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Performance Analysis of Finite Load Sources in 802.11b Multirate Environments

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Abstract: Automatic rate adaptation in CSMA wireless networks may cause drastic throughput degradation for high speed bit rate stations (STAs). The CSMA/CA medium access method guarantees equal long-term channel access probability to all hosts when they are saturated. In previous work it has been shown that the saturation throughput of any STA is limited by the saturation throughput of the STA with the lowest bit rate in the same infrastructure. In order to overcome this problem, we first introduce in this paper a new model for finite load sources with multirate capabilities. We use our model to investigate the throughput degradation outside and inside the saturation regime. We define a new fairness index based on the channel occupation time to have more suitable definition of fairness in multirate environments. Further, we propose two simple but powerful mechanisms to partly bypass the observed decline in performance and meet the proposed fairness. Finally, we use our model for finite load sources to evaluate our proposed mechanisms in terms of total throughput and MAC layer delay for various network configurations.

Key-words: Stochastic processes/Queueing theory, Network measurements, Experimentation with real networks/testbeds

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Analyse des Performances de 802.11b pour les Sources non saturées à Débits multiples

Résumé : Le mécanisme d'adaptation automatique de la capacité de la couche physique implanté dans les réseaux 802.11 de type CSMA peut dégrader fortement les performances obtenues par les stations à grande capacité. Il a été montré que débit saturé de n'importe quelle station est limité par le débit saturé de la station qui a la plus petite capacité. Pour résoudre ce problème, nous introduisons tout d'abord un nouveau modèle pour des sources finies qui utilisent des capacités différentes. Nous utilisons ce modèle pour analyser la dégradation de débit qui se produit dans des régimes saturés et non-saturés. Nous avons défini un nouveau paramètre d'équité, basé sur le temps d'occupation du médium, afin de mieux prendre en compte les caractéristiques des environnements multi-capacité. De plus, nous proposons deux mécanismes pour éliminer la dégradation de performance et obtenir une équité entre les différentes stations. Enfin, nous utilisons notre modèle de sources finies afin d'évaluer les nouveaux débits et délais obtenus avec notre mécanisme pour différentes configurations du réseau.

Mots-clés : Processus stochastique/Théorie des file d'attente, Mesure dans des réseaux, Expérimentation avec des vraies réseaux

1 Introduction

In recent years, the IEEE 802.11 protocol for wireless LAN (WLAN) has become very popular as access scheme for wireless and mobile Internet users. Access Points (APs) can be deployed wherever service customers need fast and mobile access to information. Such environment can be an airport, a campus or a business building. The IEEE 802.11 standard specifies the Medium Access Control (MAC) layer as well as the physical (PHY) layer. Currently, for the MAC layer, the standard defines two medium access coordination functions: the contention-based Distributed Coordination Function (DCF) and the contention free based Point Coordination Function (PCF) [1]. In this paper we only consider the DCF access method. The PCF access method is not mandatory and, therefore, is rarely implemented in current 802.11b products.

The DCF access method is based on the *Carrier Sense Multiple Access* with *Collision Avoidance* (CSMA/CA) principle. Each STA has the same priority when competing for an empty slot time, which guarantees long-term fairness in access probability. Before an STA attempts a *first* packet transmission, it has to sense the medium. If the medium is found idle for the minimum time equal to the Distributed Inter Frame Space (DIFS), the packet will be transmitted directly. Otherwise, the STA enters into backoff and randomly sets its backoff timer within the range of the Contention Window (CW). The timer is decremented by one every slot time until 0 is reached and the next transmission attempt is started. Upon the correct receipt of a packet, the receiver has to send an acknowledgment (ACK) after a time equal to the Short Inter Frame Space (SIFS). If no ACK is received, the sending STA assumes a collision, doubles its current CW and randomly resets its backoff timer.

The IEEE 802.11b specifications for the PHY layer allow channel bit rates up to 11Mbps, thus opening the door to various audio and video applications. As in any wireless communication system, bit errors due to noise and interference from the Industrial-Science-Medical (ISM) band are of fundamental concern. High bit error rates in wireless environments require not only sophisticated channel coding but also control over the channel modulation rate. It is well known that a decrease in the symbol period increases the probability of an incorrect detection. The 802.11b standard tackles this problem by offering four different modulation rates. The mechanism, which is implemented in current 802.11b products, counts the number of unsuccessful frame transmission and reduces its channel bit rate accordingly from 11Mbps to either 5.5Mbps, 2Mbps or 1Mbps. However, the standard does not consider that packet transmissions at 1Mbps might take up to eleven times longer than an equal packet size transmission at 11Mbps. The standard still guarantees all STAs the same long-term medium access probability. As a result, the medium underlies a completely unfair time allocation for STAs with different rates. This unfairness is especially reflected in the throughput of the STA with the highest bit rate, namely 11Mbps. It has been proven in [3] that, if there are two different bit rates in the same environment, the saturation throughput of any STA will be equal to the saturation throughput of the STA with the lowest channel bit rate. This *performance anomaly* has been analyzed in [3] using a simplified model and assuming saturated sources, further no solutions are proposed in [3]. We define a saturated source as an STA having to send a packet at any given point in time. In [6] the complex

behavior of 802.11 protocol is analyzed with Markov chains, assuming one single modulation rate and saturated sources. In our real 802.11b testbed we conduct experiments which show that the throughput degradation faced by high-rate STAs, strongly depends on how loaded the low-rate STAs are. This explains the need for a model considering non-saturated as well as saturated sources. An analytical model, based on [6], for non-saturated sources is proposed in [4], however, the assumptions only hold for very low traffic load. Although an infinite MAC buffer is considered, the model in [4] discards all packets in the buffer after the first packet has been taken by the DCF. In [5], a different approach is taken to analyze the performance under statistical traffic. The on-off characteristics of the STAs are modeled with a single server queue where the service time for the different states are estimated from the saturation throughput obtained in [6]. This model assumes equal service time and equal packet sending rates for all participating nodes and, therefore, cannot be applied to multirate environments. This motivates us to develop a model for finite load sources with a MAC buffer for multirate environments. The observed performance anomaly drives the need for a different fairness metric. Thus, we propose a new fairness index giving equal channel occupation time to all STAs. We provide two solutions (optimal minimum CW and optimal payload size) to meet our fairness index and to considerably improve the total throughput in multirate environments.

The rest of this paper is organized as follows. In the following section, we introduce and derive our proposed model for finite load sources. In Section 3, we validate our model based on realistic experiments in our 802.11b testbed. In Section 4, we define a new fairness index and evaluate our two proposed mechanisms. Finally in Section 5, we conclude our work.

2 DCF Model for finite load Sources

In our model, for any source load and for multirate environments, we take a novel approach by actually modeling the MAC buffer with an $M/G/1$ queue. Further, our model is generalized to support n_S STAs at a physical rate of S (indexed $k = 1, 2, \ldots n_S$) and n_F STA at a physical rate of F (indexed $k = n_S + 1, n_S + 2, \ldots n_F + n_S$). Let $n = n_S + n_F$ be the total number of STAs. In our experiments we mostly use 1Mbps for the rate S and 11Mbps for the rate F. For the rest of this paper we call STAs with rate S *slow* whereas STAs with rate F *fast*. We choose a Poisson process with rate λ_k packets/second to model the arrivals of packets at the MAC buffer of STA k. Even though the Poisson assumption may not be realistic, it provides insightful results and allows our model to be tractable. Our model is based on the following assumptions:

1. The effects of bit errors due to noise are ignored. Consequently, packets are lost only when they encounter collisions due to other simultaneous transmissions.

