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The NumPy array: a structure for efficient numerical computation

Stéfan van der Walt, Stellenbosch University SOUTH AFRICA

S. Chris Colbert, Enthought USA

Gael Varoquaux, INRIA Saclay FRANCE

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In the Python world, NumPy arrays are the standard representation for numerical data. Here, we show how these arrays enable efficient implementation of numerical computations in a high-level language. Overall, three techniques are applied to improve performance: vectorizing calculations, avoiding copying data in memory, and minimizing operation counts.

We first present the NumPy array structure, then show how to use it for efficient computation, and finally how to share array data with other libraries.

Introduction

The Python programming language provides a rich set of high-level data structures: lists for enumerating a collection of objects, dictionaries to build hash tables, etc. However, these structures are not ideally suited to high-performance numerical computation.

In the mid-90s, an international team of volunteers started to develop a data-structure for efficient array computation. This structure evolved into what is now known as the N-dimensional NumPy array.

The NumPy package, which comprises the NumPy array as well as a set of accompanying mathematical functions, has found wide-spread adoption in academia, national laboratories, and industry, with applications ranging from gaming to space exploration.

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A NumPy array is a multidimensional, uniform collection of elements. An array is characterized by the type of elements it contains and by its shape. For example, a matrix may be represented as an array of shape $(M \times N)$ that contains numbers, e.g., floating point or complex numbers. Unlike matrices, NumPy arrays can have any dimensionality. Furthermore, they may contain other kinds of elements (or even combinations of elements), such as booleans or dates.

Underneath the hood, a NumPy array is really just a convenient way of describing one or more blocks of computer memory, so that the numbers represented may be easily manipulated.

Basic usage

Throughout the code examples in the article, we assume that NumPy is imported as follows:

```
import numpy as np
```

Code snippets are shown as they appear inside an [IPython] prompt, such as this:

```
In [3]: np.__version__  
Out [3]: '1.4.1'
```

Elements contained in an array can be indexed using the [] operator. In addition, parts of an array may be retrieved using standard Python slicing of the form `start:stop:step`. For instance, the first two rows of an array `x` are given by `x[:2, :]` or columns 1 through 3 by `x[:, 1:4]`. Similarly, every second row is given by `x[::2, :]`. Note that Python uses zero-based indexing.

The structure of a NumPy array: a view on memory

A NumPy array (also called an “ndarray”, short for N-dimensional array) describes memory, using the following attributes:

Data pointer the memory address of the first byte in the array.

Data type description the kind of elements contained in the array, for example floating point numbers or integers.

Shape the shape of the array, for example (10, 10) for a ten-by-ten array, or (5, 5, 5) for a block of data describing a mesh grid of x-, y- and z-coordinates.

Strides the number of bytes to skip in memory to proceed to the next element. For a (10, 10) array of bytes, for example, the strides may be (10, 1), in other words: proceed one byte to get to the next column and ten bytes to locate the next row.

Flags which define whether we are allowed to modify the array, whether memory layout is C- or Fortran-contiguous¹, and so forth.

NumPy’s strided memory model deserves particular attention, as it provides a powerful way of viewing the same memory in different ways without copying data. For example, consider the following integer array:

```
# Generate the integers from zero to eight and
# re pack them into a 3x3 array
```

```
In [1]: x = np.arange(9).reshape((3, 3))
```

```
In [2]: x
Out[2]:
array([[0, 1, 2],
       [3, 4, 5],
       [6, 7, 8]])
```

```
In [3]: x.strides
Out[3]: (24, 8)
```

On our 64-bit system, the default integer data-type occupies 64-bits, or 8 bytes, in memory. The strides therefore describe skipping 3 integers in memory to get to the next row and one to get to the next column. We can

¹In C, memory is laid out in “row major” order, i.e., rows are stored one after another in memory. In Fortran, *columns* are stored successively.

now generate a view on the same memory where we only examine every second element.

```
In [4]: y = x[:, ::2, ::2]
```

```
In [5]: y
Out[5]:
array([[0, 2],
       [6, 8]])
```

```
In [6]: y.strides
Out[6]: (48, 16)
```

