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# Fine-Tuning MAC-Level Protocols for Optimized Real-Time QoS

Mathieu Grenier, Nicolas Navet

## Abstract

In distributed real-time systems, meeting the real-time constraints is mandatory but the satisfaction of other application-dependent criteria is most generally required as well. In particular, Networked Control Systems (NCS) are known to be sensitive to communication delays such as frame response time jitters. Well known Medium Access Control (MAC) algorithms such Non-Preemptive Deadline Monotonic (NP-DM) or Non-Preemptive Earliest Deadline First (NP-EDF) are efficient in terms of bandwidth usage but they may perform poorly regarding other application dependent performance criteria. This paper highlights a class of on-line scheduling policies targeted at scheduling frames at the MAC level, and provides a schedulability analysis that is valid for all policies within the considered class. As it will be shown, these algorithms are implementable on COTS components (e.g., Controller Area Network controllers) and offer good trade-offs between feasibility and the satisfaction of other application-dependent criteria such as the response time jitter.

## Index Terms

Real time systems, control systems, communication systems, scheduling, protocols, field buses.

## I. INTRODUCTION

*Context of paper:* In distributed real-time systems, the respect of timing constraint is a basic requirement but other application-dependent criteria besides feasibility are of interest. For instance, in Networked Control Systems (NCS), where the control system is distributed through a network, message exchanges induce non-constant delays in the control-loop, which affects the performance and even the stability of the controlled system [1], [2], [3]. The frame scheduling algorithm at the Medium Access Control (MAC) has a large influence on these delays and thus, should be chosen according to the application's performance requirements.

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*Problem definition:* The problem is to devise MAC level scheduling algorithms that are efficient in terms of bandwidth usage as well as for the satisfaction of application dependent criteria. Moreover, as far as possible, these algorithms should be implementable on COTS hardware and induce small overhead. In the following, we will consider that the MAC scheduling algorithm is implemented on top of a priority bus, such as CAN [4], [5], VAN [6] or J1850 [7]. Indeed, priority buses have proven to be effective in a real-time context, and are widely available and used (see, for instance, [8] for CAN timing analysis). In this study, the case where there are statically assigned CAN identifiers is not addressed, how to extend the proposals in that direction is sketched out in the conclusion.

*Related work :* Many studies have been devoted to find scheduling solutions that are well suited to the application's requirements, both for the scheduling of tasks (see [9] for an overview of the studies in that line of research) and the scheduling of messages. In particular, efficient message scheduling schemes have been proposed in [10] and [11] to ensure fairness and bandwidth isolation between streams of messages sent on a CAN bus, respectively with a centralized (i.e., a master node has full control over the scheduling) and decentralized scheme.

Other studies proposed solutions for implementing Non-Preemptive Earliest Deadline First (NP-EDF) in order to achieve a higher network utilization rate while meeting timing constraints. This is done on CAN in [12], [13], [14] with solutions where deadlines are encoded on a logarithmic time scale, which has been shown to minimize the priority inversions due to the limited number of priority bits. In [15], a NP-EDF implementation is proposed on top of FTT-CAN while [16] addresses the same problem when the application makes use of the standardized CAN application layers CAL CiA [17] and CANOpen [18].

Another scheme, published in [19], allows to reduce the response time jitter due to bit-stuffing by introducing some restrictions on the priorities that can be allocated to the stream of frames on a CAN network. To achieve the same goal, the authors in [20], [21] propose a genetic algorithm to adjust the initial offsets of messages in order to reduce transmission jitter (same goal as [22] for the uniprocessor case).

*Overview of the approach:* In this study, the problem addressed is to efficiently grant access to the network at the MAC level. The performance criteria are the schedulability of the systems and the satisfaction of application dependant criteria. The method can handle any criterion as long as there is a way to evaluate the criterion value for all possible configurations. Here, since NCS is the focus of the paper, the response time jitter is the criterion of interest and it is evaluated by simulation. The proposal is comprised of three distinct steps:

- 1) define the properties that a "good" MAC-level real-time scheduling policy must possess and identify a sub-class, particularly promising in terms of performances,
- 2) derive a schedulability analysis for this sub-class class of scheduling policies and address the

implementation issues,

- 3) explore the search space and find out the most efficient policies. Two cases can be distinguished. The case where the policy has to be efficient on average (it can be used with different traffic streams whose characteristics are a priori not known). And, the case where the policy should be fine tuned for a particular application.

*Organisation of the paper:* In section II, the computational model is stated. In section III, the properties required from a “good” scheduling algorithm in the real-time context are exhibited. Among this set of “good” policies, the sub-class considered in the following is presented. In section IV, the implementation issues on top of the CAN priority bus are discussed. Section V is devoted to the schedulability analysis. Finally, experiments showing the effectiveness of the proposal are summarized in section VI.

## II. NETWORK MODEL

This study deals with the scheduling of frames at the Medium Access Control level; in particular it is assumed that segmentation takes place in the upper layers of the communication stack. The access to the bus is granted by an algorithm (e.g., priority based, token bus, etc.) that is termed the *scheduling policy* in the rest of the paper.

### A. Traffic stream model

A set  $\mathcal{F}$  of  $m$  traffic streams is considered. Nodes, interconnected through a network, send the streams. There may be several traffic streams sent by the same node. Each traffic stream  $f_k$  generates and queues periodically frames, where  $f_{k,n}$  denotes the  $n^{th}$  frame of the traffic stream  $f_k$ . By analogy to the periodic task model used in CPU scheduling, a traffic stream  $f_k$  is characterized by a triple  $(C_k, \overline{D}_k, T_k)$  where  $C_k$  is the *worst-case transmission time* of a frame belonging to the stream,  $\overline{D}_k$  the *relative deadline* (i.e. maximum tolerable delay between the transmission request and the reception at all receiving nodes), and  $T_k$  the *inter-arrival time* between two instances of  $f_k$  (as classically done, sporadic streams can be handled by considering the minimum interarrival time as the period). The release time of a frame  $f_{k,n}$  is denoted by  $A_{k,n}$ . For the sake of clarity, jitters in the availability dates are not considered here but they are treated in technical report [9].

### B. Feasibility and optimality

A *concrete* traffic stream  $(f_i, A_{i,1})$  is a stream for which the release time of its first frame  $A_{i,1}$  is known before run-time while the release times of *non-concrete* streams are unknown. A concrete set of traffic streams  $\omega$  is said *feasible* (or *schedulable*) if no frame of the system is received after its

absolute deadline  $D_{k,n} = A_{k,n} + \overline{D}_k$ . A non-concrete set of traffic streams  $\Omega$  is feasible, if all the concrete sets  $\omega$ , which can be generated from  $\Omega$ , are feasible.

A scheduling policy is *optimal* with respect to a certain criterion (e.g. feasibility, average response time) within its class if no other policy of the class performs better with respect to the criterion. In the following, *optimal* is used to mean *optimal* with respect to feasibility. A scheduling policy is *non-concrete optimal* (with respect to feasibility) if it successfully schedules all the non-concrete sets that are schedulable with a policy of the class. As shown in [23], Non-Preemptive Earliest Deadline First (NP-EDF - smaller the absolute deadline, greater the priority) is non-concrete optimal within the class of non-idling policy, where non-idling means that the network is not idle when there are frames waiting for transmission.

