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INSTITUT NATIONAL DE RECHERCHE EN INFORMATIQUE ET EN AUTOMATIQUE

Throughput Optimization by Software Pipelining of Conditional Reservation Tables

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— Embedded and Real Time Systems —

*R*apport
de recherche

Throughput Optimization by Software Pipelining of Conditional Reservation Tables

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Theme : Embedded and Real Time Systems
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Abstract: Reservation tables are used at various levels in embedded systems design to represent the allocation of resources in cyclic computations. They model system-level static realtime task schedules in fields like automotive or avionics, but also model the cycle-accurate ordering of instructions at microarchitectural level, as used in software pipelining. To optimize system throughput, successive execution cycles can be pipelined, subject to resource constraints and intercycle data dependencies. In this paper we take inspiration from software pipelining and predicate-aware scheduling to define system-level pipelining techniques for task schedules given under the form of reservation tables. Our algorithms start from predicated reservation tables output by state-of-the-art latency-optimizing embedded design tools. They significantly optimize system throughput while maintaining the required strictly periodic execution model and the end-to-end latency guarantees of the input reservation table. We demonstrate the approach on real-life scheduling problems.

Key-words: embedded systems, real-time, distributed applications, scheduling, computation cycles, code generation, software pipelining

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[†] The authors added some improvements to the algorithms, as well as a more detailed explanation of their work

Optimisation du débit de sortie par pipelinage logiciel de tables de réservation conditionnelles

Résumé : Les tables de réservation sont utilisées à différents niveaux dans le design des systèmes embarqués, afin de représenter l'allocation des ressources dans le cas de calculs cycliques. Elles modélisent l'ordonnancement statique de tâches temps-réel au niveau du système dans des champs d'application tels que l'automobile ou l'avionique, mais aussi l'ordre d'exécution des instructions d'un cycle de calcul au niveau microarchitectural, comme dans le cas du pipelinage logiciel. Pour optimiser le débit de sortie du système, des cycles d'exécution successifs peuvent être pipelinés, en prenant garde aux contraintes dues aux ressources et aux dépendances de données inter-cycles. Dans cet article, nous nous inspirons du pipelinage logiciel pour définir des techniques de pipelinage au niveau du système pour les ordonnancements statiques de tâches donnés sous la forme de tables de réservation/d'ordonancement. Nous autorisons l'utilisation de tables conditionnelles où l'exécution des opérations peut être soumise à la valeur d'un prédicat. Nos algorithmes optimisent le débit de sortie du système, tout en maintenant les garanties sur le temps de réponse définies dans la table d'ordonnement initiale. Nous illustrons notre approche par des exemples tirés de problèmes réels d'ordonnement de tâches.

Mots-clés : systèmes embarqués, temps réel, applications distribuées, ordonnancement, cycles de calcul, génération de code, pipelinage logiciel

1 Introduction

Embedded systems design brings together research and engineering communities that used to be only loosely connected. This new interaction helps bring forth common problems that are central to more than one community. This cross-fertilization ideally results in the development of common formalisms and general modeling, analysis, and code generation techniques.

Our paper follows this paradigm for a specific problem: The *efficient execution of cyclic computations over synchronous architectures comprising several computing and communication resources*. Instances of this problem are present at several levels of the embedded design cycle. At low level, compilers are expected to improve code speed by taking advantage of micro-architectural instruction level parallelism[11]. To minimize synchronization overhead, *pipelining* compilers usually rely on reservation tables to represent an efficient (possibly optimal) static allocation of the computing resources (execution units and/or registers) with a timing precision equal to that of the hardware clock. Executable code is then generated that enforces this allocation, possibly with some timing flexibility. But on *VLIW architectures*, where each instruction word may start several operations, this flexibility is very limited, and generated code is virtually identical to the reservation table. The scheduling burden is mostly supported here by the compilers, which include *software pipelining* techniques [3] designed to increase the throughput of loops by allowing one loop cycle to start before the completion of the previous one.

A very similar picture can be seen in the system level design of safety-critical real-time embedded control systems with *distributed (parallel, multi-core)* hardware platforms. The timing precision is here coarser, both for starting dates, which are typically given by timers, and for durations, which are characterized with worst-case execution times (WCET). However, safety and efficiency arguments[9] lead to the increasing use of tightly synchronized *time-triggered* architectures and execution mechanisms, defined in well-established standards such as TTA, FlexRay[17], ARINC653[1], or AUTOSAR[2]. Systems based on these platforms typically have hard real-time constraints, and their correct functioning must be guaranteed by a schedulability analysis. In this paper, we are interested in statically scheduled systems where resource allocation can be described under the form of a reservation/scheduling table which constitutes, by itself, a proof of schedulability. Such systems include:

- Periodic time-triggered systems[5, 21, 12, 8, 14] that are naturally mapped over ARINC653, AUTOSAR, TTA, or FlexRay.
- Systems where the scheduling table describes the reaction to some sporadic input event (meaning that the table must fit inside the period of the sporadic event). Such systems can be specified in AUTOSAR, allowing, for instance, the modeling of computations synchronized with engine rotation events [4].
- Some systems with a mixed event-driven/time-driven execution model, such as those synthesized by SynDEx[10].

Synthesis of such systems starts from specifications written in domain-specific formalisms such as Simulink or SCADE[5]. These formalisms allow the descrip-

tion of *concurrent* data computations and communications that are *conditionally activated* at each cycle of the embedded control algorithm depending on the current *input* and *state* of the system.

The optimal implementation of such specifications onto platforms with multiple execution and communication resources (distributed, parallel, multi-core) is undecidable. Existing implementation techniques and tools [5, 21, 10, 14, 8] *heuristically* solve the simpler problem of synthesizing a scheduling table of *minimal length* which implements one generic cycle of the embedded control algorithm. As the successive executions of the scheduling table are exclusive at runtime, this means that the cycles of the embedded control algorithm cannot overlap, which negatively affects the throughput of the system.

