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# Transforming Password Protocols to Compose

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## Abstract

Formal, symbolic techniques are extremely useful for modelling and analysing security protocols. They improved our understanding of security protocols, allowed to discover flaws, and also provide support for protocol design. However, such analyses usually consider that the protocol is executed in isolation or assume a bounded number of protocol sessions. Hence, no security guarantee is provided when the protocol is executed in a more complex environment.

In this paper, we study whether password protocols can be safely composed, even when a same password is reused. More precisely, we present a transformation which maps a password protocol that is secure for a single protocol session (a decidable problem) to a protocol that is secure for an unbounded number of sessions. Our result provides an effective strategy to design secure password protocols: (i) design a protocol intended to be secure for one protocol session; (ii) apply our transformation and obtain a protocol which is secure for an unbounded number of sessions. Our technique also applies to compose different password protocols allowing us to obtain both inter-protocol and inter-session composition.

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**Keywords and phrases** Security, cryptographic protocols, composition

## 1 Introduction

Password-based cryptographic protocols are a prominent means to achieve authentication or to establish authenticated, shared session keys, *e.g.* EKE [10], SPEKE [23], or the KOY protocol [24]. The advantage of such schemes is that they do not rely on a key infrastructure but only on a shared password, which is often human chosen or at least human memorable. However, such passwords are generally *weak* and may be subject to dictionary (also called guessing) attacks. In an *online* dictionary attack an adversary tries to execute the protocol for each possible password. While such attacks are difficult to avoid they can be made impracticable by limiting the number of password trials or adding a time-out of few seconds after a wrong password. In an *offline* guessing attack an adversary interacts with one or more sessions in a first phase. In a second, offline phase the attacker uses the collected data to verify each potential password. In this paper we concentrate on the second type of attacks.

It has been widely acknowledged that security protocol design is extremely error prone and rigorous security proofs are a necessity. Formal, symbolic models, in the vein of Dolev and Yao's seminal work [21], provide effective and often automated methods to find errors or prove protocols correct. While most of these methods focus on secrecy and authentication, resistance against offline guessing attacks has been considered in some works [26, 9, 17]. We will in particular focus on an elegant definition of resistance against offline guessing attacks by Corin *et al.* [17] which was introduced in the framework of the applied pi calculus [1] and for which tool support exists [11, 9].

Nowadays, state-of-the-art protocol analysis tools are able to analyse a variety of protocols. However, this analysis is generally carried out in isolation, *i.e.*, analysing one protocol



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at a time. This is motivated by the fact that in models like the applied pi calculus, security properties, even if shown in isolation, hold in the presence of an arbitrary (public) environment. This is similar to *universal composition* (UC) [14] in computational models. However, these arbitrary environments are public, in the sense that they don't have access to the secrets of the protocol under analysis. This is of course necessary as otherwise a completely arbitrary environment could simply output all secret cryptographic key material and trivially break the protocol's security. While not sharing key material may be a reasonable hypothesis in some cases it is certainly not the case when we compose the same sessions of a same protocol or in a situation where the same password is used in different protocols — it is indeed unreasonable to assume that all users have different passwords for each application.

### Our contributions

In this paper we propose a simple protocol transformation which ensures that a same password can safely be shared between different protocols. More precisely, our results can be summarized as follows. We use a safe transformation which replaces a weak password  $w$  by  $h(t, w)$  where  $t$  is some *tag* and  $h$  a hash function. Then, we show how to use this tagging technique to compose different protocols. Consider  $n$  password protocols such that each protocol resists separately against guessing attacks on  $w$ . When we instantiate the tag  $t$  to a unique protocol identifier *pid*, one for each of the  $n$  protocols, we show that the parallel composition of these tagged protocols resists against guessing attacks on  $w$ , where  $w$  is the password shared by each of these protocols. Next we show how to dynamically establish a session identifier *sid*. Instantiating the tag  $t$  by this session identifier allows us to compose different sessions of a same protocol. Hence it is sufficient to prove resistance against guessing attacks on a single session of a protocol to conclude that the transformed protocol resists against guessing attacks for an unbounded number of sessions. These techniques can also be combined into a tag which consists of both the protocol and session identifier obtaining both inter-protocol and inter-session composition. One may note that resistance against guessing attack is generally not the main goal of a protocol, which may be authentication or key exchange. It follows however from our proofs that trace properties such as authentication will also be preserved. Detailed proofs of our results can be found in [16].

### Related Work

In recent years, compositional reasoning has received a lot of attention. Datta *et al.* [19] provide a general strategy whereas our composition result identifies a specific class of protocols that can be composed. In [22, 5, 18], some criteria are given to ensure that parallel and in some works sequential composition is safe. In [6] the issue of composition of sessions of a same protocol is addressed using a transformation similar to the one considered in this paper. None of these works considers password protocols and resistance to guessing attacks. Composition of different password protocols (but not of sessions of the same protocol) using a protocol identifier tag was shown in [20]. In this paper we generalize these results to allow composition of sessions of a same protocol. Moreover, the composition theorem given in [20] only applies to two protocols (and cannot be iterated). This shortcoming was overseen by the authors of [20] and we adapt their result to apply to an arbitrary number of protocols in parallel.

