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► **To cite this version:**

Isabelle Herlin, Dominique Béréziat, Nicolas Mercier. Recovering missing data on satellite images. Heyden, A. and Kahl, F. SCIA 2011 - Scandinavian Conference on Image Analysis, May 2011, Ystad Saltsjöbad, Sweden. Springer Verlag, 6688, pp.697-707, 2011, Lecture Notes in Computer Science. <10.1007/978-3-642-21227-7_65>. <inria-00612328>

HAL Id: inria-00612328

<https://hal.inria.fr/inria-00612328>

Submitted on 14 Oct 2011

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Recovering missing data on satellite images

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Abstract. Data Assimilation is commonly used in environmental sciences to improve forecasts, obtained by meteorological, oceanographic or air quality simulation models, with observation data. It aims to solve an evolution equation, describing the dynamics, and an observation equation, measuring the misfit between the state vector and the observations, to get a better knowledge of the actual system’s state, named the reference. In this article, we describe how to use this technique to recover missing data and reduce noise on satellite images. The recovering process is based on assumptions on the underlying dynamics displayed by the sequence of images. This is a promising alternative to methods such as space-time interpolation. In order to better evaluate our approach, results are first quantified for an artificial noise applied on the acquisitions and then displayed for real data.

1 Introduction

Satellite acquisitions are commonly contaminated during the acquisition process: images display noise of various extent. Moreover, part of the data are covered by clouds. These structures are considered as occlusions in case of ocean images. The issue of recovering noisy and missing data has been extensively studied by the scientific community, in order to allow a better visualization and understanding of the information. A first class of methods groups the interpolation techniques [1,8]. Interpolation is used to convert data acquired on an irregular grid to a regular one. B-splines are frequently chosen as they allow a good compromise between the adequacy to input data and the regularity of the result. If interpolation is applied to the issue of recovering missing data, regions can be recovered with multi-scale B-splines [10]. Another possibility is to use a normalized convolution [9] applying only on valid pixels. The kernel convolution, usually chosen Gaussian, can be driven by the local image gradient orientation [12]. However, if the surface of missing data is too large, these techniques become insufficient. A second class of methods concerns the so-called “inpainting” approaches, which make use of oriented diffusion processes. Using the local orientation of image gradient, it becomes possible to close interrupted lines [6], and even, to recover large regions by diffusing the image texture in the direction of the image gradient [4,5,7,11,14]. However, these methods are either spatial or space-time techniques, with time only considered as an additional dimension:

they do not use any knowledge on the underlying dynamics that is visualized by the image sequence. In this paper, we propose an alternative and design a new data assimilation method to recover missing data, based on assumptions over the dynamics.

Section 2 briefly summarizes the weak formulation of variational data assimilation, that is applied in the paper. Section 3 describes its application to the issue of recovering missing data while Section 4 displays results and quantifies them on artificial data.

2 Variational Data Assimilation

Let us first summarize the principles of variational data assimilation.

2.1 Mathematical setting

Let \mathbf{X} being a state vector depending on the spatial location \mathbf{x} ($\mathbf{x} = (x, y)$ for 2D images) and time t . \mathbf{X} is defined on $A = \Omega \times [0, \mathbf{T}]$, Ω being the bounded spatial domain and $[0, \mathbf{T}]$ the temporal domain.

We assume \mathbf{X} is evolving in time according to:

$$\frac{\partial \mathbf{X}}{\partial t}(\mathbf{x}, t) + \mathbb{M}(\mathbf{X})(\mathbf{x}, t) = \mathcal{E}_m(\mathbf{x}, t) \quad (1)$$

\mathbb{M} , named *evolution model*, is supposed differentiable. As \mathbb{M} describes approximately the effective evolution of the state vector, based on assumptions, a *model error* \mathcal{E}_m is introduced to quantify the deviation in space and time.