### C. Defining policies through priority function.

Priority functions are a convenient way of formally defining in a non-ambiguous manner scheduling policies, which to our best knowledge, was introduced for the first time in [24]. The priority function  $\Gamma_{k,n}(t)$  indicates the priority of a frame  $f_{k,n}$  at time  $t$ . The network is allocated, at each time, according to the *Highest Priority First* (HPF) paradigm.

Function  $\Gamma_{k,n}(t)$  takes its value from a totally ordered set  $\mathcal{P}$ , which is chosen in [24] to be the set of multi-dimensional  $\mathbb{R}$ -valued vectors  $\mathcal{P} = \{(p_1, \dots, p_n) \in \mathbb{R}^n \mid n \in \mathbb{N}\}$  provided with a lexicographical order. Between two vectors, coordinates are compared one by one starting from the left, the first different coordinate decides the priority order with the convention “the smaller the numerical value, the higher the priority”. For instance,  $\Gamma_{i,j}(t) = (3, 4, 5)$  and  $\Gamma_{k,n}(t) = (3, 4, 6)$  implies that  $f_{i,j}$  has a higher priority than  $f_{k,n}$  at time  $t$ . Priority vectors of different sizes can be compared with the same rule as above and the convention that a missing coordinate is the lowest numerical value (e.g.,  $\Gamma_{i,j}(t) = (3, 4, 5)$  and  $\Gamma_{k,n}(t) = (3, 4)$  means that  $f_{k,n}$  has a higher priority than  $f_{i,j}$  at time  $t$ ). Finally, two vectors are equal iff they have the same size and if the components are equal one by one. As it will be explained in section IV, on a priority bus such as CAN, the priority vector can be mapped to the priority coded in the Identifier field of the frames. This allows to take advantage of the “native” arbitration mechanism of the priority bus to perform the arbitration according to the scheduling policy defined by the priority function  $\Gamma_{k,n}(t)$ .

Most real-time scheduling policies can be defined easily using priority functions. For instance, the priority of a frame  $f_{k,n}$  under NP-EDF becomes:

$$\Gamma_{k,n}^{NP-EDF}(t) = \begin{cases} (A_{k,n} + \overline{D}_k, k, n) & \text{if } t < B_{k,n} \\ (-\infty, k, n) & \text{if } t \geq B_{k,n} \end{cases} \quad (1)$$

where  $B_{k,n}$  is the transmission beginning of  $f_{k,n}$  (the last two coordinates  $k, n$  are needed to

ensure decidability, see paragraph III-A). To formally define  $B_{k,n}$ , a scheduling function, denoted by  $\Pi_{k,n}(t) \in \{0, 1\}$ , see [24], indicates which frame  $f_{k,n}$  is being transmitted at time  $t$  (i.e.,  $\Pi_{k,n}(t) = 1$  if  $f_{k,n}$  is being transmitted and  $\Pi_{k,n}(t) = 0$  otherwise). Since single resource systems are considered, at each time  $t$ , there is only one frame being transmitted (i.e., if  $\Pi_{k,n}(t) = 1$  then  $\forall (i, j) \neq (k, n)$   $\Pi_{i,j}(t) = 0$ ), and thus when  $(k, n) \neq (i, j)$  then  $B_{k,n} \neq B_{i,j}$ . The  $-\infty$  value of the first component of the priority vector after the start of transmission (i.e.  $t \geq B_{k,n}$ ) ensures non-preemptiveness. A class of policies of particular interest, to which NP-EDF and NP-DM belong, is the *Priority Promotion at Execution Beginning* policies.

**Definition 1** [24] *A scheduling policy  $\mathcal{A}$  is a Priority Promotion at Execution Beginning (PPEB) policy if the priority of a frame may change only at the start of transmission  $B_{k,n}$  of the frame:*

$$\Gamma_{k,n}^{PPEB}(t) = \begin{cases} \vec{P}_{k,n} & \text{if } t < B_{k,n} \\ \vec{Q}_{k,n} & \text{if } t \geq B_{k,n} \end{cases}, \quad (2)$$

where the priority vector of a frame  $f_{k,n}$  before (resp. after) its execution beginning is  $\vec{P}_{k,n}$  (resp.  $\vec{Q}_{k,n}$ ).

Besides providing non-ambiguous definition of the scheduling policy, priority functions enable us to distinguish classes of scheduling policies and to derive generic results that are valid for all the policies within a certain class. The next section presents the sub-class of non-preemptive scheduling policies that will be studied in the rest of the paper.

### III. STUDY DOMAIN

An arbitrary priority function does not necessarily define a scheduling of interest for real-time computing nor a policy that can be implemented in practice. In this section, the properties required from a ‘good’ scheduling policy are precised, where ‘good’ means a policy that can be implemented in practice and that is suited to real-time computing. Then, among the set of all good policies, the particular class of scheduling policies considered in this study is defined.

#### A. ‘Good’ scheduling policies

A ‘good’ policy must meet a certain number of criteria, which are needed for the policy to be implemented in a real-time context.

*Decidable policies:* Policies must be *decidable*: at any time  $t$ , there is exactly one frame of maximal priority among the set of active frames (i.e. frames which contend for the channel). This concept of decidability was introduced in [24] for the uniprocessor case.

**Definition 2** [24] A priority function is decidable iff, at each time  $t$  such that work is pending, there is exactly one frame with the highest priority among the set of pending frames.

For instance, the last two components of  $\vec{P}_{k,n}^{NP-EDF} = (A_{k,n} + \overline{D}_k, k, n)$  ensure decidability in case of equal deadlines. Note that this property is also required for an implementation on a priority bus.

“Temporal invariant” policies: In this study, for the sake of the system predictability, the only scheduling policies of interest are such that the relative priority between two frames does not depend on the numerical value of the local clocks. This property is required since stations are desynchronized in an unpredictable manner, and it implies that the relative priorities remain the same if the arrivals are “shifted” to the left or to the right. In this case, the policy is independent of the values of the local clocks at start-up time.

Such policies are said *shift temporal invariant* (STI) policies. NP-EDF is a STI policy since the priority between two frames only depends on the offset between arrival dates and on relative deadlines. On the contrary, a policy defined by  $\vec{P}_{k,n} = (C_k \cdot A_{k,n}, k, n)$  is not STI; just consider  $f_{i,1}$  and  $f_{j,1}$  with  $A_{i,1} = 0$ ,  $C_i = 10$  and  $A_{j,1} = 1$  with  $C_j = 1$  and the same two frames except that the arrival dates are shifted to the right by one unit of time.

**Definition 3** Let two concrete traffic stream sets be  $\omega = \{(f_1, A_{1,1}), (f_2, A_{2,1}) \dots (f_n, A_{n,1})\}$  and  $\omega' = \{(f_1, A_{1,1} + \Phi), (f_2, A_{2,1} + \Phi) \dots (f_n, A_{n,1} + \Phi)\}$  where  $\omega'$  is a “shifted” version of  $\omega$  (with  $\Phi \in \mathbb{Z}$ ).

A scheduling policy  $\mathcal{A}$  is Shift Temporal Invariant (STI) iff for all possible  $\Phi \in \mathbb{Z}$ ,  $\forall i, j, k, n$  such that  $(k, n) \neq (i, j)$  (two distinct frames), one has:

$$\begin{aligned} \forall t, \Gamma_{k,n}^{\mathcal{A},\omega}(t) &> (\text{respectively } <) \Gamma_{i,j}^{\mathcal{A},\omega}(t) \implies \\ \Gamma_{k,n}^{\mathcal{A},\omega'}(t + \Phi) &> (\text{respectively } <) \Gamma_{i,j}^{\mathcal{A},\omega'}(t + \Phi) \end{aligned}$$

where  $\Gamma_{k,n}^{\mathcal{A},\omega}(t)$  is the priority of  $f_{k,n}$  of the concrete traffic stream set  $\omega$  at time  $t$ .