In computational models, Boyko *et al.* [13] presented a security model for password-based key-exchange based on simulation proofs, ensuring security in case of composition. A more generic solution was proposed by Canetti *et al.* [15] who propose a protocol based on KOY,

which is secure in the UC model [14]. This work has been extended to active adversaries [4], group key exchange [3] and to define distributed public-key cryptography from passwords in *e.g.* [2]. A main difference between works in the UC model and our work (besides the obvious differences between symbolic and computational models) is that in the UC model designers generally apply an “ad-hoc recipe” (often using “magical” session identifiers given by the framework) and show that one session of a protocol fulfills the given requirements. The UC theorem then ensures composition, *i.e.*, composition follows from the strong security definition which has to be proven. In our work we make explicit the construction of session identifiers in our transformation and prove that a generic protocol transformation can be used to achieve composition. Note, however, that despite this difference, both approaches share many essential ideas.

Finally, we may note that *tagging* is a well known technique. We have already mentioned its use to achieve some forms of composition [6, 18]. Other forms of tagging were used to ensure termination of a verification procedure [12], safely bound the length of messages [7] or obtain decidability for the verification of some classes of protocols [27].

## 2 Modeling Protocols

In this section, we recall the cryptographic process calculus defined in [20] for describing protocols. This calculus is a simplified version of the applied pi calculus [1]. In particular we only consider one channel, which is public (*i.e.* under the control of the attacker) and we only consider finite processes, *i.e.* processes without replication.

### 2.1 Messages

A protocol consists of some agents communicating on a network. The messages sent by the agents are modelled using an abstract term algebra. For this, we assume an infinite set of *names*  $\mathcal{N}$ , for representing keys, data values, nonces, and names of agents, and we assume a *signature*  $\Sigma$ , *i.e.* a finite set of *function symbols* such as `senc` and `sdec`, each with an arity. Given a signature  $\Sigma$  and an infinite set of variables  $\mathcal{X}$ , we denote by  $\mathcal{T}(\Sigma)$  (resp.  $\mathcal{T}(\Sigma, \mathcal{X})$ ) the set of *ground terms* (resp. *terms*) over  $\Sigma \cup \mathcal{N}$  (resp.  $\Sigma \cup \mathcal{N} \cup \mathcal{X}$ ). We write  $fn(M)$  (resp.  $fv(M)$ ) for the set of names (resp. variables) that occur in the term  $M$ . A *substitution*  $\sigma$  is a mapping from a finite subset of  $\mathcal{X}$  called its domain and written  $\text{dom}(\sigma)$  to  $\mathcal{T}(\Sigma, \mathcal{X})$ . The application of a substitution  $\sigma$  to a term  $T$  is written  $T\sigma$ . We also allow *replacement of names by terms*: the term  $M\{N/n\}$  is the term obtained from  $M$  after replacing any occurrence of the name  $n$  by the term  $N$  (assuming that  $n$  does not occur in  $N$ ). We sometimes abbreviate the sequence of terms  $t_1, \dots, t_n$  by  $\tilde{t}$  and write  $\{\tilde{t}/\tilde{x}\}$  for  $\{t^1/x_1, \dots, t^n/x_n\}$ .

To model algebraic properties of cryptographic primitives, we define an *equational theory* by a finite set  $E$  of equations  $U = V$  with  $U, V \in \mathcal{T}(\Sigma, \mathcal{X})$  such that  $U, V$  do not contain names. We define  $=_E$  to be the smallest equivalence relation on terms, that contains  $E$  and that is closed under application of function symbols and substitutions of terms for variables.

► **Example 1.** Consider the signature  $\Sigma = \{\text{sdec}, \text{senc}, \langle \rangle, \text{proj}_1, \text{proj}_2, \text{exp}\}$ . The function symbols `sdec`, `senc`, `⟨⟩` and `exp` of arity 2 represent respectively symmetric encryption and decryption, pairing as well as exponentiation. Functions `proj1` and `proj2` of arity 1 model projection of the first and the second component of a pair. As an example that will be useful for modelling the SPEKE protocol [23], we consider the equational theory  $E$ , defined by the following equations:

$$\begin{aligned} \text{sdec}(\text{senc}(x, y), y) &= x & \text{proj}_i(\langle x_1, x_2 \rangle) &= x_i & (i \in \{1, 2\}) \\ \text{senc}(\text{sdec}(x, y), y) &= x & \text{exp}(\text{exp}(x, y), z) &= \text{exp}(\text{exp}(x, z), y) \end{aligned}$$

Let  $T_1 = \text{senc}(\text{proj}_2(\langle a, b \rangle), k)$  and  $T_2 = \text{senc}(b, k)$ . We have that the terms  $T_1$  and  $T_2$  are equal modulo  $\mathbf{E}$ , written  $T_1 =_{\mathbf{E}} T_2$ , while obviously the syntactic equality  $T_1 = T_2$  does not hold.