Observations $\mathbf{Y}(\mathbf{x}, t)$, which are satellite image acquisitions in this paper, are available at location \mathbf{x} and date t and linked to the state vector through an observation equation:

$$\mathbf{Y}(\mathbf{x}, t) = \mathbb{H}(\mathbf{X}(\mathbf{x}, t)) + \mathcal{E}_O(\mathbf{x}, t) \quad (2)$$

The *observation error* \mathcal{E}_O simultaneously represents the imperfection of the observation operator \mathbb{H} and the measurement errors.

We consider having some knowledge on the initial condition of the state vector at $t = 0$:

$$\mathbf{X}(\mathbf{x}, 0) = \mathbf{X}_b(\mathbf{x}) + \mathcal{E}_b(\mathbf{x}) \quad (3)$$

with \mathbf{X}_b named the *background value* and \mathcal{E}_b the *background error*.

\mathcal{E}_m , \mathcal{E}_O and \mathcal{E}_b are assumed to be Gaussian and characterized by their covariance matrices Q , R and B [13].

2.2 Variational formulation

In order to solve the system (1), (2), (3) with respect to \mathbf{X} having a maximal a posteriori probability given the observations, the functional (4) is defined and

has to be minimized. This is called “weak formulation” of 4D-Var, because the first term corresponds to a non perfect model.

$$\begin{aligned}
E(\mathbf{X}) = & \frac{1}{2} \int_A \left(\frac{\partial \mathbf{X}}{\partial t} + \mathbb{M}(\mathbf{X}) \right)^T (\mathbf{x}, t) Q^{-1}(\mathbf{x}, t) \left(\frac{\partial \mathbf{X}}{\partial t} + \mathbb{M}(\mathbf{X}) \right) (\mathbf{x}, t) dx dt \\
& + \int_A (\mathbf{Y} - \mathbb{H}(\mathbf{X}))^T (\mathbf{x}, t) R^{-1}(\mathbf{x}, t) (\mathbf{Y} - \mathbb{H}(\mathbf{X})) (\mathbf{x}, t) dx dt \\
& + \int_{\Omega} (\mathbf{X}(\mathbf{x}, 0) - \mathbf{X}_b(\mathbf{x}))^T B^{-1}(\mathbf{x}) (\mathbf{X}(\mathbf{x}, 0) - \mathbf{X}_b(\mathbf{x})) dx
\end{aligned} \tag{4}$$

\mathcal{E}_m , \mathcal{E}_O and \mathcal{E}_b are assumed to be independent with no correlation between two space-time location and the functional E represents the log-density of the joint probability law [2]. The minimization is carried out by solving the associated Euler-Lagrange equation with an auxiliary variable λ , named *adjoint variable*:

$$\lambda(\mathbf{x}, \mathbf{T}) = 0 \tag{5}$$

$$-\frac{\partial \lambda}{\partial t} + \left(\frac{\partial \mathbb{M}}{\partial \mathbf{X}} \right)^* \lambda = \left(\frac{\partial \mathbb{H}}{\partial \mathbf{X}} \right)^* (\mathbf{x}, t) R^{-1} (\mathbf{Y} - \mathbb{H}(\mathbf{X})) (\mathbf{x}, t) \tag{6}$$

$$\mathbf{X}(\mathbf{x}, 0) = B\lambda(\mathbf{x}, 0) + \mathbf{X}_b(\mathbf{x}) \tag{7}$$

$$\frac{\partial \mathbf{X}}{\partial t} + \mathbb{M}(\mathbf{X}) = Q\lambda(\mathbf{x}, t) \tag{8}$$

As the initial condition for λ is given at time \mathbf{T} (Equation (5)), λ is computed backward in time using (6). Equation (6) makes use of two *adjoint operators* denoted by $\left(\frac{\partial \mathbb{M}}{\partial \mathbf{X}} \right)^*$ and $\left(\frac{\partial \mathbb{H}}{\partial \mathbf{X}} \right)^*$ that are formally the dual operators of $\frac{\partial \mathbb{M}}{\partial \mathbf{X}}$ and $\frac{\partial \mathbb{H}}{\partial \mathbf{X}}$. Solving Equations (5–8), also named the Optimality System, is however not straightforward: the state vector is determined from Equations (7) and (8) using the adjoint variable and the adjoint variable is determined from Equations (5) and (6) using the state vector. To break this deadlock, an incremental method is applied, that is fully described in [3].