The arrays *x* and *y* point to the same memory (i.e., if we modify the values in *y* we also modify those in *x*), but the strides for *y* have been changed so that only every second element is seen along either axis. *y* is said to be a *view* on *x*:

```
In [7]: y[0, 0] = 100
```

```
In [8]: x
Out[8]:
array([[100, 1, 2],
       [ 3, 4, 5],
       [ 6, 7, 8]])
```

Views need not be created using slicing only. By modifying strides, for example, an array can be transposed or reshaped at zero cost (no memory needs to be copied). Moreover, the strides, shape and dtype attributes of an array may be specified manually by the user (provided they are all compatible), enabling a plethora of ways in which to interpret the underlying data.

```
# Transpose the array, using the shorthand "T"
In [9]: xT = x.T
```

```
In [10]: xT
Out[10]:
array([[100, 3, 6],
       [ 1, 4, 7],
       [ 2, 5, 8]])
```

```
In [11]: xT.strides
Out[11]: (8, 24)
```

```
# Change the shape of the array
In [12]: z = x.reshape((1, 9))
In [13]: z
Out[13]: array([[100, 1, 2, 3, 4, 5, 6, 7, 8]])
```

```
In [14]: z.strides
Out[14]: (72, 8)
```

```
# i.e., for the two-dimensional z, 9 * 8 bytes
# to skip over a row of 9 uint8 elements,
# 8 bytes to skip a single element
```

```
# View data as bytes in memory rather than
# 64bit integers
In [15]: z.dtype = np.dtype('uint8')

In [16]: z
Out[17]:
array([[100, 0, 0, ...,
        0, 0, 0, 0, 0, 0]], dtype=uint8)

In [18]: z.shape
Out[19]: (1, 72)

In [20]: z.strides
Out[20]: (72, 1)
```

In each of these cases, the resulting array points to the same memory. The difference lies in the way the data is interpreted, based on shape, strides and data-type. Since no data is copied in memory, these operations are extremely efficient.

Numerical operations on arrays: vectorization

In any scripting language, unjudicious use of for-loops may lead to poor performance, particularly in the case where a simple computation is applied to each element of a large data-set.

Grouping these element-wise operations together, a process known as vectorisation, allows NumPy to perform such computations much more rapidly. Suppose we have a vector *a* and wish to multiply its magnitude by 3. A traditional for-loop approach would look as follows:

```
In [21]: a = [1, 3, 5]

In [22]: b = [3*x for x in a]

In [23]: b
Out[23]: [3, 9, 15]
```

The vectorized approach applies this operation to all elements of an array:

```
In [24]: a = np.array([1, 3, 5])

In [25]: b = 3 * a

In [26]: b
Out[26]: array([ 3,  9, 15])
```

Vectorized operations in NumPy are implemented in C, resulting in a significant speed improvement. Operations are not restricted to interactions between scalars and arrays. For example, here

NumPy performs a fast element-wise subtraction of two arrays:

```
In [27]: b - a
Out [27]: array([2,  6, 10])
```

When the shapes of the two arguments are not the same, but share a common shape dimension, the operation is *broadcast* across the array. In other words, NumPy expands the arrays such that the operation becomes viable:

```
In [28]: m = np.arange(6).reshape((2,3))

In [29]: m
Out [29]:
array([[0, 1, 2],
       [3, 4, 5]])

In [30]: b + m
Out [30]:
array([[ 3, 10, 17],
       [ 6, 13, 20]])
```

Refer to “Broadcasting Rules” to see when these operations are viable.

To save memory, the broadcasted arrays are never physically constructed; NumPy simply uses the appropriate array elements during computation²

Broadcasting Rules

Before broadcasting two arrays, NumPy verifies that all dimensions are suitably matched. Dimensions match when they are equal, or when either is 1 or None. In the latter case, the dimension of the output array is expanded to the larger of the two.

