routing [167][62][140] and covering [49], clustering techniques exploiting the spatial properties can be applied to structure the set of input nodes. Different clustering algorithms using geographical proximity have been used such as K-means [72][68], density based clustering [62], and ANNs [154]. This approach has been also applied to other families of problems such as scheduling [118][17], in which clustering of jobs is carried out [3].

In stochastic and robust optimization, the clustering approach can also be applied for the set of input scenario [44][182]. In [119], a hierarchical clustering approach is proposed to select representative scenario clusters for a robust optimization in order to avoid redundant simulations and improve robustness in uncertain environments. In [44], clustering has been used to enhance a progressive hedging-based metaheuristic for a network design problem that models demand uncertainty with scenario. The metaheuristic solves successive multi-scenario subproblems associated to different clusters of scenario.

- Decision space decomposition: in this problem decomposition approach, the set of decision
 variables is divided into several subsets in order to remove the inter-relationship between
 subsets. The subproblems are assumed to be independent or loosely coupled. A popular
 decomposition technique is time-based decomposition in which the time horizon is used as a
 splitting criterion [110].
 - ML can also be used to fix some variables to certain values and then solve the reduced associated subproblem. The fixed variables are selected using some knowledge (e.g. elite solutions, interdependance between variables). For instance, this approach is used in *coevolutionary algorithms* for global optimization problems [123][85], and *Benders decomposition* for mixed optimization problems (MIP) [207].
- **Objective space decomposition:** in multi-objective optimization problems, reducing the number of objective is an important issue for the search efficiency. Indeed, the difficulties in solving many-objective optimization problems are the inefficiency of dominance relations, important computational cost and complexity in visualization of the objective space. Reducing the number of objectives using ML approaches represents a popular approach to handle this difficulty: *offline reduction* using *Principle Component Analysis (PCA)* [178] or *online reduction* based on the clustering of the Pareto front [27][142]. In [27], an unsupervised clustering algorithm is applied in the objective space at different iterations of the metaheuristic. For each cluster, only representative objectives are selected to guide the search during next iterations.

4 ML IN LOW-LEVEL COMPONENTS OF METAHEURISTICS

Although the effectiveness of metaheuristics has been demonstrated in solving difficult and large-size optimization problems in various areas, the design of the appropriate setting usually requires a deep expert knowledge in order to obtain competitive results. Here, ML can be used to find good designs for various search components or parameters of metaheuristics such as the initial solutions(s), neighborhoods, variation operators, stopping criteria and various parameters associated.

4.1 Initial solution(s)

 The most commonly used method in the generation of initial solution(s) is randomness. In general, a population of random solutions is characterized by a bad quality and do not even ensure a good diversification in the search space. ML-assisted initialization techniques can improve the solution quality, reduce the computational costs, and improve the robustness in terms of the variation of the solutions found [102]. Hence, ML has been applied in the initialization of solution(s) following different methodologies (Fig.6):

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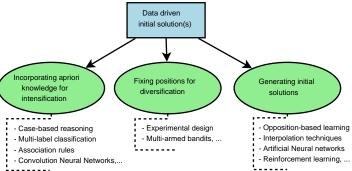


Fig. 6. Data-driven initial solution(s) initialization.

- Incorporating a priori knowledge for intensification: knowledge extracted from previous problems solving can be used to generate solutions which integrate "good" patterns. ML can learn good properties of the obtained solutions and then help to generate good quality initial solutions in promising regions of the search space. The general learning methodology is shown in Figure 7. First, by selecting a set of training instances of the problem and obtaining a set of elite solutions for this set. Then, some features of the elite set of solutions are found using ML models. Finally, the obtained ML model is used to generate initial solutions for a new problem instance. Defining features and similarity metrics for a given problem are the main issues of this methodology. Such approaches have been proposed using case-based reasoning in EAs [121], association rules and attribute-oriented induction in P-metaheuristics [134], multi-label classification using decision trees [117], logistic regression [80][180] and neural networks [157] in S-metaheuristics. Recently, some deep architectures for neural networks have been explored. In [129], Convolution Neural Networks (CNNs) models learn the optimal solution for the traveling salesman problem as an image and extract the patterns (i.e. edges) to be included in a solution. This methodology can also be applied in solving similar problems by applying transfer learning approaches. There is an opportunity to exploit the structure of similar problems that have been already solved for which we have a lot of knowledge.
- Fixing positions for diversification: diversification is an important issue in metaheuristics. ML has been applied to improve diversification in P-metaheuristics by using for instance orthogonal experimental design [114], and in iterative S-metaheuristics by using for instance multi-armed bandits (epsilon-greedy Q-learning) [35]. Indeed, the problem of selecting a region to explore can be defined as a multi-armed bandit: a reinforcement learning problem that exemplifies the exploration-exploitation tradeoff dilemma, in which each arm is represented by a region of the search space [208].
- **Generating initial solutions:** ML can also help to generate "good" quality initial solution(s). An example of such approaches are:
 - Opposition-based learning: using a one-to-one mapping function in the decision space, opposition-based learning (OBL) allows to obtain complementary solutions in order to improve the convergence of the search process and the coverage of the search space.