2. Propagation delays and hidden terminals are not considered.

3. The collision probability is independent of the number of retransmissions.

4. Each STA is assumed to have an infinite buffer and new packets are assumed to arrive according to a Poisson distribution.

2.1 Our Approach

Our proposed model, depicted in Fig. 1, consists of an aggregation of states in which an STA can reside. As defined in the standard, an STA has to run at least one backoff between two successive transmissions [1]. Therefore, after each successful transmission, the CW is reset to its minimum value W_0 and the STA enters into a backoff even if there is no packet in the queue. In our model, we check the queue after each successful transmission or after having reached the maximum number of retransmissions m. If there is a packet, we enter into backoff directly, otherwise, if the queue is empty, we enter into a separate backoff which we call *post-backoff*. In Fig. 1, q denotes the probability of having an empty queue after a packet has been successfully transmitted or after having reached the maximum number of retransmissions. The MAC queue is checked again after the post-backoff has expired. If there is a packet, it will be transmitted directly in next slot time, otherwise the STA will reside in a vacation state $notx$ until the next packet arrives. $p_{pb \to notx}$ denotes the probability of having no packet in the queue at the end of the post-backoff. If in the $notx$ state the medium is sensed idle at the occurrence of the first packet in the MAC queue, the STA sends the packet immediately from state $frtx$. For the case the medium is sensed busy at the first arrival, the STA enters into backoff and the packet is transmitted when the backoff timer reaches 0. With probability $p_{notx \to frtx}$ the medium is sensed idle at the first packet arrival and with probability $p_{notx \to bo}$ the medium is sensed busy at the first arrival.

For a general STA k, $k \in [1, n]$, we use the tuple (s, r) to represent the different states in the backoff stages, with s being the backoff stage number $s = 0', 0, 1, \ldots, m', \ldots, m$, and r being the value of the backoff timer in the range $[0, W_s - 1]$. W_s is the size of the CW at stage s and computed by $W_s = 2^s W_0$ if $s \leq m'$. Otherwise, if $s \in [m', m]$, W_s is kept at its maximum value $W_{max} = 2^{m'} W_0$. With m we denote the maximum number of packet retransmissions before the packet is dropped. According to [1], the default value for m' is 5 and it is 7 for m. We use $s = 0'$ to account for the post-backoff stage. $\pi_{s,r}$ will denote the probability to be in state (s, r). For the remaining two states, $notx$ and $frtx$, we denote with π_{notx} and π_{frtx} their respective state probabilities. With p we denote the probability that the packet transmitted by STA k collides, which is equal to the probability that at least one other STA transmits a packet. We assume that the packet collision process is Bernoulli. This assumption has been made in [6] and has shown good performance in computing the throughput of 802.11 STAs, especially when the number of concurrent STAs is high. The Bernoulli assumption on the packet collision process allows us to describe the state of an STA with the discrete time Markov chain depicted in Fig. 1. The state transitions appear at the beginning of each slot time, where such a transition may be executed after a transmission or an empty slot time. Therefore, the interval between the beginnings of two consecutive slot times may have either the length of an empty slot time σ_0 or of a packet transmission (successful or not).

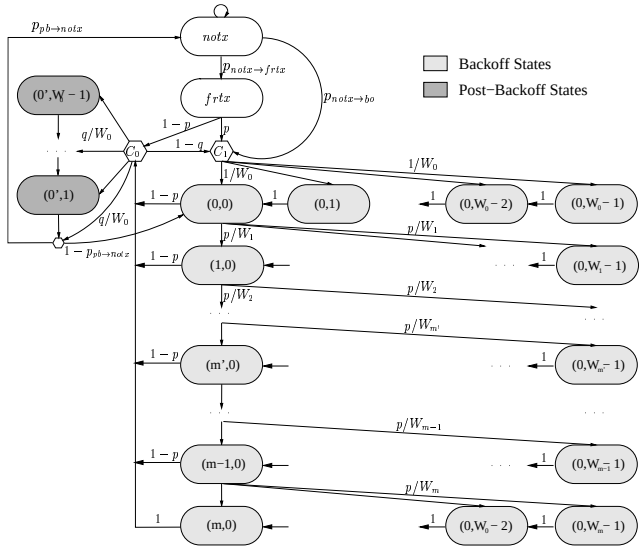

Figure 1: Finite load source model for DCF

It can be seen that our Markov chain is ergodic, therefore, a unique stationary distribution exists. Also note that only the oval forms represent states where actually time is spent. The hexagons in Fig. 1 represent circuit points which we name C_0 and C_1. We use lower case c_0 (resp. c_1) to denote the probability to cross C_0 (resp. C_1). In Appendix A we derive expressions for c_0 and c_1 as a function of $\pi_{0,0}$.

2.2 Transmission Probability

We now derive the expression for the state probabilities in steady state of a general STA k, $k \in [1, n]$. In a first step we express all state probabilities in terms of $\pi_{0,0}$. Later, we use the normalization condition to obtain $\pi_{0,0}$ itself. From the balance equation in the steady state we obtain the following relations:

$$\pi_{0',r} = \frac{W_0 - r}{W_0} q\ c_0 \qquad r \geq 1, \tag{1}$$

$$\pi_{0,r} = \frac{W_0 - r}{W_0} c_1 \qquad r \geq 0, \tag{2}$$

$$\pi_{s,r} = \frac{W_s - r}{W_s} p^s\ \pi_{0,0} \qquad 1 \leq s \leq m, \tag{3}$$

where W_s is the length of the CW in stage s and is equal to:

$$W_s = 2^s W_0 \qquad 0 \leq s \leq m', \tag{4}$$

$$W_s = 2^{m'} W_0 \qquad m' \leq s \leq m. \tag{5}$$

The probability π_{notx} to be in state $notx$ is equal to:

$$\pi_{notx} = \frac{c_0 \; q \; p_{pb \to notx}}{p_{notx \to frtx} + p_{notx \to bo}}. \tag{6}$$

Using (6) the state probability π_{frtx} becomes:

$$\pi_{frtx} = p_{notx \to frtx} \; \pi_{notx}. \tag{7}$$

The expressions for the transition probabilities $p_{pb \to notx}$, $p_{notx \to frtx}$, $p_{notx \to bo}$ and q are derived in the next subsections. Equations (1), (2), (3), (6) and (7) express all state probabilities as a function of $\pi_{0,0}$. Then $\pi_{0,0}$ is obtained by using the normalization condition:

$$1 = \sum_{s=0}^{m} \sum_{r=0}^{W_s - 1} \pi_{s,r} + \sum_{r=1}^{W_0 - 1} \pi_{0',r} + \pi_{notx} + \pi_{frtx} \tag{8}$$

From (8) we obtain $\pi_{0,0}$ as a function of p. The collision probability p is equal to the probability $p_{k,otr}$ that at least one of the other $n-1$ STAs transmits a packet. Therefore, p for STA k can be written as:

$$p = p_{k,otr} = 1 - \prod_{\substack{i=1 \\ i \neq k}}^{n} (1 - \tau_i), \tag{9}$$

where τ_i denotes the probability that an STA i transmits a packet in a randomly chosen slot time. Such a transmission occurs either if the backoff timer r of an STA reaches zero or if an STA, after some idle period in state $notx$, conducts a first transmission from state $frtx$. The transmission probability for STA k can be obtained from:

$$\tau_k = \sum_{s=0}^{m} \pi_{s,0} + \pi_{frtx}, \qquad k \in [1, n]. \tag{10}$$

Using (10) we can setup a non-linear system of equations where the τ_k are the unknowns. Indeed, τ_k can be expressed using (9), (10) and the state probabilities of the Markov chain of the STA k as a function of p, and hence as a function of the transmission probabilities of the other $n-1$ STAs:

$$\tau_k = f\left(\tau_1, \tau_2, \ldots, \tau_{k-1}, \tau_{k+1}, \ldots, \tau_{n_S + n_F}\right). \tag{11}$$

Thus, we obtain $n_S + n_F$ equations with the same number of unknowns, which allows us to compute all τ_k. We solve this non-linear system using the numerical method $fsolve$ implemented in the MATLAB optimization toolbox.