3 Recovering of missing data

To recover the missing data, we define the quantities described in Section 2.1 in the following way. \mathbf{X} is defined as $(\mathbf{W} \quad \mathbf{q})^T$: $\mathbf{W} = (\mathbf{u} \quad \mathbf{v})^T$ is the motion vector, and \mathbf{q} is a tracer that is compared to the image observations during the assimilation phase.

In Equation (1), \mathbb{M} is equal to $(\mathbb{M}_{\mathbf{W}} \quad \mathbb{M}_{\mathbf{q}})^T$, with $\mathbb{M}_{\mathbf{W}}$ and $\mathbb{M}_{\mathbf{q}}$, respectively, the evolution models of \mathbf{W} and \mathbf{q} . A stationary assumption is used for the velocities and $\mathbb{M}_{\mathbf{W}}$ reduces to 0. This simple heuristics is acceptable for a large range of marine processes if the velocity is less than 0.1 to 0.5 meters per second. The evolution of \mathbf{q} is modeled with its transport by the velocity \mathbf{W} and $\mathbb{M}_{\mathbf{q}} =$

$\nabla \mathbf{q}^T \mathbf{W}$. Moreover, we assume that \mathcal{E}_m reduces to its component on the evolution of \mathbf{q} .

As the quantity \mathbf{q} , which is compared to the image data, is one component of \mathbf{X} , \mathbb{H} is a projection and Equation (2) reduces to:

$$I(\mathbf{x}, t) = \mathbf{q}(\mathbf{x}, t) + \mathcal{E}_O \quad (9)$$

The variance R of the Gaussian noise \mathcal{E}_O is chosen so that $R^{-1}(\mathbf{x}, t)$ (used in Equation (2)) is almost infinitesimal, on noisy pixels. These are then discarded from the computation.

The background value \mathbf{X}_b depends on the available knowledge. A null value is given for the background of motion \mathbf{W}_b and the first observation is taken as background of the tracer \mathbf{q}_b .

4 Results

The approach, described in Section 3, is applied on satellite acquisitions and compared with state-of-the-art methods. First, an artificial noise is added to the original data, in order to quantify results. Second, our approach is used on a sequence displaying missing data, in order to illustrate its potential to recover information on satellite acquisitions.

4.1 Artificial noise

A sequence of satellite Sea Surface Temperature (SST) images has been acquired by NOAA-AVHRR over the Black Sea in July 2005⁴ (see Fig. 1).

In a first experiment, a noise has been added to the second image as a black square (10×10) (see Fig. 2). Data assimilation is then applied as explained in Section 3. Bertalmio *et al* [4] and Tschumperlé *et al* [14] are also used on the same data. Results are displayed on Fig. 2. Their quality is quantified, in Table 1, by the mean, minimum and maximum of the difference between the recovered image and the original image whose grey level values over the whole sequence range from 23.428595 to 25.71952.

Method	Mean	Min	Max
Our approach	-0.001010	-0.215643	0.382748
Bertalmio <i>et al</i>	-0.004595	-0.254509	0.145491
Tschumperlé <i>et al</i>	-0.000339	-0.299999	0.299999

Table 1. Statistics on the recovered images.

In a second experiment, the noise is a 50×50 square added to the second image (see Fig. 3). The same methods are again applied and results are displayed

⁴ Data have been provided by E. Plotnikov and G. Korotaev from the Marine Hydrophysical Institute of Sevastopol, Ukraine.