*Implementable policies:* For being *implementable* in practice, components of the priority vector must be representable by a limited number of bits (for instance, 11 bits on standard CAN). In the following, coordinates of the priority vector take their value in the set of rational numbers  $\mathbb{Q}$ ; the imprecision due to the limited number of available bits, called “quantization error” as in [12], will be taken into account in the schedulability analysis developed in paragraph V.

Any “good” MAC-level scheduling algorithm intended to be implemented on top of a priority bus has to fulfill the aforementioned properties: the policy must be decidable, shift temporal invariant and implementable. In the next paragraph, the class of non-preemptive policies studied in the rest of the paper is defined.

### B. Search space

The search space belongs to the class of Non-Preemptive “Arrival Time Dependent” policies. First, this class of policies is defined and this choice is justified.

*Non-Preemptive “Arrival Time Dependent” policies:* The term Non-Preemptive “Arrival Time Dependent” (NP-ATD) policies comes from the fact that, within this class, the priority of a frame depends on its arrival time. NP-ATD policies is a sub-class of PPEB policies introduced earlier (see definition 1).

**Definition 4** A Non-Preemptive Arrival Time Dependent policy is a policy whose priority function can be put under the form:

$$\Gamma_{k,n}(t) = \begin{cases} \vec{P}_{k,n} = (A_{k,n} + p_k, k, n) & \text{if } t < B_{k,n} \\ \vec{Q}_{k,n} = (-\infty, k, n) & \text{if } t \geq B_{k,n} \end{cases} \quad (3)$$

where  $p_k$  is a non-negative real number associated to each stream  $f_k$ .

$p_k$  can be an arbitrary numerical value or it can be dependent of some characteristics of the traffic stream (i.e.  $\bar{D}_k$ ,  $T_k$  or  $C_k$ ). For instance, for NP-EDF,  $p_k$  is equal to the relative deadline  $\bar{D}_k$ .

*Motivations for Non-Preemptive Arrival Time Dependent policies:* First of all, NP-ATD policies are “good” scheduling policies:

- decidability is ensured by the last two components of the priority vectors,
- NP-ATD policies are Shift Temporal Invariant, see definition 3, since the relative priority between two frames  $f_{k,n}$  and  $f_{i,j}$  depends only on the offset between arrival dates and on the values of  $p_k$  and  $p_i$ ,
- the policies are implementable; section IV is devoted to the implementation issues.

Second, NP-ATD policies are promising in terms of performances. Indeed, NP-EDF, which is optimal with respect to feasibility with non-concrete traffic streams (see [23]), belongs to this class but there may exist other policies that perform close to NP-EDF in terms of feasibility while having a much better behavior with respect to application-dependent criteria. The experiments presented in paragraph VI confirm this intuition. Third, as it will be shown in paragraph IV, a generic feasibility analysis, through response time bound computation, can be derived for all NP-ATD policies.

## IV. SCHEDULING FRAMES WITH NP-ATD POLICIES

This section deals with the practical issues of implementing NP-ATD policies for scheduling messages at the MAC level. In the following, an implementation on top of the CAN network is considered. Indeed, CAN network is widely used, very cheap and it is a well mastered technology that possesses interesting features for a wide-range of real-time systems. The mechanisms discussed in



the following can be adapted in a straightforward manner to all other priority buses, such as VAN [6] and the J1850 [7].

Several studies [25], [12], [13], [14] have tackled the problem of scheduling messages with NP-EDF, which belongs to NP-ATD policies, on top of CAN. In the following, the solutions in [12] and refined later in [13], [14] are extended to NP-ATD policies.

#### A. Basics of CAN MAC protocol

On CAN, any node may start a transmission when the bus is idle. Possible conflicts are resolved by a priority-based arbitration process. In case of simultaneous transmissions, the highest priority frame will be sent despite the contention with lower priority frames. The arbitration is determined by the identifier of the frames (i.e. their priority) with the convention “the smaller the numerical value, the higher the priority”. There is no need that successive instances of a recurrent frame have the same identifier. This allows the implementation of policies with dynamic priorities such as NP-EDF and NP-ATD policy.

#### B. NP-ATD policies scheduling on CAN

With NP-ATD policies, priority of frames are inversely proportional to  $A_{k,n} + p_k$ . The basic idea [25] is to encode the priority of the frame in the largest part of the identifier. Since it is imposed on CAN that all frames have distinct identifiers, some bits are kept to ensure the uniqueness of the identifier. A solution is to assign a bit pattern distinct for each traffic stream. However, scheduling messages with NP-ATD policies on CAN raises several problems. These problems, explicitly stated in [25], are the same as NP-EDF:

- 1) priorities  $A_{k,n} + p_k$  become larger and larger with time since  $A_{k,n}$  depends on the current clock value,
- 2) the mapping of the priorities to a limited number of bits induces so-called “quantization” errors (see Appendix A): two distinct priorities can be assigned the same identifier due to its limited number of bits.

Without loss of generality, the time can be considered discrete where its granularity is the bit-time (i.e., the time between the emission of two successive bits of the same frame). To solve problem 1, the authors in [25], [12], [13], [14] propose to express the priority relatively to a time origin that is increasing over time. Precisely, the time origin  $t_{start}$  is updated to each new transmission beginning (i.e.  $t_{start} = \max_{k,n}(B_{k,n} \leq t)$ ): it is equal to the transmission time of the very first bit of the frame (Start of Frame bit). The priority of each pending message has to be updated at each new transmission start. This computation induces small overhead. For instance, it is was estimated [14] to be less than 3% on the widely used Siemens C167CR microcontroller.

An effective solution to Problem 2 was developed in [12]. The authors use a logarithmic scale to map deadlines. One can exactly reuse this technique for priorities of NP-ATD policies. The timeline is divided in so-called blocks whose size are exponentially increasing (see Fig. 5 in Appendix A). All blocks are subdivided into the same number of slots. The identifier of a frame is then set to the index of the slot where the deadline falls. This scheme allows to map a set of frames having a large range of priorities to a limited number of priority bits. In [12], it is formally proven that this technique greatly improves the schedulability of the system by limiting quantization errors. Details of priority encoding using logarithmic scale applied to NP-ATD policies are given in Appendix A. Thanks to the technique used, quantization errors are reduced but they cannot be fully avoided and thus have to be taken into account. In the following, a schedulability analysis of NP-ATD policies that includes quantization errors is proposed. It is worth pointing out that, the implementation of NP-ATD policies can be adapted to Token-Ring and CSMA-CD networks as made in [14] for NP-EDF.

## V. SCHEDULABILITY ANALYSIS OF NP-ATD POLICIES

Schedulability can be analysed under NP-EDF using feasibility tests [23] and computation of bounds on the Worst Case Response Times (WCRT) [26], [27]. The aim of this section is to present a schedulability analysis through WCRT bounds with arbitrary deadlines and taking into account the quantization errors. This extends the analysis made in [12], [13], [14] where only the case where deadlines are lower than periods is handled. First, paragraph V-A summarizes existing results on WCRT and applies them to NP-ATD policies. Then, paragraph V-B introduces the overhead brought by quantization errors.