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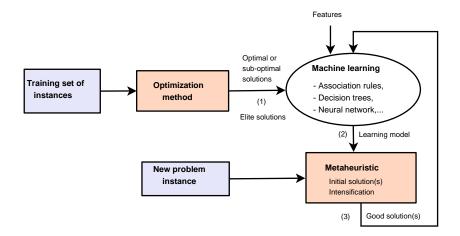


Fig. 7. Extracting knowledge from the history of the search and its use into initial solutions for intensification. (1) Selecting the training problem instances and obtaining the elite solutions (optimal or near-optimal solutions). (2) ML is applied using the elite set of solutions and the selected features of instances. (3) The extracted ML model will be used to generate the initial solutions(s) for solving a new problem instance.

Opposite solutions are generated during the initialization of a population using different types of mapping functions: Type-I opposition, Type-I Quasi-opposition, Type-I Super Opposition, Type-II opposition, Center-based sampling, Generalized OBL, and Quasi-reflection OBL [172]. This methodology has been carried out in Differential Evolution (DE) [5][202][159][214][18], Evolutionary Algorithms [224][53], Harmony Search [183][185], and Particle Swarm Optimization (PSO) [213][212][187][69]. It has also been applied for solving multi-objective optimization problems [113][122] and noisy problems [79].

- Artificial neural networks (ANN): different architectures of ANNs have been investigated to generate good quality solution for optimization problems: Hopfield neural networks (HNN) [223][197][218], Recurrent Neural Networks (RNN) [19][135], Pointer networks [209], Self Organizing Map (SOM) [131][40].
- Interpolation techniques: from a given population of solutions, new solutions can be generated using interpolation techniques such as quadratic interpolation [143][7]. Using a quadratic interpolation of three solutions, a new solution lying at the minimum of the quadratic curve crossing through the three solutions is obtained. It helps to improve the convergence rate of the algorithms.
- Reinforcement learning (RL): RL can be seen as a greedy optimization approach in which a complete solution is constructed by successive addition of decisions [104][103].
 Recently, some deep architectures have been investigated such as Deep RL [125], and Deep Q Network [215].
- Transfer learning: transfer learning has been expoited for the population initialization
 in solving dynamic multi-objective optimization problems [91]. It allows to generate an
 initial population by reusing past experience to speed up the search process.

4.2 Search operators design

 This section deals with the application of ML into the design of search operators: constructive (i.e. greedy) operators, unary operators (e.g. neighborhood in local search, mutation in EAs), binary

operators (e.g. crossover in EAs), indirect operators (e.g. probabilistic models in estimation of distribution algorithms), intensification, and diversification search operators:

- Constructive operators: some metaheuristics such as Ant Colony Optimization and GRASP use greedy operators to generate new solutions. Association rules and clustering (e.g. self-organizing maps) have been used to extract patterns that are incorporated into greedy procedures [170][45]. Reinforcement learning have been integrated into constructive operators, such as Q-learning in ant colony based optimization [54]. This approach is very popular in solving control problems such as mobile robots [75]. Indeed reinforcement learning is a natural framework for sequential learning in greedy procedures. This RL framework has also been applied to many combinatorial optimization problems such as the maximum cut, minimum vertex cover, and traveling salesman [104].
- Unary operators: one of the key issues in designing efficient unary operators is ensuring that they search in the appropriate neighborhood. Two different issues have been addressed using online learning:
 - **Size of the neighborhood:** the size of the neighborhood can be learned online during search; for instance the step size in Evolution strategies (ES) [179].
 - Sampling of the neighborhood: ML models can be extracted from a set of good generated solutions to guide the generation of the candidate neighbors. Other than applying a random or complete generation of the neighborhood, a reduced set of candidate neighbors are generated. This methodology has been applied to many metaheuristics such as EAs [176], and VNS [199]. In [176], probabilistic models are learned from the population in EAs. New solutions are generated by sampling the probabilistic model. In [201] a linkage tree genetic algorithm based on hierarchical clustering is proposed. It allows to identify the problem variables that have a high mutual information in a population of good solutions. In the generation of new solutions, these linked variables determine the neighborhood where the metaheuristic searches for better solutions by sampling values for these problem variables from the current population. This neighborhood learning is guided by the linkage hierarchical clustering found so far during the search.
- **Binary operators:** the knowledge extracted during the search can be incorporated into binary operators such as recombination operators in EAs for the generation of new solutions (Fig. 8). From a set of solutions (e.g. current population, elite solutions), some learning models are extracted, that will participate in:
 - Recombination of solutions: association rules [175], decision trees [99] are some examples of ML approaches that have been applied in the croosover operator in EAs. In [175], an elite set of solutions is maintained by an EA. The frequent itemsets are discovered using the Apriori algorithm of association rules. Then those frequent itemsets will guide the crossover operator by a greedy procedure. In [128], a set of decision rules describing the generated solutions are found, using the *AQ learning algorithm*. The extracted rules are incorporated into the crossover operator.
- Selection of solutions: in general, the selection of solutions to be recombined is based only on their qualities (e.g. roulette or tournament selection). The candidates for crossover can be chosen using some distance measures. Hence, hierarchical clustering has been proposed to select solutions in neighboring clusters [6][144]. Indeed, recombining only neighboring solutions may improve the efficiency of crossover operators.
- Indirect operators: in blackboard-based metaheuristics (e.g. EDA), ML models are used to generate new solutions: probabilistic models [148], Bayesian networks [152], incremental learning [11], dependency trees [12], and Markov random fields [181]. Similarly, *cultural*

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algorithms use good quality solutions to induce beliefs guiding the generation of solutions by evolutionary operators [168]. Cultural evolution allows populations to learn and adapt faster than biological evolution.

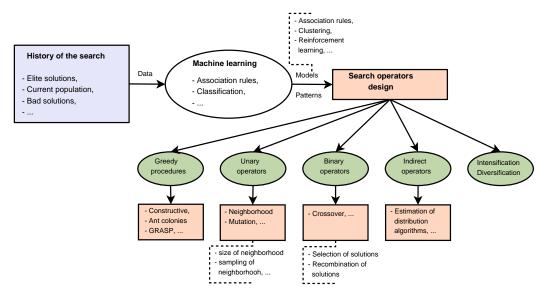


Fig. 8. Extracting knowledge from the search history and its use into search operators.

Other important search operators can be handled by ML:

- Intensification⁷: this approach uses a learning process to guide the underlying metaheuristic toward good regions of the search space. It allows to make deeper search aroud promising regions of the search space. The features of good solutions are extracted using online learning such as clustering [153] and frequent itemsets using association rules [48][169]. Then a deeper search is carried out around solutions characterized by those patterns.
- **Diversification**⁸: this approach uses a learning process to guide the underlying metaheuristic toward unvisited regions of the search space. A learning component keeps track of all visited solutions by storing some informations: spheres in the decision space [153], intervals for decision variables [191], Self-Organizing Maps (SOM) [9], binary space-partitioning (BSP) trees [228]. In order to guide the underlying metaheuristic toward unexplored regions, the learning component generate solutions far away from the visited solutions.
- 4.2.1 Operator selection. In many metaheuristics there exists a lot of alternatives in terms of search operators design: neighborhoods and more generally unary operators such as mutation in EAs, and binary operators such as crossover in EAs. ML can be used for the selection of the best suited search operator. Sequential learning approaches (e.g. reinforcement learning, multi-armed bandit) are well suited for the selection of search operators [56].