To work around this limitation, we looked for solutions in the software pipelining community. We encountered two main problems. The first one concerns predication. For an efficient mapping of our conditional specifications, it is important to allow an independent, predicated (conditional) control of the various computing resources. However, most existing techniques for software pipelining [3, 19, 20, 6] significantly constrain or simply prohibit predicated resource control. One common problem is that two different operations cannot be scheduled at the same date on a given resource (functional unit), even if they have exclusive predicates (like the branches of a test). The only exception we know to this rule is *predicate-aware scheduling (PAS)*¹ [18]. The drawback of PAS is that sharing the same resource at the same date is only possible for operations of the same cycle, due to limitations in the dependency analysis phase.

The second problem is that most software pipelining techniques are tailored for optimizing processing *speed* (throughput) of loops while preserving the computing *function* [20]. In addition to function, we also seek to preserve existing real-time *end-to-end latency* guarantees, and a *periodic* execution model.

To work around these limitations, we developed a novel software pipelining approach adapted to our framework. We start from the output of existing tools, given as a reservation table defining the non-pipelined time-triggered implementation of the embedded control specification. We allow the use of *predicated scheduling tables* where each operation can be guarded by an activation condition, allowing a natural modeling of control applications having several (nominal or degraded) execution modes.

We define algorithms that synthesize pipelined implementations where a new computation cycle can begin before the previous one has completed, subject to resource and inter-cycle data dependency constraints. The algorithms optimize the *throughput* of the system, but each computation cycle is executed exactly as specified by the input reservation table, so that all *latency* guarantees are preserved, along with *functionality* and *periodicity*. The pipelined implementation is represented using a *pipelined reservation table*. The result is a **scheduling flow that optimizes both latency and throughput, with priority to latency**.

Pipelining is based on a dependency analysis determining the exclusiveness of predicates of operations from successive cycles. Knowledge of the pipelining technique is used to bound the complexity of the dependency analysis. By com-

¹It is interesting to note that our execution platforms satisfy the PAS architecture requirements.

parison, existing pipelining and predicate-aware scheduling techniques either assume that the dependency graph is fully generated before starting the pipelining algorithm [16], or use the predicates for the analysis of a single cycle[19].

Our algorithms give the best results on specifications without temporal partitioning, like the previously-mentioned AUTOSAR or SynDEx applications and, to a certain extent, applications using the FlexRay dynamic segment. For partitioned applications like those mapped over ARINC 653, TTA, or FlexRay (the static segment), our algorithms currently cannot exploit conditional control information, but allow pipelining and synthesize a new partitioning of the computation and communication cycles.

Related work. In addition to the software pipelining techniques mentioned in the introduction, we are aware of two other approaches aiming at relaxing the frontiers between execution cycles of an embedded control system. Unlike our approach, which works at a time-triggered *implementation* level and assumes no knowledge of the process generating this implementation, these approaches intervene at a synchronous dataflow *specification* level. This specification is re-organized to allow the generation of better real-time schedules using existing synthesis tools. In one approach, specification re-organization is semi-automatic[5]. The drawback is that expert human intervention and actual changes in the specification itself are needed. In the second approach, re-organization is based on an automatable retiming technique [13], but retiming techniques work in a pure dataflow context (not predicated).

Outline. The remainder of the paper is structured as follows. Section 2 defines our model of time-triggered system implementation. Section 3 extends this model to allow the representation of pipelined implementations and gives an overview of our technique. It also provides a complex example. Section 4 deals with data dependency analysis. Section 5 gives experimental results, and Section 6 concludes.

2 Implementation model

We define here the formalism we use to model non-pipelined implementations. Inspired from [14, 10], our formalism remains at a significantly lower abstraction level. The models of [14, 10] are fully synchronous: Each variable has at most one value at each execution cycle, and moving one value from a cycle to the next can only be done through explicit *delay* constructs. In our model, each variable (called a memory cell) can be assigned several times during a cycle, and values are by default passed from one execution cycle to the next.

This lower abstraction level allows the simple modeling of existing implementations, but complexifies the pipelining algorithms, as we shall see in the following sections.

2.1 Architecture model

We model execution architectures using a very simple language defining *sequential execution resources*, *memory blocks*, and their *interconnections*. Formally, an architecture model is a bipartite undirected graph $\mathcal{A} = \langle \mathcal{P}, \mathcal{M}, \mathcal{C} \rangle$, with

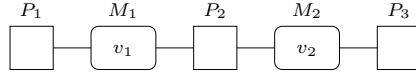


Figure 1: Simple architecture

$\mathcal{C} \subseteq \mathcal{P} \times \mathcal{M}$. The elements of \mathcal{P} are called *processors*, but they model all the computation and communication devices capable of independent execution (CPU cores, accelerators, DMA and bus controllers, etc.). We assume that each processor can execute only one operation at a time. We also assume that each processor has its own sequential or time-triggered program. This last assumption is natural on actual CPU cores. On devices such as DMAs and accelerators, it models the assumption that the cost of control by some other processor is negligible.

The elements of \mathcal{M} are RAM blocks. We assume each RAM block is structured as a set of disjoint *cells*. We denote with $Cells$ the set of all memory cells in the system, and with $Cells_M$ the set of cells on RAM block M . Our model does not specify memory size limits. Instead, we provide in Section 3.3 a mechanism that uses architecture model manipulations to prohibit memory cell replication during pipelining.

Processor P has direct access to memory block M whenever $(P, M) \in \mathcal{C}$. All processors directly connected to a memory block M can access M at the same time. Therefore, care must be taken to prohibit concurrent read-write or write-write access by two or more processors to a single memory cell, in order to preserve functional determinism (we will assume this is ensured by the input system model, and will be preserved by the pipelined one).

The simple architecture of Fig. 1 has 3 processors (P_1 , P_2 , and P_3) and 2 memory blocks (M_1 and M_2). Each of the M_i blocks has only one memory cell v_i .

2.2 Implementation model

On such architectures, we execute time-triggered implementations of embedded control applications with a *periodic non-preemptive* execution model. We represent such an application with a scheduling/reservation table, which is a finite time-triggered activation pattern. This pattern defines the computation of one period (also called an *execution cycle*). The infinite execution of the embedded system is the infinite succession of periodically-triggered execution cycles.