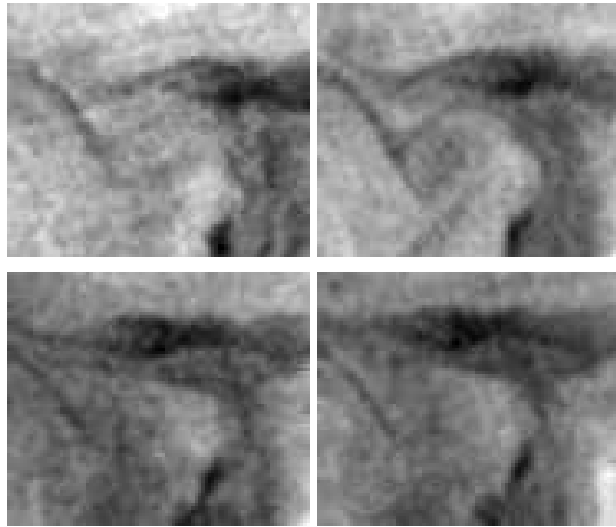
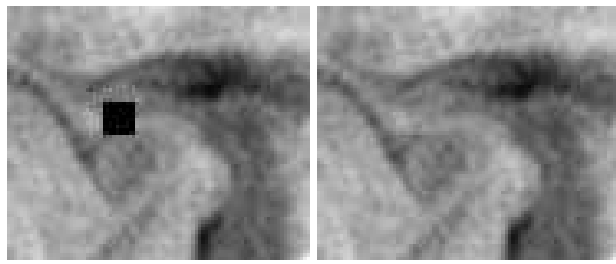
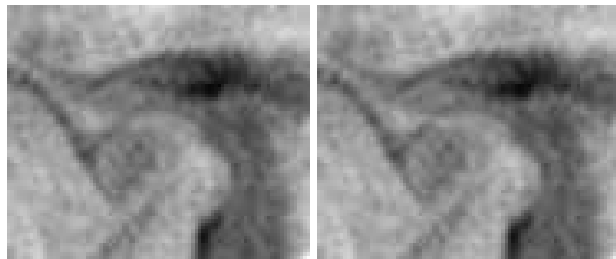


Fig. 1. NOAA-AVHRR images.



(a) Noisy image

(b) Our approach



(c) Bertalmio *et al*

(d) Tschumperlé *et al*

Fig. 2. Recovering of the noisy data.

on Fig. 3. Statistics are given in Table 2. We also provide the correlation value between recovered and real data.

These experiments demonstrate that our approach is ahead of state-of-the-art techniques as the size of the noisy region increases. First order statistics, correlation and visual results are much more better with our approach in the case of the 50×50 square. This demonstrates the usefulness of dynamics information in the process.

Method	Mean	Min	Max	Correlation
Our approach	0.008273	-0.543972	0.769663	0.702
Bertalmio <i>et al</i>	0.023610	-0.867842	0.950588	0.482
Tschumperlé <i>et al</i>	0.026362	-0.799999	1.000000	0.572

Table 2. Statistics on the recovered images.

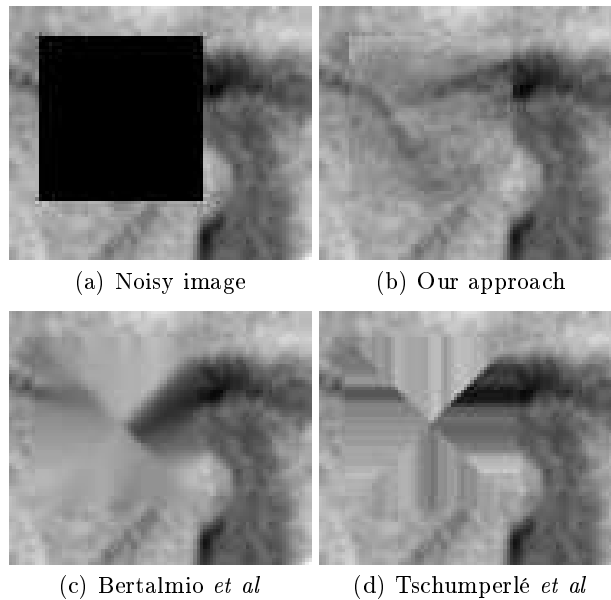


Fig. 3. Recovering of the noisy data.