2.3 Transition Probabilities

We now derive the expressions for the transition probabilities. These probabilites are not equal for all STAs, so we use the index k to refer to STA for which we are computing the probabilities. Note that we use for the derivation both variables p and $p_{k,otr}$, although they have the same value and meaning. We use p when we know that STA k attempts a transmission. p is the probability that this transmission fails due to collisions. We use $p_{k,otr}$ for the cases where STA k is not involved in a medium access for the current slot. $p_{k,otr}$ is the probability that one or more stations other than k attempt to transmit a packet in the current slot time.

The transition probability from the post-backoff stage to the $notx$ state is denoted by $p_{pb\rightarrow notx}$ and is equal to the probability of not receiving any packet during the time spent in the post backoff. The timer for the post-backoff is a RV B, which is uniformly distributed over the interval $[0, W_0 - 1]$. Note that if the timer is chosen to be 0, then the STA will enter directly into the $notx$ state with probability 1. Further, we introduce a random vector $\overline{\sigma} = \{\sigma_1, \ldots, \sigma_B\}$ of length B representing the sequence of slot lengths observed by STA k. The time STA k resides in the post-backoff stage is equal to the sum over all σ_i. Knowing B and $\overline{\sigma}$ one can write:

$$p_{pb\rightarrow notx|B,\overline{\sigma}} = e^{-\lambda_k \sum_{i=1}^{B} \sigma_i}. \tag{12}$$

Now using the uniform distribution of B and the assumption that all σ_i are independent and identically distributed, we show in Appendix B that $p_{pb\rightarrow notx}$ can be written as follows:

$$p_{pb\rightarrow notx} = \frac{1}{W_0} \sum_{b=0}^{W_0-1} E\left[e^{-\lambda_k \sigma}\right]^b. \tag{13}$$

To compute (13) we need the distribution of the RV σ, which is the length of a random slot time observed by an STA k. The RV σ may take different values in six cases depending on the transmission events of the other active STAs. With σ_0, we refer to the length of an idle slot time and is in our case equal to 20μs. T_s is the time the medium is sensed busy if a successful transmission occurs. When T_s is indexed with S, the transmission is done at physical rate S, and when indexed with F, the rate is F. Analog to this nomination, T_c represents the time the medium is busy when a collision occurs. We will give later the explicit expressions for T_c and T_s. To derive the distribution of σ, we introduce four new probabilities whose explicit equations are given in Appendix C. The probabilities that at least one of the n_S slow STAs and one of the n_F fast STAs transmit a packet are denoted respectively by $p^S_{k,otr}$ and $p^F_{k,otr}$. With $p^S_{k,os}$ we indicate the probability of having a successful transmission by one of the n_S slow STAs knowing that at least one slow STA transmits a packet. We give an equivalent meaning for $p^F_{k,os}$. Using the nomination from above, the probability distribution for σ is equal to:

1. If no other STA transmits a packet, σ is equal to the length of an idle slot time σ_0 with probability:

$$P\{\sigma = \sigma_0\} = 1 - p_{k,otr}. \tag{14}$$

2. Further, if one of the n_S slow STAs successfully transmits a packet, the slot length is equal to T_s^S. Such a slot length can be observed with probability:

$$P\{\sigma = T_s^S\} = p_{k,otr}^S \; p_{k,os}^S. \tag{15}$$

3. Similarly, if one of the n_F fast STAs successfully transmits a packet, the slot length becomes T_s^F and has probability:

$$P\{\sigma = T_s^F\} = p_{k,otr}^F \; p_{k,os}^F. \tag{16}$$

4. A slot length of T_c^S can be observed if at least two STAs out of the n_S slow STAs transmit packets simultaneously and so cause a collision. In addition, the condition that none of the other fast n_F STAs transmits a packet has to be imposed, to be sure that the collision happens explicitly between the n_S slow STAs. Therefore, such a slot length can be observed with probability:

$$P\{\sigma = T_c^S\} = p_{k,otr}^S(1 - p_{k,os}^S - p_{k,otr}^F). \tag{17}$$

5. Similarly, a collision explicitly within at least two STAs out of the n_F fast STAs implies a slot length of T_c^F and has probability:

$$P\{\sigma = T_c^F\} = p_{k,otr}^F(1 - p_{k,os}^F - p_{k,otr}^S). \tag{18}$$

6. The last case is that at least one out of the n_S slow STAs and one out of the n_F fast STAs are involved in a collision. Then, the length of a slot time will be the maximum of either T_c^S or T_c^F with probability:

$$P\{\sigma = \max\left(T_c^S, T_c^F\right)\} = p_{k,otr}^S \; p_{k,otr}^F. \tag{19}$$

The transition probability from state $notx$ to state $frtx$ is denoted by $p_{notx \to frtx}$ and is given by the probability of the event that during an empty slot σ_0, at least one packet arrival occurs:

$$p_{notx \to frtx} = P\{\sigma = \sigma_0\}(1 - e^{-\lambda_k \sigma_0}). \tag{20}$$

The probability to transit from state $notx$ to backoff stage 0 considers all complementary events from (20) and so its probability can be expressed as:

$$p_{notx \to bo} = E\left[1 - e^{-\lambda_k \sigma}\right] - p_{notx \to frtx}. \tag{21}$$

2.4 Computation of the probability q

The properties of the $M/G/1$ MAC buffer are reflected in q, which is the probability of having no packet in the queue upon packet departures. In an $M/G/1$ queue, q is simply equal to

$$q = \max\left(0, 1 - \lambda_k E[S_{T,k}]\right), \tag{22}$$

where $E[S_{T,k}]$ is the first moment of the service time for packet from STA k. The $M/G/1$ queue has the property that the distribution of queue length is the same at packet arrivals, packet departures, and at random time [7]. In our model, $S_{T,k}$ is the time that a packet spends in the MAC layer from the point of leaving the MAC buffer until its successful transmission (or until the abortion of its transmission).