Formally, a reservation/scheduling table is a triple $\mathcal{S} = \langle p, \mathcal{O}, Init \rangle$, where p is the *activation period* of execution cycles, \mathcal{O} is the set of *scheduled operations*, and $Init$ is the *initial state* of the memory.

The activation period gives the (fixed) duration of the execution cycles. All the operations of one execution cycle must be completed before the following execution cycle starts. The activation period thus sets the *length* of the scheduling/reservation table, and is denoted by $len(\mathcal{S})$.

The set \mathcal{O} defines the operations of the scheduling table. Each scheduled operation $o \in \mathcal{O}$ is a tuple defining:

- $In(o) \subseteq Cells$ is the set of memory cells read by o .

| time | Processor | | |
|------|-----------|--------|--------|
| | P1 | P2 | P3 |
| 0 | A@true | | |
| 1 | | B@true | |
| 2 | | | C@true |

Figure 2: Simple (non-pipelined) scheduling table

- $Out(o) \subseteq Cells$ is the set of cells written by o .
- $Guard(o)$ is the execution condition of o , defined as a predicate over the values of memory cells. We denote with $GuardIn(o)$ the set of memory cells used in the computation of $Guard(o)$.
- $Res(o) \subseteq \mathcal{P}$ is the set of processors used during the execution of o .
- $t(o)$ is the start date of o .
- $d(o)$ is the duration of o . The duration is viewed here as a time budget the operation must not exceed. This can be statically ensured through a worst-case execution time analysis.

All the resources of $Res(o)$ are exclusively used by o after $t(o)$ and for a duration of $d(o)$ in cycles where $Guard(o)$ is true. The sets $In(o)$ and $Out(o)$ are not necessarily disjoint, to model variables that are both read and updated by an operation. For lifetime analysis purposes, we assume that input and output cells are used for all the duration of the operation. The cells of $GuardIn(o)$ are all read at the beginning of the operation, but we assume the duration of the computation of the guard is negligible (zero time).²

To cover cases where a memory cell is used by one operation before being updated by another, each memory cell can have an *initial value*. For a memory cell m , $Init(m)$ is either *nil*, or some constant.

The simple scheduling table pictured in Fig. 2 uses the architecture of Fig. 1. It has a length of 3 and contains 3 operations (A , B , and C). Operation A reads no memory cell, but writes v_1 , so that $In(A) = \emptyset$ and $Out(A) = \{v_1\}$. Similarly, $In(B) = \{v_1\}$, $Out(B) = In(C) = \{v_2\}$, and $Out(C) = \emptyset$. All 3 operations are executed at every cycle, so their guard is *true* (guards are graphically represented with “@true”). The 3 operations are each allocated on one processor: $Res(A) = \{P_1\}$, $Res(B) = \{P_2\}$, $Res(C) = \{P_3\}$. Finally, $t(A) = 0$, $t(B) = 1$, $t(C) = 2$, and $d(A) = d(B) = d(C) = 1$. No initialization of the memory cells is needed (the initial states are all *nil*).

2.3 Well-formed properties

The formalism above provides the syntax of our implementation models, and allows the definition of operational semantics. However, not all syntactically

²The memory access model where an operation reads its inputs at start time, writes its outputs upon completion, and where guard computations take time can be represented on top of our model.

| time | P1 | P2 | P3 | |
|------|-----------------------|-----------------------|-----------------------|-----------------|
| 0 | A@true iteration 1 | | | Prologue |
| 1 | A@true iteration 2 | B@true iteration 1 | | |
| 2 | A@true iteration 3 | B@true iteration 2 | C@true iteration 1 | Steady state |
| 3 | A@true iteration 4 | B@true iteration 3 | C@true iteration 2 | |
| | ... | ... | ... | |

Figure 3: Pipelined execution trace

correct specifications model correct implementations. Some of them are non-deterministic due to data races or due to operations exceeding their time budgets. Others are simply un-implementable, for instance because an operation is scheduled on processor P , but accesses memory cells on a RAM block not connected to P . A set of correctness properties is therefore necessary to define the well-formed implementation models.

However, some of these properties are not important in this paper, because we assume that the input of our pipelining technique is already correct. Our pipelining techniques will preserve most correctness properties because they preserve all allocation and scheduling choices *inside each execution cycle*. We only formalize here two correctness properties that will need attention in the following sections.

We say that two operations o_1 and o_2 are *non-concurrent*, denoted $o_1 \perp o_2$, if either their executions do not overlap in time ($t(o_1) + d(o_1) \geq t(o_2)$ or $t(o_2) + d(o_2) \geq t(o_1)$), or if they have exclusive guards ($Guard(o_1) \wedge Guard(o_2) = false$). With this notation, the following correctness properties are assumed respected by input (non-pipelined) implementation models, and must be respected by the output (pipelined) model:

Sequential processors. No two operations can use a processor at the same time. Formally, for all $o_1, o_2 \in \mathcal{O}$, if $Res(o_1) \cap Res(o_2) \neq \emptyset$ then $o_1 \perp o_2$.

No data races. If some memory cell m is written by o_1 ($m \in Out(o_1)$) and is used by o_2 ($m \in In(o_2) \cup Out(o_2)$), then $o_1 \perp o_2$.

3 Pipelining technique overview

In this section, we define our model of pipelined implementation, which builds over the non-pipelined one, enriching it with temporal information. We also explain how a pipelined implementation is constructed once the pipelining analysis (described later in the paper) has been performed.

For the example in Fig. 2, an execution where successive cycles do not overlap in time is clearly sub-optimal. Our objective is to allow the pipelined execution of Fig. 3, which ensures a maximal use of the computing resources. In the pipelined execution, a new instance of operation A starts as soon as the previous one has completed, and the same is true for B and C . The first two time units of the execution are the *prologue* which fills the pipeline. In the *steady state* the pipeline is full and has a throughput of one computation cycle (of the non-pipelined system) per time unit. If the system is allowed to terminate,

| time | P1 | P2 | P3 |
|------|------------------------|------------------------|------------------------|
| 0 | A@true $fst(A) = 0$ | B@true $fst(B) = 1$ | C@true $fst(C) = 2$ |

Figure 4: Pipelined scheduling table

then completion is realized by the *epilogue*, not pictured in our example, which empties the pipeline.

