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Key Reduction of McEliece's Cryptosystem Using List Decoding

Morgan Barbier* Paulo S. L. M. Barreto†

Abstract

Different variants of the code-based McEliece cryptosystem were proposed to reduce the size of the public key. All these variants use very structured codes, which open the door to new attacks exploiting the underlying structure. In this paper, we show that the dyadic variant can be designed to resist all known attacks. In light of a new study on list decoding algorithms for binary Goppa codes, we explain how to increase the security level for given public key sizes. Using the state-of-the-art list decoding algorithm instead of unique decoding, we exhibit a key size gain of about 4% for the standard McEliece cryptosystem and up to 21% for the adjusted dyadic variant.

1 Introduction

The past few years have seen a renewed interest in code-based cryptosystems due to their resistance to known quantum attacks [9]. The famous McEliece asymmetric cryptosystem [19] is perhaps the most studied of them. The private key is the generator matrix of a code \mathcal{C} and the public key is obtained from this generator matrix by a permutation of its columns followed by a multiplication by an random invertible matrix. This public key is thus a generator matrix of a code \mathcal{C}' equivalent to \mathcal{C} . The encryption consists in encoding the plaintext into a codeword $c' \in \mathcal{C}'$ using the public key and randomly adding as many errors as made possible by the decoding algorithm of \mathcal{C} . The decryption step consists in decoding the ciphertext over \mathcal{C} , thanks to the private key.

The McEliece cryptosystem delivers high encryption and decryption speeds compared to other systems like RSA [20] but suffers from the large size of the associated keys which makes it unpractical. Lately, a lot of effort has been put into the design of variants based on different code families in order to reduce the size of the keys. For example, in 2008, a solution was proposed for signature

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schemes using double-circulant matrices [1]. In [4], the authors proposed a key reduction for the McEliece cryptosystem using quasi-cyclic alternant codes. The same year, a method using the sub-family of classical binary Goppa codes, called quasi-dyadic codes, was introduced in [20], adapting the idea from [4]. Another key reduction technique formulated in [5] hides the structure of a subcode of generalized Reed-Solomon codes. Generally speaking, all of these key reduction techniques involve the introduction of some kind of additional structure. As a cryptographic rule of thumb, the presence of unneeded structure is often seen as a potential angle of attack. Indeed, cryptanalysts quickly proposed new structural attacks against the aforementioned variants [14, 23, 27].

Roughly speaking, we can distinguish between two types of attacks. The first type tries to recover the plaintext from the cyphertext, without the knowledge of the private key. It is clear that increasing the number of errors during the encryption step will make this kind of attacks more difficult. Bernstein, Lange and Peters contributed to assess the effectiveness of such attacks in [11] by giving asymptotic analysis of different decoding algorithms for code-based cryptography. Moreover, working within a strict complexity model, Finiasz and Sendrier exhibited lower bounds for system designers [15] by taking into account the costs of the best decoding attacks [27].

The second type of attacks consists in retrieving the private key from the available public one. Such an attack was recently introduced in [14] and boils down to computing a Groebner basis to find the structure of an alternant code. The McEliece variant with the parameters proposed in [4] is considered to be broken by this attack. While the dyadic instance from [20] is also vulnerable, this variant can be made more robust as shown in Section 3.

This paper is organised as follows. Section 2 is devoted to the decoding of binary Goppa codes, most precisely on the correction radius of different decoding algorithms. In Section 3 we show how the dyadic variant can be made more secure against [14] and present our results on keysize reduction obtained using the best known list decoding algorithm for the classical and modified, hardened variants of the McEliece cryptosystem.

2 List decoding of binary Goppa Codes

Since a major part of the cryptanalysis of code-based cryptography is intimately linked to error correction, a natural idea is to add as many errors as possible during the encryption step, provided that the recipient is still able to correct them. Decoding a random code is a hard problem; indeed it was shown that decoding general codes is NP-complete [6]. The McEliece cryptosystem originally used binary Goppa codes. Some variants are based on different types of codes (*e.g.* [5]), but most of them have been broken (*e.g.* [23]). In

the following, we briefly recall the state of the art of the decoding of binary Goppa codes, which are perhaps the most promising for McEliece cryptosystems.