In a third experiment, noise is added on all images, except the first one (see Fig. 4). Our approach is applied and results are displayed on Fig. 5. Table 3 provides statistics (Mean, Min, Max) of the three corrupted frames, over the 10×10 squares, for the original, result and difference data.

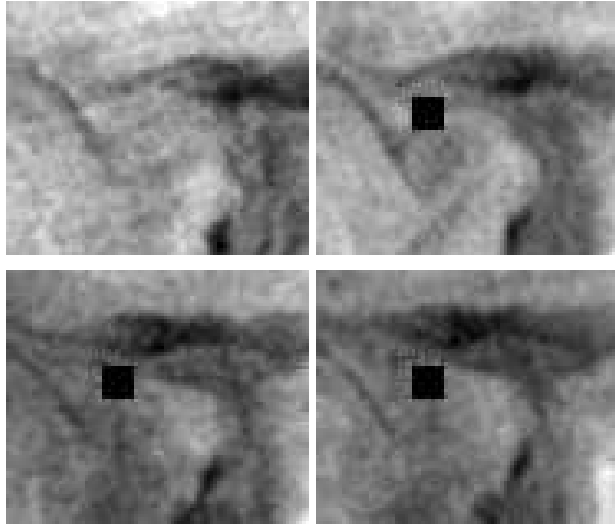


Fig. 4. Noisy sequence (squares are 10×10).

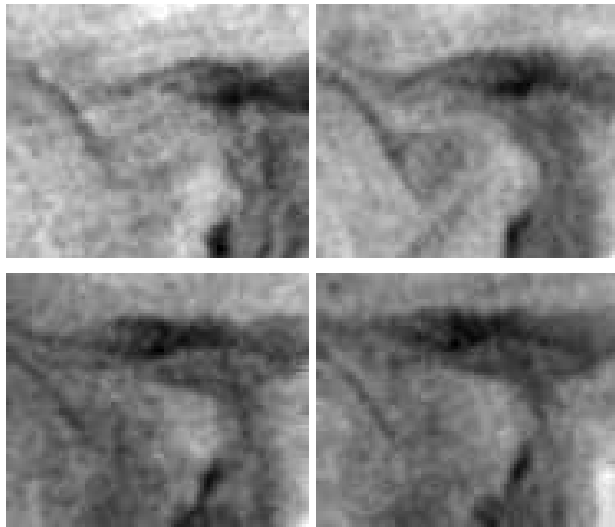


Fig. 5. Recovering of the noisy data.

Frame	Stat.	Original	Result	Difference
2	Mean	24.652100	24.563805	-0.001706
	Min	23.415665	23.415922	-0.482744
	Max	25.715666	25.716354	0.220243
3	Mean	24.652100	24.652100	0.001935
	Min	23.642063	23.642063	-0.461876
	Max	26.042063	26.042063	0.151356
4	Mean	24.652100	24.652100	-0.00124
	Min	23.543968	23.543968	-0.361067
	Max	26.143969	26.143969	0.250856

Table 3. Error statistics.

These three experiments demonstrate that our approach successfully recover missing or noisy data of limited extension.

4.2 Real noise

A sequence of six SST acquisitions acquired by NOAA-AVHRR over the Black Sea in May 2005 is displayed on Fig. 6. Noise is mainly due to clouds. Using metadata linked to the image, a null radiometric value is given to these noisy pixels that are displayed in cyan. A specific value is given to ground pixels, which are displayed in black. This is the case for region at the left corner.