Reinforcement learning has been applied to learn the optimal search operator based on the performance of operators. The operator selection problem is formulated as reinforcement learning problem. It is applied to learn optimal policies by maximizing the accumulated rewards. According

⁷i.e. exploitation

⁸i.e. exploration

 to the calculated Q function value of each candidate operator, an optimal operator can be selected to maximize the learned Q reward value. This approach has been used for various unary operators such as mutation [231], and neighborhood selection in VNS (Variable Neighborhood Search) [1][55][109]. VNS integrate a set of different neighborhoods, which are explored in a predefined sequence. ML approaches allows to select the most appropriate neighborhood at a given iteration.

Other sequential learning approaches have been proposed such as *multi-armed bandit* for operator selection in EA [47], and neighborhood selection in VNS [38], and *adaptive pursuit algorithm* [57]. *Ensemble methods* represent alternatives to sequential learning that have been investigated for this task [124].

4.3 Parameter tuning

Many quantitative parameters compose metaheuristics. Quantitative parameters represent numerical values to be initialized such as the probability of application of variation operators (e.g. mutation, crossover) in EAs, the tabu list size in tabu search, and the velocity is particle swarm optimization. The various parameters of metaheuristics have a significant impact on their efficiency [50]. In general, metaheuristics designers tune the parameters by hand, guided by their experience and some rules of thumb. Finding good parameter setting is a tedious and time-consuming task [60].

There are a lot of similarities between the parameter tuning problem and problems faced in ML [21] and Design of Experiments (DoE) [63]. Offline or static parameter tuning addresses the finding of good parameters before the execution of a metaheuristic [89]. Online or dynamic parameter tuning addresses the dynamic change of parameters during the search. A hybridization of both approaches is generally required for finding satisfactory solutions.

- 4.3.1 Offline parameter tuning. There is no general optimal parameter setting for metaheuristics. For any metaheuristic, an optimal parameter setting can vary considerably depending on the problem, and even between instances of the same problem. Three main ML methodologies can be applied:
 - Unsupervised learning: unsupervised learning has been explored to improve the efficiency of factorial experimental design for parameter tuning. The main idea is to reduce the parameter space in order to reduce the computational complexity: Design of Experiments (DoE) [43], Taguchi fractional experimental design [2], fractional factorial design [76], correlation graph decomposition [111]. This methodology can be described in an unified way by the following three steps:
 - Parameter selection: the main goal of this step is to select the significant parameters which influence the performance of the metaheuristic. Given the input set of parameters, the selection step tries to rank these parameters to determine the importance of parameters. This step allows to reduce the parameters space to be explored by eliminating some non significant parameters.
 - Parameter space exploration: it consists in decomposing the parameter space in different clusters. A model-based approximation (e.g. linear regression [43], response surface [88][76], logistic regression [160], decision tree [15]) is built to find relationship between the parameters and the objective function value. This step allows to find promising clusters in the parameters space.
 - Parameter space exploitation: in each cluster, an optimization process is applied to find
 the best parameters. Any metaheuristic can be used for this step (e.g. local search [43],
 evolutionary algorithms [111]).

• **Supervised learning:** optimal parameters setting may differ function of the problem instances of the problem at hand. Supervised learning can be applied in order to predict the best parameters value for a given instance of the problem. Each instance is characterized by some features [163]. Two different steps can be considered (Fig.9):

- **Training and learning:** for different set of initial parameter values, a metaheuristic is applied to generate solutions for a finite training set of problem instances. Then, the obtained performance data are carried out by ML to build a model.
- Prediction: supervised ML is trained with the data from the first stage in order to give recommendations for parameters for any new problem instance. ML is therefore used for the recognition of good initial parameter settings for new problem instances. Parameters values for new problem instances can be retrieved in real time using supervised learning, once the training phase is carried out. Different models have been used such as artificial neural networks (ANN) [52], Bayesian networks [147], linear regression [34], and SVM [112].
- Surrogate-based optimization: parameters tuning can be formulated as an expensive optimization problem, in which the decision variables are the parameters, and the objective function is the solution quality obtained by the optimization algorithm. Hence, surrogate-based optimization techniques has been applied to reduce the complexity of the meta-optimization process [219].

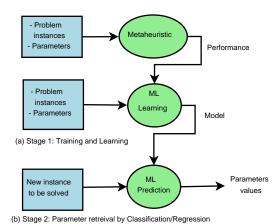


Fig. 9. ML and parameter tuning: training, learning and prediction.