The first algebraic decoding algorithm for classical Goppa codes was proposed by Patterson in 1975 [25]. This algorithm, basically a variation of the Berlekamp-Massey algorithm [7], runs in quadratic time in the code length. Patterson's method performs an unambiguous decoding, up to the error capacity t of the code. Since classical Goppa codes are alternant, that is they are subfield subcodes of generalised Reed-Solomon codes [18], we are able to perform the well-known Guruswami-Sudan list decoding (GS-LD) algorithm [16]. This method makes it possible to correct up to the generic Johnson bound given by $n \left(1 - \sqrt{1 - \frac{2t}{n}}\right)$ errors, which is larger than t (see Figure 1). Consequently, this type of decoding does not ensure the uniqueness of the returned codewords anymore. The GS-LD algorithm is originally not tailored to the binary Goppa codes. Using specific properties of binary Goppa codes, Bernstein was able to extend Patterson's algorithm to perform a list decoding up to $n \left(1 - \sqrt{1 - \frac{2t+2}{n}}\right)$ [8], which is larger than the generic Johnson bound. Recently, a technical report [2] revisits previous works to exhibit a list decoding algorithm for square-free binary Goppa codes which decodes up to the *binary* Johnson bound given by $\tau_2 \triangleq \frac{n}{2} \left(1 - \sqrt{1 - \frac{4t+2}{n}}\right)$, which is larger than the two former bounds. As shown in Figure 1, the closer the normalized distance is to 0.5, the better the binary Johnson bound is compared to the others. We will show in Section 3 that using binary Goppa codes with normalized minimum distances closer to 0.5 makes it possible to correct more errors and ultimately, to reduce the size of the keys.

List decoding algorithms basically involve two steps. The first stage finds, by interpolation, a bivariate polynomial connecting the received word with the support of the code. The second step consists in finding the roots of this polynomial. The cost of the algorithm from [2] is dominated by the interpolation step. This algorithm has an overall complexity of $\mathcal{O}(n^2 \epsilon^{-5})$ and corrects up to $(1 - \epsilon)\tau_2$ errors, where τ_2 is the binary Johnson bound. Decoding τ_2 errors is obviously prohibitively expensive but trade-offs between running time and number of corrected errors are easily achieved, making it possible to keep the cost of list decoding under control.

The classical McEliece or equivalently the Niederreiter cryptosystems [17,21] suffer from chosen cyphertext attacks [28]. Indeed, since a given plaintext can be encrypted to give different cyphertexts, an attacker could compare these different cyphertexts to extract the original plaintext. Different methods were proposed to make these cryptosystems more robust to chosen cyphertext attacks [13,24,26] leading to so-called CCA2-secure variants. When adding more errors than can be uniquely corrected, the decryption step will return a list of potential plaintexts. As already remarked in [10], CCA2-secure variants make

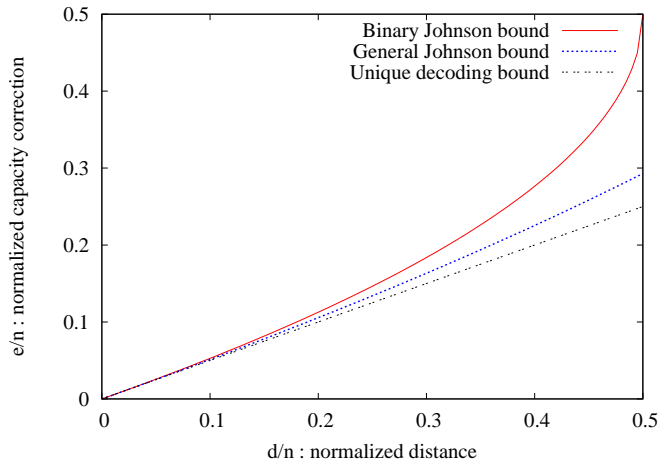


Figure 1: Comparison between the unambiguous decoding, generic and binary Johnson’s bounds.

it possible to distinguish the original plaintext between all candidates returned by the list decoding algorithm used in the decryption process. Consequently, it is possible to make the task for an attacker much more difficult by adding more errors than the correction capacity. Using CCA2-secure variants and state-of-the-art list decoding algorithm, these extra-errors only add a small burden on the recipient to find the original plaintext.

3 Key reduction

Encrypting and decrypting with the McEliece cryptosystem is significantly faster than with more widespread cryptosystems based on number theory such as the ubiquitous RSA [20]. The main and perhaps only handicap holding back the McEliece cryptosystem is the substantially larger size of the public keys. We propose to address this problem not by using a well structured code as is often the case, but by adding as many errors as permitted by the best known list decoding algorithm [2]. For a given keysize, this increases the security level. Symmetrically, this makes it possible to use shorter keys while keeping a similar security level. Using a list decoding algorithm can thus lead to shorter keys at the expense of a moderately increased decryption time.

We focus on the family of square-free binary Goppa codes, which includes the traditionally used family of irreducible binary Goppa codes. In this case the error capacity t is equal to r the degree of Goppa polynomial. The algorithm decoding the largest number of errors for these codes is studied in [2]. This list decoding algorithm works for all alternant codes, but using proposition 1

improves the correction radius and leads to even shorter keys. We numerically searched for codes parameters yielding short keys and correcting up to $\lceil \tau_2 \rceil - 1$. We illustrate the benefits of list decoding by presenting examples for both the generic and dyadic variants.