We represent this pipelined implementation using the *pipelined scheduling table* pictured in Fig. 4. Its length is 1, corresponding to the throughput of the pipelined system. The operation set contains the same operations A , B , and C , but there are significant changes. The start dates of B and C are now 0, as the 3 operations are started at the same time in each *pipelined cycle*. To avoid confusion, we reserve the name *computation cycle* for full computations, as specified by the initial scheduling table. A computation cycle spans over several pipelined cycles, but each pipelined cycle starts exactly one computation cycle.

To account for the prologue phase, where operations progressively start to execute, each operation is assigned a *start index* $fst(o)$. If an operation o has $fst(o) = n$ it will first be executed in the pipelined cycle of index n (indices start at 0). Due to pipelining, the instance of o executed in the pipelined cycle m belongs to the computation cycle of index $m - fst(o)$. For instance, operation C with $fst(C) = 2$ is first executed in the 3rd repetition of the table (of index 2), but belongs to the first computation cycle.

Note that the prologues of our pipelined implementations are obtained by incremental activation of the steady state operations. This property, which allows periodic implementation, is not present in classical software pipelining approaches. Periodicity, plus the requirement that the pipelined implementation executes each computation cycle as specified by the non-pipelined table, means that the pipelined scheduling table can be fully built using Procedure 1 starting from the non-pipelined table and from the period of the pipelined system. The procedure first determines the start index and new start date of each operation by folding the non-pipelined table onto the new period. Procedure *AssembleSchedule* then determines which memory cells need to be replicated due to pipelining, using the technique provided in Section 3.2.

Algorithm 1 BuildSchedule

Input: \mathcal{S} : non-pipelined scheduling table

\hat{p} : new period of the system

Output: $\hat{\mathcal{S}}$: pipelined schedule table

for all o in \mathcal{O} **do**

$fst(o) := \lceil \frac{t(o)}{\hat{p}} \rceil$

$\hat{t}(o) := t(o) - fst(o) * \hat{p}$

$\hat{\mathcal{S}} := AssembleSchedule(\mathcal{S}, \hat{p}, fst, \hat{t})$

When comparing with existing software pipelining techniques, the most obvious difference is that our approach allows optimization along a single degree of freedom (the period). Resource allocation and scheduling inside a computation cycle are fixed. This approach limits the throughput optimization space. How-

ever, throughput optimization is not our only objective. As explained in the introduction, we apply our transformations as part of a larger implementation flow. In this flow, the pipelining phase must preserve the end-to-end latency guarantees of each computation cycle (ensured by other tools), and the periodic implementation model. Our approach satisfies these requirements. A simpler pipelining technique also has the advantage of speed, and of allowing us to focus on the predication-related issues, where the real complexity and gain of our approach stands. The approach also gives good results on real-life scheduling problems.

3.1 Dependency graph and maximal throughput

In our approach, the period of the pipelined system is determined by the data dependencies between successive execution cycles. We represent these dependencies as a *Data Dependency Graph (DDG)* – a formalism that is classical in software pipelining based on modulo scheduling techniques[3]. In this section we define DDGs and we explain how the new period is computed from them. The computation of DDGs is detailed in Section 4.

Given an implementation model $\mathcal{S} = \langle p, \mathcal{O}, Init \rangle$, the DDG associated to \mathcal{S} is a directed graph $DG = \langle \mathcal{O}, \mathcal{V} \rangle$ where $\mathcal{V} \subseteq \mathcal{O} \times \mathcal{O} \times \mathbb{N}$. Ideally, the elements of \mathcal{V} are all the triples (o_1, o_2, n) such that there exists an execution of the implementation and a computation cycle k such that operation o_1 is executed in cycle k , operation o_2 is executed in cycle $k+n$, and o_1 must be executed before o_2 , for instance because some value produced by o_1 is used by o_2 . In practice, any \mathcal{V} including all the arcs defined above (any over-approximation) will be acceptable, leading to correct (but possibly sub-optimal) implementations.

The DDG represents all possible dependencies between operations, both inside a cycle (when $n = 0$) and between successive cycles at distance $n \geq 1$. Given the statically scheduled implementation model, with fixed dates for each operation, the pipelined schedule must respect *unconditionally* all these dependencies.

For each operation $o \in \mathcal{O}$, we denote with $t_n(o)$ the date where operation o is executed in cycle n , if its guard is true. By construction, we have $t_n(o) = t(o) + n * p$. In the pipelined implementation of period \hat{p} , this date is changed to $\hat{t}_n(o) = t(o) + n * \hat{p}$. Then, for all $(o_1, o_2, n) \in \mathcal{V}$ and $k \geq 0$, the pipelined implementation must satisfy $\hat{t}_{k+n}(o_2) \geq \hat{t}_k(o_1) + d(o_1)$, which implies:

$$\hat{p} \geq \max_{(o_1, o_2, n) \in \mathcal{V}, n \neq 0} \left\lceil \frac{t(o_1) + d(o_1) - t(o_2)}{n} \right\rceil$$

Our objective is to build pipelined schedules satisfying this lower bound constraint and which are well-formed in the sense of Section 2.3.

3.2 Memory management issues

Assuming that $\hat{\mathcal{S}}$ is the pipelined version of \mathcal{S} , we denote with $max_par = \lceil len(\mathcal{S}) / len(\hat{\mathcal{S}}) \rceil$ the maximal number of simultaneously-active computation cycles of the pipelined implementation. Note that $max_par = 1 + \max_{o \in \mathcal{O}} fst(o)$.