- 4.3.2 Online parameter tuning. In online tuning, the parameters are adapted during the search. For instance, the initialization of the probability of application of a given search operator may be adjusted adaptively by computing the progress of the last applications of the search operator [203][82]. Hence, it becomes possible to determine the probabilities of application of a given operator in an adaptive manner where the more efficient an operator is, the likelier is its application. Knowledge extracted during the search may serve to dynamically change at run time the values of parameters, using various learning methodologies:
 - Sequential learning approach: the most popular online approach is sequential learning: adaptive pursuit [200], multi-armed bandit [47], and reinforcement learning [59][4]. Multi-armed bandit strategies treat each parameter as a separate arm and fix their probabilities by

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learning the expected rewards [47]. Reinforcement learning uses feedback from the search to define states and actions which represent parameters values [59].

- Classification/regression approach: classifiers (e.g. SVM [229]) or regression models [112] can be used to predict effective parameters settings on the basis of the current status of the search and problem/instance informations.
- Clustering approach: clustering approaches have also been applied. In [232], the distribution of the population in the search space is clustered at each iteration. Using the K-means algorithm, the parameters are adapted according to the knowledge extracted from clusters. Some rules based on the relative size of the cluster containing the best solution and the one containing the worst solution are used to adapt the probabilities of the application of variation operators in EAs.

ML IN HIGH-LEVEL COMPONENTS OF METAHEURISTICS

Metaheuristics can be seen as high-level algorithms composed of low-level search operators (e.g. greedy versus iterative). On one hand, many metaheuristic families exist in the literature (e.g. EAs, swarm intelligence, local search) and then various heuristics can be designed. On the other hand, for a given optimization problem, a heuristic can be automatically generated by fixing a configuration from the design space of low-level search operators. According to the nature of the design space of metaheuristics, one can consider the metaheuristic selection problem for selecting existing algorithms, and the metaheuristic generation problem for generating automatically algorithms from the search components of existing ones (Fig.10).

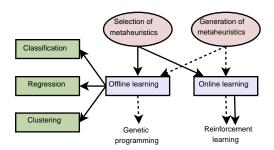


Fig. 10. ML in high-level components of metaheuristics.

Selection of metaheuristics

The design space of metaheuristics is very large. Moreover the steady development of new metaheuristics makes the selection of the best metaheuristic for a given problem or instance an important challenge [108]. The algorithm selection involves selecting an algorithm from a given portfolio of algorithms in order to take into account the varying performance of algorithms over a set of instances and problems [171]. It is well-known that a global best metaheuristic for all optimization problems does not exist. We have to accept that no single metaheuristic will produce the best performance on all problems and instances [220]. One is especially interested in giving metaheuristic recommendations for certain families of optimization problems which differ in the kind of exhibited problem features.

The research literature on the algorithm selection problem show the efficiency of using ML for the problem [22][26]. For the metaheuristic selection problem, one can distinguish between offline and online learning. The advantage of online learning is an adaptive selection of algorithm, whereas the cost for this additional effectiveness is an important overhead:

- Offline learning: the idea is to gather knowledge from a set of training instances by using
 instance features, that will hopefully generalize to solve new instances. One can consider
 three approaches for the metaheuristic selection problem:
 - Classification: a multi-class classifier predict the best performing metaheuristic over the *k* possible ones. A predictive model is trained on empirical performance data and metaheiristics. Many supervised ML techniques can be used such as ANN [204][77][205], Bayesian networks [78], nearest neighbors [71], support vector machines [84], decision trees [41], logistic regression [158], ensembles [190], and deep neural networks [46].
 - Regression: the performance of each metaheuristic is predicted via a regression model and then selects the one with the best predicted performance. Several ML regression approaches have been proposed: linear regression [115], support vector regression [23], and Lasso regression [87].
 - Clustering: it consists in clustering the problem instances in feature space, then selects the
 best metaheuristic for each cluster and finally affects to each new instance the metaheuristic
 associated with the instance's predicted cluster.
- Online learning: the learning takes place during the search. For instance, this idea has been widely explored in the *hyper-heuristic* framework [30]. The most used ML strategies are mainly based on sequential learning. In a reinforcement learning formulation of the problem, the metaheuristics represent actions, states correspond to solutions, and the value function (i.e. reward) represents the performance of the metaheuristic, while the environment is represented by the instance problem [173] (Fig.11). Most of the considered RL approaches usually use only a single instance [133][31][141][222]. For a problem domain (i.e. set of instances), the reward can be represented by the average performance over the set of instances. The main issue of different RL algorithms (e.g. temporal difference learning [173]) is to estimate the value functions.