3.1 Generic variant

Tables 1, 2 and 3 show the keysize reduction obtained using the best known list decoding algorithm [2], for workfactors (WF) equal to 2^{80} , 2^{112} , 2^{192} and 2^{256} . For each workfactors, McEliece keysizes are given for Unambiguous Decoding (U.D.) and List Decoding (L.D.). The involved codes are defined by m , the degree of the extension where G and \mathcal{L} are defined, the length n , the dimension k , the degree r of the Goppa polynomial G , and τ_2 is the binary Johnson bound reached by the list decoding algorithm. The workfactors have been estimated using the complexity model and the lower bounds given in [15].

Table 1: Comparison between the public keysize of generic McEliece cryptosystem using unambiguous and list decoding for given workfactors.

| Method | m | n | k | r | τ_2 | WF | Keysize | gain (%) |
|--------|-----|------|------|-----|----------|---------|---------|----------|
| U.D. | 11 | 1893 | 1431 | 42 | | 80.025 | 661122 | |
| L.D. | 11 | 1876 | 1436 | 40 | 41 | 80.043 | 631840 | 4.43 |
| U.D. | 12 | 2887 | 2191 | 58 | | 112.002 | 1524936 | |
| L.D. | 12 | 2868 | 2196 | 58 | 59 | 112.026 | 1475712 | 3.23 |
| U.D. | 12 | 3307 | 2515 | 66 | | 128.007 | 1991880 | |
| L.D. | 12 | 3262 | 2482 | 65 | 66 | 128.021 | 1935960 | 2.81 |
| U.D. | 13 | 5397 | 4136 | 97 | | 192.003 | 5215496 | |
| L.D. | 13 | 5269 | 4021 | 96 | 98 | 192.052 | 5018208 | 3.78 |
| U.D. | 13 | 7150 | 5447 | 131 | | 256.002 | 9276241 | |
| L.D. | 13 | 7008 | 5318 | 130 | 133 | 257.471 | 8987420 | 3.11 |

Table 1 refers to the generic McEliece system where the size of the public keys is given by $(n - k) \times k = mkr$. As shown in figure 1, using a list decoding algorithm is all the more interesting as the normalized minimum distance $(2r + 1)/n$ gets closer to 0.5, which has apparently an adverse effect on the keysize. However, even in this unfavorable case, we were still able to exhibit a keysize reduction of about 4%.

3.2 Dyadic case

The attack proposed by Faugère, Otmani, Perret and Tillich in [14] uses Groebner basis computations to recover the private key from the only knowledge on the public one. It was specifically designed to break the compact key McEliece

variants proposed in [4, 20], which use the structure of alternant codes. The variant proposed in [20] uses binary Goppa codes in dyadic form, which are also alternant codes. The attack in [14] thus applies and can recover an equivalent private key in an alternant code form. However, this is not sufficient to break the system when using Goppa codes. Indeed, the attack does not directly retrieve the Goppa polynomial G of degree r which is crucial to decode [2, 25], but finds a generator matrix of an alternant code without a Goppa structure and with designed minimum distance $r + 1$. However, when using a Goppa code, the private key is a generator matrix of a code with designed minimum distance $2r + 1$ thanks to the following proposition, demonstrated in [2, 12]:

Proposition 1. *Let G be a square-free polynomial in \mathbb{F}_{2^m} and \mathcal{L} be a list of n elements of \mathbb{F}_{2^m} which are not roots of G . Then*

$$\Gamma(\mathcal{L}, G) = \Gamma(\mathcal{L}, G^2),$$

where $\Gamma(\mathcal{L}, G)$ is the Goppa code generated by \mathcal{L} and G .

The direct consequence is that the attacker won't be able to decode. Indeed, this attack retrieves n/r variables Y and n variables X such that $Y_i = G(X_i)^{-1}$. In order to protect against a potential interpolation of the Goppa polynomial G of degree r , we impose that $r + 1 > \frac{n}{r}$, that is $r(r + 1) > n$. Consequently, this attack does not totally break the McEliece variant based on dyadic forms. Moreover, as stated in [14], the attack becomes unpractical, for the moment, when the extension degree m is greater than 16. Working with such an extension degree slightly increases the public keysize of McEliece compared to the parameters proposed in [20], while staying drastically smaller than with the generic form, as shown in tables 1, 2 and 3.