To represent the knowledge of an attacker (who may have observed a sequence of messages  $M_1, \dots, M_\ell$ ), we use the concept of *frame*. A frame  $\phi = \nu\tilde{n}.\sigma$  consists of a finite set  $\tilde{n} \subseteq \mathcal{N}$  of *restricted* names (those unknown to the attacker), and a substitution  $\sigma$  of the form  $\{M_1/z_1, \dots, M_\ell/z_\ell\}$  where each  $M_i$  is a ground term. The variables  $z_i$  enable an attacker to refer to each  $M_i$ . The *domain* of the frame  $\phi$ , written  $\text{dom}(\phi)$ , is  $\text{dom}(\sigma) = \{z_1, \dots, z_\ell\}$ .

Given a frame  $\phi$  that represents the information available to an attacker, and an equational theory  $\mathbf{E}$  on  $\Sigma$ , we may ask whether a given ground term  $M$  may be *deduced* from  $\phi$ . This relation is written  $\phi \vdash_{\mathbf{E}} M$  and is formally defined below.

► **Definition 2 (deduction).** Let  $M$  be a ground term and  $\phi = \nu\tilde{n}.\sigma$  be a frame. We have that  $M$  is *deducible from*  $\phi$ , denoted  $\nu\tilde{n}.\sigma \vdash_{\mathbf{E}} M$ , if and only if there exists a term  $N \in \mathcal{T}(\Sigma, \mathcal{X})$  such that  $\text{fn}(N) \cap \tilde{n} = \emptyset$  and  $N\sigma =_{\mathbf{E}} M$ .  $N$  is called a *recipe* of the term  $M$ .

Intuitively, the set of deducible messages is obtained from the messages  $M_i$  in  $\phi$ , the names that are not restricted in  $\phi$ , and closed under equality modulo  $\mathbf{E}$  and application of function symbols.

► **Example 3.** Consider the theory  $\mathbf{E}$  given in Example 1. Let  $\phi = \nu b, k. \{\text{senc}(b, k)/z_1, k/z_2\}$ . We have that  $\phi \vdash_{\mathbf{E}} k$ ,  $\phi \vdash_{\mathbf{E}} b$  and  $\phi \vdash_{\mathbf{E}} a$ . Indeed  $z_2$ ,  $\text{sdec}(z_1, z_2)$  and  $a$  are recipes of the terms  $k$ ,  $b$  and  $a$  respectively.

Two frames are considered equivalent when the attacker cannot detect the difference between the two situations they represent, that is, his ability to distinguish whether two recipes  $M, N$  produce the same term does not depend on the frame. Formally,

► **Definition 4 (static equivalence).** We say that two frames  $\phi_1 = \nu\tilde{n}.\sigma_1$  and  $\phi_2 = \nu\tilde{n}.\sigma_2$  are *statically equivalent*,  $\phi_1 \approx_{\mathbf{E}} \phi_2$ , when  $\text{dom}(\phi_1) = \text{dom}(\phi_2)$ , and for all terms  $M, N$  such that  $\text{fn}(M, N) \cap \tilde{n} = \emptyset$ , we have that:  $M\sigma_1 =_{\mathbf{E}} N\sigma_1$  if, and only if,  $M\sigma_2 =_{\mathbf{E}} N\sigma_2$ .

Static equivalence is useful to model the notion of security we consider in this paper, namely *resistance against guessing attacks*. To resist against a guessing attack, the protocol must be designed such that the attacker cannot decide on the basis of the data collected whether his current guess of the password is the actual password or not. Assume  $\phi = \nu\tilde{w}.\phi'$  is the frame representing the information gained by the attacker by eavesdropping one or more sessions and let  $\tilde{w}$  be the sequence of weak passwords. The frame  $\phi$  is resistant to guessing attacks if the attacker cannot distinguish between a situation in which he guesses the correct passwords  $\tilde{w}$  and a situation in which he guesses incorrect ones, say  $\tilde{w}'$ .

► **Definition 5 (frame resistant to guessing attacks).** The frame  $\nu\tilde{w}.\phi'$  is *resistant to guessing attacks* against the sequence of names  $\tilde{w}$  if  $\nu\tilde{w}.\phi' \approx \nu\tilde{w}.\nu\tilde{w}'.\phi'\{\tilde{w}'/\tilde{w}\}$  where  $\tilde{w}'$  is a sequence of fresh names.

This definition was proposed in [17, 9]. A slightly simpler formulation requiring  $\phi' \approx \phi'\{\tilde{w}'/\tilde{w}\}$  (without the name restrictions) was shown equivalent in [20] and will be used in this paper.