A packet may have different average service times depending on the state of the queue upon its arrival. We consider the cases of having an empty or nonempty queue, therefore, $E[S_{T,k}]$ has to be conditioned on q and is equal to:

$$E[S_{T,k}] = (1-q)E[T_{bo,k}] + qE[T_{pb,k}]. \tag{23}$$

We first derive an expression for $E[T_{bo,k}]$, which is the average service time of a packet that finds the queue non empty when it arrives. We have:

$$\begin{aligned} E[T_{bo,k}] = & \sum_{s=0}^{m} p^s \frac{W_s - 1}{2} E[\sigma] + (1-p^{m+1})T_{s,k} + \\ & + \sum_{s=1}^{m+1} p^s (1-p) s E[T_{col}]. \end{aligned} \tag{24}$$

The first term in (24) accounts for the total time needed to attain a transmission state, which is called $(s,0)$, where $s = 0, \ldots, m$. A transmission state is the state which represents the value 0 of the backoff timer, and therefore triggers directly a packet transmission. The second term is the expected value of the time needed to actually accomplish the physical transmission and the receipt of the ACK. If $k \in [1, n_S]$, $T_{s,k}$ is equal to T_s^S (38), otherwise $T_{s,k}$ is equal to T_s^F (39). The third term accounts for the expected number of collisions that the STA k might enter. $E[T_{col}]$ is the average time that STA k spends in a collision. For anyone of the n_S slow STAs, k is within the interval $[1, n_S]$, $E[T_{col}]$ becomes:

$$E[T_{col}] = \frac{(1-p_{k,otr}^F)p_{k,otr}^S}{p_{k,otr}} T_c^S + \frac{p_{k,otr}^F}{p_{k,otr}} \max\left(T_c^F, T_c^S\right). \tag{25}$$

For anyone of the n_F fast STAs, k is within $[n_S+1, n_S+n_F]$, $E[T_{col}]$ is equal to:

$$E[T_{col}] = \frac{(1-p_{k,otr}^S)p_{k,otr}^F}{p_{k,otr}} T_c^F + \frac{p_{k,otr}^S}{p_{k,otr}} \max\left(T_c^F, T_c^S\right). \tag{26}$$

We now seek for an expression of the second term $E[T_{pb,k}]$ in (23). With $E[T_{pb,k}]$ we denote the average service time of a packet that at its arrival finds the MAC queue empty. As it is shown in Fig. 1, a packet may arrive either while the node resides in the post-backoff, or it may arrive after the post-backoff has already expired and so finds the node in state $notx$. We introduce a Bernoulli RV V to condition on whether the STA enters after the post-backoff into the vacation state $notx$ or enters directly into state $(0,0)$. We define V as follows:

$$V = \begin{cases} 1 & \text{with probability } p_{pb \to notx} \\ 0 & \text{with probability } (1 - p_{pb \to notx}). \end{cases}$$

Therefore, if V is equal to 0, the node conducts a transmission attempt directly from state $(0,0)$, otherwise, if V is equal to 1, the node will reside in $notx$ and will wait for the next packet arrival. Therefore, we can condition the value of $E[T_{pb}]$ upon V and write:

$$\begin{aligned} E[T_{pb,k}]=&(1-p_{pb\to notx})(E[T_{inpb}]+E[T_{pb\to bo}\mid V=0]) \\ &+p_{pb\to notx}E[T_{pb\to bo}\mid V=1]. \end{aligned} \tag{27}$$

With $E[T_{inpb}]$ we express the expected time the packet waits since its arrival before being transmitted, knowing that it arrives during the post-backoff. This time is strictly positive if the packet arrives before the post-backoff timer reaches 0. In order to find $E[T_{inpb}]$, we generalize the problem to find the average residual time $R(X)$ for a packet that arrives at rate λ, given the observation interval $[0,X]$. Suppose that the packet arrives at instant $x_0 < X$, then $R(X) = X - x_0$, else if the packet arrives at an instant $x_0 > X$, $R(X)$ becomes zero. We propose the following function for $R(X)$ and prove it in Appendix D.

$$R(X) = X + \frac{e^{-\lambda X}}{\lambda} - \frac{1}{\lambda} \tag{28}$$

$E[T_{inpb}]$ can now be found by setting X to the length of the post-backoff (sum of all σ_i) and conditioning it on the fact that we know that at least one packet arrived in the desired interval. As X consists of a random vector $\overline{\sigma}$ and a RV B, $R(X)$ has to be computed, similar to (13), by taking its expected value with respect to $\overline{\sigma}$ and B. Therefore, we can write the following relation:

$$(1-p_{pb\to notx})\cdot E[T_{inpb}] = E[R\left(\sum_{i=1}^{B}\sigma_i\right)]. \tag{29}$$

Making the same assumption about independence as for computing (13), one can obtain the following expression for $E[T_{inpb}]$:

$$E[T_{inpb}] = \frac{\frac{1}{W_0}\sum_{b=0}^{W_0-1}\left(bE[\sigma]+\frac{1}{\lambda_k}E\left[e^{-\lambda_k\sigma}\right]^b\right)-\frac{1}{\lambda_k}}{1-p_{pb\to notx}} \tag{30}$$

Further from (27), assuming that at least one packet arrives during the post-backoff (V=0), $E[T_{pb\to bo}\mid V=0]$ accounts for the time needed to send successfully the packet (or to abort its transmission) starting in the transmission state $(0,0)$.

$$E[T_{pb\to bo}\mid V=0] = (1-p)T_{s,k} + pE\left[T_{col}+T_{bo,k}^{(i=1)}\right], \tag{31}$$

where the index $(i=1)$ denotes that (24) is computed starting from stage one instead of stage zero.

If V turns out to be equal to 1, then we start counting the time for a successful transmission upon the packet arrival in the state $notx$. Two cases have to be treated: One is that

the packet arrives when the medium is busy, another is that the packet arrives during an empty slot time.

$$E[T_{pb\to bo} \mid \ V = 1] = (1 - p_{k,otr})E[T_{ftx}] + p_{k,otr}E[T_{noftx}], \tag{32}$$

where $E[T_{ftx}]$ considers that the medium is idle upon the arrival of the packet:

$$E[T_{ftx}] = \frac{P\{\sigma = \sigma_0\}R(\sigma_0)}{p_{notx\to frtx}} + pE[T_{col} + T_{bo,k}] + (1-p)T_{s,k}, \tag{33}$$

and $E[T_{noftx}]$ treats the case where the medium is sensed busy upon the packet arrival, and so the STA enters directly into backoff without conducting a first transmission attempt from state $frtx$:

$$E[T_{noftx}] = E[T_{bo,k}] + \frac{E[R(\sigma)] - (1 - p_{k,otr})R(\sigma_0)}{p_{notx\to bo}}. \tag{34}$$

Finally, combining (22) and (23) the following expression for q can be obtained:

$$q = 1 - \min\left(1, \frac{\lambda_k E[T_{pb,k}]}{1 - \lambda_k E[T_{bo,k} - T_{pb,k}]}\right), \tag{35}$$

where the second term is strictly larger than 0 and therefore it has only to be upper bounded by 1.

2.5 Throughput analysis

We derive now the throughput of each individual STA. Analog to the RV σ, we introduce the RV σ_G which gives the length of a general slot time accounting for all n STAs. The distribution of σ_G is equivalent to that given by equations (14)-(19) except that now the kth STA should also be considered as a transmitting STA.

The throughput Z_k for any STA k is by definition the volume of data STA k successfully transmits in a slot time divided by the average slot length $E[\sigma_G]$:

$$Z_k = \frac{1}{E[\sigma_G]}\tau_k(1 - p_{k,otr})P_k, \tag{36}$$

where P_k is the payload size of STA k. P_k is equal to P_S for a slow STA and equal to P_F for a fast STA.