### A. WCRT under NP-EDF: a recap

The response time  $r_k(a)$  of a frame is the time elapsed between its arrival  $a$  and its completion. The set of traffic streams is feasible under a given scheduling policy if the response time of each frame is lower than or equal to the relative deadline. In general, it is not possible to compute the response times of all frames for all foreseeable trajectories of the system; a solution for assessing feasibility is to compute bounds on response times. Such an analysis was derived for preemptive EDF in [28], later for NP-EDF in [26], [27]. In [26], it is shown that the worst case response time of a frame of a traffic stream occurs after a certain arrival pattern termed the ‘‘As Soon As Possible’’ pattern (ASAP for short). The authors use the concept of ‘‘deadline busy period’’ for a frame  $f_{k,n}$ , which is a period of network utilization without idle-time during which only frames with deadline not greater than  $f_{k,n}$  are executed.

**Lemma 1** (lemma 5 in [26]) *A bound on the response time of a frame  $f_k(a)$ , belonging to traffic stream  $f_k$ , released  $a$  units of time after the beginning of its deadline busy period can be found in the deadline busy period induced by the ASAP pattern. The ASAP pattern is the situation where:*

- *all traffic streams, with a relative deadline  $\overline{D}_i$  smaller than or equal to  $a + \overline{D}_k$ , are released from time  $t = 0$  at their maximum rate,*
- *the largest frame among all traffic streams with relative deadline greater than  $a + \overline{D}_k$ , if any, is released at time  $t = -1$ . This constitutes the so-called blocking factor due to non-preemptiveness.*

This lemma allows to compute a bound on the response time  $r_k(a)$  of a traffic stream  $f_k$  released at time  $a$ , denoted  $f_k(a)$  in the following. It was proven [26] that the execution of  $f_k(a)$  starts, at the latest, at the time  $t$  solution of the following equation which can be solved by recurrence:

$$t = W_k(a, t) + \mathcal{B}_k(a) + \left\lfloor \frac{a}{T_k} \right\rfloor \cdot C_k. \quad (4)$$

in which  $t$  is the length  $L_k(a)$  of the “deadline busy period”, and where  $W_k(a, t)$  is an upper bound for the higher priority workload (i.e. work induced by frames of lower or equal deadlines) in an interval of length  $t$  ( $(x)^+ \stackrel{\text{def}}{=} \min(x, 0)$ ):

$$W_k(a, t) = \sum_{i \neq k} \underbrace{\left( \min \left( \left\lfloor \frac{t}{T_i} \right\rfloor + 1, \left\lfloor \frac{a + \overline{D}_k - \overline{D}_i}{T_i} \right\rfloor + 1 \right) \right)^+}_{\substack{\text{maximum number of instances in} \\ \text{interval } t \text{ with a deadline lower} \\ \text{than or equal to } a + \overline{D}_k}} \cdot C_i \quad (5)$$

with  $\mathcal{B}_k(a)$  the blocking factor (i.e. the longest frame having a greater deadline than frame  $f_k(a)$ ):

$$\mathcal{B}_k(a) = \max_{i=1..m} \{C_i \mid \overline{D}_i > a + \overline{D}_k\} - 1 \quad (6)$$

and where the work of the other frames of traffic stream  $f_k$  is:

$$\left\lfloor \frac{a}{T_k} \right\rfloor \cdot C_k \quad (7)$$

Thus, a bound on the response time of a frame  $f_k(a)$  is:

$$r_k(a) = \max \{C_k, L_k(a) + C_k - a\}. \quad (8)$$

The response time bound for  $f_k$  is  $\max_a r_k(a)$ . It would be very time consuming to compute  $r_k(a)$  for all values of  $a$  but it is proven in [28], [26] that the only “significant” values of  $a$  are the elements of the following set  $\mathbf{A}_k$ :

$$\mathbf{A}_k = \{t = n \cdot T_i + \overline{D}_i - \overline{D}_k \mid t \geq 0, t \leq \mathcal{L} - C_k, n \in \mathbb{N}, i = 1..m\} \quad (9)$$

where  $\mathcal{L}$  is the longest busy period (longest time interval in which the resource is not idle, see [28] for computation details). The significant values are the values which imply changes in the higher priority workload computed with equation 5. The next section shows how this analysis can be adapted when priority inversions may occur due to the limited number of bits available for encoding the deadlines.

### B. WCRT under NP-EDF with quantization error

When the logarithmic scale is used, frames which have distinct deadlines can belong to the same slot. The initial priority ordering given by deadlines is then lost and priority inversions may take place. In the worst-case, when computing the WCRT bound of a frame  $f_k(a)$ , all frames having a deadline in the same slot are assumed to be of higher priority than  $f_k(a)$ . Precisely, the higher priority workload is now made of all frames having a deadline lower or equal than  $A_{k,n} + \overline{D}_k + S_k(a, t)$ , where  $S_k(a, t)$  is a bound on the size of the slot where  $a + \overline{D}_k - t_{start}$  falls. Thus the higher priority workload  $W_k(a, t)$  becomes:

$$W_k(a, t) = \sum_{i \neq k} \left( \min \left( \left\lfloor \frac{t}{T_i} \right\rfloor + 1, \left\lfloor \frac{a + \overline{D}_k + S_k(a, t) - \overline{D}_i}{T_i} \right\rfloor + 1 \right) \right)^+ \cdot C_i \quad (10)$$

*Proof:* Let  $u$  be the beginning of a deadline busy period. The goal is to bound, for each traffic stream  $f_i$ , the work induced by frames of  $f_i$  in  $[u, u + t]$ . The number of frames of  $f_i$  in the interval  $[u, u + t]$  is  $n = j_1 - j_0 + 1$  where  $A_{i,j_0} = \min\{A_{i,j} \mid j \in \mathbb{N}, A_{i,j} \geq u\}$  and  $A_{i,j_1} = \max\{A_{i,j} \mid j \in \mathbb{N}, A_{i,j} \leq u + t\}$  are respectively the release times of the first and the last frame of the traffic stream  $f_i$  in the deadline busy period. Let  $A_{i,j_0} \stackrel{\text{def}}{=} u + s_i$ . The work of the last frame of traffic stream  $f_i$  arrived at  $A_{i,j_1}$  is taken into account iff:

- 1)  $f_{i,j_1}$  arrives before the end of the interval  $[u, u + t]$ :

$$A_{i,j_1} \leq u + t \implies A_{i,j_0} + (n - 1) \cdot T_i \leq u + t$$

since  $A_{i,j_0} \stackrel{\text{def}}{=} u + s_i$ ,  $n \leq \frac{t - s_i}{T_i} + 1$  thus  $n = \left\lfloor \frac{t - s_i}{T_i} \right\rfloor + 1$  because  $n \in \mathbb{N}$ .

- 2) Furthermore, the last frame  $f_{i,j_1}$  must have a priority greater than  $f_k(a)$ . For this purpose, we assume that all frames having a deadline belonging to the same slot as  $A_{k,n} + \overline{D}_k - t_{start}$  are of higher priority than  $f_k(a)$ . Thus, frames having a deadline lower or equal than  $A_{k,n} + \overline{D}_k + S_k(a, t)$  are considered to have a higher priority ( $S_k(a, t)$  is an upper bound on the size of the slot to which  $A_{k,n} + \overline{D}_k - t_{start}$  belongs, see [13]).

$$\begin{aligned} A_{i,j_1} + \overline{D}_i - t_{start} &\leq u + a + \overline{D}_k + S_k(a, t) - t_{start} \\ \implies n &\leq \frac{a + \overline{D}_k + S_k(a, t) - \overline{D}_i - s_i}{T_i} + 1 \end{aligned}$$

thus  $n \leq \left\lfloor \frac{a + \overline{D}_k + S_k(a, t) - \overline{D}_i - s_i}{T_i} \right\rfloor + 1$ .