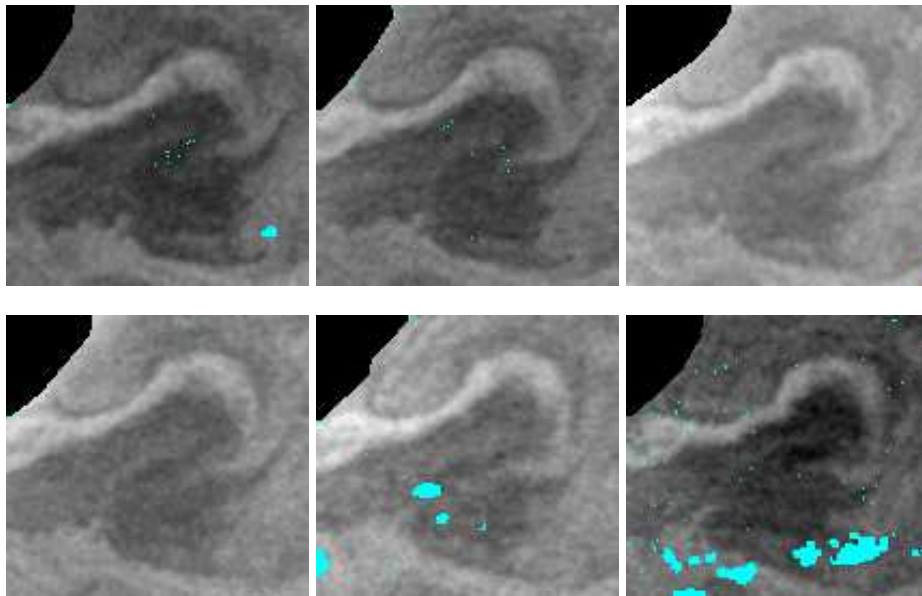


Fig. 6. Satellite acquisitions.

Using Bertalmio *et al* [4], a pre-processing is applied on the first image (see Fig. 7) in order to fill in the missing data (excepted ground pixels).

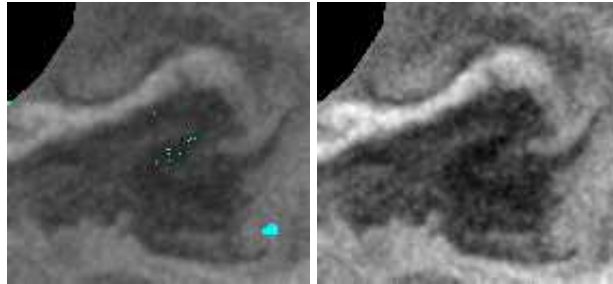


Fig. 7. First frame: original data and result of preprocessing.

Our approach is applied. The comparison between the original and result data is displayed on Fig. 8. This demonstrates the potential of our approach.

5 Conclusion

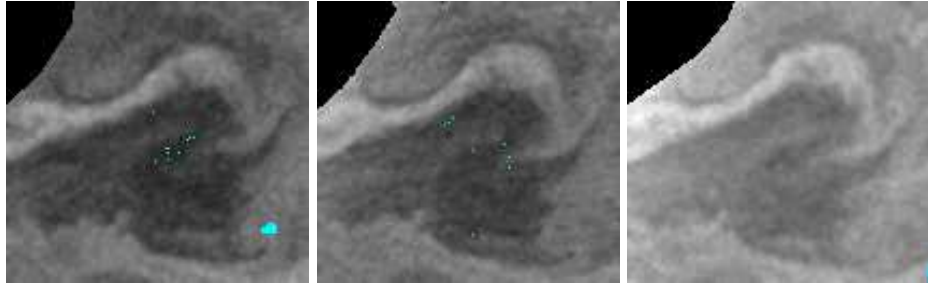
In this paper, we describe an approach to recover missing data on a sequence of satellite images, based on the underlying dynamics. This is an alternative to the use of spatial properties as commonly done in the state-of-the-art. The method relies on an evolution equation, describing the dynamics, and a variational data assimilation algorithm that solves the evolution equation with constraints from the observations. Given an image sequence, the data assimilation method computes a tracer \mathbf{q} and a velocity field \mathbf{W} on the space-time domain. The resulting $\mathbf{q}(\mathbf{x}, t)$ is the recovered image value.