In our analysis we do not consider the RequestToSend / ClearToSend (RTS/CTS) access method and the throughput is computed at the application layer. The packet header from the transport, network and data link control layer [8] is equal to:

$$H = MAC_{hdr} + IP_{hdr} + TRANSPORT_{hdr}. \tag{37}$$

Upon a successful receipt of a packet, an ACK is transmitted at the physical rate of the received packet. The duration of an ACK is t^S_{ACK} for a slow STA and t^F_{ACK} for a fast one. In

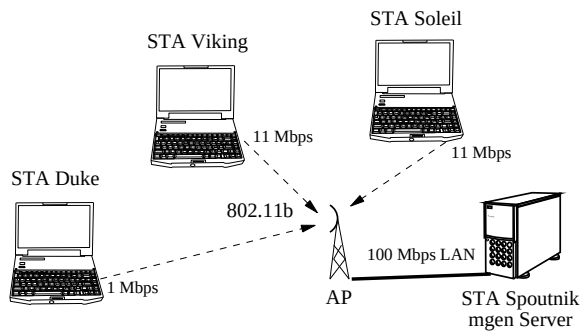

Figure 2: Experiment setup in our 802.11b testbed

addition, the PHY layer adds to each transmission a constant Physical Layer Convergence Protocol (PLCP) preamble and header of total duration t_{PLCP}. Similar to [6], the slot time duration T_s and T_c become:

$$T_s^S = 2t_{PLCP} + DIFS + t_D^S + SIFS + t_{ACK}^S, \quad (38)$$

$$T_s^F = 2t_{PLCP} + DIFS + t_D^F + SIFS + t_{ACK}^F, \quad (39)$$

$$T_c^S = t_{PLCP} + DIFS + t_D^S, \quad (40)$$

$$T_c^F = t_{PLCP} + DIFS + t_D^F, \quad (41)$$

where the index t_D^S (resp. t_D^F) denotes the time needed to transmit a packet of length $H + P_S$ (resp. $P_F + H$) at rate rate S (resp. F).

3 Measurements

In order to verify our model, we set up the platform depicted in Fig. 2 with three notebooks (*Duke*, *Viking*, *Soleil*) sharing a 802.11b wireless infrastructure. The three notebooks are running Linux RedHat 8.0 (Kernel 2.4.18) with Netgear MA401 wireless cards based on the Intersil Prism II chipset. We measure the throughput using the UDP traffic generator *mgen* [12] while varying payload size as well the data sending rate. Each measurement is done over 40 seconds and repeated five times. The traffic is always directed from the mobile host towards our server *Spoutnik*. In order to get a better insight into the *performance anomaly* studied in our paper and described in [3], we conduct the experiments with STA *Duke* running at 1 Mbps and the others at 11Mbps. All three notebooks are placed within two meters from the AP and are not in movement.

We actually change the linux-wlan driver for *Duke* such that only the physical transmission rate 1Mbps is supported. The system parameters of the IEEE 802.11b protocol are summarized in Table 1. Further, we do not use the RTS/CTS option in our testbed. We validate our model based on two experiments, which we discuss in the next subsections.

Table 1: 802.11b Protocol parameters and header definitions

t_{PLCP}	194 μs	ACK	112 bits
DIFS	50 μs	MAC_{hdr}	34 bytes
SIFS	10 μs	IP_{hdr}	20 bytes
σ_0	20 μs	$TRANSPORT_{hdr}$	8 bytes

3.1 The slow STA with different data rates

As shown in Fig.2, *Viking* and *Soleil* are forced to have a physical rate of 11Mbps. For this experiment both STAs generate saturated UDP traffic, which means that immediately after a successful packet transmission, a new packet is ready to be sent. Further, all three STAs use a payload size of 1470 bytes. *Duke*, which has a physical rate of 1Mbps, changes its data sending rate from 50 to 750kbps. As the two fast STAs should perform equally, we only measure the throughput of *Viking* and *Duke*. The model and experimental results are compared in Fig. 3. We can see, as the data sending rate of the slow STA goes above 670 kbps, that all three STAs have the same throughput. We call this regime *saturated* because all three STAs generate saturated traffic. In saturation, the 802.11 access method guarantees equal access probability for all STAs. Therefore, all τ_k are equal and consequently the throughput of each STA computed with (36) returns the same value. This phenomenon has also been observed in [3].

3.2 The slow STA with different payload sizes

Similar to the previous experiment, *Viking* and *Soleil* generate saturated UDP traffic with a bit rate of 11Mbps. This time we limit the data rate of STA *Duke*. With the *mgen* client running on *Duke*, we generate Poisson traffic with an average rate of 320Kbps. The payload size of the two fast STAs is fixed to 1470 bytes. We change the payload size for slow STA *Duke* and plot the resulting throughput for *Duke* and the fast STA *Viking*. Fig. 4 shows the good match between experiment and model. It can be seen that *Duke* does not attain the throughput of 320Kbps until its payload size becomes larger than 300 bytes. We call the regime below this value *saturated*. In this regime, the number of packets to send is so high that the sending queue of *Duke* is always full, and so *Duke* attains its saturation throughput for these particular payload sizes. In the saturated regime, increasing the payload size of the slow STA increases the degradation of the throughput of the fast STA, because the channel occupation time of the slow STA increases too. Above 300 bytes, the slow STA is not saturated anymore and the fast STA can continuously improve its throughput. This is because above 300 bytes the number of packets transmitted by the slow STA decreases, consequently the fast STAs have more chances to access the channel.

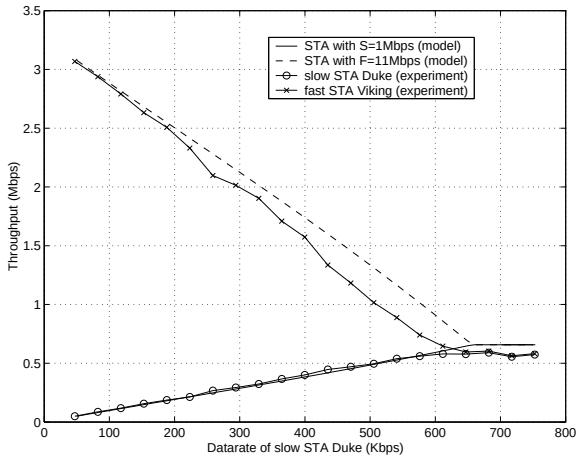

Figure 3: Perfect match between model and experiment when *Duke* has low data rates. The saturation throughput of *Duke* is slightly overestimated in our model (670 instead of 620Kbps), which automatically changes the decline of the fast STA. This mismatch can be seen if the slow STA uses a high data rate. This inaccuracy comes from the infinite MAC buffer assumption and the perfect medium assumption.

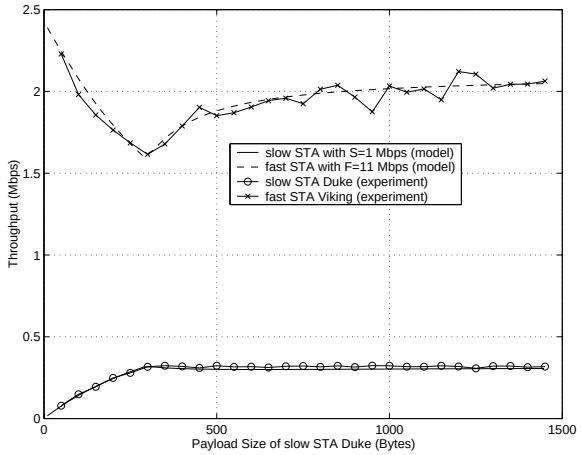

Figure 4: Throughput for a fast and a slow STA. The fast STAs are saturated with a fixed payload size of 1470 bytes. The data rate for the slow STA Duke is limited to 320Kbps.

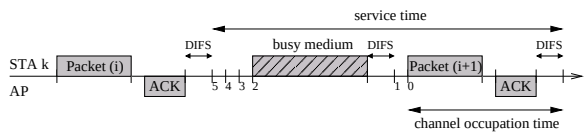

Figure 5: Service time and channel occupation time.