Hence, an upper bound on the number of frames  $n$  induced by a traffic stream  $f_i$  arrived  $s_i$  units of time after

the beginning of the deadline busy period of length  $t$  is:

$$\min \left( \left\lfloor \frac{t - s_i}{T_i} \right\rfloor + 1, \left\lfloor \frac{a + \bar{D}_k + S_k(a, t) - \bar{D}_i - s_i}{T_i} \right\rfloor + 1 \right). \quad (11)$$

This quantity is maximized by the ASAP pattern where  $s_i = 0$ , and the bound becomes:

$$\min \left( \left\lfloor \frac{t}{T_i} \right\rfloor + 1, \left\lfloor \frac{a + \bar{D}_k + S_k(a, t) - \bar{D}_i}{T_i} \right\rfloor + 1 \right).$$

■

*Which  $a$  to analyze:* As shown in [28], [26], the only significant values of  $a$  that are really needed to be analyzed are values which imply changes in the higher priority workload computed by equation 10. Precisely, these values are integral values of the form  $n \cdot T_i + \bar{D}_i - \bar{D}_k - S_k(a, t)$ ; a problem is that the length of the slot  $S_k(a, t)$  is a priori unknown since it depends also on  $a$ . The logarithmic encoding scheme presented in Appendix A ensures that, at any time, the length of a slot takes its value in  $[U, 2^{k_{max}}U]$ , where  $U$  is the length of the first time slot. A solution to capture a change in the higher priority workload is thus to consider all possible values for the slot's length; the set of  $a$  to analyse becomes:

$$\mathbf{A}_k = \{t = n \cdot T_i + \bar{D}_i - \bar{D}_k - x \mid t \geq 0, t \leq \mathcal{L} - C_k, \\ n \in \mathbb{N}, x \in \mathbb{N}, x = U \dots 2^{k_{max}}U, i = 1 \dots m\}. \quad (12)$$

The next section shows how this analysis can be easily adapted to Arrival Time Dependent policies.

### C. WCRT for NP-ATD policies with quantization error

A frame  $f_{k,n}$  under NP-EDF possesses an initial priority vector  $\vec{P}_{k,n}$ , equal to  $(A_{k,n} + \bar{D}_k, k, n)$ ; NP-EDF is thus a particular case of NP-ATD policy where  $p_k = \bar{D}_k$  (see definition of NP-ATD policies in paragraph III-B). In the following, it will be shown that Lemma 1 as well as the set of arrival dates to consider after the ASAP pattern (see equation 9) remain valid with the condition that  $\bar{D}_k$  is replaced by  $p_k$ . “Deadline busy periods” becomes “priority busy periods” for a frame  $f_{k,n}$  which are intervals of network utilization without idle-time during which only frames with higher priority than  $f_{k,n}$  are executed.

**Lemma 2** *A bound on the response time of a frame  $f_k(a)$ , belonging to traffic stream  $f_k$ , released  $a$  units of time after the beginning of its priority busy period can be found in the priority busy period induced by the ASAP pattern. The ASAP pattern is the situation where:*

- all traffic streams with  $p_i$  smaller than or equal to  $a + p_k$ , are released from time  $t = 0$  at their maximum rate,
- the largest frame among all traffic streams with  $p_i$  greater than  $a + p_k$ , if any, is released at time  $t = -1$ . This constitutes the so-called blocking factor due to non-preemptiveness.

*Proof:* Consider virtual NP-EDF, a modified version of NP-EDF that would schedule frames not by taking into account their deadline  $A_{k,n} + \overline{D}_k$  but an arbitrary “virtual” deadline  $A_{k,n} + p_k$ . The priority function of this virtual NP-EDF would be:

$$\Gamma_{k,n}^{virtual\ NP-EDF}(t) = \begin{cases} \vec{P}_{k,n} = (A_{k,n} + p_k, k, n) & \text{if } t < B_{k,n} \\ \vec{Q}_{k,n} = (-\infty, k, n) & \text{if } t \geq B_{k,n} \end{cases}.$$

It is possible to reproduce the proof of equation 11 with  $\overline{D}_k = p_k$  since  $p_k$ , as  $\overline{D}_k$ , possesses the property that its value is equal for all frames of traffic stream  $f_k$ . One obtains an upper bound on the number of frames  $n$  induced by a traffic stream  $f_i$  arrived  $s_i$  unit of time after the beginning of a priority busy period of length  $t$ :

$$\min \left( \left\lfloor \frac{t - s_i}{T_i} \right\rfloor + 1, \left\lfloor \frac{a + p_k + S_k(a, t) - p_i - s_i}{T_i} \right\rfloor + 1 \right), \quad (13)$$

which implies that shifting a frame to the left (i.e., reducing  $s_i$ ) increases the higher priority workload. Thus lemma 1 holds true for virtual NP-EDF as well. According to lemma 1, a response time bound for  $f_k$  under virtual-NP-EDF occurs after the ASAP pattern where  $\overline{D}_k$  is replaced by  $p_k$  in the equations 5, 6 and 9. To assess the feasibility, the response time bounds just have to be compared with the actual relative deadlines  $\overline{D}_k$ . ■

The way to compute the worst case response times under a NP-ATD policy is the same as under NP-EDF except that  $\overline{D}_k$  is replaced by the  $p_k$  value corresponding to the policy in equations 6 and 10.

## VI. EXPERIMENTS

In this following, the performances of NP-ATD scheduling policies are assessed in the context of Networked Control Systems, which is an important application field of our proposal.

### A. Search space

The aim is to find scheduling policies that perform well in terms of feasibility, for optimizing the use of the network bandwidth, but that are also efficient with respect to the criteria important for NCS (defined in VI-B1 and VI-C2). In the following, simulations are done within a sub-class of NP-ATD policies having a priority vector  $\vec{P}_{k,n}$  expressed as:

$$\vec{P}_{k,n} = (A_{k,n} + c \cdot C_k + d \cdot \overline{D}_k, k, n) \text{ with } c \in [0, 50] \text{ and } d \in [0, 1], \quad (14)$$

which means that, in definition 4, one has  $p_k = c \cdot C_k + d \cdot \overline{D}_k$ . Thus, a policy belonging to our search space is defined by a priority function having the form of equation 14. Simulations have shown that parameters  $c \in [0, 50]$  and  $d \in [0, 1]$  define a search space where, most generally, the policies of interest are to be found.

This sub-class of NP-ATD policies was chosen because it is expected to contain policies providing a good trade-off between feasibility and the satisfaction of the other criteria important for NCS

(see VI-B1). Indeed, NP-EDF actually belongs to this class ( $p_k = \overline{D}_k$ ) and policies whose priority function is “close” to NP-EDF are expected to perform similarly in terms of schedulability. On the other hand, introducing a term that depends on the transmission time should help to improve the other criteria. In particular, it has been shown that preemptive Shortest Remaining Processing Time First (SRPTF) is optimal for average response times (see [29], [30] quoted in [31]) and, in our simulations, Non-Preemptive Shortest Maximum Processing Time First (NP-SMPTF), which is the non-preemptive version of SRPTF defined with  $\vec{P}_{k,n} = (C_k, k, n)$ , outperformed NP-EDF for all considered criteria besides feasibility.