► **Example 6.** Consider the following protocol where  $h$  is a unary function symbol modelling a hash function (no equation on  $h$ ):

$$A \rightarrow B : \text{senc}(n, w) \quad B \rightarrow A : \text{senc}(h(n), w)$$

An interesting problem arises if the shared key  $w$  is a weak secret, *i.e.* vulnerable to brute-force off-line testing. Indeed, the frame representing the knowledge of the attacker at the end of a normal execution of this protocol is  $\phi = \nu w. \phi' = \nu w. \nu n. \{\text{senc}(n, w) / z_1, M / z_2\}$  where:

$$M = \text{senc}(h(\text{sdec}(\text{senc}(n, w), w)), w) =_{\text{E}} \text{senc}(h(n), w).$$

The frame  $\phi$  is not resistant to guessing attacks against the password  $w$ . Indeed, the test  $h(\text{sdec}(z_1, w)) \stackrel{?}{=} \text{sdec}(z_2, w)$  is a witness of the non-equivalence  $\phi' \not\approx_{\text{E}} \phi' \{w' / w\}$ .

## 2.2 Protocol Language and Semantics

### Syntax

The grammar for processes is given below. One has plain processes  $P, Q, R$  and extended processes  $A, B, C$  that allow the use of active substitutions and restrictions.

$P, Q, R :=$	plain processes	$A, B, C :=$	extended processes
$0$	null process	$P$	plain processes
$P \mid Q$	parallel composition	$A \mid B$	parallel composition
$\text{in}(x).P$	message input	$\nu n.A$	restriction
$\text{out}(M).P$	message output	$\{M/x\}$	active substitution
$\text{if } M = N \text{ then } P \text{ else } Q$	conditional		

As usual, names and variables have scopes, which are delimited by restrictions and inputs. We write  $fv(A)$ ,  $bv(A)$ ,  $fn(A)$ ,  $bn(A)$  for the sets of free and bound variables (resp. names). Moreover, we consider processes such that  $bn(A) \cap fn(A) = \emptyset$ ,  $bv(A) \cap fv(A) = \emptyset$ , and each name and variable is bound at most once in  $A$ . An extended process is *closed* if all free variables are in the domain of an active substitution. An *instance* of an extended process is a process obtained by a bijective renaming of its bound names and variables. We observe that given processes  $A$  and  $B$ , there always exist instances  $A'$  and  $B'$  of  $A$ , respectively  $B$ , such that the process  $A' \mid B'$  will respect the disjointness conditions on names and variables.

► **Example 7.** We illustrate our syntax with the SPEKE protocol (see [23] for a complete description).

$$\begin{aligned} A \rightarrow B : M_1 &= \text{exp}(w, ra) \\ B \rightarrow A : M_2 &= \text{exp}(w, rb) \\ A \rightarrow B : M_3 &= \text{senc}(ca, \text{exp}(\text{exp}(w, rb), ra)) \\ B \rightarrow A : M_4 &= \text{senc}(\langle ca, cb \rangle, \text{exp}(\text{exp}(w, ra), rb)) \\ A \rightarrow B : M_5 &= \text{senc}(cb, \text{exp}(\text{exp}(w, rb), ra)) \end{aligned}$$

The goal of this protocol is to mutually authenticate  $A$  and  $B$  with respect to each other, provided that they share an initial secret  $w$ . This is done by a simple Diffie-Hellman exchange from a shared secret  $w$ , creating a common key  $\text{exp}(\text{exp}(w, ra), rb) =_{\text{E}} \text{exp}(\text{exp}(w, rb), ra)$ , followed by a challenge-response transaction. The data  $ra, ca$  (resp.  $rb, cb$ ) are nonces that are freshly generated by  $A$  (resp.  $B$ ). In our calculus, we model one session of the protocol as  $\nu w.(A \mid B)$ :

$$\begin{aligned} A &= \nu ra, ca. \text{out}(\text{exp}(w, ra)). \text{in}(x_1). \\ &\quad \text{out}(\text{senc}(ca, ka)). \text{in}(x_2). \\ &\quad \text{out}(\text{senc}(\text{proj}_2(\text{sdec}(x_2, ka)), ka)) \\ B &= \nu rb, cb. \text{in}(y_1). \text{out}(\text{exp}(w, rb)). \\ &\quad \text{in}(y_2). \text{out}(\text{senc}(\langle \text{sdec}(y_2, kb), cb \rangle, kb)). \\ &\quad \text{in}(y_3). \text{if } \text{sdec}(y_3, kb) = cb \text{ then } P \text{ else } 0. \end{aligned}$$

where  $ka = \text{exp}(x_1, ra)$ ,  $kb = \text{exp}(y_1, rb)$ , and  $P$  models an application that is executed when  $B$  has been successfully authenticated.

An *evaluation context* is an extended process with a hole instead of an extended process. Given an extended process  $A$  we denote by  $\phi(A)$  the frame obtained by replacing any embedded plain processes in it with  $0$ .