We quantify the relevance of our approach on satellite data, corrupted by an artificial noise and provide comparisons with state-of-the-art methods. Our approach has also been tested on satellite images displaying natural missing data.

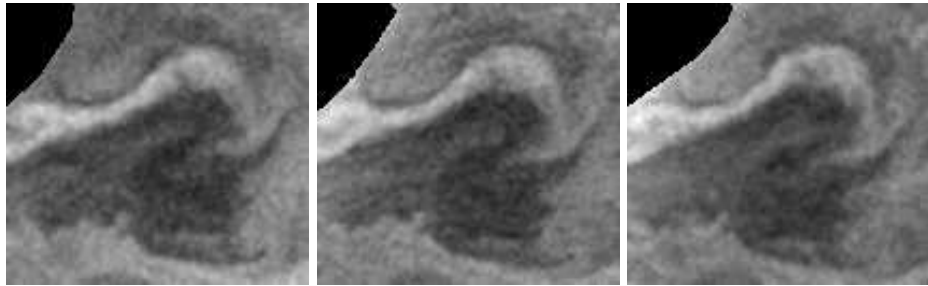
In order to improve the quality of results, alternative evolution equations should be considered. For instance, shallow water equations are known to correctly describe the surface velocity of SST acquisitions. Their use should allow a better recovering process. Moreover, the illumination change, due to various acquisition times over the sequence, should be better modeled in the evolution equation.

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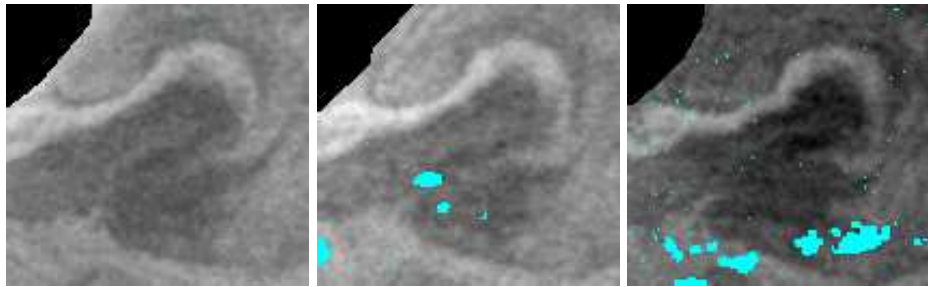
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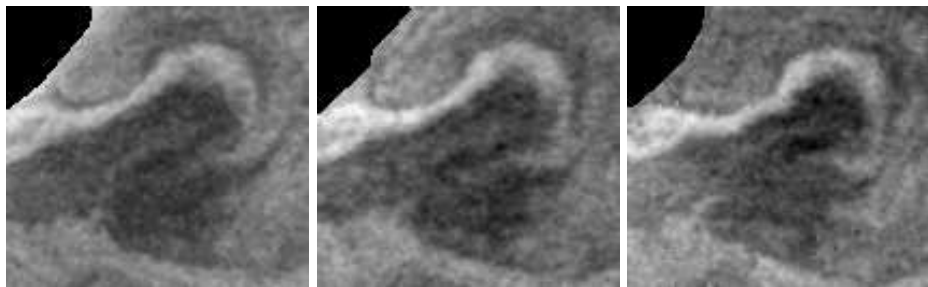
(a) Observations: frames 1, 2 and 3



(b) Results: frames 1, 2 and 3



(c) Observations: frames 4, 5 and 6



(d) Results: frames 4, 5 and 6

Fig. 8. Observations and results.

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