For example, consider arrays *x* and *y* with shapes (2, 4, 3) and (4, 1) respectively. These arrays are to be combined in a broadcasting operation such as *z = x + y*. We match their dimensions as follows:

$$\begin{array}{r} x \quad (2, 4, 3) \\ y \quad (\quad 4, 1) \\ \hline z \quad (2, 4, 3) \end{array}$$

Therefore, the dimensions of these arrays are compatible, and yield and output of shape (2, 4, 3).

Vectorization and broadcasting examples Evaluating Functions

Suppose we wish to evaluate a function *f* over a large set of numbers, *x*, stored as an array.

² Under the hood, this is achieved by using strides of zero.

Using a for-loop, the result is produced as follows:

```
In [31]: def f(x):
...:     return x**2 - 3*x + 4
...:
In [32]: x = np.arange(1e5)
In [33]: y = [f(i) for i in x]
```

On our machine, this loop executes in approximately 500 milliseconds. Applying the function `f` on the NumPy array `x` engages the fast, vectorized loop, which operates on each element individually:

```
In [34]: y = f(x)
In [35]: y
Out[35]:
array([ 4.0000e+0,  2.0000e+0,  2.0000e+0, ...,
        9.9991e+9,  9.9993e+9,  9.9995e+9])
```

The vectorized computation executes in 1 millisecond.

As the length of the input array `x` grows, however, execution speed decreases due to the construction of large temporary arrays. For example, the operation above roughly translates to

```
a = x**2
b = 3*x
c = a - b
fx = c + 4
```

Most array-based systems do not provide a way to circumvent the creation of these temporaries. With NumPy, the user may choose to perform operations “in-place”—in other words, in such a way that no new memory is allocated and all results are stored in the current array.

```
def g(x):
    # Allocate the output array with x-squared
    fx = x**2
    # In-place operations: no new memory allocated
    fx -= 3*x
    fx += 4
    return fx
```

Applying `g` to `x` takes 600 microseconds; almost twice as fast as the naive vectorization. Note that we did not compute `3*x` in-place, as it would modify the original data in `x`.

This example illustrates the ease with which NumPy handles vectorized array operations, without relinquishing control over performance-critical aspects such as memory allocation.

Note that performance may be boosted even fur-

ther by using tools such as [Cython], [Theano] or [numexpr], which lessen the load on the memory bus. Cython, a Python to C compiler discussed later in this issue, is especially useful in cases where code cannot be vectorized easily.

Finite Differencing

The derivative on a discrete sequence is often computed using finite differencing. Slicing makes this operation trivial.

Suppose we have an $n + 1$ length vector and perform a forward divided difference.

```
In [36]: x = np.arange(0, 10, 2)
In [37]: x
Out[37]: array([ 0,  2,  4,  6,  8])
In [38]: y = x**2
In [39]: y
Out[39]: array([ 0,  4, 16, 36, 64])
In [40]: dy_dx = (y[1:]-y[:-1])/(x[1:]-x[:-1])
In [41]: dy_dx
Out[41]: array([ 2,  6, 10, 14, 18])
```

In this example, `y[1:]` takes a slice of the `y` array starting at index 1 and continuing to the end of the array. `y[:-1]` takes a slice which starts at index 0 and continues to one index short of the end of the array. Thus `y[1:] - y[:-1]` has the effect of subtracting, from each element in the array, the element directly preceding it. Performing the same differencing on the `x` array and dividing the two resulting arrays yields the forward divided difference.

If we assume that the vectors are length $n + 2$, then calculating the central divided difference is simply a matter of modifying the slices:

```
In [42]: dy_dx_c = (y[2:]-y[:-2])/(x[2:]-x[:-2])
In [43]: dy_dx_c
Out[43]: array([ 4,  8, 12, 16])
```

In Pure Python, these operation would be written using a for loop. For `x` containing 1000 elements, the NumPy implementation is 100 times faster.