4 Solutions and Discussion

Motivated by the results of our previous experiments, we propose in this section two different mechanisms to gain control over the throughput degradation which occurs in a multirate environment. In Fig.3 it can be seen that avoiding data rates of the slow STAs above a certain rate can help a lot to improve the throughput of the fast STAs running at 11Mbps. In our first mechanism we propose to change the minimum CW of the slow STAs in order to lower their saturation throughput. In the second mechanism, we propose to reduce the packet size of the slow STAs, which also increases the throughput of the fast STAs as shown in Fig. 4. Our mechanisms are not supposed to maximize the total throughput, which could actually be done by turning off the slow STAs. Our objective is to attain fairness between slow and fast saturated STAs, which is achieved when all STAs use the medium equally long in the time domain. To do so, for each STA k we define the ratio of time it is actually using the medium as the ratio between its channel occupation time $T_{s,k}$ and its average service time $E[S_{T,k}]$ (see Fig. 5). With the vector $\overline{x}$ we denote the time allocation, where the kth element of $\overline{x}$ is equal to:

$$x_k = \frac{T_{s,k}}{E[S_{T,k}]} = \frac{T_{s,k}}{E[T_{bo,k}]}. \tag{42}$$

The second equality in (42) is true because in the saturated regime, the probability q of having no packet in the MAC buffer becomes 0, hence (23) equals (24). Now, we use Jain's fairness index [9] to evaluate how fair a particular allocation $\overline{x}$ is. We call this fairness index F_J and it is defined as:

$$F_J(\overline{x}) = \frac{\left[\sum_{k=1}^{n} x_k\right]^2}{n \sum_{k=1}^{n} x_k^2}, \tag{43}$$

where n is the total number of STAs. In [9] it is shown that $F_J \leq 1$, and the equality holds if, and only if, all n x_k have the same value. Therefore, our mechanisms aim at finding the value for the minimum CW (subsection 4.1) and the packet size (subsection 4.2) which maximizes the fairness index F_J.

4.1 Mechanism 1: Fair value for the minimum CW

An STA can limit its data rate by lowering its priority for the medium access. This can be accomplished by either increasing the minimum CW (W_0) or by increasing the $DIFS$ time, which is similar to what is proposed in the new standard 802.11e [2] for the maintenance of

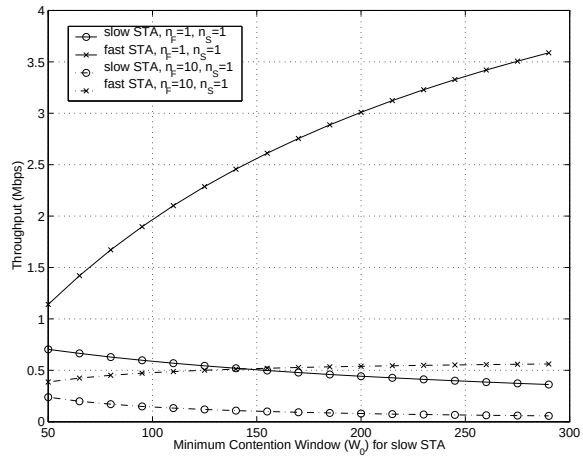

Figure 6: Saturation throughput for the fast and slow STAs with different W_0 of the slow STA. All STAs have a packet size of 1470 bytes. W_0 of the fast STA is fixed to 32.

Quality of Service (QoS). In our work, we are interested in finding the value of W_0, which maximizes the fairness index defined in (43). In a first case, we investigate the fairness in $(n_S = a, n_F = b)$ networks, with the rate of the slow STA fixed at 1Mbps, that of the fast STA is fixed at 11Mbps. The parameters a and b are the scale factors for the number of slow and fast STAs. In Fig. 6, we fix n_S to 1 and we take two values for n_F: 1 and 10. We apply our analytical model to plot the throughput of the slow STA and for one fast STA versus the W_0 value of the slow STA. Note that we only change W_0 of the slow STA and do not limit its maximum CW (W_{max}). Therefore, W_{max} changes dynamically and its value is computed with $W_0 \cdot 2^5$. The minimum CW of the other n_F fast STAs is kept at its default value of 32. It can be seen that the throughput of the fast STAs can considerably be improved by increasing the value of W_0 of the slow STA.

In Fig. 7 we plot the fairness index defined in (43) versus the value of W_0 of the slow STA. We show the curves of F_J for different sizes of networks. Fairness is achieved by setting W_0 to 242, independently from the number of slow and fast STAs! This value of 242 for the optimal minimum CW (W_{opt}) does not apply in cases where the rate S is equal to 2 or 5.5Mbps or F is not equal to 11Mbps. The values for W_{opt} for different physical rates are summarized in Table 2. To use Table 2, at least one STA should operate at physical rate F. Currently, we cannot obtain results with our model if the number of different modulation rates exceeds two. However, we will consider such scenarios in our future work. We are also investigating the fact that W_{opt} is independent of the network size and only depends on the bit rates S and F.

To support this mechanism, we propose that the optimal minimum CW for each STA is computed by the AP, which is aware of the modulation rate of the individual STAs. The

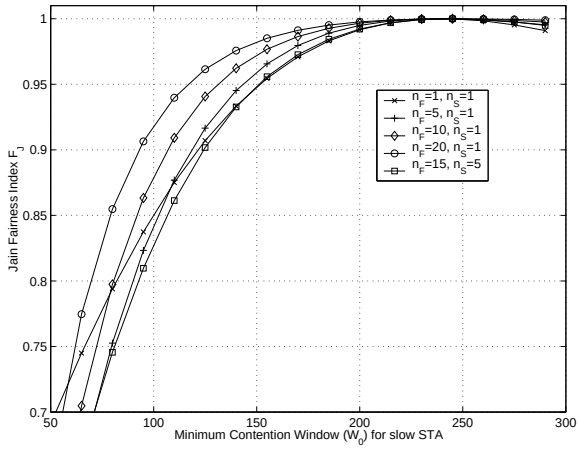

Figure 7: Fairness of a time allocation for different W_0 of the slow STA. W_{max} of the slow STA is dynamic. W_0 of the fast STAs is fixed to 32. All STAs have a payload size of 1470 bytes and generate saturated traffic.

Table 2: Optimal Values for W_0 (W_{opt})

PHY Rate (Mbps)	W_{opt} **Value**
S=1, F=11	242
S=2, F=11	120
S=5.5, F=11	51

optimal values for the CW can then be broadcasted with a beacon frame, where each STA can find its mapping for the correct minimum CW.

The same idea could have been implemented by using a fixed W_{max}. We repeat the same computation, limiting the maximum CW for all STAs to 1024. Fig. 8 shows the results. As expected, W_{opt} is no longer a single value it is sensitive to the number of STAs. An implementation of this case requires continuous adaptation of W_0 to the current network size and, therefore, increases the complexity. So, we give the preference to the implementation using a dynamic W_{max} and do not evaluate the performance of the second implementation further.