### Semantics

We here only give an informal account of the semantics and refer the reader to [20] for the complete definition. We consider a basic *structural equivalence*, denoted  $\equiv$ , which includes for instance  $A \mid B \equiv B \mid A$ ,  $A \mid 0 \equiv A$  and  $\nu n_1, n_2. A \equiv \nu n_2, n_1. A$ . In particular, using structural equivalence, every extended process  $A$  can be rewritten to consist of a substitution and a plain process with some restricted names, *i.e.*,

$$A \equiv \nu \tilde{n}. (\{M_1/z_1\} \mid \dots \mid \{M_k/z_k\} \mid P).$$

Moreover, any frame can be rewritten as  $\nu n. \sigma$  matching the notion of frame introduced in Section 2.1.

*Labelled operational semantics* is the smallest relation  $A \xrightarrow{\ell} A'$  between extended processes which is closed under structural equivalence ( $\equiv$ ), application of evaluation context, and a few usual rules for input, output and conditional where  $\ell$  is a label of one of the following forms:

- a label  $\text{in}(M)$ , where  $M$  is a ground term such that  $\phi(A) \vdash_{\mathbf{E}} M$ ;
- a label  $\text{out}(M)$ , where  $M$  is a ground term, which corresponds to an output of  $M$  and which adds an active substitution  $\{M/z\}$  in  $A'$ ;
- a label  $\tau$  corresponding to a silent action (the evaluation of a conditional).

We denote by  $\rightarrow$  the relation  $\{\xrightarrow{\ell} \mid \ell \in \{\text{in}(M), \text{out}(M), \tau\}, M \in \mathcal{T}(\Sigma)\}$  and by  $\rightarrow^*$  its reflexive and transitive closure. Note that these semantics take the viewpoint that the attacker controls the entire network. Any message is sent to the attacker (who may or not forward it to the intended recipient) and the processes do not have any means to communicate directly.

► **Example 8.** We illustrate our semantics with the SPEKE protocol presented in Example 7. The derivation below represents a normal execution of the protocol. For simplicity of this example we suppose that  $\text{fv}(P) = \emptyset$ .

$$\begin{array}{l} \nu w. (A \mid B) \\ \xrightarrow{\text{out}(\text{exp}(w, ra))} \nu w, ra, ca. (\text{in}(x_1). \text{out}(\text{senc}(ca, ka)). \text{in}(x_2). \dots \mid \{M_1/z_1\} \mid B) \\ \xrightarrow{\text{in}(\text{exp}(w, ra))} \nu w, ra, ca, rb, cb. (\text{in}(x_1). \text{out}(\text{senc}(ca, ka)). \text{in}(x_2). \dots \mid \{M_1/z_1\} \mid B') \\ \xrightarrow{*} \nu w, ra, ca, rb, cb. (\{M_1/z_1, M_2/z_2, M_3/z_3, M_4/z_4, M_5/z_5\} \mid P) \end{array}$$

where  $B'$  represents the remaining actions of  $B$  in which  $y_1$  is replaced by  $\text{exp}(w, ra)$ , and  $M_1, \dots, M_5$  are defined in Example 7. The first step is an output of  $M_1$  performed by  $A$ . The active substitution  $\{M_1/z_1\}$  allows the environment (*i.e.* the attacker) to access the message  $M_1$  via the handle  $z_1$ . The handle  $z_1$  is important since the environment cannot itself describe the term that was output, except by referring to it using  $z_1$ . Since  $M_1$  is accessible to the environment via  $z_1$ , the next input action can be triggered: we have that  $\nu w, ra, ca. \{M_1/z_1\} \vdash_{\mathbf{E}} \text{exp}(w, ra)$  using the the recipe  $z_1$ .

In the remaining, we will focus our attention on password-based protocols.

► **Definition 9** ( $\ell$ -party password protocol specification). An  $\ell$ -party password protocol specification  $\mathcal{P}$  is a process such that:

$$\mathcal{P} = \nu w.(\nu \tilde{m}_1.P_1 \mid \dots \mid \nu \tilde{m}_\ell.P_\ell)$$

where each  $P_i$  is a closed plain processes. The processes  $\nu \tilde{m}_i.P_i$  are called the roles of  $\mathcal{P}$ .

The process  $\nu w.(A \mid B)$  described in Example 7 is a 2-party password protocol specification with roles  $A$  and  $B$ . The notion of security we will mainly concentrate on is resistance against guessing attacks.

► **Definition 10** (process resistant to guessing attacks). Let  $A$  be an extended, closed process and  $\tilde{w} \subseteq \text{bn}(A)$ . We say that a process  $A$  is *resistant to guessing attacks* against  $\tilde{w}$  if, for every process  $B$  such that  $A \rightarrow^* B$ , we have that the frame  $\phi(B)$  is resistant to guessing attacks against  $\tilde{w}$ .

### 3 Composition Results for Password-based Protocols

In this section, we present several composition results that hold for an arbitrary equational theory  $E$ . The only requirement we have is that there exists a function symbol  $h$ , which is a free symbol in  $E$ , *i.e.*  $h$  does not occur in any equation in  $E$ . Intuitively,  $h$  models a hash function.