In the following, the performances of NP-ATD policies are evaluated against NP-SMPTF and NP-EDF. In addition, Non-Preemptive Deadline Monotonic (NP-DM) is also considered because it is known for its good performances in terms of schedulability<sup>1</sup> and its ease of implementation.

## B. Performance wrt scheduling

1) *Performance criteria*: Classically, a control loop is comprised of the sampling (i.e. data are read from sensors), the computation of the control, and the actuation (i.e. transmission of the control outputs to the actuators). Specific delays have been identified to impact the stability and, more generally, the performances of the system (see, for instance, studies in [32], [1], [3]). These delays include:

- *the input-output latency*: the time elapsed between the sampling and the actuation,
- *the sampling interval*: the time interval between two consecutive sampling points,
- *the sampling latency*: the time elapsed between the theoretical sampling time and its actual occurrence.

In NCS, where the control loop is distributed over a network, data transferred from the sensors to the controller, and from the controller to the actuators are exchanged over a network. The communications from sensors to controller (response time denoted by  $t_{sc}$ ) and from controller to actuators (response time denoted by  $t_{ca}$ ) induce non-constant delays in the input-output latency (equal to  $t_{sc} + \text{computation time} + t_{ca}$ ), and its variability is known to have a crucial influence on the control-loop performances (see, for instance, [1] and experiments of paragraph VI-C). An efficient communication systems should thus minimize communication delays and their variabilities. In the experiments that follow, the impact of NP-ATD policies on the response times of the traffic streams (i.e., delay between the queuing time and the transmission end) is studied.

2) *Simulation setup*: One considers several traffic streams exchanged on a CAN network. As to our best knowledge there are no analytic techniques for evaluating the values of our criteria, simulation is employed. A given criterion is evaluated for a policy as the average value over all traffic streams.

<sup>1</sup>Non-Preemptive Deadline Monotonic is optimal wrt to feasibility for the non preemptive scheduling with  $\overline{D}_k \leq T_k$  when  $\overline{D}_k \leq \overline{D}_i$  implies  $C_k \leq C_i$ , see [26].

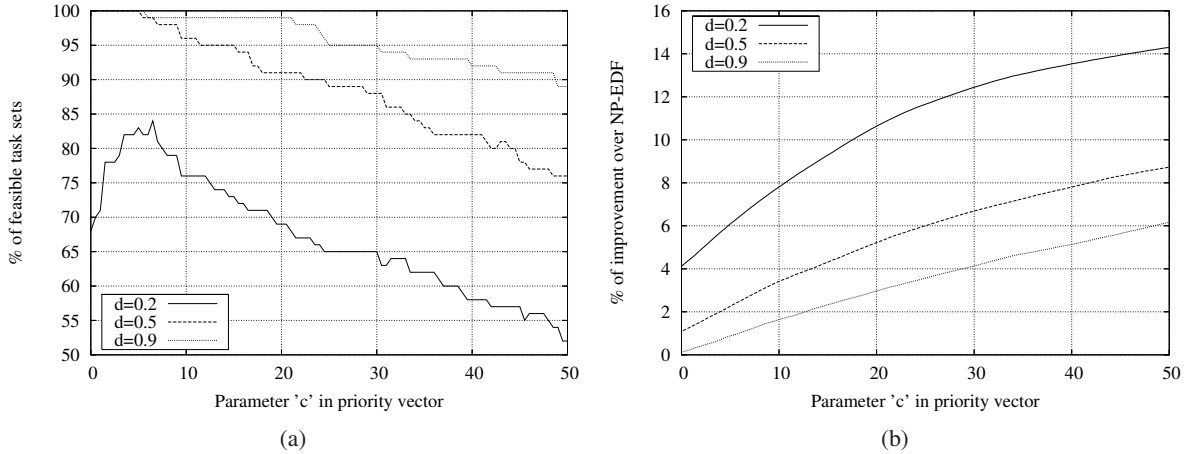


Fig. 1. Feasibility and average response time jitters for policies defined by equation 14 with  $d \in \{0.2, 0.5, 0.9\}$  and  $c$  ranging from 0 to 50. Each point is the average value over 1500 simulations of task sets of cardinality 10 with an average load of 0.65. (a) Feasibility. (b) Average response time jitters.

The byte transmission time is the smallest time unit, which means that the propagation delay and the bit-stuffing are neglected (since bit-stuffing depends on the actual data transmitted, it is out of the scope of this study). The transmission time of a frame, denoted by  $C_k$ , is randomly chosen between 8 and 16 according to a uniform law. The utilisation rate ( $\frac{C_k}{T_k}$ ) of traffic stream  $f_k$  is uniformly distributed in  $[\frac{U}{m} \cdot 0.9, \frac{U}{m} \cdot 1.1]$  where  $U$  is the network load and  $m$  the total number of traffic streams. The relative deadlines  $\bar{D}_k$  are uniformly chosen in the interval  $[T_k - \frac{T_k - C_k}{2}, T_k + \frac{T_k - C_k}{2}]$ . Simulation consists in scheduling concrete sets of traffic streams, which are generated from non-concrete ones by randomly choosing the initial offset for each traffic stream  $f_k$  in the interval  $[0, T_k]$ . Response time bound computations and simulations have been implemented in C++, and an applet version of the simulator is freely available at <http://www.loria.fr/~grenier/logiciel/SimApplet.html>.

3) *Influence of parameters:* In this paragraph it is assessed how the parameters  $c$  and  $d$  influence feasibility and average response time jitters, as measured by the standard deviation of the response times. For the former criterion, the performance for a policy  $\mathcal{A}$  is the percentage of traffic streams that are feasible under NP-EDF and that remains feasible under  $\mathcal{A}$ .

Fig. 1(a) and 1(b) show the performances of the set of policies defined by equation 14 where  $d \in \{0.2, 0.5, 0.9\}$  and  $c$  takes its value in  $[0, 50]$  with steps equal to 0.5. The performances are presented in terms of feasibility in Fig. 1(a) and average response time jitter in Fig. 1(b). The average values are computed over 1500 simulation runs: 100 non-concrete sets of 10 traffic streams with 15 different offsets with a global load randomly chosen in the interval  $[0.6, 0.7]$ . Only task sets that are feasible under NP-EDF were selected.

Two guidelines can be drawn from Fig. 1:

- the larger the value of  $c$  in  $\vec{P}_{k,n}$ , the better the average response time jitters. The counterpart is



that feasibility significantly diminishes when  $c$  increases.

- the larger the value of  $d$  in  $\vec{P}_{k,n}$ , the better the feasibility with the drawback that response time jitters increase.

Indeed, when  $c$  becomes large in equation 14,  $c \cdot C_k$  has more influence than  $A_{k,n}$  and  $d \cdot \bar{D}_k$  on the frame priority. Thus, the policy tends to behave in a similar manner as Non-Preemptive Shortest Maximum Processing Time First (see paragraph VI-A). The same reason explains that when  $d$  increases, the policy performs close to NP-EDF for both criteria. It is worth noting that no significant differences among policies for the average response times are observed. This fact is due to the relatively small variations of transmission time  $C_k$  imposed by the CAN protocol.