4.2 Mechanism 2: Fair value for the payload size P_S

A more intuitive way to attain fairness is to change the payload size according to the current physical transmission rate. In saturation, the service time for all STAs is the same, assuming that all STAs use the same parameters. From (42) it can be seen that the problem of finding

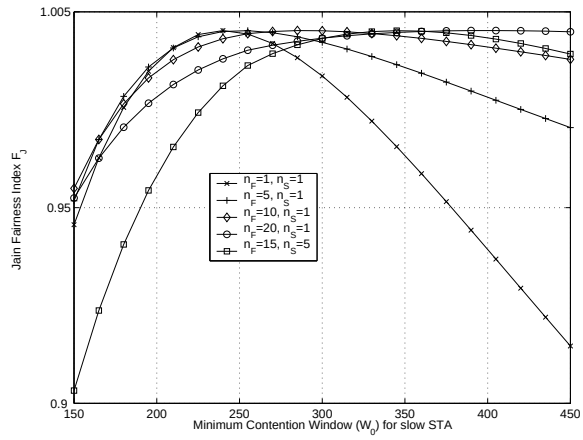

Figure 8: Fairness of a time allocation for different W_0 of the slow STA. W_{max} is static fixed to 1024 for all STAs.

the fair allocation is reduced to the problem of making all $T_{s,k}$ equal. In this work we take a reference physical rate of 11Mbps, consequently the reference transmission time becomes T_s^F. Fairness is achieved if all STAs have the same transmission time T_s^F. Therefore, the slow STA has to reduce its payload such that its T_s^S equals T_s^F. As we compute the throughput at the application level, we also define the parameters to obtain fairness at this level. The optimal payload size can be obtained by setting (38) and (39) equal and determining P_S.

We denote with P_{opt} the payload size for which the maximum fairness ($F_J = 1$) is achieved. P_{opt}, expressed in payload bits, is equal to:

$$P_{opt} = \frac{S \cdot P_F - (F - S)(H + ACK)}{F}. \tag{44}$$

H denotes the packet header and is defined in (37). ACK denotes the length in bits of the acknowledgment sent by the AP. The optimal payload size P_{opt} of the n_S slow STAs yields fairness for any configuration of the network, as long as at least one STA operates at the maximum rate F. This mechanism could be implemented in the MAC layer of each node. If a node's physical transmission rate drops to either 5.5, 2 or 1Mbps, it adapts its MTU size according to its rate, i.e.:

$$P_{opt}^{MTU} = P_{opt} + IP_{hdr} + TRANSPORT_{hdr}. \tag{45}$$

Table 3 shows the optimal MTU values for different configurations. The disadvantage of this method is that it causes strong fragmentation at the higher layers, thereby increasing the overhead even further. Note that fragmentation overhead could be avoided if one could inform the application layer to generate packets respecting the optimal MTU size. We propose to use the Path MTU (PMTU) discovery technique as described in [10]. However,

Table 3: Values for P_{opt} and P_{opt}^{MTU} in bytes

PHY Rates (Mbps)	P_{opt} **(bytes)**	P_{opt}^{MTU} **(bytes)**
S=1, F=11	65	93
S=2, F=11	205	233
S=5.5, F=11	697	725

in our particular case the MAC layer has to act like a router. For example, if TCP is used as end-to-end protocol, when the MAC receives a datagram that exceeds the optimal MTU size, it can return an *ICMP Destination Unreachable* message to the TCP source, with the code indicating "*fragmentation needed and DF set*" [11], and with the optimal MTU size to use. If UDP is used, it is still possible to use such a technique but only if the application can be modified to respond to such an ICMP packet.

4.3 Discussion

We analyze mechanisms 1 and 2 in terms of their total throughput and delay. We consider a network where we have one slow STA ($n_S = 1$) and a varying number of fast STAs. In Fig. 9, the total throughput of mechanism 1 and 2 is compared to the basic configuration. With basic configuration we mean that all STAs have the same packet size and the same value of W_0. Both mechanisms clearly outperform the basic configuration. This clear improvement of the total throughput is achieved because the slow STA has been *punished* by either lowering its transmission probability or by lowering its payload size. Further, it can be seen that the two proposed mechanisms have almost the same total throughput. However, as we will see in Fig. 10, this does not imply that the individual STAs in mechanism 1 and 2 perform equally. It can also be observed that once the number of participating STAs is larger than ten, collisions occur more often and the total throughput starts declining. This phenomenon could be avoided by using RTS/CTS instead of the basic access mechanism, which would help to attain an almost constant total throughput over the number of STAs.

Next, we use the delay as a metric to evaluate the degradation that the slow STA might face when using W_{opt} and P_{opt} as adaptive parameters. In order to find the average delay per packet, we model the 802.11b MAC with an $M/G/1$ queue, where the first moment of the service time is given in (23). Note that taking this model, we assume that the MAC buffer has infinite length. To simplify the calculation, we fit the service time to a cumulative distribution function of an exponential RV shifted by the minimum service time. Note that for a slow STA the minimum service time is deterministic and equal to T_s^S. We denote the service time with the RV X, which is equal to the sum of an exponential RV with expected value $1/\mu$ and T_s^S. We obtain μ from the following relation:

$$E[X] = T_s^S + \frac{1}{\mu} = E[S_T]. \tag{46}$$

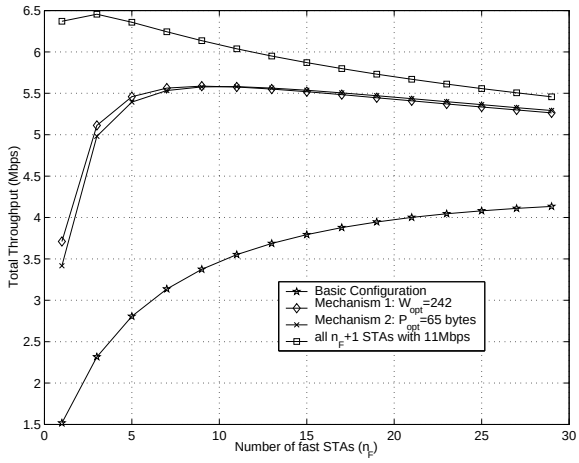

Figure 9: Total throughput versus number of fast STAs. All STAs are saturated

We can now compute the second moment of X and use it in the Pollaczek-Khinchin formula [8] to get the expected waiting time $E[W]$ in the queue. The average packet delay for our system is then the sum of average service time $E[X]$ and the obtained waiting time $E[W]$. We evaluate the packet delay versus throughput of a slow STA (running at 1Mbps) in the two different network sizes: $n_S = 1, n_F = 1$ and $n_S = 1, n_F = 5$. The tradeoff of mechanism 1 (W_{opt}) against mechanism 2 (P_{opt}) is shown in Fig. 10. In each case, the fast STAs generate fully saturated traffic. Setting W_0 to W_{opt}, rather than using the optimal payload size mechanism, can help to achieve a much higher throughput for a slow STA . This can partly be explained by the fact that a packet with a payload size of 65 bytes has a huge relative overhead. On the other hand, a small packet size and an equal W_0 value for all STAs lead to less delay, if the throughput of the slow STA is low. The minimum CW method is based on the idea of introduce a certain delay to the slow STAs, thereby increasing the service time. This delay is fixed for any network configuration and cannot be bypassed. Therefore, a CW of 242 introduces long waiting times even for a low loaded network. Giving preference to one of the two mechanisms is very difficult, because their performance strongly depends on the MAC buffer size and on how much delay can be accepted by the end-to-end protocol. More analysis with finite buffer length are required to find the best scheme.