Consider now our example. In its non-pipelined version, both A and B use memory cell v_1 at each cycle. In the pipelined table A and B work in parallel, so they must use two different copies of v_1 . We say that the replication factor of v_1

is $rep(v_1) = 2$. Each memory cell v is assigned its own replication factor, which must allow concurrent computation cycles using different copies of v to work without interference. Obviously, we can bound $rep(v)$ by max_par . We use a tighter margin, based on the observation that most variables (memory cells) have a limited lifetime inside a computation cycle. We set $rep(v) = 1 + lst(v) - fst(v)$, where:

$$fst(v) = \min_{o \in In(o) \cup Out(o)} fst(o)$$

$$lst(v) = \max_{o \in In(o) \cup Out(o)} lst(o)$$

Through replication, each memory cell v of the non-pipelined scheduling table is replaced by $rep(v)$ memory cells, allocated on the same memory block as v , and organized in an array \bar{v} , whose elements are $\bar{v}[0], \dots, \bar{v}[rep(v) - 1]$. These new memory cells are allocated cyclically, in a static fashion, to the successive computation cycles. More precisely, the computation cycle of index n is assigned the replicas $\bar{v}[n \bmod rep(v)]$ for all v . The computation of $rep(v)$ ensures that if n_1 and n_2 are equal modulo $rep(v)$, but $n_1 \neq n_2$, then computation cycles n_1 and n_2 cannot access v at the same time.

For systems like our simple example, where no information is passed from one computation cycle to the next, this static allocation allows for a simple code generation, which consists in replacing v with $\bar{v}[(cid - fst(o)) \bmod rep(v)]$ in the input and output parameter lists of every operation o that uses v . Here, cid is the index of the current pipelined cycle. It is represented in the generated code by an integer. When execution starts, cid is initialized with 0. At the start of each subsequent pipelined cycle, it is updated to $(cid + 1) \bmod R$, where R is the least common multiple of all the values $rep(v)$.

When a computation cycle uses values produced by previously-started computation cycles,³ code generation is more complicated, because a computation cycle may access memory cells different than its own. The code generation problem is complicated by the fact that it is impossible, in the general case, to statically determine which cell must be read (because the cell was written at an arbitrary distance in time). Thus, we need a dynamic mechanism to identify which cell to read. If more static pipelined implementations are needed, different pipelining techniques should be designed, either limiting the class of accepted non-pipelined systems, or allowing the copying of one memory cell onto another, which we do not allow because it may introduce timing penalties.

Our memory access mechanism is supported by a new data structure which associates to each memory cell v of the non-pipelined scheduling table an array $src(v)$ of length $rep(v)$, and allocated on the same memory block as \bar{v} . In this context, code is generated as follows:

At execution start, all the values of src are initialized with 0 (pointing to the initial values of the memory cells).

At the start of each pipelined cycle, for each cell v of the initial scheduling table, assign to

$src(v)[(cid - fst(v)) \bmod rep(v)]$ the value of $src(v)[(cid - fst(v) - 1) \bmod rep(v)]$. This assignment indicates that the value of v initially used during computation cycle cid is that used (but not necessarily produced) during computation cycle $cid - 1$ and stored in memory cell $\bar{v}[src(v)[(cid - fst(v) - 1) \bmod rep(v)]]$.

³This is necessary to represent systems having an internal state.

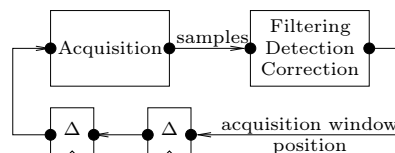


Figure 5: Knock control functional specification

When an operation o of the non-pipelined scheduling table reads v , its counterpart in the pipelined table will read $\bar{v}[src(v)[(cid - fst(o)) \bmod rep(v)]]$. The same is true for cells used by the computation of execution conditions.

When o writes v in the non-pipelined table, there are 2 cases: If o also reads v , then the counterpart of o in the pipelined table will write the same memory cell it reads (as defined above). If o does not read v , then o writes the memory cell normally assigned to this computation cycle by the replication process ($\bar{v}[x]$, where

$x = (cid - fst(o)) \bmod rep(v)$). An operation is added after o and on the same execution condition to set $src(v)[x]$ to x .

The last aspect of memory management is initialization. In our case, v_1 requires no initialization, so that none of its replicas do. In the general case, if $Init(v) \neq nil$, we need to initialize $\bar{v}[0]$ with $Init(v)$, but not the other replicas.

3.3 The knock control example

We complete this section with a larger example that illustrates several key points of our approach, including the use of conditional scheduling tables and the pipelining of sporadic systems. Knock control is one of the functions of the engine control unit (ECU) of gasoline spark-ignition engines. At each rotation of the engine, it chooses for each cylinder an ignition time that maximizes power output while keeping engine-destructive knocks (autoignition events) at an acceptable level.

We provide in Fig. 5 a simplified high-level description of the knock control functionality. The model is based on an industrial case study and on the description of [4]. The behavior is as follows: One computation cycle is triggered at each rotation of the engine crankshaft. The cycle starts with the acquisition of knock noise data. Acquisition is performed over a *knock acquisition window* where autoignition can occur. It is performed using a vibration sensor sampled at 100kHz, and the samples are stored in a buffer. The samples are used by the *filtering, detection, and correction (FDC)* function to adjust the ignition time (not figured here) and the position and size of the acquisition window. The configuration data produced by the computation cycle of index n controls the acquisition of cycle $n + 2$. This delayed feedback is realized using two unit delays (labeled Δ). Acquisition is performed by a specialized device (labeled AD in Fig. 6) of the ECU, whereas the FDC function is computed by the ECU microcontroller (μC).