For the sake of comparison, table I presents the performances of NP-SMPTF and NP-DM by comparison to NP-EDF with the same simulated task sets. From Fig. 1 and table I, one sees that a

	Feasibility (%)	Avg response time jitter : improvement over NP-EDF
NP-SMPTF	57.5	17.9
NP-DM	100	-4.5

TABLE I  
FEASIBILITY AND AVERAGE RESPONSE TIME JITTERS (IN %) FOR NP-SMPTF AND NP-DM.

well-chosen NP-ATD policy clearly outperforms NP-SMPTF in terms of feasibility (when  $c$  lower than 40), and is better than NP-DM and NP-EDF for the response time jitters. For instance, the policy defined by  $\vec{P}_{k,n} = (A_{k,n} + 18 \cdot C_k + \frac{2}{10} \bar{D}_k, k, n)$  leads to feasible schedules for about 70% of the sets of traffic streams while achieving an average improvement of 10.2% over NP-EDF for the response time jitter. On the same simulation setup, NP-SMPTF is feasible for 57.5% of the traffic stream sets while improving jitters of 17.9%. On the other hand, NP-DM leads to 100% feasible schedules but is worst than NP-EDF regarding the jitters.

In practice, most NCS will have better performances (i.e., lower response time jitter in the simulations) with a well-chosen NP-ATD policy ensuring feasibility than under NP-EDF or NP-DM. Furthermore, feasibility with NP-ATD policy is much better than under NP-SMPTF. NP-ATD policies enable the application designer to implement a MAC level protocol providing a good trade-off between feasibility and application-dependent criteria such as jitter minimization.

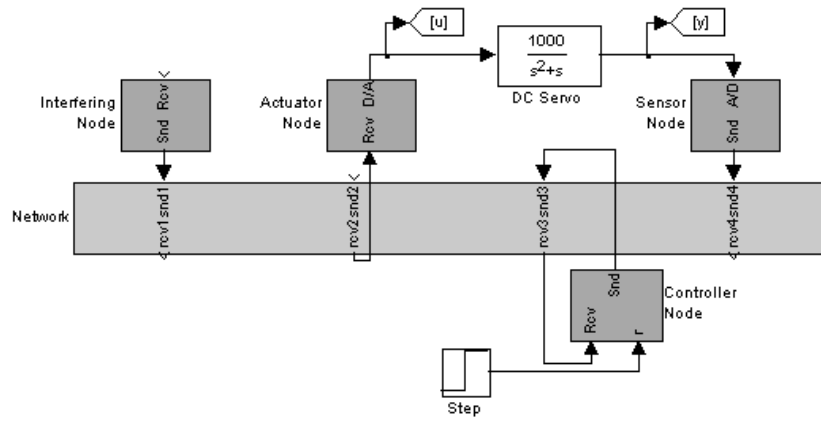


Fig. 2. The architecture of the NCS consists of a control-loop where the sensor, the controller and the actuator nodes are distributed over a CAN network at 125kbit/s. An interfering node generates disturbing traffic.

### C. Control performance

In this part, a particular NCS is studied and the performances of the best feasible NP-ATD policy found are compared to the performances of NP-EDF. The process is a DC servo with a transfer function defined as  $G(s) = \frac{1000}{s^2+s}$ . The system, see Fig. 2, consists of a control-loop where the sensor, the controller and the actuator nodes are distributed over a CAN network at 125kbit/s. There is also an interfering node generating network traffic that models the other real-time traffic streams exchanged on the bus. This system is simulated with the toolbox TrueTime under Matlab/Simulink, and is described in more detail in [33]. For this study, the NP-ATD MAC layer protocol described in section IV-A has been implemented in TrueTime.

1) *Architecture overview:* Precisely, as in [33], the NCS is constituted of:

- a sensor node (one task - periodic) where the sensor task samples the process with a period of 0.01s. Then, the task sends the result  $y(k)$  to the controller over the network ( $C = 80$ bits). The delay between the sampling time and the queuing time is set to  $9 \cdot 10^{-4}$ s.
- a controller node (one task - event driven) where the controller task, each time it receives a frame from the sensor, computes the control output signal  $u(k)$  and sends it to the actuator. The delay between the reception of the frame and the queuing of the control signal frame ( $C = 80$ bits) is set to  $5 \cdot 10^{-4}$ s. A PD-controller is used, and implemented according to the following equations:

$$u(k) = P(k) + D(k),$$

$$P(k) = 1.5 \cdot (r(k) - y(k)),$$

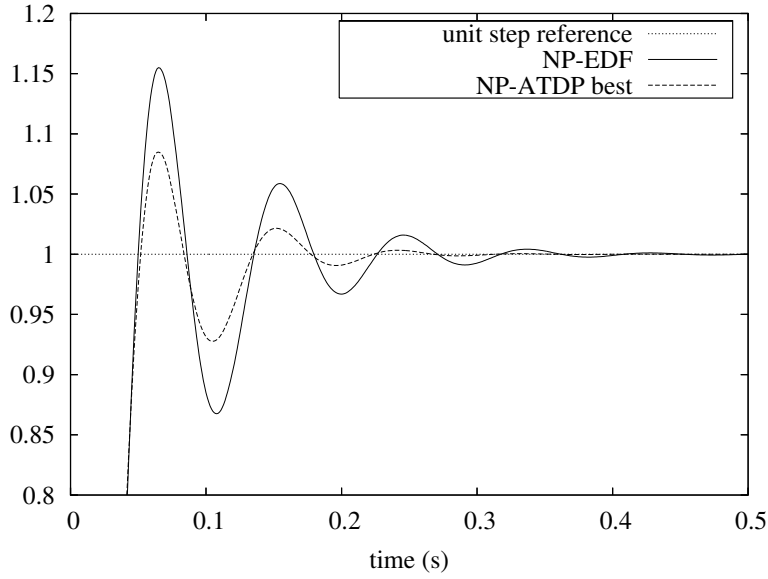


Fig. 3. Unit step response of the NCS with NP-EDF and the best feasible NP-ATD policy found by an exhaustive search ( $c = 35$  and  $d = 0.4$ ). The load is equal to 0.5 .

$$D(k) = 3.5 \cdot 10^{-5} \cdot D(k-1) + 5.25 \cdot (y(k-1) - y(k)),$$

where  $r(k)$ , the reference, is a unit step (see [33] and [34] for more details).

- an actuator node (one task - event-driven) controls the actuator according to the data received in the controller's frame. The delay between the reception of the frame and the actuation is  $5 \cdot 10^{-4}$ s.
- the interfering node (one task - time-driven) generates the disturbing traffic. The set of its traffic streams is randomly generated as follows: for a given load  $U$ , a random traffic stream is iteratively added until the load of the node becomes higher than  $U$ . The period of each traffic stream is set at random according to the uniform law in the set  $\{0.01, 0.02, 0.05, 0.1, 0.5\}$ , and the number of data bytes takes a random value in the interval  $[1, 8]$ .

2) *Performance criteria:* The unit step response of the system (in our simulation, if  $t < 0$ ,  $r(t) = 0$  else  $r(t) = 1$ ) is used with the overshoot  $\bar{O}$ , the settling time  $T_{settling}$  and the *IAE* (Integral of the Absolute magnitude Error) as the performance metrics. In this study,  $IAE = \int_0^{T_{sim}} |e(t)| dt$ , where  $T_{sim} = 0.5$ s is the duration of the simulation, and the settling time  $T_{settling}$  is the time required for the system to settle within 10%.

3) *Simulation results:* Fig. 3 shows an instance of the unit step response of the system (at a load  $U = 0.5$ ) with the best feasible NP-ATD policy of the search space and with NP-EDF. As one can see, the overshoot is reduced from 1.155 to 1.085, while  $T_{settling}$  drops from  $46 \cdot 10^{-3}$  to  $119 \cdot 10^{-3}$  with the best feasible NP-ATD policy.