Some hybrid approaches combining offline and online learning have been proposed [130]. By combining metaheuristic portfolios and online selection, the goal is to develop a problem-independent methodology with diverse problem solving capability.

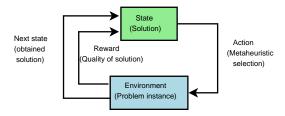


Fig. 11. Online selection of a metaheuristic using a reinforcement learning approach.

5.2 Generation of metaheuristics

 There are so many various characteristics of problem instances encountered in practice. An automated design of a metaheuristic can be performing well and cost effective for a given problem or instance. The generated metaheuristic can produce better solutions than those obtained by human created metaheuristics. Moreover, the automated process is less demanding on human time, and is

therefore appealing. One can find offline and online learning strategies for the automatic generation of heuristics:

- Offline learning: *Genetic programming (GP)* is the most widely used approach for that purpose [174][32][105]. The automated design of effective heuristics is carried out via evolution, in which the heuristic is represented by a GP-tree. Other used methodologies for automatically generating a new heuristic for a given problem/instance are based on apprenticeship learning [10], Learning Classifier Systems (LCS) [138], ANN [139] and logistic regression [137].
- Online learning: the most used online ML approach is the reinforcement learning (RL) to generate greedy [58] and iterative metaheuristics [225]. In [225], deep RL using graph neural networks (GNN) has been used to generate local search heuristics to solve SAT problems. Local search has been formalized as Markov decision process (MDP). Generating a good heuristic consists to find an optimal policy π which maximizes the expected accumulated reward obtained by a local search algorithm. This methodology is also popular in swarm of robots, for which at each iteration the best metaheuristic is generated to perform a given number of predefined actions [227].

6 CONCLUSIONS AND PERSPECTIVES

The fields of ML and metaheuristics are increasingly intertwined. In this paper we have investigated the different opportunities for applying ML into metaheuristics. We have defined in a unified way the various synergies that may be achieved. A detailed taxonomy has been proposed according to the concerned search component: target optimization problem, low-level and high-level search components of metaheuristics. Many of those data-driven metaheuristics have generated high quality results and represent state-of-the-art optimization algorithms. One has to keep the overhead of learning low. Indeed, the integration of ML techniques in metaheuristics incurs additional costs which have to be considered in the performance evaluation measures.

Research in designing metaheuristics using ML techniques is witnessed to have an important impact in the future. We expect the interplay of metaheuristics and ML will increase. Indeed, data-driven metaheuristics opens up a wealth of perspectives. From the optimization point of view, investigating the integration of ML into exact optimization techniques (e.g. mathematical programming, branch and bound, dynamic programming, constraint programming) is an important research challenge. Solving more complex optimization problems such as multi-objective optimization, dynamic optimization, optimization under uncertainty, and bi-level optimization, opens also many other research issues.

From the machine learning perspective, the use of more sophisticated and modern ML techniques such as deep learning models will represent an interesting alternative to solve more complex problems. *Transfer learning* can help to reuse the past experience for speeding up the metaheuristic search process for dynamic and cross-domain optimization problems. Indeed, integrating transfer leaning in metaheuristics can improve performance and robustness in solving similar and evolving problems and instances.

It could also be interesting to explore the design and implementation of parallel models for data-driven metaheuristics. High-performance computing is evolving toward Exascale supercomputers composed of millions of cores provided in heterogeneous devices mainly multi-core processors with various architectures, GPU (Graphics Processing Units) accelerators and TPUs (Tensor Processing Units) and other AI-dedicated ASICS (Application-Specific integrated Circuits). Finally, the coupling of software frameworks dealing with the two classes of algorithms (i.e. metaheuristics and ML

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algorithms) is an important issue for the future. This enables to reduce the complexity of developing data-driven metaheuristics approaches and makes them increasingly popular.

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