Creating a grid using broadcasting

Suppose we want to produce a three-dimensional grid of distances $R_{ijk} = \sqrt{i^2 + j^2 + k^2}$ with $i = -100 \dots 99$, $j = -100 \dots 99$, and

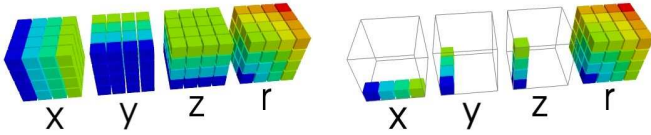


Figure 1: Computing dense grid values without and with broadcasting. Note how, with broadcasting, much less memory is used.

$k = -100 \dots 99$. In most vectorized programming languages, this would require forming three intermediate 200×200 arrays, i , j , and k as in:

```
In [44]: i, j, k = np.mgrid[-100:100, -100:100,
...: -100:100]
```

```
In [45]: print i.shape, j.shape, k.shape
(200, 200, 200) (200, 200, 200) (200, 200, 200)
```

```
In [46]: R = np.sqrt(i**2 + j**2 + k**2)
```

```
In [47]: R.shape
Out[47]: (200, 200, 200)
```

Note the use of the special `mgrid` object, which produces a meshgrid when sliced.

In this case we have allocated 4 named arrays, i , j , k , R and an additional 5 temporary arrays over the course of the operation. Each of these arrays contains roughly 64MB of data resulting in a total memory allocation of ~ 576 MB. In total, 48 million operations are performed: 200^3 to square each array and 200^3 per addition.

In a non-vectorized language, no temporary arrays need to be allocated when the output values are calculated in a nested for-loop, e.g. (in C):

```
int R[200][200][200];
int i, j, k;

for (i = -100; i < 100; i++)
  for (j = -100; j < 100; j++)
    for (k = -100; k < 100; k++)
      R[i][j][k] = sqrt(i*i + j*j + k*k);
```

We can achieve a similar effect using NumPy's broadcasting facilities. Instead of constructing large temporary arrays, we instruct NumPy to combine three one-dimensional vectors (a row-vector, a column-vector and a depth-vector) to form the three-dimensional result. Broadcasting does not require large intermediate arrays.

First, construct the three coordinate vectors (i for the x-axis, j for the y-axis and k for the z-axis):

```
# Construct the row vector: from -100 to +100
i = np.arange(-100, 100).reshape(200, 1, 1)
```

```
# Construct the column vector
j = np.reshape(i, (1, 200, 1))
```

```
# Construct the depth vector
k = np.reshape(i, (1, 1, 200))
```

NumPy also provides a short-hand for the above construction, namely

```
i, j, k = np.ogrid[-100:100, -100:100, -100:100]
```

Note how the arrays contain the same number of elements, but that they have different orientations. We now let NumPy broadcast i , j and k to form the three-dimensional result, as shown in Fig. 1.:

```
In [48]: R = np.sqrt(i**2 + j**2 + k**2)
```

```
In [49]: R.shape
Out[49]: (200, 200, 200)
```

Here, the total memory allocation is only 128MB: 4 named arrays totalling ~ 64 Mb (1.6 KB $\times 3 + 64$ MB) and 5 temporary arrays of ~ 64 MB (1.6 KB $\times 3 + 320$ KB + 64MB). A total of approximately 16 million operations are performed: 200 to square each array, 200^2 for the first addition, and 200^3 each for the second addition as well as for the square root.

When using naive vectorization, calculating R requires 410ms to compute. Broadcasting reduces this time to 182ms—a factor 2 speed-up along with a significant reduction in memory use.

Computer Vision

Consider an $n \times 3$ array of three dimensional points and a 3×3 camera matrix:

```
points = np.random.random((100000, 3))
camera = np.array([[500., 0., 320.],
                  [ 0., 500., 240.],
                  [ 0., 0., 1.]])
```

Often, we want to transform the 3D coordinates into their 2D pixel locations on the image, as viewed by the camera. This operation involves taking the matrix dot product of each point with the camera matrix, and then dividing the resulting vector by its third component. With NumPy, it is written as:

```
# Perform the matrix product on the coordinates
vecs = camera.dot(points.T).T

# Divide resulting coordinates by their z-value
pixel_coords = vecs/vecs[:, 2, np.newaxis]
```

The `dot` function³ implements the matrix product, in contrast to the element-wise product `*`. It can be applied to one- or two-dimensional arrays. This code executes in 9 milliseconds—a 70x speedup over a Python for-loop version.