For reasons related to the physics of engines and to computing resource limitations in the ECU, the successive computation cycles must sometimes be pipelined, by allowing the acquisition and FDC operations of successive cycles to be executed in parallel. Such a pipelining can be directly constructed using

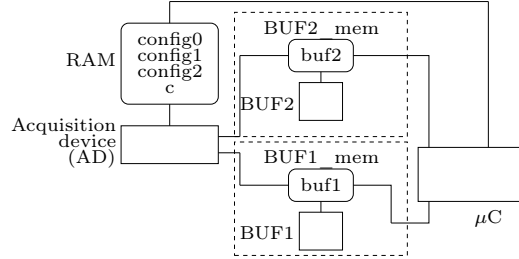


Figure 6: Engine control unit (ECU) architecture

| rotation units | AD | BUF1 | BUF2 | μC |
|----------------|---------------|----------------|----------------|----------------|
| 0 | book@true | | | |
| 1 | Acq_1 @c | Acq_2 @¬c | | |
| 2 | | Acq_1 @c | Acq_2 @¬c | |
| 3 | | FDC_1 @c | FDC_2 @¬c | FDC_1 @c |
| 4 | | | | FDC_2 @¬c |
| 5 | | | | |

Figure 7: Non-pipelined scheduling table for the knock control

our approach, using the code generation scheme of the previous section. However, our code generation may conflict with memory constraints or pre-existent implementation choices. We will assume here that the system designers have already fixed the maximal number of buffers to 2, placed them at fixed places in memory, and written the protocol that alternates the use of the buffers in both acquisition and FDC. The remaining difficulties are the computation of the pipelined period and the management of all memory cells that are not constrained.

Representing the memory replication constraints is best done as in Fig. 6, with two memory cells (*buf1* and *buf2*) on separate memory blocks (BUF1_mem, resp. BUF2_mem). Each memory block has its own memory controller (BUF1, resp. BUF2) that ensures exclusive access and makes memory cell replication impossible during pipelining.

In this implementation model, the scheduling table of one computation cycle is represented in Fig. 7. Memory cell *c* is a Boolean used in guards to determine which buffer to use in the current computation cycle to pass data from the acquisition function to *FDC*. In the beginning of each computation cycle, the bookkeeping operation *book* flips the value of *c* by executing “*c*:=¬*c*”. In cycles where the new value is *true*, buffer *buf1* is used. Otherwise, *buf2* is used. If we denote with c^n the value of *c* used in guards throughout computation cycle *n*, we have $c^n = \neg c^{n-1}$ for all *n* positive. The bookkeeping operation also implements the function of the unit delays.

The scheduling table represents both activation scenarios, corresponding to different initial values of *c*. In order not to introduce special memory access operations, we split the acquisition and *FDC* operations in two. Both Acq_1 and Acq_2 perform acquisition. But the first writes its samples in *buf1* and is executed on condition *c*, while the second writes them in *buf2* and is guarded

| rotation units | AD | | BUF1 | | BUF2 | | μC |
|----------------|-------------------------------|-------------------------------|-------------------------------|-------------------------------|-------------------------------|-------------------------------|-------------------------------|
| 0 | book ⁰ @true | | | | | | |
| 1 | Acq ₁ ⁰ | Acq ₂ ⁰ | Acq ₁ ⁰ | | | Acq ₂ ⁰ | |
| 2 | @c ⁰ | @-c ⁰ | @c ⁰ | | | @-c ⁰ | |
| 3 | book ¹ @true | | | | | | |
| 4 | Acq ₂ ¹ | Acq ₁ ¹ | FDC ₁ ⁰ | | | FDC ₂ ⁰ | FDC ₁ ⁰ |
| 5 | @-c ¹ | @c ¹ | @c ⁰ | Acq ₁ ¹ | Acq ₂ ¹ | @-c ⁰ | @c ⁰ |
| 6 | book ² @true | | | | | | |
| 7 | Acq ₂ ² | Acq ₁ ² | FDC ₁ ¹ | FDC ₂ ¹ | | FDC ₂ ¹ | FDC ₁ ¹ |
| 8 | @c ² | @-c ² | Acq ₂ ² | @c ¹ | @-c ¹ | Acq ₂ ² | @-c ¹ |
| | ... | | ... | | | ... | ... |

Figure 8: Pipelined execution of the knock control

| rotation units | AD | | BUF1 | | BUF2 | | μC |
|----------------|------------------|------------------|-------------------|------------------|------------------|--------------------|--------------------------------------|
| 0 | book@true | | FDC ₁ | | | FDC ₂ | FDC ₁ FDC ₂ |
| 1 | Acq ₂ | Acq ₁ | @c ⁿ⁻¹ | Acq ₁ | Acq ₂ | @-c ⁿ⁻¹ | @c ⁿ⁻¹ @-c ⁿ⁻¹ |
| 2 | @-c ⁿ | @c ⁿ | fst = 1 | @c ⁿ | @-c ⁿ | fst = 1 | fst = 1 fst = 1 |

Figure 9: Pipelined scheduling table for the knock control

by $-c$. Each of the Acq_i and FDC_i operations use two resources: One of AD and μC and one of the memory controllers BUF1 and BUF2.

The operation durations must be interpreted here as upper WCET bounds in an *engine rotation referential*. More precisely, each duration gives the maximal rotation (in degrees) of the engine crankshaft during the execution of the operation. For the acquisition operation, this is the maximal acquisition window size. The FDC function runs on a microcontroller, and its duration is characterized with a classical WCET (in real time). Conversion to the engine rotation referential is performed by assuming the maximal engine rotation speed.

The algorithms of the next section determine that successive computation cycles can be at best pipelined as pictured in Fig. 8. To do so, they determine that $c^n = -c^{n-1}$ for all n , thus allowing the acquisition and FDC operations of successive computation cycles to be executed in parallel. Note that a resource can be allocated to two operations at the same date if their guards are exclusive. Like in Fig. 7, we represent here both activation scenarios, corresponding to different initial values of c .