#### 3.1 Disjoint State

First, we note that, as usual, composition preserves security properties as soon as protocols have disjoint states, *i.e.*, they do not share any restricted names. Intuitively, this is due to the fact that when other protocols do not share any secrets of the analyzed protocol, then the attacker can completely simulate all messages sent by these other protocols. This has been formally shown in [20].

► **Theorem 11.** [20] *Let  $A_1, \dots, A_k$  be  $k$  extended processes such that for all  $i$ , we have that  $A_i$  is resistant to guessing attack against  $w_i$ . We have that  $A_1 \mid \dots \mid A_k$  is resistant to guessing attack against  $w_1, \dots, w_k$ .*

#### 3.2 Joint State

As soon as two protocols share a restricted name, *e.g.* a password, composition does not necessarily preserve security properties (see [20] for an example). We will use a tagging technique to avoid confusion between messages that come from different protocols. More precisely we will tag each occurrence of a password. Intuitively, we consider protocols that are well-tagged w.r.t. a secret  $w$ : all occurrences of  $w$  are of the form  $h(t, w)$  for some tag  $t$ .

#### Composing protocols

When each process is well-tagged with a different tag, it can be shown that the processes can be safely composed. One may think of these tags as protocol identifiers, which uniquely identify which protocol is executed, and avoid messages from different protocols to interfere with each other.

► **Theorem 12.** *Let  $\alpha_1, \dots, \alpha_k$  be  $k$  distinct names, and  $\nu w.A_1, \dots, \nu w.A_k$  be  $k$  processes such that  $\alpha_i \notin \text{bn}(A_i)$  for any  $i \in \{1, \dots, k\}$ . If each  $\nu w.A_i$  is resistant to guessing attack*



against  $w$  then the process  $\nu w.(A_1\{\mathbf{h}(\alpha_1, w)/w\} \mid \dots \mid A_k\{\mathbf{h}(\alpha_k, w)/w\})$  is resistant to guessing attack against  $w$ .

Actually, this result is a small adaptation from [20] (the result was shown for  $k = 2$  only). This result can also be seen as a consequence of Proposition 15 and Lemma 16 (stated in Section 4) and a theorem showing that adding tags preserves resistance against guessing attacks (this last theorem is stated and proved in [20]).

The previous result is useful to compose distinct protocols. However, when we want to compose different sessions from the same protocol, we cannot assume that participants share a distinct tag for each possible session. In the following, we define a way to dynamically establish such a session tag.

### Composing sessions from the same protocol

We now define a protocol transformation which establishes a dynamic tag that will guarantee composition. To establish such a tag that serves as a session identifier all participants generate a fresh nonce, that is sent to all other participants. This is similar to the establishment of session identifiers proposed by Barak [8]. The sequence of these nonces is then used to tag the password. Note that an active attacker may interfere with this initialization phase and may intercept and replace some of the nonces. However, since each participant generates a fresh nonce, these tags are indeed distinct for each session. This transformation is formally defined as follows.

► **Definition 13** (transformation  $\overline{\mathcal{P}}$ ). Let  $\mathcal{P} = \nu w.(\nu \tilde{m}_1.P_1 \mid \dots \mid \nu \tilde{m}_\ell.P_\ell)$  be a password protocol specification. Let  $n_1, \dots, n_\ell$  be fresh names and  $\{x_i^j \mid 1 \leq i, j \leq \ell\}$  be a set of fresh variables. We define the protocol specification  $\overline{\mathcal{P}} = \nu w.(\nu \tilde{m}_1, n_1.\overline{P}_1 \mid \dots \mid \nu \tilde{m}_\ell, n_\ell.\overline{P}_\ell)$  as follows:

$$\overline{P}_i = \text{in}(x_i^1) \dots \text{in}(x_i^{i-1}).\text{out}(n_i).\text{in}(x_i^{i+1}).\text{in}(x_i^\ell).P_i\{\mathbf{h}(\text{tag}_i, w)/w\}$$

where  $\text{tag}_i = \langle x_i^1, \dots, \langle x_i^{\ell-1}, x_i^\ell \rangle \rangle$  and  $x_i^i = n_i$ .

We can now state our composition result for sessions of a same protocol: if a protocol resists against guessing attacks on  $w$  then any number of instances of the transformed protocol will also resist to guessing attacks on  $w$ .

► **Theorem 14.** Let  $\mathcal{P} = \nu w.(\nu \tilde{m}_1.P_1 \mid \dots \mid \nu \tilde{m}_\ell.P_\ell)$  be a password protocol specification that is resistant to guessing attacks against  $w$ . Let  $\mathcal{P}'$  be such that  $\overline{\mathcal{P}} = \nu w.\mathcal{P}'$ , and  $\mathcal{P}'_1, \dots, \mathcal{P}'_p$  be  $p$  instances of  $\mathcal{P}'$ . Then we have that  $\nu w.(\mathcal{P}'_1 \mid \dots \mid \mathcal{P}'_p)$  is resistant to guessing attacks against  $w$ .