Aside from the optimized NumPy `dot` product, we make use of NumPy’s array operations with element-by-element division and the broadcasting machinery. The code `new_vecs / new_vecs[:, 2, np.newaxis]` divides each column of `new_vecs` by its third column (in other words, each row is divided by its third element). The `np.newaxis` index is used to change `new_vecs[:, 2]` into a column-vector so that broadcasting may take place.

The above examples show how vectorization provides a powerful and efficient means of operating on large arrays, without compromising clear and concise code or relinquishing control over aspects such as memory allocation.

It should be noted that vectorization and broadcasting is no panacea; for example, when repeated operations take place on very large chunks of memory, it may be better to use an outer for-loop combined with a vectorised inner loop to make optimal use of the system cache.

Sharing data

As shown above, performance is often improved by preventing repeated copying of data in memory. In this section, we show how NumPy may make use of foreign memory—in other words, memory that is not allocated or controlled by NumPy—without copying data.

Efficient I/O with memory mapping

An array stored on disk may be addressed directly without copying it to memory in its entirety. This technique, known as *memory mapping*, is useful for addressing only a small portion of a very large array. NumPy supports

³ The `dot` function leverages accelerated BLAS implementations, if available.

memory mapped arrays with the same interface as any other NumPy array. First, let us construct such an array and fill it with some data:

```
In [50]: a = np.memmap('/tmp/myarray.memmap',
...: mode='write', shape=(300, 300),
...: dtype=np.int)

# Pretend "a" is a one-dimensional, 300*300
# array and assign values into it
In [51]: a.flat = np.arange(300* 300)

In [52]: a
Out[52]:
memmap([[ 0, 1, ..., 298, 299],
 [ 300, 301, ..., 598, 599],
 [ 600, 601, ..., 898, 899],
 ...,
 [89100, 89101, ..., 89398, 89399],
 [89400, 89401, ..., 89698, 89699],
 [89700, 89701, ..., 89998, 89999]])
```

When the “flush” method is called, its data is written to disk:

```
In [53]: a.flush()
```

The array can now be loaded and parts of it manipulated; calling “flush” writes the altered data back to disk:

```
# Load the memory mapped array
In [54]: b = np.memmap('/tmp/myarray.memmap',
...: mode='r+', shape=(300, 300),
...: dtype=np.int)

# Perform some operation on the elements of b
In [55]: b[100, :] *= 2

# Store the modifications to disk
In [56]: b.flush()
```

The array interface for foreign blocks of memory

Often, NumPy arrays have to be created from memory constructed and populated by foreign code, e.g., a result produced by an external C++ or Fortran library.

To facilitate such exchanges without copying the already allocated memory, NumPy defines an **array interface** that specifies how a given object exposes a block of memory. NumPy knows how to view any object with a valid `__array_interface__` dictionary attribute as an array. Its most important values are `data` (address of the data in memory), `shape` and `typestr` (the kind of elements stored).

The following example defines a `MutableString` class that allocates a string `_s`. The `MutableString` represents a foreign block of memory, now made available to NumPy by defining the `__array_interface__` dictionary.