The corresponding pipelined scheduling table is provided in Fig. 9. The system is schedulable if the length of this table is smaller than the engine rotation interval between successive triggers of computation cycles. In turn, this is given by the number of cylinders and structure of the engine. If the system is schedulable, the code generation technique of Section 3.2 can be used to automatically generate the book keeping memory cells and code. Thus, **we automate the analysis of [4] and also allow automatic code generation.**

| time | P1 | P2 | P3 |
|------|--------|--------|--------|
| 0 | A@true | | |
| 1 | | B@true | |
| 2 | | | C@true |
| 3 | D@true | | |

Figure 10: Dependency analysis example, non-pipelined

| time | P1 | P2 | P3 |
|------|------------------------|------------------------|------------------------|
| 0 | A@true $fst(A) = 0$ | | C@true $fst(C) = 1$ |
| 1 | D@true $fst(D) = 1$ | B@true $fst(B) = 0$ | |

Figure 11: Dependency analysis example, pipelined

4 Dependency analysis and main routine

In this section, we provide algorithms that determine if and when a new computation cycle can be started while another one is still active. The core of this computation is a dependency analysis which builds the DDG of Section 3.1. Dependency analysis is performed by the lines 1-10 of Algorithm 3, which act as a driver for Algorithm 2. The remainder of Algorithm 3 uses DDG-derived information to drive the pipelining routine (Algorithm 1).

Both the data dependency analysis and pipelining driver take as input a flag that chooses between two pipelining modes with different complexities and capabilities. To understand the difference, consider the non-pipelined scheduling table of Fig. 10. Resource P_1 has an idle period between operations A and B where a new instance of A can be started. However, to preserve a periodic execution model, A should not be restarted just after its first instance (at date 1). Indeed, this would imply a pipelined throughput of 1, but the fourth instance of A cannot be started at date 3 (only at date 6). The correct pipelining starts A at date 2, and results in the pipelined scheduling table of Fig. 11. Note that the pipelined system is strictly periodic, of period 2, because every instance of D is bound to its slot of size 1 between two instances of A (and vice-versa).

Determining if the reuse of idle spaces between operations is possible requires a complex analysis which looks for the smallest integer n greater than the lower bound of Section 3.1, smaller than the length of the initial table, such that a *well-formed* pipelined table of length n can be constructed. This computation is performed by lines 14-17 of Algorithm 3. We do not provide here the code of function *WellFormed*, which checks the respect of the well-formed properties of Section 2.3.

This complex computation can be avoided when idle spaces between two operations are excluded from use at pipelining time. This can be done by creating a dependency between any two operations of successive cycles that use a same resource and have non-exclusive execution conditions. In this case, the pipelined system period is exactly the lower bound of Section 3.1, and the output scheduling table is produced with a single call to Algorithm 1 (*BuildSchedule*).

in line 12 of Algorithm 3. Of course, Algorithm 2 needs to consider (in lines 9-12) the extra dependencies.

Excluding the idle spaces from pipelining also has the advantage of supporting a sporadic execution model. In sporadic systems the successive computation cycles can be executed with the maximal throughput specified by the pipelined table, but can also be triggered arbitrarily less often, for instance to tolerate timing variations, or to minimize power consumption in systems where the demand for computing power varies.

Algorithm 2 DependencyAnalysisStep

Inputs: \mathcal{S} : non-pipelined scheduling table

l : the list of events of \mathcal{S}

n : integer (cycle index)

$fast_pipelining_flag$: boolean

InputOutputs: $\overline{\mathcal{S}}$: annotated scheduling table

$curr$: current variable assignments

DDG : Data Dependency Graph

1: $\overline{\mathcal{S}} := Concat(\overline{\mathcal{S}}, Annotate(\mathcal{S}, n))$

2: **while** l not empty **do**

3: $e := head(l)$; $l := tail(l)$

4: **if** $e = start(o)$ **then**

5: Replace $Guard(o^n)$ by:

$$\bigvee_{w_i @ C_i \in curr(v_i), i=1, \dots, k} (C_1 \wedge \dots \wedge C_k) \wedge g_o(w_1, \dots, w_k)$$

where $Guard(o) = g_o(v_1, \dots, v_k)$.

6: **for all** p operation in \mathcal{S} , $u \in Out(p)$, $v \in In(o)$ **do**

7: **if** $u_p^0 @ C \in curr(v)$ and $C \wedge Guard(o^n) \neq false$ **then**

8: $DDG := DDG \cup \{(p^0, o^n, n)\}$

9: **if** $fast_pipelining_flag$ **then**

10: **if** $Res(o) \cap Res(p) \neq \emptyset$ **then**

11: **if** $Guard(o^n) \wedge Guard(p^0) \neq false$ **then**

12: $DDG := DDG \cup \{(p^0, o^n, n)\}$

13: **else**

14: */* e = end(o) */*

15: **for all** $v \in Out(o)$ **do**

16: $new_curr := \{v_o^n @ Guard(o^n)\}$

17: **for all** $v_p^k @ C \in curr(v)$ **do**

18: $C' := C \wedge \neg Guard(o^n)$

19: **if** $C' \neq false$ **then**

20: $new_curr := new_curr \cup \{v_p^k @ C'\}$

21: $curr(v) := new_curr$

The remainder of this section details the dependency analysis phase. The output of this analysis is the lower bound defined in Section 3.1, computed as *period_minorant*. The analysis is organized around the **repeat** loop which incrementally computes, for $cycle \geq 1$, the DDG dependencies of the type $(o_1, o_2, cycle)$. The computation of the DDG is not complete: We bound it using a loop termination condition derived from our knowledge of the pipelining algo-

rithm. This condition is based on the observation that if $period_minorant * k \geq len(\mathcal{S})$ then execution cycles n and $n + k$ cannot overlap in time (for all n).

The DDG computation works by incrementally unrolling the non-pipelined scheduling table. At each unrolling step, the result is put in the SSA-like data structure $\overline{\mathcal{S}}$ that allows the computation of (an over-approximation of) the dependency set. Unrolling is done by annotating each instance of an operation o with the cycle n in which it has been instantiated. The notation is o^n . Putting in SSA-like form is based on splitting each memory cell v into one version per operation instance producing it (v_o^n , if $v \in Out(o)$), and one version for the initial value (v_{init}). Annotation and variable splitting is done on a per-cycle basis by the *Annotate* routine (not provided here) which changes for each operation o its name to o^n , and replaces $Out(o)$ with $\{v_o^n \mid v \in Out(o)\}$ (n is here the cycle index parameter). Instances of \mathcal{S} produced by *Annotate* are then assembled into $\overline{\mathcal{S}}$ by the *Concat* function which simply adds to the date of every operation in the second argument the length of its first argument.