### Discussion

Note that it is possible to combine these two ways of tagging. Applying successively the two previous theorems we obtain that a tag of the form  $\mathbf{h}(\langle n_1, \dots, n_\ell \rangle, \mathbf{h}(\alpha, w))$  allows to safely compose different sessions of a same protocol, and also sessions of other protocols. It would also be easy to adapt the proofs to directly show that a simpler tag of the form  $\mathbf{h}(\langle \alpha, \langle n_1, \dots, n_\ell \rangle \rangle, w)$  could be used.

The notion of security we consider is resistance to guessing attacks. While generally resistance against guessing attacks is indeed a necessary condition to ensure security properties, this property is not a goal in itself. However, the way we prove our composition

results allows us also to ensure that those protocols can be safely composed w.r.t. more classical trace-based security properties such as secrecy or authentication.

Finally, we note that our composition result yields a simple design methodology. It is sufficient to design a protocol which is secure for a single session. After applying the above protocol transformation we conclude that the transformed protocol is secure for an arbitrary number of sessions. Note that even though our protocol language does not include replication, our composition results for sessions ensure security for an unbounded number of sessions. Indeed, as any attack requires only a finite number of sessions, any attack on a transformed protocol which is secure for a single instance would yield a contradiction. As deciding resistance to guessing attacks is decidable for a bounded number of sessions (for a large class of equational theories) [9] our result can also be seen as a new decidability result for an unbounded number of sessions on a class of tagged protocols.

## 4 Proof of our main result

The goal of this section is to give an overview of the proof of Theorem 14. This proof is done in 4 main steps.

### Step 1

Assume, by contradiction, that  $P = \nu w.(\mathcal{P}'_1 \mid \dots \mid \mathcal{P}'_p)$  admits a guessing attack on  $w$ . Hence there exists an attack derivation  $P \rightarrow^* Q$  for some process  $Q$  such that  $\phi(Q)$  is not resistant to a guessing attack against  $w$ .

Thanks to our transformation, we know that each role involved in  $P$  has to execute its preamble, *i.e.*, the preliminary nonce exchange of our transformation, at the end of which it computes a tag. Let  $t_1, \dots, t_k$  be the distinct tags that are computed during this derivation. Then, we group together roles (*i.e.* a process) that computed the same tag in order to retrieve a situation that is similar to when we use static tags. We note that the tags are constructed such that each group contains at most one instance of each role of  $\bar{\mathcal{P}}$ . Our aim is to show that an attack already exists on one of these groups, and so the attack is not due to composition. However, one difficulty comes from the fact that once the preambles have been executed, the tags that have been computed by the different roles may share some names in addition to  $w$ .

### Step 2

The fact that some names are shared between the processes we would like to separate in order to retrieve the disjoint case significantly complicates the situation. Indeed, if composition still works, it is due to the fact that names shared among differently tagged processes only occur at particular positions. To get rid of shared names, we show that we can mimic a derivation by another derivation where tags  $t_1, \dots, t_k$  are replaced by constants  $c_1, \dots, c_k$  and different password are used ( $w_1, \dots, w_k$  instead of  $w$ ). We denote by  $\delta_{w_i, w}$  the replacement  $\{w/w_1\} \dots \{w/w_k\}$ , by  $\delta_{w_i, h(c_i, w_i)}$  the replacement  $\{h(c_1, w_1)/w_1\} \dots \{h(c_k, w_k)/w_k\}$  and by  $\delta_{c_i, t_i}$  the replacement  $\{t_1/c_1\} \dots \{t_k/c_k\}$ .

► **Proposition 15.** *Let  $t_1, \dots, t_k$  be distinct ground terms modulo  $\mathbf{E}$  and  $c_1, \dots, c_k, w_1, \dots, w_k$  be distinct fresh names. Let  $\nu \tilde{n}.A$  be an extended process such that  $bn(A) = \emptyset$ ,  $w \notin fn(A)$ , and  $A =_{\mathbf{E}} A' \delta_{w_i, h(c_i, w_i)}$  for some  $A'$  such that  $c_1, \dots, c_k \notin fn(A')$ . Moreover, we assume that  $w, w_1, \dots, w_k, c_1, \dots, c_k \notin \tilde{n}$ .*

Let  $\bar{B}$  be such that  $\nu w.\nu\tilde{n}.(A\delta_{c_i,t_i}\delta_{w_i,w}) \xrightarrow{\ell} \bar{B}$ . Moreover, when  $\ell = \text{in}(\tilde{M})$  we assume that  $w_1, \dots, w_k, c_1, \dots, c_k \notin \text{fn}(\tilde{M})$ . Then there exists extended processes  $B, B'$ , and labels  $\ell_0, \ell'$  such that:

- $\bar{B} \equiv \nu w.\nu\tilde{n}.(B\delta_{c_i,t_i}\delta_{w_i,w})$  with  $\text{bn}(B) = \emptyset$  and  $w \notin \text{fn}(B)$ ,  $\ell = \ell_0\delta_{c_i,t_i}\delta_{w_i,w}$ , and
- $B =_{\text{E}} B'\delta_{w_i,h(c_i,w_i)}$  with  $c_1, \dots, c_k \notin \text{fn}(B')$ ,  $\ell_0 =_{\text{E}} \ell'\delta_{w_i,h(c_i,w_i)}$ , and
- $\nu w_1 \dots \nu w_k.\nu\tilde{n}.A \xrightarrow{\ell_0} \nu w_1 \dots \nu w_k.\nu\tilde{n}.B$ .