5 Conclusion

In this paper, we have presented a first analytical model for finite load sources using the IEEE 802.11b DCF protocol. We used a novel approach by modeling the MAC buffer with an $M/G/1$ queue. In addition, the model is generalized such that two different modulation

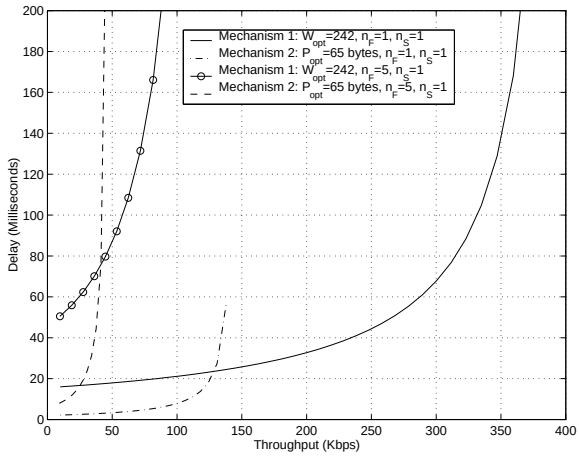

Figure 10: MAC layer delay for the slow STA using either Mechanisms 1 or 2. The fast STA generate saturated UDP traffic at 11Mbps and use a payload size of 1470 bytes.

rates can be supported simultaneously. Our model shows good performance when comparing it against real measurements from our 802.11b testbed.

Motivated by the current unsatisfying performance and fairness in a 802.11b multirate infrastructure, we come up with a new fairness metric for general CSMA multirate networks. This metric is used to propose two different mechanisms that meet our fairness and provide a considerably better total throughput. Our proposed mechanisms are only executed on slow STAs and change either W_0 or the packet size to precomputed values. This procedure shows a very low complexity and therefore makes our mechanisms suitable for an implementation in the MAC protocol stack.

A Appendix A

We derive here the probabilities to enter into the circuit points C_0 and C_1. Using the balance equations, c_0 can be obtained from:

$$\begin{aligned} c_0 &= \sum_{i=0}^{m-1} \pi_{i,0}(1-p) + \pi_{m,0} + (1-p)\pi_{frtx} \\ &= \pi_{0,0} + \frac{c_0\ (1-p)q\ p_{notx\to frtx}\ p_{pb\to notx}}{p_{notx\to bo} + p_{notx\to frtx}}. \end{aligned}$$

Knowing c_0, c_1 becomes:

$$\begin{aligned} c_1 &= c_0(1-q) + \\ &\quad + \frac{c_0\ q\ p_{pb\to notx}(p\ p_{notx\to frtx} + p_{notx\to bo})}{p_{notx\to bo} + p_{notx\to frtx}}. \end{aligned}$$

B Appendix B

Suppose that the value for the backoff counter and the length of each slot time is known. Then, the probability that no packet arrives during the post-backoff is equal to:

$$p_{pb\to notx|B,\overline{\sigma}} = e^{-\lambda \sum_{i=1}^{B} \sigma_i}.$$

B is uniformly distributed. If we condition on every possible value of B, still knowing the length of each slot time, we can write:

$$\begin{aligned} p_{pb\to notx|\overline{\sigma}} &= \sum_{b=0}^{W_0-1} \frac{1}{W_0} e^{-\lambda \sum_{i=1}^{b} \sigma_i} \\ &= \frac{1}{W_0} \sum_{b=0}^{W_0-1} \prod_{i=1}^{b} e^{-\lambda \sigma_i}. \end{aligned}$$

Finally, we assume that σ_i are independent and identically distributed, therefore $p_{pb\to notx}$ becomes:

$$p_{pb\to notx} = \frac{1}{W_0} \sum_{b=0}^{W_0-1} E\left[e^{-\lambda\sigma}\right]^b.$$

C Appendix C

With the index k, we refer to the STA which is actually observing the medium without accessing it. The probability that at least one of the n_S STAs transmits a packet holds:

$$p^S_{k,otr} = 1 - \prod_{\substack{i=1 \\ i\neq k}}^{n_S} (1-\tau_i). \tag{47}$$

The probability that at least one of the n_F STAs transmits a packet holds:

$$p^F_{k,otr} = 1 - \prod_{\substack{i=n_S+1 \\ i\neq k}}^{n} (1-\tau_i). \tag{48}$$

The probability to observe a successful transmission by one of the n_S STA, knowing that there is a transmission by one of the n_S STAs, is equal to:

$$p^S_{k,os} = \frac{1}{p^S_{k,otr}} \sum_{\substack{i=1 \\ i \neq k}}^{n_S} \tau_i \prod_{\substack{y=1 \\ y \neq i,k}}^{n} (1 - \tau_y). \tag{49}$$

The probability to observe a successful transmission by one of the n_F STA, knowing that there is a transmission by one of the n_F STAs, is equal to:

$$p^F_{k,os} = \frac{1}{p^F_{k,otr}} \sum_{\substack{i=n_S+1 \\ i \neq k}}^{n} \tau_i \prod_{\substack{y=1 \\ y \neq i,k}}^{n} (1 - \tau_y). \tag{50}$$

D Appendix D

We know that we have at instant 0 no packet in the queue. Therefore, the time of the next arrival is distributed according to an exponential RV. With t we denote the time of the packet arrival, and so the remaining time in the interval of interest $[0, X]$ is equal to $X - t$ and denoted by *residual time*. The residual time has to condition for every possible arrival time and therefore $R(X)$ can be derived as follows:

$$\begin{aligned} R(X) &= \int_0^X \lambda e^{-\lambda t} (X - t)\, dt \\ &= X + \frac{e^{-\lambda X}}{\lambda} - \frac{1}{\lambda}. \end{aligned}$$

References

[1] IEEE Std 802.11-1999, "Part 11: Wireless LAN Medium Access Control (MAC) and Physical Layer (PHY) specifications," 1999.

[2] IEEE 802.11 WG, "Draft Supplement to Part 11: Wireless Medium Access Control (MAC) and Physical Layer (PHY) specifications: MAC Enhancements for Quality of Service (QoS)", *IEEE 802.11e/Draft 4.1,* February 2003.

[3] M. Heusse, F. Rousseau, G. Berger-Sabbatel, A. Duda "Performance Anomaly of 802.11b" *IEEE Infocom 2003*, March 2003.

[4] F. A.-Shabdiz, S. Subramaniam "A Finite Load Analytical Model for the IEEE 802.11 Distributed Coordination Function MAC" *WiOpt'03 workshop*, INRIA Sophia Antipolis, March 2003.

[5] C. H. Foh, M. Zukerman "Performance Analysis of the IEEE 802.11 MAC Protocol" *Proceedings of the EW 2002 Conference*, Florence, Italy pp. 184-190, February 2002.

[6] Giuseppe Bianchi "Performance Anaylsis of the IEEE 802.11 Distributed Coordination Function", *IEEE Journal on Selected Areas in Communications*, Vol. 18, Number 3, March 2000.

[7] L. Kleinrock " Queueing Systems, Vol. I: Theroy", *Wiley*, 1975.

[8] D. Bertsekas, R. Gallager " Data Networks, second edition", *Prentice-Hall International Editions*, 1987.

[9] R. Jain, D. Chiu, W. Hawe "A Quantitative Measure of Fairness and Discrimination for Resource Allocation in Shared Computer Systems", *DEC Report*, DEC-TR-301, September 1984.

[10] J. Mogul, S. Deering "Path MTU Discovery", *RFC 1191,* November 1990.

[11] J. Postel, "Internet Control Message Protocol", *RFC 792,* SRI Network Information Center, September 1981.

[12] The MGEN Multi-Generator Toolset is available at: manimac.itd.nrl.navy.mil/MGEN/.

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