Eventual Consistency

Marc Shapiro, Bettina Kemme

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None

In a replicated database, the consistency level defines whether and how the values of the replicas of a logical object may diverge in the presence of updates. Eventual consistency is the weakest consistency level that guarantees convergence. Informally, it requires that all replicas of an object will eventually reach the same, correct, final value, assuming that no new updates are submitted to the object.

Eventual consistency is an important correctness criteria in systems with a lazy, update-anywhere strategy, also referred to as *optimistic replication* (q.v.). Update operations can be submitted and executed on any node, and the propagation of updates occurs lazily after commit. Conflict resolution and reconciliation must ensure that all replicas (copies) of a logical object eventually converge to the same value. Different objects are considered independent.

In a system where updates are continuously submitted, eventual consistency can be defined by a weak form of schedule equivalence [1]. A schedule S_n^x describes the sequence of update operations node n performs on its replica of object x. An element of S_n^x represents the execution of an operation w_i that operates on x, submitted by some user. S_n^x contains $\overline{w_i}$ for an operation, if w_i was received by n, but either not executed, or aborted due to conflict resolution.

Typically, two schedules are defined equivalent by restricting how the order of operations in the two schedules may differ. However, for eventual consistency only the convergence of object values matters. Thus, equivalence is defined by comparing the final state of the replicas. Two schedules are said *state equivalent* when, starting from the same initial state, they produce the same final state. For instance: (i) schedules $S = w_1 w_2$ and $S' = w_2 w_1$ are state-equivalent if w_1 and w_2 commute; (ii) schedules $S = w_1 w_2$ and $S' = w_2$ are state-equivalent if w_2 sets the state of the object to a completely new value (e.g., $x := 2$).

Eventual consistency of a replicated object x is defined by the following conditions, which must hold at all times, at any node n with a replica of x [1]. It is assumed that all replicas have the same initial state.

- There is a prefix of the schedule S_n^x that is state-equivalent to a prefix of the schedule $S_{n'}^x$ of any other node n' holding a replica of x. Such a prefix is called a *committed prefix* of S_n^x.

- The committed prefix of S_n^x grows monotonically over time, i.e., the set of operations and their relative order remains unchanged.

- For every operation w_i submitted by a user, either w_i or $\overline{w_i}$ eventually appears in the committed prefix of S_n^x (but not both, and not more than once).

- An operation w_i in the committed prefix satisfies all its preconditions (e.g., the state of the object immediately before the execution of the operation fulfills certain conditions).

As an example, assume operation w_1 sets x to 2, and w_2 sets it to 5. Operation w_1 is submitted and executed at n_1 while w_2 is first executed at n_2. At this time the local schedules are $S_1 = w_1$ and $S_2 = w_2$ and the committed prefix at both nodes is the empty schedule. Now w_1 is propagated to n_2 and w_2 is propagated to n_1. When n_1 receives w_2 it must detect that w_1 and w_2 are concurrent and conflict. Conflict reconciliation could prioritize one of the operations, e.g., w_1. Then, w_2 is simply not executed and the new schedule is $S_1^x = w_1\overline{w_2}$. At n_2, when w_1 arrives, the conflict is also detected, w_2 is undone, w_1 is executed and the final schedule is $S_2 = \overline{w_2}w_1$. At this time, S_1 and S_2 are themselves the committed prefixes. Note that further concurrent operations on x might move the schedules further, but the extensions would still be tentative and only become committed once they are reconciled at all replicas.

Optimistic Replication and Resolution, WAN Replication, Consistency Models for Replicated Data

References

[1] Y. Saito and M. Shapiro. Optimistic Replication. *ACM Computer Surveys*, 37(1): 42-81, 2005.