This proposition shows how to map an execution of  $P \equiv \nu n_1 \dots \nu n_k \nu w.(A_1\delta_{c_i,t_i}\delta_{w_i,w} \mid \dots \mid A_k\delta_{c_i,t_i}\delta_{w_i,w})$  (same password) to an execution of  $\nu n_1 \nu w_1.A_1 \mid \dots \mid \nu n_k \nu w_k.A_k$  (different password) by maintaining a strong connection between these two derivations. Intuitively, the process  $A_j\delta_{c_i,t_i}\delta_{w_i,w}$  contains the roles in  $P$  that computed the tag  $t_j$  in the attack derivation.

Note that, except for  $w$ , a name that is shared between  $A_j\delta_{c_i,t_i}\delta_{w_i,w}$  and  $A_{j'}\delta_{c_i,t_i}\delta_{w_i,w}$  ( $j \neq j'$ ) necessarily occurs in a tag position in one of the process. Now that tags have been replaced by some constants, and the password  $w$  has been replaced by different passwords according to the tag, the processes  $A_j$  and  $A_{j'}$  do not share any name.

This proposition is actually sufficient to establish that security properties, like authentication, are preserved by composition. However, to establish resistant against guessing attacks, we need more.

### Step 3

We show that if a frame, obtained by executing several protocols that share a same password and that are tagged with terms  $t_i$ , is vulnerable to guessing attacks then the frame obtained by the corresponding execution of the protocols with different passwords and tagged with constants  $c_i$  is also vulnerable to guessing attacks.

► **Lemma 16.** *Let  $t_1, \dots, t_k$  be distinct ground terms modulo  $\text{E}$ . Let  $c_1, \dots, c_k, w_1, \dots, w_k$  be distinct fresh names, and  $\phi = \nu\tilde{n}.\sigma$  be a frame such that  $c_1, \dots, c_k, w_1, \dots, w_k \notin \tilde{n}$ , and  $\sigma =_{\text{E}} \sigma_0\delta_{w_i,h(c_i,w_i)}$  for some substitution  $\sigma_0$ . Let  $w$  be a fresh name, and  $\psi = \nu\tilde{n}.(\sigma\delta_{c_i,t_i}\delta_{w_i,w})$ . For each  $1 \leq i \leq k$ , we also assume that  $\nu w.\psi \vdash t_i$ .*

*If  $\nu\tilde{w}.\phi$  is resistant to guessing attacks against  $\tilde{w} = \{w_1, \dots, w_k\}$ , then  $\nu w.\psi$  is resistant to guessing attacks against  $w$ .*

The proof of the lemma is technical because mapping all  $w_i$ 's on the same password can introduce additional equalities between terms. However, each occurrence of the password is tagged, and the purpose of this design is to avoid the introduction of equalities between terms. Again, the lemma holds because the frames are well-tagged.

Thanks to Proposition 15 and Lemma 16 we obtain a guessing attack on the process  $\nu n_1 \nu w_1.A_1 \mid \dots \mid \nu n_k \nu w_k.A_k$  against  $w_1, \dots, w_k$ .

### Step 4

Applying Theorem 11 (combination for disjoint state protocols), we conclude that there is a guessing attack on  $\nu n_i \nu w_i.A_i$  for some  $i \in \{1, \dots, k\}$ . Then, it remains to show that the attack also works on the original protocol, *i.e.* the non-tagged version of the protocol. This is a direct application of Theorem 2 in [20]. This leads us to a contradiction since we have assumed that  $\mathcal{P}$  is resistant to guessing attacks against  $w$ .

## 5 Conclusion

In this paper we propose a transformation for password protocols based on a simple tagging mechanism. This transformation ensures that security is preserved when protocols are composed with other protocols which may use the same password. We show that when protocols are tagged using a simple protocol identifier, we are able to compose different protocols. Computing a dynamic session identifier allows one to also compose different sessions of a same protocol. Hence, it is sufficient to prove that a protocol is secure for one session in order to conclude security under composition.

Currently, as stated, our composition results allow to preserve resistance against offline guessing attacks. As already discussed it also follows from our proofs that trace properties would be preserved. Formalizing for instance preservation of authentication should be a rather straightforward extension. A more ambitious direction for future work would be the composition of more general, indistinguishability properties, expressed in terms of observational equivalence. We also plan to investigate sufficient conditions to ensure composition of protocols in the vein of [25] avoiding to change existing protocols.

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