Note the use of the `ctypes` library, which allows Python to execute code directly from dynamic C libraries. In this instance, we use its utility function, `create_string_buffer`, to allocate a string in memory and `addressof` to establish its position in memory.

```
import ctypes

class MutableString(object):
    def __init__(self, s):
        # Allocate string memory
        self._s = ctypes.create_string_buffer(s)

        self.__array_interface__ = {
            # Shape of the array
            'shape': (len(s),),

            # Address of data,
            # the memory is not read-only
            'data': (ctypes.addressof(self._s), False),

            # Stores 1-byte unsigned integers.
            # "|" indicates that Endianess is
            # irrelevant for this data-type.
            'typestr': '|u1',
        }

    def __str__(self):
        "Convert to a string for printing."
        return str(buffer(self._s))
```

The above class is instantiated, after which NumPy is asked to interpret it as an array, which is possible because of its `__array_interface__` attribute.

```
# Create an instance of our mutable string class
In [57]: m = MutableString('abcde')

# View the character byte values as an array
In [58]: am = np.asarray(m)

In [59]: am
Out[59]: array([ 97,  98,  99, 100, 101],
               dtype=uint8)

# Modify the values of the array
In [60]: am += 2

In [61]: am
Out[61]: array([ 99, 100, 101, 102, 103],
               dtype=uint8)
```

```
# Since the underlying memory was updated,
# the string now has a different value.
In [62]: print m
cdefg
```

This example illustrates how NumPy is able to interpret any block of memory, as long as the necessary information is provided via an `__array_interface__` dictionary.

Structured data-types to expose complex data

NumPy arrays are homogeneous, in other words, each element of the array has the same data-type. Traditionally, we think of the fundamental data-types: integers, floats, etc. However, NumPy arrays may also store compound elements, such as the combination (1, 0.5) – an array *and* a float. Arrays that store such compound elements are known as structured arrays.

Imagine an experiment in which measurements of the following fields are recorded:

- Timestamp in nanoseconds (a 64-bit unsigned integer)
- Position (x- and y-coordinates, stored as floating point numbers)

We can describe these fields using a single data-type:

```
In [63]: dt = np.dtype([('time', np.uint64),
...:                   ('pos', [('x', float),
...:                             ('y', float)])])
```

An array of measurements can then be constructed using this data-type as

```
In [64]: x = np.array([(1, (0, 0.5)),
...:                  (2, (0, 10.3)),
...:                  (3, (5.5, 1.1))],
...:                  dtype=dt)
```

The individual fields of such a structured array can be queried:

```
# Display all time-stamps
In [65]: x['time']
Out[65]: array([1, 2, 3], dtype=uint64)

# Display x-coordinates for all timestamps >= 2
In [66]: times = (x['time'] >= 2)

In [67]: print times
[False True True]

In [68]: x[times]['pos']['x']
Out[68]: array([ 0. ,  5.5])
```


Structured arrays are useful for reading complex binary files. Suppose we have a file “foo.dat” that contains binary data structured according to the data-type ‘dt’ introduced above: for each record, the first 8 bytes are a 64-bit unsigned integer time stamp and the next 16 bytes a position comprised of a 64-bit floating point ‘x’ position and a floating point ‘y’ position.

Loading such data manually is cumbersome: for each field in the record, bytes are read from file and converted to the appropriate data-type, taking into consideration factors such as endianness.

In contrast, using a structured data-type simplifies this operation to a single line of code:

```
In [69]: data = np.fromfile("foo.dat", dtype=dt)
```

Conclusion

We show that the N-dimensional array introduced by NumPy is a high-level data structure that facilitates vectorization of for-loops. Its sophisticated memory description allows a wide variety of operations to be performed without copying any data in memory, bringing significant performance gains as data-sets grow large. Arrays of multiple dimensions may be combined using *broadcasting* to reduce the number of operations performed during numerical computation.

When NumPy is skillfully applied, most computation time is spent on vectorized array operations, instead of in Python for-loops (which are often a bottleneck). Further speed improvements are achieved by optimizing compilers, such as Cython, which better exploit cache effects.

NumPy and similar projects foster an environment in which numerical problems may be described using high-level code, thereby opening the door to scientific code that is both transparent and easy to maintain.

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NumPy’s documentation is maintained using a Wikipedia-like community forum, available at <http://docs.scipy.org/>. Discussions take place on the project mailing list (<http://www.scipy.org/MailingLists>). NumPy is a volunteer effort.