Recall that we are only interested in dependencies between operations in different cycles. Then, in each call to Algorithm 2 we determine the dependencies between operations of cycle 0 and operations of cycle n , where n is the current cycle. To determine them, we rely on a symbolic execution of the newly-added part of $\overline{\mathcal{S}}$, *i.e.* the operations o^k with $k = n$. Symbolic execution is done through a traversal of list l , which contains all operation start and end events of \mathcal{S} , and therefore $\overline{\mathcal{S}}$, ordered by increasing date. For each operation o of \mathcal{S} , l contains two elements labeled $start(o)$ and $end(o)$. The list is ordered by increasing event date using the convention that the date of $start(o)$ is $t(o)$, and the date of $end(o)$ is $t(o) + d(o)$. Moreover, if $start(o)$ and $end(o')$ have the same date, the $start(o)$ event comes first in the list.

At each point of the symbolic execution, the data structure *curr* identifies the possible producers of each memory cell. For each cell v of the initial table, $curr(v)$ is a set of pairs $w@C$, where w is a version of v of the form v_o^k or v_{init} , and C is a predicate over memory cell versions. In the pair $w@C$, C gives the condition on which the value of v is the one corresponding to its version w at the considered point in the symbolic simulation. Intuitively, if $v_o^k@C \in curr(v)$, and we symbolically execute cycle n , then C gives the condition under which in any real execution of the system v holds the value produced by o , $n - k$ cycles before. The predicates of the elements in $curr(v)$ provide a partition of true. Initially, $curr(v)$ is set to $\{v_{init}@true\}$ for all v . This is changed by Algorithm 2 (lines 15-21), and by the call to *InitCurr* in Algorithm 3. We do not provide this last function, which performs the symbolic execution of the nodes of $\overline{\mathcal{S}}$ annotated with 0. Its code is virtually identical to that of Algorithm 2, lines 1 and 6-12 being excluded.

At each operation start step of the symbolic execution, *curr* allows us to complete the SSA transformation by recomputing the guard of the current operation over the split variables (line 5 of Algorithm 2). In turn, this allows the computation of the dependencies (lines 6-12). Predicate comparisons are handled by a SAT solver that also considers a Boolean abstraction of the operations of the algorithm. In our knock control example, the Boolean abstraction of the *book* operation provides the information that $c_n = \neg c_{n-1}$.

Algorithm 3 PipeliningDriver

Input: \mathcal{S} : non-pipelined schedule table
 $fast_pipelining_flag$: boolean
Output: $\hat{\mathcal{S}}$: pipelined schedule table

- 1: $l := BuildEventList(\mathcal{S})$
- 2: $period_minorant := 0$
- 3: $cycle := 0$
- 4: $\bar{\mathcal{S}} := Annotate(\mathcal{S}, cycle)$
- 5: $curr := InitCurr(\bar{\mathcal{S}})$
- 6: **repeat**
- 7: $cycle := cycle + 1$
- 8: $(\bar{\mathcal{S}}, curr, DDG) := DependencyAnalysisStep(\mathcal{S}, l,$
 $cycle, fast_pipelining_flag, \bar{\mathcal{S}}, curr, DDG)$
- 9: $period_minorant := \max(period_minorant,$
 $\max_{(o_1, o_2, cycle) \in DDG} \lceil \frac{t(o_1) + d(o_1) - t(o_2)}{cycle} \rceil)$
- 10: **until** $period_minorant * cycle \geq len(\mathcal{S})$
- 11: **if** $fast_pipelining_flag$ **then**
- 12: $\hat{\mathcal{S}} := BuildSchedule(\mathcal{S}, period_minorant)$
- 13: **else**
- 14: **for** $new_period := period_minorant$ **to** $len(\mathcal{S})$ **do**
- 15: $\hat{\mathcal{S}} := BuildSchedule(\mathcal{S}, new_period)$
- 16: **if** $WellFormed(\hat{\mathcal{S}})$ **then**
- 17: **goto** 18
- 18: **return**

5 Experimental results

We have applied our pipelining algorithms on 3 significant, real-life examples of real-time implementation problems (there are no standardized benchmarks). The results are synthesized in Table 12.

The largest example we use is the embedded control application of the CyCab electric car [15]. The control application we use allows the CyCab to be driven manually or in an autonomous “platooning” mode where it follows the vehicle in front of it, letting it make the speed and direction change decisions. The embedded software runs on a platform composed of 3 micro processors connected through a CAN bus. Our pipelining technique allows a significant reduction of 27% in cycle time. This reduction means that the application can be significantly complexified while maintaining I/O latency.

| example | Scheduling table length | | |
|---------|-------------------------|-----------|------|
| | initial | pipelined | gain |
| cycab | 1482 | 1083 | 27% |
| ega | 84 | 79 | 6% |
| knock | 6 | 3 | 50% |
| simple | 3 | 1 | 66% |

Figure 12: Experimental results

The second example is an adaptive equalizer. This filter is normally part of a larger control application, but we considered it here in isolation. The particularity of this example is that it has already been carefully designed to exploit the parallelism of the execution platform (it can be seen as “manually pipelined”). The cycle length reduction after application of our technique is not very large, but it is still significant in spite of the very optimized starting point.

The third example is the knock controller of Section 3.3. We also add a line for our toy example. The comparison is interesting, because this example allows for an ideal pipelining with a resource usage of 100%.

6 Conclusion

We have defined a *latency-preserving* software pipelining approach allowing the optimization of the throughput of *periodic and sporadic real time systems* defined through *predicated* scheduling tables. We apply it on the output of well-established latency-optimizing scheduling tools, resulting in a scheduling flow that optimizes latency and throughput, with priority to latency. We applied our technique, with good results, on several real-life systems.

Many open problems remain. One of them is the exploitation of execution guards over partitioned architectures. Using the n-synchronous formalism[7] should allow us to express and exploit regular repetition patterns in the pipelining process. Another important goal is to integrate pipelining in the initial scheduling process, so that different trade-offs between latency, throughput, and resource usage can be obtained.

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