Table 2: Comparison between the public keysize of dyadic McEliece cryptosystem with $r(r+1) > n$ using unambiguous and list decoding for given workfactors.

| Method | m | n | k | r | τ_2 | WF | Keysize | gain (%) |
|--------|-----|-------|------|-----|----------|---------|---------|----------|
| U.D. | 11 | 1792 | 1088 | 64 | | 82.518 | 11968 | |
| L.D. | 11 | 1728 | 1024 | 64 | 67 | 82.976 | 11264 | 5.88 |
| U.D. | 12 | 2944 | 1408 | 128 | | 116.735 | 16896 | |
| L.D. | 13 | 2816 | 1280 | 128 | 134 | 113.896 | 15360 | 9.09 |
| L.D. | 13 | 7680 | 1024 | 512 | 552 | 113.084 | 13312 | 21.21 |
| U.D. | 12 | 3200 | 1664 | 128 | | 131.235 | 19968 | |
| L.D. | 12 | 3072 | 1536 | 128 | 134 | 129.745 | 18432 | 7.69 |
| U.D. | 13 | 5888 | 2560 | 256 | | 205.804 | 33280 | |
| L.D. | 13 | 5632 | 2304 | 256 | 269 | 199.473 | 29952 | 10.00 |
| U.D. | 15 | 11264 | 3584 | 512 | | 279.002 | 53760 | |
| L.D. | 15 | 10752 | 3072 | 512 | 539 | 258.223 | 46080 | 14.29 |

Table 3: Comparison between the public keysize of dyadic McEliece cryptosystem with $m \geq 16$ using unambiguous and list decoding for given workfactors.

| Method | m | n | k | r | τ_2 | WF | Keysize | gain (%) |
|--------|-----|-------|------|------|----------|---------|---------|----------|
| U.D. | 16 | 5120 | 1024 | 256 | | 81.765 | 16384 | |
| L.D. | 16 | 5120 | 1024 | 256 | 134 | 86.216 | 16384 | 0 |
| U.D. | 16 | 3840 | 1792 | 128 | | 113.785 | 28672 | |
| L.D. | 16 | 5632 | 1536 | 256 | 269 | 116.400 | 24576 | 14.29 |
| U.D. | 16 | 5888 | 1792 | 256 | | 132.470 | 28672 | |
| L.D. | 16 | 9728 | 1536 | 512 | 542 | 133.534 | 24576 | 14.29 |
| U.D. | 16 | 10752 | 2560 | 512 | | 199.067 | 40960 | |
| L.D. | 16 | 10752 | 2560 | 512 | 539 | 209.414 | 40960 | 0 |
| U.D. | 16 | 11776 | 3584 | 512 | | 264.846 | 57344 | |
| L.D. | 16 | 19456 | 3072 | 1024 | 1085 | 267.203 | 49152 | 14.29 |

In table 2, we look at the case of the dyadic variant with countermeasure $r(r+1) > n$. The size of the public key now becomes mk [20], removing the conflicting constraints on r . Key reduction up to 21% can now be achieved. Finally, results on the dyadic variant with countermeasure $m \geq 16$ are presented in table 3. As previously discussed, we expect better reductions than in the generic case. Indeed, our experiments showed a key reduction of more than 14%. Note that in this case, the degree r of the Goppa polynomial is the same as the dimension k of the code. This is easily explained: the large extension degree becomes such a strong constraint on the parameters that it removes all freedom when choosing the code dimension.

Table 4 displays the recommended key sizes for cryptosystems based on the Discrete Logarithm Problem over finite fields (DLP), for different security levels [3,22]. For the sake of comparison, we also include the smallest key sizes obtained with McEliece variants although in all impartiality, it should be stressed that we lack sufficient perspective to correctly assess the true security level of these fairly new variants. While the key sizes for the McEliece cryptosystem are still larger than their discrete logarithm counterparts, the gap significantly narrows when going at higher security levels. Moreover, the costs for McEliece encryption and decryption rise much more slowly with the security level than they do with DLP based or RSA systems [20].

4 Conclusion

In light of the recent study on the list decoding of binary Goppa codes [2], we compared the size of public keys for different variants of the McEliece cryptosystem. We showed that using list decodable codes in McEliece cryptosystems deliver compelling benefits. We explained how to secure the dyadic

Table 4: Keysize comparison between cryptosystem based on discrete logarithm over finite fields and McEliece cryptosystem using list decoding.

| Security level | Discrete Logarithm | McEliece | ratio |
|----------------|--------------------|----------|-------|
| 80 | 1024 | 11264 | 11.0 |
| 112 | 2048 | 13312 | 6.5 |
| 128 | 3072 | 18432 | 6.0 |
| 192 | 7680 | 29952 | 3.9 |
| 256 | 15360 | 46080 | 3.0 |

variant against currently known attacks while reducing the size of the keys using list decoding. For example, for a workfactor of 2^{80} , list decoding lowers the public keysize from 661,122 bits for the generic variant to 11,264 bits for the dyadic variant. It is worth mentioning that contrary to previous attempts at reducing the McEliece key sizes, using list decoding does not introduce any additional structure that could be used to attack the system.

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