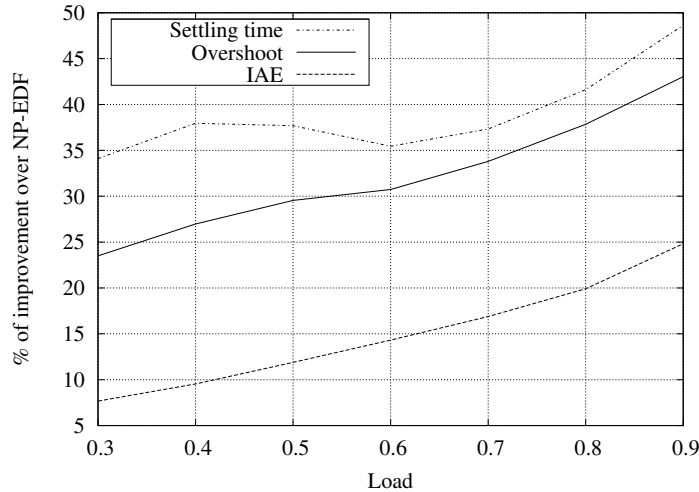


Fig. 4. Average improvement of overshoot, settling time and  $IAE$  over NP-EDF with the best feasible NP-ATD policy found by an exhaustive search.

Fig. 4 presents the average performances improvement (over 100 runs for each point) of the best feasible NP-ATD policy found over NP-EDF for the three performance metrics of interest. It provides clear-cut evidences of the improvement brought by NP-ATD over NP-EDF for the NCS under study. Indeed, the improvement is significant whatever the load and increases with it. For instance, at a load equal to 0.6, the improvement over NP-EDF is 35.5% for the settling time, 30.1% for the overshoot and 14.3% for the  $IAE$ .

## VII. CONCLUSION AND FUTURE WORK

This paper introduces the class of Non-Preemptive Arrival Time Dependent (NP-ATD) policies intended for the scheduling of frames at the MAC level. These policies are implementable on COTS components (e.g., CAN controllers) and provide a good trade-off between feasibility and the satisfaction of other application-dependent criteria such as the response time jitter. An NP-ATD policy can be “built” for the performance requirements of a particular application or be chosen to provide good average performances on random sets of traffic streams.

In order to assess the feasibility of systems using NP-ATD policies, a schedulability analysis that is generic for all policies of the class was proposed. In the context of Networked Control Systems where delays and jitters impact the performances of the control loop, simulations have shown that well chosen policies can bring significant improvements over plain NP-EDF or NP-DM.

In some applications, it can be needed that some CAN identifiers are statically assigned to traffic

streams, which means that NP-ATD would be jointly used with Fixed Priority policy for scheduling the frames at the MAC level. This will require to extend the schedulability analysis presented here, for instance, by adapting the proposals made in [35], [36] to the case of NP-ATD.

In a future work, a more accurate evaluation of the impact of the scheduling policies on the controlled system is intended to be done on real platforms. Another improvement would be to come up with more efficient search techniques for exploring the policy search space; preliminary experiments have shown that a simple neighbourhood technique such a hill-climbing with a Tabu list is more efficient than the exhaustive search. Finally, this work could be extended to other class of policies such as time-sharing policy (e.g., Round-Robin [35], Pfair [37]); the main problem will be here to come up with a schedulability analysis valid for all policies of the class.

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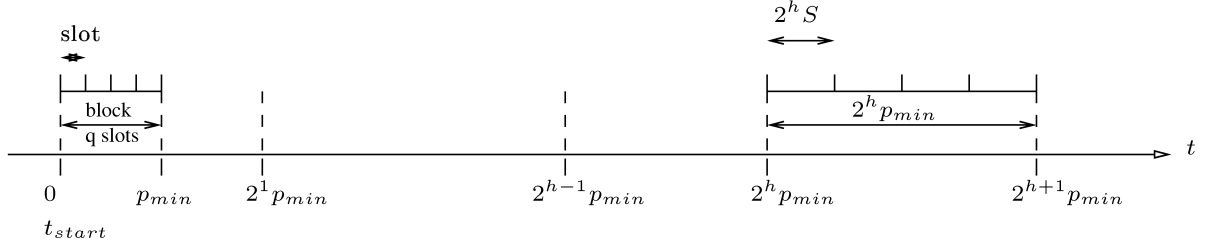


Fig. 5. Logarithmic scale starting at  $t_{start}$ , where  $p_{min}$  is the minimum relative deadline in the traffic stream,  $h$  is the index of the block computed with equation 15 and  $S$  is the size of the first time slot (i.e.  $\frac{p_{min}}{q}$ ).

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## APPENDIX A

### LOGARITHMIC SCALE TO MAP PRIORITY

This appendix presents the logarithmic scale, introduced in [12] for the deadline case, to map the priority  $A_{k,n} + p_k$  of a frame  $f_{k,n}$  to a limited number  $n$  of priority bits in order to reduce quantization errors by providing finer resolution for closer deadline.

An example of a logarithmic scale is shown in Fig. 5. The time origin of the logarithmic scale, denoted by  $t_{start}$ , is updated at each new transmission beginning ( $t_{start} \stackrel{\text{def}}{=} \max_{k,n}(B_{k,n} \leq t)$ , where  $t$  is the current time). Timeline, from  $t_{start}$  to  $p_{max}$  ( $p_{max} \stackrel{\text{def}}{=} \max_{\tau_k \in \mathcal{T}}(p_k)$ ) is divided in blocks of increasing length. Each block is divided into  $q$  slots where  $q$  is an integer known at the design stage (see equation 16). The priority of a frame corresponds to the index of the slot containing the current deadline  $A_{k,n} + p_k - t_{start}$ . Index  $i$ , from [12], is computed as follow:

$$i = h \cdot q + \left\lfloor \frac{A_{k,n} + p_k - t_{start} - 2^h p_{min}}{2^h S} \right\rfloor,$$

where  $U$  is the size of the first time slot ( $U \stackrel{\text{def}}{=} \frac{p_{min}}{q}$  and  $p_{min} \stackrel{\text{def}}{=} \min_{\tau_k \in \mathcal{T}}(p_k)$ ). The index of the block, called  $h$ , where the current deadline  $A_{k,n} + p_k - t_{start}$  falls, from [12], is:

$$h = \begin{cases} \left\lfloor \log_2 \frac{A_{k,n} + p_k - t_{start}}{D_{min}} \right\rfloor & \text{if } A_{k,n} + p_k - t_{start} > p_{min} \\ 0 & \text{otherwise} \end{cases} \quad (15)$$

The number of slots  $q$  in a block (see Appendix A of [12] for computation details) is given by:

$$q = \left\lfloor \frac{2^n}{\left\lceil \log_2 k_{max} \right\rceil + \frac{k_{max}}{2^{\left\lceil \log_2 k_{max} \right\rceil}}} \right\rfloor, \quad (16)$$

where  $k_{max} \stackrel{\text{def}}{=} \frac{p_{max}}{p_{min}}$ . By definition, the size of the slot where  $A_{k,n} + p_k - t_{start}$  "falls" is equal to  $2^h S$ .

When the logarithmic scale is used (or when a limited number of bits are devoted for priority

encoding), frames which have distinct deadlines can belong to the same slot and an inversion of priority may occur. In such a case, these errors are called quantization errors.



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